

## **Question 1– Exoplanet Characterization**

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**12.07.2025**

### **Question (a): What is the inclination of GJ 8999 b?**

The inclination angle ( $i$ ) is the angle between a planet's orbital plane and the sky plane as seen by the observer. This angle plays a critical role in determining whether or not the planet transits.

#### **What Does Transit Observation Tell Us?**

Since GJ 8999 b transits, it means we observe a decrease in light as the planet passes in front of the star. This event only occurs when the planet's orbit is nearly edge-on to the observer's line of sight.

**Conclusion:** Since GJ 8999 b exhibits a transit, its inclination angle is approximately  $90^\circ$ .

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### **Question (b): What is the period of this exoplanet?**

- The first graph (28-day observation): There are periodic drops in the total flux of star GJ 8999, which indicate the planet's transits.
- The second graph: A zoomed-in view of one of those dips, focusing on a single transit event.

The planet's orbital period is determined by the time interval between successive transits:

In other words, the recurring interval between dips in the star's light represents one full orbit of the planet.

**Reading the Period from the Graph:** The first graph shows 28 days of data and reveals 6 distinct dips. So, we can reason: There are 6 transits spread across 28 days. Therefore, the time between transits is approximately 5 days.

**Estimated Result:** The orbital period of exoplanet GJ 8999 b is approximately 5 days.

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**Question (c): What is the radius of this planet?**

The transit depth tells us how much light the planet blocks when it passes in front of its star.

$$\text{Transit depth} = Z = (1 - 0.9975)/(1.0000) \times 100\% = 0.25\%$$

$$R_p = R_s \times \sqrt{Z} = 0.2 R \times \sqrt{0.0025} = 0.2 R \times 0.05 = 0.01 R$$

$$0.01 \times 109 = 1.09$$

The radius of planet GJ 8999 b is approximately 0.01 times the radius of the Sun. This means it's about 1.09 times the radius of Earth.

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**Question (d): What is the semi-amplitude (K) of this planetary signal?**

In the graphic, 1 m/s == 1263.5729 mm

$$v_{\text{max}} == 2787.9066 \text{ mm} == 2.206 \text{ m/s}$$

$$v_{\text{min}} == -2699.077 \text{ mm} == -2.136 \text{ m/s}$$

$$\text{semi-amplitude, } K = (v_{\text{max}} - v_{\text{min}})/2 = (2.206 - (-2.136))/2 = 2.171 \text{ m/s}$$

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**Question (e): What is the mass of this planet?**

$$M_p = K / (\sin(i) \cdot ((2 \pi G / P (M_s)^2))^{1/3})$$

$$K = 2.171 \text{ m/s}$$

$$P = 5 \text{ days} = 432000 \text{ s}$$

$$M = 0.2 M_{\odot} = 0.2 \cdot (2 \cdot 10^{30}) \text{ kg} = 4 \cdot 10^{28} \text{ kg}$$

$$G = 6.674 \times 10^{-11} \text{ m}^3 \text{kg}^{-1} \text{s}^{-2}$$

$$i = 90^\circ, \sin i = 1$$

$$M_p = 1.187 \cdot 10^{25} \text{ kg} = 1.99 M_{\text{earth}}$$

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**Question (f): What is the composition of GJ 8999 b?**

$$R_p = 0.01 R_{\text{sun}} = 0.01 \times 6.957 \times 10^8 \text{ m} = 1.092 R_{\text{earth}}$$

$$M_p = 1.187 \times 10^{25} \text{ kg} = 1.99 M_{\text{earth}}$$

Since the mass is 1.99 Earth masses, it's represented as  $10^{0.299} M_{\oplus}$  on a logarithmic axis.

in graph,

$0.25 R_{\text{Earth}} = 33 \text{pt}$

so,

$0.092 R_{\text{Earth}} \sim 12 \text{pt}$

1 unit in the x-axis = 158pt so, 0.299 units  $\sim 47 \text{pt}$

From the graph, it's clear that the composition of the planet is very near to 33% Rock, 67% Iron.