

COMP 478 DD

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Assignment 1

Theoretical Questions

1)

Transform is Cumulative Distribution Function: $s = T(r) = (L - 1) \int_0^r p_r(\omega) d\omega$

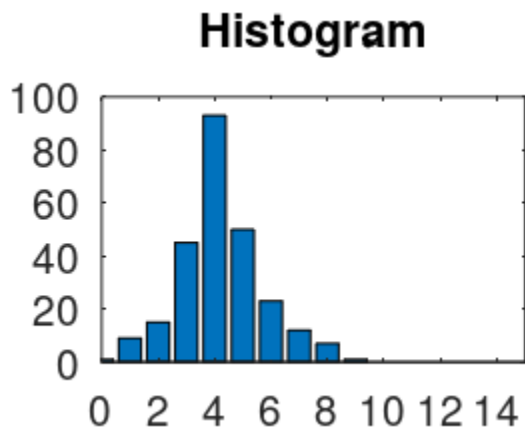
CDF of r:

$$\begin{aligned} T(r) &= \int_0^r -2t + 2 dt \\ &= [-t^2 + 2t] \text{ from } 0 \text{ to } r \\ &= -r^2 + 2r \end{aligned}$$

The transformation from r to z:

$$z = T(r) = -r^2 + 2r$$

2.a)



2.b)

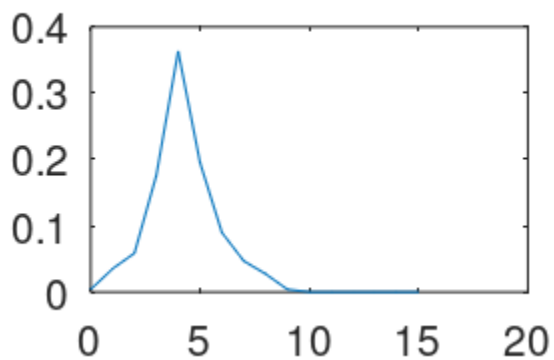
n = 256, L = 15

i)

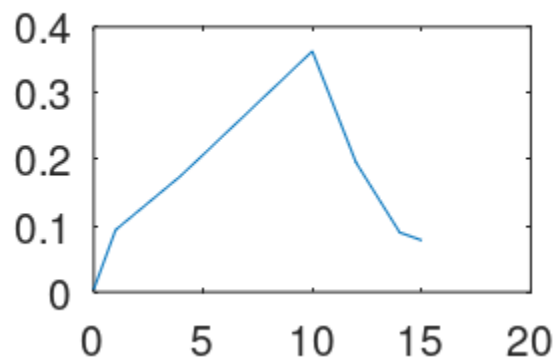
r_k (grey levels)	# of pixels (n_k)	$p_r(r_k) = n_k/n$	$s_k = (L-1) \sum_{j=0}^k \frac{n_j}{n}$	s_k (grey levels integers)	n_{s_k}	$p_s(s_k)$
0	1	0.00390625	0.05859375	0	1	0.00390625
1	9	0.03515625	0.5859375	1		
2	15	0.05859375	1.46484375	1	24	0.09375
3	45	0.17578125	4.1015625	4	45	0.17578125
4	93	0.36328125	9.55078125	10	93	0.36328125
5	50	0.1953125	12.48046875	12	50	0.1953125
6	23	0.08984375	13.828125	14	23	0.08984375
7	12	0.046875	14.53125	15		
8	7	0.02734375	14.94140625	15		
9	1	0.00390625	15	15		
10	0	0	15	15		
11	0	0	15	15		
12	0	0	15	15		
13	0	0	15	15		
14	0	0	15	15		
15	0	0	15	15	20	0.078125

ii)

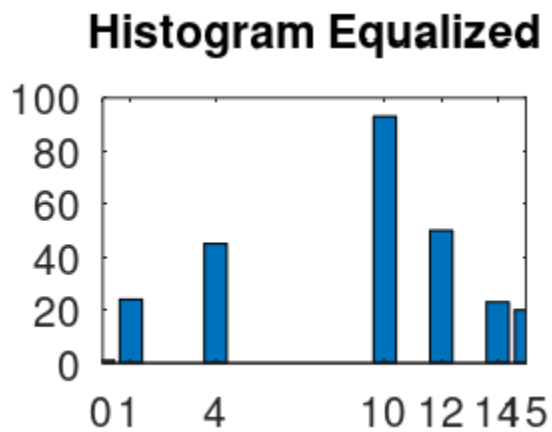
pr(rk)



ps(sk)



2.c)



3)

By performing the arithmetic operation $f(x,y) - g(x,y)$ the resulting image will lower pixel intensity by c , so it will be darker. The histogram of $f(x,y) - g(x,y)$ will shift to the left by c units, but it will still maintain its shape as the number of pixels will remain the same but will have lower values. Any pixels with value of c or lower will be cut from the histogram because they will have negative values.

4)

Convert image to binary:

0000	0001	1000	0110
0010	0010	0001	0001
0001	1111	1110	1100
0011	0110	1001	1010

Bit Planes:

0	0	1	0
0	0	0	0
0	1	1	1
0	0	1	1

0	0	0	1
0	0	0	0
0	1	1	1
0	1	0	0

0	0	0	1
1	1	0	0
0	1	1	0
1	1	0	1

0	1	0	0
0	0	1	1
1	1	0	0
1	0	1	0

Programming Questions

```
pkg load image
pkg load statistics
```

```
%% Question 1
```

```
% Read the images
```

```
brain_mri = imread('brain-mri.png');
landscape = imread('landscape.png');
```

```
%% Question 2
```

```
% Calculate histograms
```

```
H1 = zeros(1, 256);
for i = 1:length(H1)
    H1(i) = sum(sum(brain_mri == i - 1));
endfor
```

```
subplot(2,2,1);
plot(H1);
title('brain-mri');
```

```
H2 = zeros(1, 256);
for i = 1:length(H2)
    H2(i) = sum(sum(landscape == i - 1));
endfor
```

```
subplot(2,2,2);
plot(H2);
title('landscape');
```

```
%% Question 3
```

```
% Calculate histograms using imhist
```

```
histo_brain_mri = imhist(brain_mri);
histo_landscape = imhist(landscape);
```

```
subplot(2,2,3);
plot(histo_brain_mri);
title('brain-mri (imhist)');
```

```
subplot(2,2,4);
plot(histo_landscape);
title('landscape (imhist)');
```

```
% The histograms used by my program look similar to the ones using imhist
```

```
%% Question 4
% Calculate cumulative distribution function
cdf = cumsum(H1 / sum(H1));
% Perform equalization
equalized1 = cdf(double(brain_mri)+1);
% Round
equalized1 = uint8(equalized1 * 255);
```

```
cdf = cumsum(H2 / sum(H2));
equalized2 = cdf(double(landscape)+1);
equalized2 = uint8(equalized2 * 255);
```

```
figure;
subplot(2,2,1);
imshow(equalized1);
title('brain-mri');
```

```
subplot(2,2,2);
imshow(equalized2);
title('landscape');
```

```
%% Question 5
% Histo Equalization using histeq
hist_eq_brain_mri = histeq(brain_mri);
hist_eq_landscape = histeq(landscape);
```

```
subplot(2,2,3);
imshow(hist_eq_brain_mri);
title('brain-mri (histeq)');
```

```
subplot(2,2,4);
imshow(hist_eq_landscape);
title('landscape (histeq)');
```

```
% The histogram-equalized images obtained using my program look similar to histeq
```

