

Recap

Set ADT

Counter ADT

Assorted
Problems

Demo: Python
Dictionaries

COMP2521 25T2

Applications of Hash Tables

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set adt
counter adt
assorted problems

Recap

Set ADT

Counter ADT

Assorted
ProblemsDemo: Python
Dictionaries

A hash table is a data structure that stores key-value pairs,
where keys are unique

jas \Rightarrow green	andrew \Rightarrow red
sasha \Rightarrow purple	
kevin \Rightarrow blue	jake \Rightarrow yellow
hayden \Rightarrow red	

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Set ADT

Counter ADT

Assorted Problems

Demo: Python Dictionaries

Operations

Insert: Insert or replace key-value pair

Lookup: Given a key, get its associated value

Delete: Given a key, delete its key-value pair

Performance

Average-case: $O(1)$

Assuming good hash function and appropriate resizing

Worst-case: $O(n)$

If all keys hash to the same value (extremely unlikely with good hash)

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Set ADT

Counter ADT

Assorted
Problems

Demo: Python
Dictionaries

Hash tables are used everywhere
due to their efficiency

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Set ADT

Counter ADT

Assorted
ProblemsDemo: Python
Dictionaries

A set is an unordered collection of distinct elements

Operations

Insert: Insert an item into the set

Membership: Check if an item is in the set

Delete: Delete an item from the set

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Set ADT

Counter ADT

Assorted
ProblemsDemo: Python
Dictionaries

```
/** Creates a new empty set */
Set SetNew(void);

/** Free memory used by set */
void SetFree(Set set);

/** Inserts an item into the set */
void SetInsert(Set set, int item);

/** Checks if an item is in the set */
bool SetContains(Set set, int item);

/** Deletes an item from the set */
void SetDelete(Set set, int item);

/** Returns the size of the set */
int SetSize(Set set);

/** Displays the set */
void SetShow(Set set);
```

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Counter ADT

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ProblemsDemo: Python
Dictionaries

Data Structure	Insert	Membership	Delete
Unordered array	$O(n)$	$O(n)$	$O(n)$
Ordered array	$O(n)$	$O(\log n)$	$O(n)$
Linked list	$O(n)$	$O(n)$	$O(n)$
AVL tree	$O(\log n)$	$O(\log n)$	$O(\log n)$
Hash table	?	?	?

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Set ADT

Counter ADT

Assorted
Problems

Demo: Python
Dictionaries

How to implement the Set ADT using a hash table?

Insert

Insert item into the hash table as a key
Can use anything as the value

Contains

Check if the item exists in the hash table

Delete

Delete the item from the hash table

Recap

Set ADT

Counter ADT

Assorted
ProblemsDemo: Python
Dictionaries

Data Structure	Insert	Membership	Delete
Unordered array	$O(n)$	$O(n)$	$O(n)$
Ordered array	$O(n)$	$O(\log n)$	$O(n)$
Linked list	$O(n)$	$O(n)$	$O(n)$
AVL tree	$O(\log n)$	$O(\log n)$	$O(\log n)$
Hash table*	$O(1)$	$O(1)$	$O(1)$

* average costs

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Set ADT

Counter ADT

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Dictionaries

A counter is a collection of items where
each distinct item has a count

Operations

Add: Add one to the count of an item

Get: Get the count of an item

Recap

Set ADT

Counter ADT

Assorted
ProblemsDemo: Python
Dictionaries

```
/** Creates a new empty counter */  
Counter CounterNew(void);  
  
/** Free memory used by counter */  
void CounterFree(Counter c);  
  
/** Add one to the count of an item */  
void CounterAdd(Counter c, int item);  
  
/** Get the count of an item */  
int CounterGet(Counter c, int item);
```

Recap

Set ADT

Counter ADT

Assorted
ProblemsDemo: Python
Dictionaries

Data Structure	Add	Get
Unordered array	$O(n)$	$O(n)$
Ordered array	$O(n)$	$O(\log n)$
AVL tree	$O(\log n)$	$O(\log n)$
Hash table	?	?

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Set ADT

Counter ADT

Assorted
ProblemsDemo: Python
Dictionaries

How to implement the Counter ADT using a hash table?

Use hash table to map **items** to their **counts**

Add

Look up item's count in the hash table
Then re-insert the item into the hash table
with count increased by 1

Get

Look up item's count in the hash table

Recap

Set ADT

Counter ADT

Assorted
ProblemsDemo: Python
Dictionaries

Data Structure	Add	Get
Unordered array	$O(n)$	$O(n)$
Ordered array	$O(n)$	$O(\log n)$
AVL tree	$O(\log n)$	$O(\log n)$
Hash table*	$O(1)$	$O(1)$

* average costs

Recap

Set ADT

Counter ADT

**Assorted
Problems**

Two sum

Odd occurring

Anagram

Demo: Python
Dictionaries

Hash tables are often used as sets or counters
to solve problems efficiently

Examples

Two sum

Odd occurring elements

Anagram

Recap

Set ADT

Counter ADT

Assorted
Problems

Two sum

Odd occurring

Anagram

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Problem

Given an array of integers and a target sum S , determine whether the array contains two integers that sum to S .

Examples

Consider the array $A = [12, 6, 3, 3, 7, 8]$

$\text{twoSum}(A, 13) \Rightarrow \text{true}$

$\text{twoSum}(A, 16) \Rightarrow \text{false}$

$\text{twoSum}(A, 3) \Rightarrow \text{false}$

$\text{twoSum}(A, 6) \Rightarrow \text{true}$

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Set ADT

Counter ADT

Assorted
Problems

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Dictionaries

Problem

Given an array of integers,
return the number of distinct integers that
occur an odd number of times.

Examples

`oddOccurring([4, 3, 4, 8, 8, 4])` \Rightarrow 2

`oddOccurring([7, 2, 1, 5, 6, 9])` \Rightarrow 6

`oddOccurring([1, 1, 3, 3, 7, 7])` \Rightarrow 0

Recap

Set ADT

Counter ADT

Assorted
Problems

Two sum

Odd occurring

Anagram

Demo: Python
Dictionaries

Problem

Given two strings s and t ,
determine whether they are anagrams.

Two strings are anagrams if they contain
the same amount of each character.

Examples

`anagram("abcde", "edcba")` \Rightarrow true

`anagram("abcde", "fdcba")` \Rightarrow false

`anagram("abcde", "abcdef")` \Rightarrow false

`anagram("aaabb", "ababa")` \Rightarrow true

`anagram("aaabb", "babab")` \Rightarrow false

Recap

Set ADT

Counter ADT

Assorted
Problems

Demo: Python
Dictionaries

Bonus content!

Python has built-in syntax for hash tables,
which are called **dictionaries**.

Recap

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Counter ADT

Assorted
ProblemsDemo: Python
Dictionaries

Operations

Create a dictionary

```
my_dictionary = {}
```

Insert a key-value pair

```
my_dictionary[key] = value
```

Check if a key exists

```
key in my_dictionary
```

Get the value associated with a key

```
my_dictionary[key]
```

Delete a key-value pair

```
del my_dictionary[key]
```