roozara_hw2

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- ECE 657A: Data and Knowledge Modelling and Analysis
- Winter 2019
- WATIAM:roozara ID: 20801583
- Homework 2:Data Normalization and

Reference used: About Feature Scaling and Normalization, Sebastian Raschka

```
In [24]: import pandas as pd
         import numpy as np
         #calculate zsore normalization and min-max normalizatio
         from sklearn import preprocessing
         #calculate the distance between datapoints
         from scipy.spatial import distance
         #importing the red-wine dataset into variable wd
         wd = pd.read_csv('data/winequality-red.csv',sep= ';')
         wd = wd.iloc[:10,:]
         #print(wd)
         wd
Out [24]:
            fixed acidity volatile acidity citric acid residual sugar chlorides \
         0
                      7.4
                                        0.70
                                                      0.00
                                                                       1.9
                                                                                0.076
         1
                      7.8
                                        0.88
                                                     0.00
                                                                       2.6
                                                                                0.098
         2
                      7.8
                                        0.76
                                                     0.04
                                                                       2.3
                                                                                0.092
                     11.2
                                                                       1.9
         3
                                        0.28
                                                      0.56
                                                                                0.075
                                                     0.00
                                                                       1.9
         4
                      7.4
                                        0.70
                                                                                0.076
         5
                      7.4
                                        0.66
                                                      0.00
                                                                       1.8
                                                                                0.075
         6
                      7.9
                                        0.60
                                                      0.06
                                                                       1.6
                                                                                0.069
         7
                      7.3
                                        0.65
                                                     0.00
                                                                       1.2
                                                                                0.065
         8
                      7.8
                                        0.58
                                                      0.02
                                                                       2.0
                                                                                0.073
         9
                      7.5
                                        0.50
                                                      0.36
                                                                       6.1
                                                                                0.071
            free sulfur dioxide total sulfur dioxide density
                                                                        sulphates
                                                                    рΗ
         0
                            11.0
                                                   34.0
                                                          0.9978 3.51
                                                                             0.56
         1
                            25.0
                                                   67.0
                                                          0.9968 3.20
                                                                             0.68
         2
                            15.0
                                                  54.0
                                                          0.9970 3.26
                                                                             0.65
         3
                            17.0
                                                  60.0
                                                         0.9980 3.16
                                                                             0.58
```

```
4
                   11.0
                                           34.0
                                                  0.9978 3.51
                                                                       0.56
5
                   13.0
                                           40.0
                                                                       0.56
                                                  0.9978 3.51
6
                   15.0
                                           59.0
                                                  0.9964 3.30
                                                                       0.46
7
                   15.0
                                           21.0
                                                  0.9946 3.39
                                                                       0.47
8
                    9.0
                                           18.0
                                                  0.9968 3.36
                                                                       0.57
9
                   17.0
                                          102.0
                                                  0.9978 3.35
                                                                       0.80
   alcohol
            quality
0
       9.4
                   5
       9.8
                   5
1
2
       9.8
                   5
3
       9.8
                   6
                   5
4
       9.4
5
                   5
       9.4
                   5
6
       9.4
7
                   7
      10.0
8
       9.5
                   7
```

1 Calculate the min-max normalized values

5

9

10.5

/home/engineer/anaconda3/envs/ece657A/lib/python3.7/site-packages/sklearn/preprocessing/data.pg
return self.partial_fit(X, y)

```
Out [25]:
            fixed acidity volatile acidity
                                              citric acid residual sugar
                                                                             chlorides
         0
                 0.025641
                                    0.700000
                                                  0.000000
                                                                   0.142857
                                                                              0.333333
         1
                 0.128205
                                    1.000000
                                                  0.000000
                                                                   0.285714
                                                                              1.000000
         2
                 0.128205
                                    0.800000
                                                  0.071429
                                                                   0.224490
                                                                              0.818182
         3
                                    0.000000
                 1.000000
                                                  1.000000
                                                                   0.142857
                                                                              0.303030
         4
                 0.025641
                                    0.700000
                                                  0.000000
                                                                   0.142857
                                                                              0.333333
         5
                 0.025641
                                    0.633333
                                                  0.000000
                                                                   0.122449
                                                                              0.303030
         6
                 0.153846
                                    0.533333
                                                  0.107143
                                                                   0.081633
                                                                              0.121212
         7
                 0.000000
                                    0.616667
                                                  0.000000
                                                                   0.000000
                                                                              0.000000
         8
                 0.128205
                                    0.500000
                                                  0.035714
                                                                              0.242424
                                                                   0.163265
```

```
9
        0.051282
                          0.366667
                                       0.642857
                                                       1.000000
                                                                  0.181818
   free sulfur dioxide
                       total sulfur dioxide
                                              density
                                                             pH sulphates \
0
                                   0.190476 0.941176
                                                                   0.294118
                 0.125
                                                        1.000000
1
                 1.000
                                   0.583333 0.647059
                                                       0.114286
                                                                   0.647059
2
                 0.375
                                   0.428571 0.705882 0.285714
                                                                   0.558824
3
                 0.500
                                   0.500000 1.000000 0.000000
                                                                   0.352941
4
                 0.125
                                   0.190476 0.941176 1.000000
                                                                   0.294118
5
                 0.250
                                   0.261905 0.941176 1.000000
                                                                   0.294118
6
                 0.375
                                   0.488095 0.529412 0.400000
                                                                  0.000000
7
                                                                   0.029412
                 0.375
                                   0.035714 0.000000 0.657143
8
                                   0.000000 0.647059
                 0.000
                                                       0.571429
                                                                   0.323529
9
                 0.500
                                    1.000000 0.941176
                                                                   1.000000
                                                       0.542857
    alcohol quality
0 0.000000
                 0.0
1 0.363636
                 0.0
2 0.363636
                 0.0
                 0.5
3 0.363636
4 0.000000
                 0.0
5 0.000000
                 0.0
6 0.000000
                 0.0
7 0.545455
                 1.0
8 0.090909
                 1.0
9
  1.000000
                 0.0
```

2 Calculate the Z-score normalized values

```
In [26]: #z-score normalized values
    std_scale = preprocessing.StandardScaler().fit(wd.iloc[:,:])
    wd_z = std_scale.transform(wd.iloc[:,:])
    wd_z=pd.DataFrame(wd_z)
    wd_z.columns =wd.columns
    #print(wd_z)
    wd_z
```

/home/engineer/anaconda3/envs/ece657A/lib/python3.7/site-packages/sklearn/preprocessing/data.pg
return self.partial_fit(X, y)

/home/engineer/anaconda3/envs/ece657A/lib/python3.7/site-packages/ipykernel_launcher.py:3: Data This is separate from the ipykernel package so we can avoid doing imports until

```
Out [26]:
            fixed acidity volatile acidity citric acid residual sugar
                                                                          chlorides
        0
                                                               -0.329398 -0.103362
                -0.498662
                                   0.451753
                                               -0.563489
                -0.135999
                                   1.630239
                                                                0.206831
        1
                                               -0.563489
                                                                           2.170608
         2
                -0.135999
                                   0.844582
                                               -0.346763
                                                               -0.022981
                                                                           1.550434
         3
                                  -2.298048
                                                               -0.329398 -0.206725
                 2.946642
                                                2.470683
                                   0.451753
                -0.498662
                                               -0.563489
                                                               -0.329398 -0.103362
```

```
5
       -0.498662
                          0.189867
                                       -0.563489
                                                       -0.406002 -0.206725
                                      -0.238399
6
       -0.045333
                         -0.202961
                                                       -0.559211 -0.826898
7
       -0.589328
                          0.124396
                                       -0.563489
                                                       -0.865627
                                                                  -1.240347
8
       -0.135999
                         -0.333904
                                       -0.455126
                                                       -0.252794 -0.413449
9
       -0.407997
                         -0.857676
                                                                 -0.620174
                                        1.387050
                                                        2.887978
   free sulfur dioxide
                        total sulfur dioxide
                                                density
                                                                   sulphates
                                                               Нq
0
             -0.896665
                                    -0.626576
                                               0.731200
                                                         1.276466
                                                                   -0.305196
1
              2.406839
                                    0.761143 -0.284356 -1.276466
                                                                    0.957683
                                    0.214466 -0.081244 -0.782350
2
              0.047193
                                                                    0.641963
3
                                    0.466778 0.934311 -1.605877
              0.519122
                                                                   -0.094716
4
             -0.896665
                                    -0.626576 0.731200
                                                        1.276466
                                                                   -0.305196
5
             -0.424736
                                    -0.374264 0.731200
                                                         1.276466
                                                                   -0.305196
6
                                    0.424726 -0.690578 -0.452940
              0.047193
                                                                   -1.357594
7
              0.047193
                                    -1.173253 -2.518578
                                                         0.288234
                                                                   -1.252354
8
             -1.368595
                                    -1.299409 -0.284356 0.041176
                                                                   -0.199956
              0.519122
                                    2.232966 0.731200 -0.041176
                                                                    2.220561
              quality
    alcohol
0 -0.880830 -0.620174
1 0.293610 -0.620174
2 0.293610 -0.620174
3 0.293610 0.620174
4 -0.880830 -0.620174
5 -0.880830 -0.620174
6 -0.880830 -0.620174
7 0.880830
            1.860521
8 -0.587220
            1.860521
9 2.348881 -0.620174
```

3 Calculate the mean subtracted normalized values

```
In [27]: # mean subtracted normalized values
         wd_mean= wd.mean()
         wd meansub norm = wd - wd.mean()
         #print (wd_meansub_norm )
         wd_meansub_norm
Out [27]:
            fixed acidity volatile acidity citric acid residual sugar
                                                                              chlorides
                     -0.55
                                        0.069
         0
                                                     -0.104
                                                                       -0.43
                                                                                 -0.001
                     -0.15
                                        0.249
                                                     -0.104
                                                                        0.27
                                                                                  0.021
         1
         2
                     -0.15
                                        0.129
                                                     -0.064
                                                                       -0.03
                                                                                  0.015
         3
                      3.25
                                                                       -0.43
                                       -0.351
                                                      0.456
                                                                                 -0.002
         4
                     -0.55
                                                     -0.104
                                                                       -0.43
                                        0.069
                                                                                 -0.001
         5
                     -0.55
                                        0.029
                                                     -0.104
                                                                       -0.53
                                                                                 -0.002
         6
                     -0.05
                                       -0.031
                                                     -0.044
                                                                       -0.73
                                                                                 -0.008
                     -0.65
                                        0.019
                                                     -0.104
                                                                       -1.13
                                                                                 -0.012
```

```
8
           -0.15
                             -0.051
                                           -0.084
                                                             -0.33
                                                                        -0.004
9
           -0.45
                             -0.131
                                            0.256
                                                               3.77
                                                                        -0.006
   free sulfur dioxide
                         total sulfur dioxide
                                                density
                                                                 sulphates
                                                             Нq
0
                   -3.8
                                         -14.9
                                                0.00072 0.155
                                                                     -0.029
1
                   10.2
                                          18.1 -0.00028 -0.155
                                                                      0.091
2
                    0.2
                                           5.1 -0.00008 -0.095
                                                                      0.061
3
                    2.2
                                          11.1 0.00092 -0.195
                                                                     -0.009
4
                   -3.8
                                         -14.9
                                                0.00072 0.155
                                                                     -0.029
5
                   -1.8
                                          -8.9 0.00072 0.155
                                                                     -0.029
6
                    0.2
                                          10.1 -0.00068 -0.055
                                                                     -0.129
7
                    0.2
                                         -27.9 -0.00248 0.035
                                                                     -0.119
8
                   -5.8
                                         -30.9 -0.00028 0.005
                                                                     -0.019
9
                    2.2
                                          53.1 0.00072 -0.005
                                                                      0.211
   alcohol
            quality
0
      -0.3
                -0.5
       0.1
                -0.5
1
2
       0.1
                -0.5
3
       0.1
                 0.5
      -0.3
4
                -0.5
5
      -0.3
                -0.5
                -0.5
6
      -0.3
7
       0.3
                 1.5
8
      -0.2
                 1.5
9
       0.8
                -0.5
```

4 Calculate Manhatten distance for each of the first 10 points

```
In [28]:
         d_matrix= distance.squareform(distance.pdist(wd,'cityblock'))
         d_matrix= pd.DataFrame(d_matrix)
         np.fill_diagonal(d_matrix.values, 'nan')
         d_matrix
Out [28]:
                  0
                                      2
                                               3
                                                        4
                                                                           6
                                                                                     7
                                                                                        \
                            1
                                                                  5
                      49.1330
                                         38.5512
         0
                NaN
                               25.6568
                                                   0.0000
                                                             8.1410
                                                                     30.2784
                                                                               20.6742
         1
            49.1330
                          {\tt NaN}
                               23.5562
                                         21.4242
                                                  49.1330
                                                            41.2740
                                                                     20.1894
                                                                              60.7652
         2
            25.6568
                     23.5562
                                   NaN
                                         13.9880
                                                  25.6568
                                                            17.7978
                                                                      6.6336
                                                                               37.2894
            38.5512
                      21.4242
                               13.9880
                                                  38.5512
                                                            30.6102
                                                                      9.0876
                                                                               48.0834
         3
                                             NaN
         4
             0.0000
                      49.1330
                               25.6568
                                         38.5512
                                                      NaN
                                                             8.1410
                                                                     30.2784
                                                                               20.6742
                     41.2740
                               17.7978
                                         30.6102
         5
             8.1410
                                                   8.1410
                                                                {\tt NaN}
                                                                     22.1374
                                                                               24.5332
           30.2784
                      20.1894
                                6.6336
                                          9.0876
                                                  30.2784
                                                            22.1374
                                                                               41.8158
                                                                         NaN
            20.6742
                      60.7652
                               37.2894
                                         48.0834
                                                  20.6742
                                                            24.5332
                                                                     41.8158
                                                                                   NaN
         8 20.9040
                     68.5150
                               44.9992
                                         55.8532
                                                  20.9040
                                                            28.9630
                                                                     49.8344
                                                                               11.0302
         9 80.3650 48.5380
                               55.6418
                                         52.4342 80.3650
                                                            72.4240
                                                                     51.7934
                                                                              91.4892
```

```
9
                                   0
                                                    20.9040
                                                                                            80.3650
                                    1
                                                    68.5150
                                                                                            48.5380
                                    2
                                                    44.9992
                                                                                            55.6418
                                                    55.8532
                                    3
                                                                                            52.4342
                                    4
                                                    20.9040
                                                                                            80.3650
                                    5
                                                    28.9630
                                                                                            72.4240
                                                    49.8344
                                                                                            51.7934
                                   6
                                   7
                                                    11.0302
                                                                                            91.4892
                                   8
                                                                                        100.0630
                                                                    NaN
                                                100.0630
                                                                                                            NaN
In [29]: man_dist=pd.DataFrame([d_matrix.idxmin(axis=0),d_matrix.min(axis=0),d_matrix.idxmax(axis=0),d_matrix.min(axis=0),d_matrix.idxmax(axis=0),d_matrix.min(axis=0),d_matrix.idxmax(axis=0),d_matrix.min(axis=0),d_matrix.idxmax(axis=0),d_matrix.min(axis=0),d_matrix.idxmax(axis=0),d_matrix.min(axis=0),d_matrix.idxmax(axis=0),d_matrix.min(axis=0),d_matrix.idxmax(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axis=0),d_matrix.min(axi
                                   man_dist.columns=["index dest", "nearest(min)", "index dest", "farthest(max)"]
                                   man_dist.index.name = ['index source']
                                   man_dist
Out [29]:
                                                                                                    index dest
                                                                                                                                                   nearest(min)
                                                                                                                                                                                                            index dest
                                                                                                                                                                                                                                                         farthest(max)
                                     [index source]
                                                                                                                                4.0
                                                                                                                                                                            0.0000
                                                                                                                                                                                                                                        9.0
                                                                                                                                                                                                                                                                                     80.3650
                                    1
                                                                                                                                6.0
                                                                                                                                                                        20.1894
                                                                                                                                                                                                                                        8.0
                                                                                                                                                                                                                                                                                     68.5150
                                    2
                                                                                                                                6.0
                                                                                                                                                                            6.6336
                                                                                                                                                                                                                                        9.0
                                                                                                                                                                                                                                                                                     55.6418
                                    3
                                                                                                                                6.0
                                                                                                                                                                                                                                        8.0
                                                                                                                                                                            9.0876
                                                                                                                                                                                                                                                                                     55.8532
                                    4
                                                                                                                                0.0
                                                                                                                                                                            0.0000
                                                                                                                                                                                                                                        9.0
                                                                                                                                                                                                                                                                                     80.3650
                                    5
                                                                                                                                0.0
                                                                                                                                                                                                                                        9.0
                                                                                                                                                                                                                                                                                     72.4240
                                                                                                                                                                            8.1410
                                    6
                                                                                                                                2.0
                                                                                                                                                                            6.6336
                                                                                                                                                                                                                                        9.0
                                                                                                                                                                                                                                                                                     51.7934
                                    7
                                                                                                                                8.0
                                                                                                                                                                        11.0302
                                                                                                                                                                                                                                        9.0
                                                                                                                                                                                                                                                                                     91.4892
                                   8
                                                                                                                                7.0
                                                                                                                                                                        11.0302
                                                                                                                                                                                                                                        9.0
                                                                                                                                                                                                                                                                                 100.0630
                                   9
                                                                                                                                1.0
                                                                                                                                                                        48.5380
                                                                                                                                                                                                                                        8.0
                                                                                                                                                                                                                                                                                 100.0630
```

5 Calculate Euclidean distance for each of the first 10 points

```
In [30]: d_eucl= distance.squareform(distance.pdist(wd, 'euclidean'))
         d_eucl= pd.DataFrame(d_eucl)
         np.fill_diagonal(d_eucl.values, 'nan')
         d_eucl
Out [30]:
                                            2
                     0
                                 1
                                                        3
                                                                                5
                                                                                  \
         0
                        35.860192
                                    20.409705
                                                26.985420
                                                            0.000000
                                                                        6.325472
                   NaN
         1
            35.860192
                              {\tt NaN}
                                    16.404589
                                                11.257696
                                                           35.860192
                                                                       29.565511
                        16.404589
            20.409705
                                          NaN
                                                 7.296300
                                                           20.409705
                                                                       14.165186
         3
            26.985420
                                     7.296300
                                                           26.985420
                                                                       20.789202
                        11.257696
                                                      {\tt NaN}
                                                                        6.325472
         4
             0.000000
                        35.860192
                                    20.409705
                                                26.985420
                                                                  NaN
             6.325472
                        29.565511
                                    14.165186
                                                20.789202
                                                            6.325472
         5
                                                                              NaN
         6
           25.326029
                        12.857342
                                     5.071906
                                                 4.186459
                                                           25.326029
                                                                       19.114166
         7
            13.779881
                        47.142170
                                    33.084192
                                                39.271562
                                                           13.779881
                                                                       19.228955
           16.254766
                       51.590491
                                    36.554474
                                               42.907828
                                                           16.254766
                                                                       22.455276
```

```
9 68.404041
                       36.085200 48.199803 42.390953
                                                          68.404041 62.289232
                    6
                                7
                                           8
                                                       9
            25.326029
                        13.779881
                                   16.254766
                                               68.404041
            12.857342
                        47.142170
                                   51.590491
                                               36.085200
             5.071906
                       33.084192
                                   36.554474
                                               48.199803
         3
             4.186459
                        39.271562
                                   42.907828
                                               42.390953
                                               68.404041
            25.326029
                       13.779881
                                   16.254766
                       19.228955
                                   22.455276
         5
            19.114166
                                              62.289232
         6
                  NaN
                        38.064344
                                  41.487320
                                              43.299401
         7
            38.064344
                                    6.793841
                                              81.200755
                              NaN
                                               84.510798
         8
           41.487320
                         6.793841
                                         NaN
         9 43.299401
                       81.200755 84.510798
                                                     NaN
In [31]: eucl_dist=pd.DataFrame([d_eucl.idxmin(axis=0),d_eucl.min(axis=0),d_eucl.idxmax(axis=0)
         eucl_dist.columns=["index dest", "nearest(min)", "index dest", "farthest(max)"]
         eucl_dist.index.name = ['index source']
         eucl_dist
Out [31]:
                          index dest nearest(min)
                                                     index dest farthest(max)
         [index source]
                                 4.0
                                          0.000000
                                                            9.0
                                                                      68.404041
         1
                                 3.0
                                          11.257696
                                                            8.0
                                                                      51.590491
         2
                                 6.0
                                                            9.0
                                          5.071906
                                                                      48.199803
         3
                                 6.0
                                          4.186459
                                                            8.0
                                                                      42.907828
         4
                                 0.0
                                                            9.0
                                          0.000000
                                                                      68.404041
         5
                                 0.0
                                          6.325472
                                                            9.0
                                                                      62.289232
         6
                                 3.0
                                          4.186459
                                                            9.0
                                                                      43.299401
         7
                                 8.0
                                                            9.0
                                          6.793841
                                                                      81.200755
         8
                                 7.0
                                          6.793841
                                                            9.0
                                                                      84.510798
         9
                                 1.0
                                         36.085200
                                                            8.0
                                                                      84.510798
```

6 Calculate cosine distance for each of the first 10 points

```
In [32]: d_cos= distance.squareform(distance.pdist(wd,'cosine'))
         d_cos= pd.DataFrame(d_cos)
         np.fill_diagonal(d_cos.values, 'nan')
         d_{cos}
Out [32]:
                   0
                              1
                                        2
                                                   3
                                                                       5
                                 0.007749
                 {\tt NaN}
                      0.015207
                                           0.007776
                                                     0.000000
                                                                0.001322
                                                                          0.011912
                                                                0.007860
         1
           0.015207
                            NaN
                                 0.004858
                                           0.005985
                                                     0.015207
                                                                          0.006094
         2 0.007749
                      0.004858
                                           0.001097
                                                      0.007749
                                                                0.003120
                                      {\tt NaN}
                                                                          0.000601
           0.007776
                      0.005985
                                 0.001097
                                                {\tt NaN}
                                                     0.007776
                                                                0.003502
                                                                          0.001635
         4 0.000000
                      0.015207
                                 0.007749
                                           0.007776
                                                                0.001322
                                                                          0.011912
                                                           {\tt NaN}
         5 0.001322
                      0.007860 0.003120
                                           0.003502 0.001322
                                                                     NaN
                                                                          0.006079
         6 0.011912
                      0.006094 0.000601
                                           0.001635
                                                     0.011912
                                                                0.006079
                                                                                NaN
         7 0.051499 0.082365 0.089001 0.086412 0.051499
                                                                0.060757 0.102130
```

```
8 \quad 0.045682 \quad 0.099274 \quad 0.088973 \quad 0.085518 \quad 0.045682 \quad 0.060301 \quad 0.101541
9 0.035050 0.019639 0.011228
                                 0.014255 0.035050 0.025574 0.007549
          7
0 0.051499 0.045682 0.035050
1 0.082365 0.099274 0.019639
2 0.089001 0.088973 0.011228
3 0.086412 0.085518 0.014255
4 0.051499 0.045682 0.035050
5 0.060757 0.060301 0.025574
6 0.102130 0.101541 0.007549
7
        NaN 0.015776 0.159302
8 0.015776
                  NaN 0.153601
9 0.159302 0.153601
                            NaN
```

Out [33]:		index dest	${\tt nearest(min)}$	index dest	farthest(max)
	[index source]				
	0	4.0	0.000000	7.0	0.051499
	1	2.0	0.004858	8.0	0.099274
	2	6.0	0.000601	7.0	0.089001
	3	2.0	0.001097	7.0	0.086412
	4	0.0	0.000000	7.0	0.051499
	5	0.0	0.001322	7.0	0.060757
	6	2.0	0.000601	7.0	0.102130
	7	8.0	0.015776	9.0	0.159302
	8	7.0	0.015776	9.0	0.153601
	9	6.0	0.007549	7.0	0.159302