Analysis of the Given Grammar

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COLORS in this document

Black: for original rules in the grammar in Language Specification document

Red: specifies needs for modifications Green: rules do not require modification

Grammar:

The nonterminal cprogram> is the start symbol of the given grammar.

1. **rogram>** ===> <otherFunctions> <mainFunction>

FOLLOW(<otherFunctions>) = FIRST(<mainFunction>) = {TK_MAIN}

Note that all function definitions precede the main function definition and the language does not have constructs for function prototype declarations.

2. <mainFunction>===> TK_MAIN <stmts> TK_END

The LL(1) property for the nonterminal <mainFunction> is satisfied trivially due to single production for it.

 $FIRST(<mainFunction>) = FIRST(\alpha) = \{TK_MAIN\}$

where α represents the right hand side of the production i.e. TK_MAIN <stmts> TK_END.

3. <otherFunctions>===> <function><otherFunctions> | eps

The nonterminal <otherFunctions> need special care for verifying the LL(1) compatibility due to a nullable production. Let us first verify that the sets FIRST(<function><otherFunctions>) and FOLLOW<otherFunctions>) are disjoint.

FIRST(<function><otherFunctions>) = FIRST(<function>) = {TK_FUNID}

Note that <function> has no nullable production.

Also from 1, we have FOLLOW(<otherFunctions>) = {TK_MAIN} i.e.

 $FIRST(<function><otherFunctions) \cap FOLLOW(<otherFunctions>) = \emptyset$

The given productions for <otherFunctions> are LL(1) compatible.

NOTE: Other properties such as ambiguity, left recursiveness, left factoring needs etc. causing violation of LL(1) compatibility of the rules will be discussed only if one or more of them exist. Otherwise I am focusing on violations due to epsilon productions. Also I will highlight the introduction of new nonterminals to incorporate the precedence of arithmetic operators and handling operations on record variables.

- 4. <function>===>TK_FUNID <input_par> <output_par> TK_SEM <stmts> TK_END
 - This has no issue of violations in LL(1) compatibility due to epsilon productions. <input_par> is an essential construct to be part of the function definition while a function may or may not return values. Hence the <output_par> can have a syntax of (6).

FIRST(<function>) = {TK_FUNID}

5. <input_par>===>TK_INPUT TK_PARAMETER TK_LIST TK_SQL <parameter_list> TK_SQR

Single production having no conflict has its FIRST set as given follows:

FIRST(<input_par>) = {TK_INPUT}

6. <output_par>===>TK_OUTPUT TK_PARAMETER TK_LIST TK_SQL <parameter_list> TK_SQR | eps

Presence of epsilon production makes us verify whether FIRST(α) \cap FOLLOW(<output_par>) = ϕ or not, where α represents the right hand side TK_OUTPUT_TK_PARAMETER TK_LIST TK_SQL parameter_list> TK_SQR

 $FIRST(\alpha) = \{TK_OUTPUT\}$

Refer rule 4 to compute the FOLLOW(<output_par>) as below

FOLLOW(<output_par>) = {TK_SEM}

This implies that $FIRST(\alpha) \cap FOLLOW(\langle output_par \rangle) = \phi$

Hence the given rules for <output_par> conform to the LL(1) specifications.

The single production for <parameter_list> is trivially LL(1) compatible.

FIRST(<parameter_list>) = FIRST(<dataType>)

```
= FIRST(<primitiveDatatype> ) ∪ FIRST(<constructedDatatype>) = {TK_INT, TK_REAL, TK_RECORD}
```

8. <dataType>===> <primitiveDatatype> |<constructedDatatype>

$$FIRST() \cap FIRST() \\ = \{TK_INT, TK_REAL\} \cap \{TK_RECORD\} \\ = \phi$$

Since there is no nullable production for <dataType>, there is no need for computing FOLLOW(<dataType>).

$$FIRST(TK_INT) \cap FIRST(TK_REAL) = \{TK_INT\} \cap \{TK_REAL\} = \emptyset$$

Hence the rules for <pri>primitiveDataType> are LL(1) compatible.

FIRST(<primitiveDatatype>) = {TK_INT, TK_REAL}

10. <constructedDatatype>===>TK_RECORD TK_RECORDID

FIRST(<constructedDatatype>) = {TK_RECORD}

11. <remaining_list>===>TK_COMMA <parameter_list> | eps

There exist a nullable production for the non-terminal <remaining_list>. The RHS (right hand side) of the other production is such that the null string eps (epsilon) is not derivable from it.

Also

FIRST(TK_COMMA <parameter_list>) \cap FOLLOW(<remaining_list>) should be empty.

FIRST(TK_COMMA <parameter_list>) = {TK_COMMA}

and

Hence,

```
FIRST(TK\_COMMA < parameter\_list>) \cap FOLLOW(< remaining\_list>) \\ = \{TK\_COMMA\} \cap \{TK\_SQR\} \\ = \phi
```

Therefore both the given rules for the non-terminal <remaining_list> conform to LL(1) specifications.

12. <stmts>===><typeDefinitions> <declarations> <otherStmts><returnStmt>

The nonterminal <stmts> specifies the grammar for the body of the function. The ordering of other nonterminals such as <typeDefinictions> , <declarations> and <returnStmt> have fixed positions within the body of the function code.

There are no epsilon productions and a single non nullable production for <stmts> is LL(1) compatible.

 $FIRST(< stmts>) = FIRST(< typeDefinitions>) \\ \cup FIRST(< declarations>) \\ \cup FIRST(< otherStatements>) \\ \cup FIRST(< returnStmt>) \\ \dots \\ using 13, 18,21 \ and 42$

 $= \{ TK_RECORD \} \cup \{ TK_TYPE \} \cup \{ TK_ID, TK_RECORD_ID, TK_WHILE, TK_IF, TK_READ, TK_WRITE, TK_SQL, TK_CALL \} \cup \{ TK_RETURN \}$

={ TK_RECORD, TK_TYPE, TK_ID, TK_RECORD_ID, TK_WHILE, TK_IF, TK_READ, TK_WRITE, TK_SQL, TK_CALL, TK_RETURN} Since the nonterminal <stmts> does not have a nullable production, we need not compute FOLLOW(<stmts>) for populating the parsing table. Recall the construction of the parsing table. The columns corresponding to the tokens in FIRST(<stmts>) corresponding to the row<stmts> are populated with the rule number 12.

13. <typeDefinitions>===><typeDefinition><typeDefinitions> |eps

The first of the above productions is not nullable as $FIRST(<typeDefinition><typeDefinition>>) = FIRST(<typeDefinition>) = {TK_RECORD}.$ Also

FOLLOW(<typeDefinitions>) = FIRST(<declarations>) = FIRST(<declaration>) = {TK_TYPE} Next,

 $FIRST(<\!\!typeDefinitionS\!\!>) \cap FOLLOW(typeDefinitionS\!\!>)$

 $= \{TK_RECORD\} \cap \{TK_TYPE\} = \emptyset$

Hence the give two productions for the non terminal <typeDefinitions> conform to the LL(1) specifications.

```
FIRST(<typeDefinition>) = FIRST(<typeDefinition>) = \{TK\_RECORD\}
```

Recall the construction of the Predictive Parsing table.

The rule <typeDefinitions>===>eps is populated as the table entry T[<typeDefinitions>, TK_TYPE] and the rule <typeDefinitions>===><typeDefinition>>typeDefinitions> is populated as the table entry T[<typeDefinition>,TK_RECORD]

14. <typeDefinition>===>TK_RECORD TK_RECORDID <fieldDefinitions> TK_ENDRECORD TK_SEM

Here on, I am ignoring the check for LL(1) if the nonterminal has a single non nullable production.

FIRST(<typeDefinition>) = {TK_RECORD}

15. <fieldDefinitions>===> <fieldDefinition><fieldDefinition><moreFields>

As two consecutive occurrences of <fieldDefinition> are there at the RHS of the above production, this imposes a requirement of atleast two fields in a record. There can be one or more fields afterwrds. As the above rule is single and non nullable, it is LL(1) compatible.

FIRST(<fieldDefinitions>) = FIRST(<fieldDefinition>) = {TK_TYPE}

16. <fieldDefinition>===> TK_TYPE <primitiveDatatype> TK_COLON TK_FIELDID TK_SEM

FIRST(<fieldDefinition>) = {TK_TYPE}

17. <moreFields>===><fieldDefinition><moreFields> | eps

FOLLOW(<moreFields>) = $\phi \cup$ FOLLOW(<fieldDefinitions>) = {TK_ENDRECORD}

....using 15 & 14

 $FIRST(< field Definition >< more Fields >) \cap FOLLOW(< more Fields >)$

- $= \{TK_TYPE\} \cap \{TK_ENDRECORD\}$
- = (

Hence, the above two rules for the non terminal <moreFields> are LL(1) compatible.

```
18. <declarations> ===> <declaration><declarations>|eps
   FOLLOW(<declarations>)
                                        FIRST(<otherStmts>) ∪ FOLLOW(<otherStmts>)
                                 = { TK_ID, TK_RECORD_ID, TK_WHILE, TK_IF, TK_READ, TK_WRITE, TK_SQL, TK_CALL}
   FIRST(<declaration><declaration>) = FIRST(<declaration>) = {TK TYPE}
   We observe that both of the above sets are disjoint. Therefore both the above productions for the non terminal <declarations> conform to LL(1)
   specifications.
19. <declaration>===> TK_TYPE <dataType> TK_COLON TK_ID TK_COLON <global_or_not> TK_SEM
      This rule has a correction as follows
   <declaration>===> TK TYPE <dataType> TK COLON TK ID <global or not> TK SEM
   Also to incorporate the optional existence of global keyword prefixed with a colon is reflected as modification in rule 20.
   FIRST(<declaration>) = {TK TYPE}
      Rule conforms to LL(1) specifications.
20. <global_or_not>===>TK_GLOBAL| eps
      This rule is also modified as follows
   <global_or_not>===>TK_COLON TK_GLOBAL| eps
   FOLLOW(<global_or_not>) = {TK_SEM}
                                                                   .....using 19
   and
   FIRST(TK\_COLON\ TK\_GLOBAL) = \{TK\_COLON\}
   As
   FOLLOW(\langle global\_or\_not \rangle) \cap FIRST(TK\_COLON\ TK\_GLOBAL) = \{TK\_SEM\} \cap \{TK\_COLON\} = \emptyset
   Therefore the new rule for <global or not> is LL(1) compatible.
21. <otherStmts>===> <stmt><otherStmts> | eps
   FOLLOW(<otherStmts>) = FIRST(<returnStmts>)
   FIRST(<otherStmts>)
                          = FIRST(<stmt>)
                                                                                 [ Note: <stmt> does not derive an empty string]
```

```
= { TK_ID, TK_RECORDID, TK_WHILE, TK_IF, TK_READ, TK_WRITE, TK_SQL, TK_CALL} .....using 22
```

22. <stmt>===> <assignmentStmt> | <iterativeStmt> | <conditionalStmt> | <funCallStmt>

Referring rules 23, 28, 29, 31 and 25, we conclude that the five productions given above for the nonterminal <stmt> are not nullable.

We must check the LL(1) property that the FIRST sets of the RHSs of all productions above are disjoint.

 $FIRST(< assignmentStmt>) \cap FIRST(< identification Stmt>) \cap F$

$$= \{TK_ID, TK_RECORDID\} \cap \qquad \{TK_WHILE\} \cap \{TK_IF\} \cap \ \{TK_READ, TK_WRITE\} \cap \{TK_SQL, TK_CALL\} \\ = \emptyset$$

Hence, the above five productions for the nonterminal <stmt> conform to LL(1) specifications. and ,

FIRST(<stmt>) = {TK_ID, TK_RECORDID, TK_WHILE, TK_IF, TK_READ, TK_WRITE, TK_SQL, TK_CALL}

23. <assignmentStmt>===><SingleOrRecId> TK_ASSIGNOP <arithmeticExpression> TK_SEM FIRST(<assignmentStmt>) = FIRST(<singleOrRecId>) = {TK_ID, TK_RECORDID}

.....using 24

24. <singleOrRecId>===>TK_ID | TK_RECORDID TK_DOT TK_FIELDID

The token TK_RECORDID is replaced with TK_ID as the identifier of record type expands with dot followed by the name of the field and not the record identifier name. You should left factor the new grammar rule to make it LL(1) compatible.

```
<singleOrRecId>===>TK_ID | TK_ID TK_DOT TK_FIELDID
```

Both of the above productions for the nonterminal <singleOrRecId> are non nullable and their first sets are not disjoint. This requires left factoring The above two rules are left factored using new non terminal <new_24>

```
<singleOrRecId>===>TK_ID <new_24>
<new 24> ===> eps | TK DOT TK FIELDID
```

```
Therefore, the above productions are LL(1) compatible. Also FIRST(<singleOrRecId>) = {TK_ID}
```

The rule must have at its end TK_SEM to represent semicolon

$$FIRST(< funCallStmt>) = FIRST(< outputParameters>) \cup FOLLOW(< outputParameters>) \\ = \{TK_SQL\} \cup \{TK_CALL\} = \{TK_SQL, TK_CALL\}$$

The above rule conforms to LL(1) specifications.

26. <outputParameters> ==> TK_SQL <idList> TK_SQR TK_ASSIGNOP | eps

FOLLOW(<outputParameters>) = {TK_CALL}

Due to the presence of the nullable production for the non terminal <outputParameters>, we check the following LL(1) property

$$FIRST(TK_SQL < idList > TK_SQR \ TK_ASSIGNOP) \cap FOLLOW(< output Parameters >)$$

$$= \{TK_SQL\} \cap \{TK_CALL\} = \emptyset$$

Hence, the productions in 26 are LL(1) compatible.

FIRST(<outputParameters>) = {TK_SQL}

- 27. <inputParameters>===> TK_SQL <idList> TK_SQR
 - LL(1) compatible with FIRST(<inputParameters>) = {TK_SQL}
- $28. < iterativeStmt> = = > TK_WHILE \ TK_OP < booleanExpression> TK_CL < stmt> < otherStmts> TK_ENDWHILE < otherStmt> = > TK_WHILE < otherStmt> = > TK_WHILE < otherStmt> =$
 - LL(1) compatible with FIRST(<iterativeStmt>) = {TK_WHILE}
- 29. <conditionalStmt>===> TK_IF <booleanExpression> TK_THEN <stmt><otherStmts> TK_ELSE <otherStmts> TK_ENDIF
- 30. <conditionalStmt>===> TK_IF <booleanExpression> TK_THEN <stmt><otherStmts> TK_ENDIF

The two rules (29) and (30) for the nonterminal <conditionalStmt> need modifications as they originally form ambigous grammar. We need to perform the left factoring as follows

 $<\!\!conditionalStmt>===>TK_IF\ TK_OP<\!\!sooleanExpression>TK_CL\ TK_THEN<\!\!stmt><\!\!otherStmts><\!\!elsePart>$

.....number rule as 29

<elsePart>===>TK_ELSE <stmt><otherStmts> TK_ENDIF | TK_ENDIF

.....number rules as 30

Notice that I also added TK_OP and TK_CL in new rule 29 to enclose boolean expression . These two tokens were missing earlier.

Also I am putting a constraint of atleast one statement within else part.

Now there is a single rule for <conditionalStmt> which is non nullable and its first set is {TK_IF}

But the newly introduced nonterminal <elsePart> has two non nullable productions and their corrsponding FIRST sets are disjoint.

 $FIRST(TK_ELSE < otherStmts > TK_ENDIF) \cap FIRST(TK_ENDIF) = \{TK_ELSE\} \cap \{TK_ENDIF\} = \emptyset$

Therefore the new set of rules for <elsePart> is also LL(1) compatible.

And,

FIRST(<conditionalStmt>) = {TK_IF}

FIRST(<elsePart>) = {TK_ELSE, TK_ENDIF}

31. <ioStmt>===>TK_READ TK_OP <allVar> TK_CL TK_SEM | TK_WRITE TK_OP <allVar> TK_CL TK_SEM

This rule needs a minor modification. The identifier and record identifier are the only arguments of the read operation.

<ioStmt>===> TK_READ TK_OP <singleOrRecId> TK_CL TK_SEM

Also the write statement is not expected to take as argument a record id. Any number, real number, identifier or constructed record identifier can be the arguments of write statement.

<ioStmt> ===> TK_WRITE TK_OP <allVar> TK_CL TK_SEM

Both the above productions are non nullable.

and,

```
FIRST(TK\_READ\ TK\_OP < singleOrRecId > TK\_CL\ TK\_SEM\ ) \cap FIRST(TK\_WRITE\ TK\_OP < all\ Var>\ TK\_CL\ TK\_SEM) \\ = \{TK\_READ\} \cap \{TK\_WRITE\} = \emptyset
```

Therefore, the above productions are LL(1) compatible. and,

FIRST(<ioStmt>) = {TK_READ, TK_WRITE}

Notice that the arguments for a write may be a number, real number, id, or a constructed record id variable. A record identifier is not the argument of WRITE directly. This is relaxed here to simplify the code generation equivalent of printing all field values of the record type variable.

32. <allVar>===><var>| TK_RECORDID TK_DOT TK_FIELDID

Trivially, the two non nullable productions above conform to LL(1) and

```
FIRST(<allVar>) = FIRST(<var>) ∪ {TK_RECORDID}
= {TK_NUM, TK_RNUM, TK_ID, TK_RECORDID}
```

33. < arithmetic Expression > = = > < arithmetic Expression > < operator > < arithmetic Expression > < operator > < arithmetic Expression > < operator > < oper

I had left a major correction for you to do in the arithmetic expression grammar. You were required to impose precedence of operators and the operations on record variables.

34. <arithmeticExpression> ====>TK_OP <arithmeticExpression> TK_CL | <var>

A replacement of <var> with a new nonterminal <all> is required to incorporate the record addition and subtraction

```
<arithmeticExpression> ====>TK_OP <arithmeticExpression> TK_CL | <all>
```

```
where <all>===> TK_ID | TK_NUM | TK_RECORDID <temp> and <temp>===> eps | TK_DOT TK_FIELD
```

An arithmetic expression is expected to take as argument an identifier, statically available number, real number, a record identifier and a record id (constructed by expanding the name using dot with a field name)

Now we reformulate the rules 33, 34(a) and 35 to impose precedence.

[Note: I have given new numbers for referring to the rules, but you can have your own numbering scheme for the rules]

Now let us verify the rules A1-7 for the nonterminals <arithmeticExpression>, <term>, <factor>, <lowPrecedenceOperators>,

<highPrecedenceOperators>, <all> and <temp>

The rule A1 needs left recursion elimination and the new set of productions are obtained by introducing new nonterminal, say <expPrime>

<arithmeticExpression> ===> <term> <expPrime>

<expPrime> ===> <lowPrecedenceOperators> <term> <expPrime> | eps

Similarly rule A2 also needs left recursion elimination. The new set of productions are obtained by introducing new nonterminal, say, <termPrime>

<term>===> <factor> <termPrime>

<termPrime> ===> <highPrecedenceOperators><factor> <termPrime> | eps

Now we have two more nonterminals <expPrime> and <termPrime>. The complete set of non left recursive, unambigous arithmetic expression grammar then becomes with new numbers A1-A9.

- A1) <arithmeticExpression> ===> <term> <expPrime>
- A2) <expPrime> ===> <lowPrecedenceOperators> <term> <expPrime> | eps
- A3) <term>===> <factor> <termPrime>
- A4) <termPrime> ===> <highPrecedenceOperators><factor> <termPrime> | eps

```
<factor> ===> TK OP <arithmeticExpression> TK CL | <all>
A5)
          <highPrecedenceOperator>===> TK MUL | TK DIV
A6)
          <lowPrecedenceOperators> ===> TK_PLUS | TK_MINUS
A7)
A8)
          <all>===> TK_ID | TK_NUM | TK_RNUM | TK_RECORDID <temp>
A9)
          <temp>===> eps | TK_DOT TK_FIELDID
   Analysis of A1: As there is only single rule available for the nonterminal <arithmetic Expression>, we must see that is not nullable
   FIRST(<arithmeticExpression>) = FIRST(<term>) = FIRST(<factor>) = {TK ID, TK NUM, TK RNUM, TK RECORDIID, TK OP}
   There is no need to go further to check LL(1) compatibility. The grammar for <arithmeticExpression> is LL(1) compatible.
   Analysis of A2: One of the productions for the nonterminal <expPrime> is nullable.
   Let us verify FIRST(<lowPrecedenceOperators> <term> <expPrime>) and FOLLOW(<expPrime>) are disjoint.
   FIRST(<lowPrecedenceOperators> <term> <expPrime>) = FIRST(<lowPrecedenceOperators>)
                                                        = {TK PLUS, TK MINUS}
                                                                                                        .....using analysis of A7
   and.
   FOLLOW(<expPrime>)
                              = FOLLOW(<arithmeticExpression>)
                                                                                                        ....using A1
                              = \{TK\_SEM\}
                                                                                                        .....using 23
   This implies that
     FIRST(<lowPrecedenceOperators> <term> <expPrime>) \cap FOLLOW(<expPrime>)
   = {TK_PLUS, TK_MINUS}∩{TK_SEM}
   = \phi
   Therefore, A2 is also LL(1) compatible.
   Analysis of A3:
   As there is only single rule available for the nonterminal <term>, we must see that is not nullable
```

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FIRST(<term>)

```
= FIRST(<factor>)
      = {TK ID, TK NUM, TK RNUM, TK RECORDIID, TK OP}
                                                                                                          .....using analysis of A5
      There is no need to go further to check LL(1) compatibility. The grammar for <term> is LL(1) compatible.
      Analysis of A4:
      One of the productions for the nonterminal <termPrime> is nullable.
      Let us verify FIRST(<highPrecedenceOperators><factor> <termPrime>) and FOLLOW(<termPrime>) are disjoint.
      FIRST(<highPrecedenceOperators><factor> <termPrime>) = FIRST(<highPrecedenceOperators>)
                                                           ={ TK_MUL, TK_DIV}
                                                                                                   ....using analysis of A6
      And,
      FOLLOW(<termPrime>)
             = FOLLOW(<term>)
                                                                                                                ....using A3
             = FIRST(<expPrime>) ∪ FOLLOW(<expPrime>)
                                                                                                                ....using A2
             = FIRST(<lowPrecedenceOperators>) ∪ FOLLOW(<expPrime>)
                                                                                                                ....using A2
             = {TK_PLUS, TK_MINUS} ∪ FOLLOW(<expPrime>)
                                                                                                                ....using analysis of A7
             = {TK_PLUS, TK_MINUS} ∪ FOLLOW(<arithmeticExpression>)
                                                                                                                ....using A1
             = \{TK\_PLUS, TK\_MINUS\} \cup \{TK\_SEM\}
                                                                                                                ....using 23
             = {TK_PLUS, TK_MINUS, TK_SEM}
Therefore,
             FIRST(<highPrecedenceOperators><factor> <termPrime>) \cap FOLLOW(<termPrime>)
             \{ TK\_MUL, TK\_DIV \} \cap \{ TK\_PLUS, TK\_MINUS, TK\_SEM \}
      Hence the rules defined by A4 conform to LL(1) specifications.
```

```
Analysis of A5: There are two productions for the non terminal <factor>.
FIRST( TK OP <arithmeticExpression> TK CL) = {TK OP}
and,
FIRST(<all>) = {TK_ID, TK_NUM, TK_RNUM, TK_RECORDIID}
                                                                                                    ..... using analysis of A8
It is now obvious that no production for <factor> is a nullable production and,
FIRST( TK_OP < arithmetic Expression > TK_CL) \cap FIRST(<all>) = \phi
Therefore the grammar for <factor> is LL(1) compatible.
and,
FIRST(<factor>) =
                  {TK_ID, TK_NUM, TK_RNUM, TK_RECORDIID, TK_OP}
Analysis of A6: The two productions of the nonterminal <highPrecedenceOperators> are trivially LL(1) compatible
                    FIRST(<highPrecedenceOperators>) = { TK_MUL, TK_DIV}
Analysis of A7: The two productions of the nonterminal <lowPrecedenceOperators> are also trivially LL(1) compatible
                    FIRST(<lowPrecedenceOperators>) = { TK_PLUS, TK_MINUS}
Analysis of A8: The two productions of the nonterminal <all> are also trivially LL(1) compatible.
                    FIRST(<all>) = { TK NUM, TK RNUM, TK ID, TK RECORDID}
Analysis of A9: There is an epsilon production for the nonterminal <temp> and it is essential to check that
FIRST(TK_DOT TK_FIELDID) ∩ FOLLOW(<temp>) is empty.
Now computing FOLLOW(<temp>),
        FOLLOW(<temp>)
      = FOLLOW(<all>)
                                                                                                          ....using A8
      = FOLLOW(<factor>)
                                                                                                          ....using A5
      = FIRST(<termPrime>)∪ FOLLOW(<termPrime>)
                                                                                                          ....using A4
      = FIRST(<highPrecedenceOperators>) ∪ FOLLOW(<termPrime>)
                                                                                                          ....using A4
      = {TK_MUL, TK_DIV} ∪ FOLLOW(<termPrime>)
                                                                                                          ....using analysis of A6
```

```
= {TK_MUL, TK_DIV} ∪ FOLLOW(<term>) .....using A3

= {TK_MUL, TK_DIV} ∪ FIRST(<expPrime>) ∪ FOLLOW(<expPrime>) .....using A2

= {TK_MUL, TK_DIV} ∪ FIRST(<lowPrecedenceOperators>) ∪ FOLLOW(<expPrime>) .....using A2

= {TK_MUL, TK_DIV} ∪ {TK_PLUS, TK_MINUS} ∪ FOLLOW(<expPrime>) .....using analysis of A7

= {TK_MUL, TK_DIV} ∪ {TK_PLUS, TK_MINUS} ∪ FOLLOW(<arithmeticExpression>) ....using A1

= {TK_MUL, TK_DIV} ∪ {TK_PLUS, TK_MINUS} ∪ {TK_SEM} ....using 23

= {TK_MUL, TK_DIV, TK_PLUS, TK_MINUS, TK_SEM}
```

Therefore,

This proves that the rules defined in A9 are LL(1) compatible. [I again insist that I am avoiding proving every rule to be unambiguous. This is left to be proved by you.]

- 35. <operator> ===> TK_PLUS | TK_MUL | TK_MINUS | TK_DIV This rule is discarded now.
- 36. <booleanExpression>===>TK_OP <booleanExpression> TK_CL <logicalOp> TK_OP <booleanExpression> TK_CL FIRST(TK_OP <booleanExpression> TK_CL <logicalOp> TK_OP <booleanExpression> TK_CL) = { TK_OP} and the production is not nullable.
- 37. <booleanExpression>===> <var> <relationalOp> <var> FIRST(<var> <relationalOp> <var>) = FIRST(<var>) = {TK_ID, TK_NUM, TK_RNUM} and the production is not nullable.

38. <booleanExpression>===> TK_NOT <booleanExpression>

Considering the above rules 36-38 for analysis, we observe that none of the three productions for the nonterminal <booleanExpression> is nullable (using First set of <var> from 39)

and, The first sets of the right hand sides of the three productions are disjoint.

FIRST(TK_OP <booleanExpression> TK_CL <logicalOp> TK_OP <booleanExpression> TK_CL)

- $= \{TK_OP\} \cap \{TK_ID, TK_NUM, TK_RNUM\} \cap \{TK_NOT\}$
- = **\phi**

Hence, the three productions for the nonterminal <booleanExpression> are LL(1) compatible.

39. <var>===> TK_ID | TK_NUM | TK_RNUM

Trivially the three non nullable productions above for the non terminal <var> are LL(1) compatible. and,

FIRST(<var>) = {TK_ID, TK_NUM, TK_RNUM}

40. <logicalOp>===>TK_AND | TK_OR

I have not defined the precedence of AND over OR or vice versa. We have the support to enclose the boolean expression in parentheses.

Trivially the productions for <logicalOp> conform to LL(1) specifications

41. <relationalOp>===> TK_LT | TK_LE | TK_EQ | TK_GT | TK_GE | TK_NE

All six productions above for the nonterminal <relationalOp> are trivially LL(1) compatible and

FIRST(<relationalOp>) = { TK_LT, TK_LE, TK_EQ, TK_GT, TK_GE, TK_NE}

42. <returnStmt>===>TK_RETURN <optionalReturn> TK_SEM

FIRST(<returnStmt>) = {TK_RETURN}

and the production is not nullable, hence the rule is LL(1) compatible.

43. <optionalReturn>===>TK_SQL <idList> TK_SQR | eps

```
and,
   FOLLOW(<optionalReturn>) = {TK_SEM}
                                                            ....using 42
   Since both of the above sets are disjoint, the grammar for the nonterminal <optionalReturn> is LL(1) compatible.
44. <idList>===> TK_ID <more_ids>
   FIRST(<idList>) = {TK_ID} and the production is not nullable, hence the rule is LL(1) compatible.
45. <more_ids>===> TK_COMMA <idList> | eps
   FIRST(TK_COMMA <idList>) = {TK_COMMA}
   and,
   FOLLOW(<more_ids>) = FOLLOW(<idList>)
                                                                                        .....using 44
                           = \{TK\_SQR\}
                                                                                        .....using 43
   This implies that
      FIRST(TK_COMMA <idList>) ∩ FOLLOW(<more_ids>)
      = \{TK\_COMMA\} \cap \{TK\_SQR\}
      = \phi
   Therefore, the rules for the nonterminal <more_ids> are LL(1) conformable.
```

FIRST(TK_SQL <idList> TK_SQR) = { TK_SQL}

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