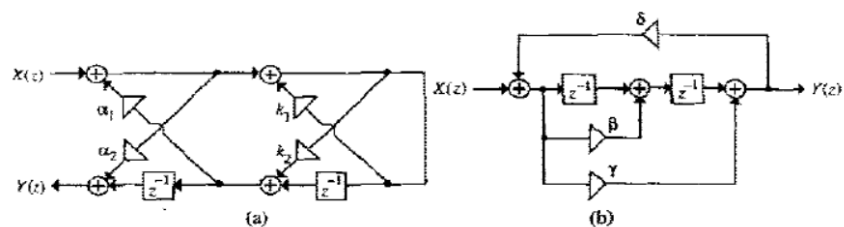


# 1 SU1

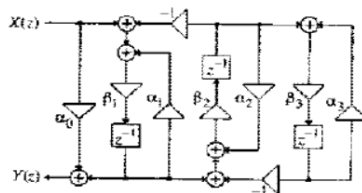
- |       |        |        |        |        |
|-------|--------|--------|--------|--------|
| • 6.2 | • 6.18 | • 6.40 | • 6.59 | • 6.75 |
| • 6.7 | • 6.24 | • 6.53 | • 6.60 |        |
| • 6.8 | • 6.27 | • 6.57 | • 6.70 | • 6.79 |
| • 6.9 | • 6.36 | • 6.58 | • 6.72 | • 6.84 |

**6.2** Determine by inspection whether or not the digital filter structures in Figure P6.2 have delay-free loops. Identify these loops if they exist. Develop equivalent structures without delay-free loops.



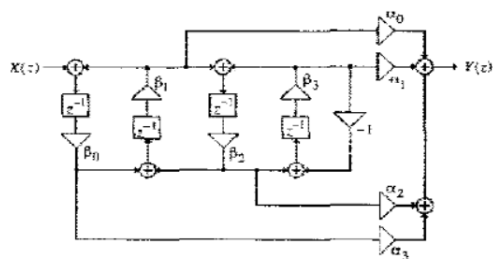
**Figure P6.2**

6.7 By using the block diagram analysis approach, determine the transfer function  $H(z) = Y(z)/X(z)$  of the digital filter structure of Figure P6.6.



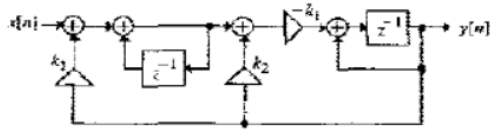
**Figure P6.6**

6.8 By using the block diagram analysis approach, determine the transfer function  $H(z) = Y(z)/X(z)$  of the digital filter structure of Figure P6.7.



**Figure P6.7**

**6.9** Determine the transfer function of the digital filter structure of Figure P6.8 [Kin72].



**Figure P6.8**

**6.18** Show that a Type 1 linear-phase FIR transfer function  $H(z)$  of length  $2M + 1$  can be expressed as

$$H(z) = z^{-M} \left[ h[M] + \sum_{n=1}^M h[M-n] (z^n + z^{-n}) \right]. \quad (6.130)$$

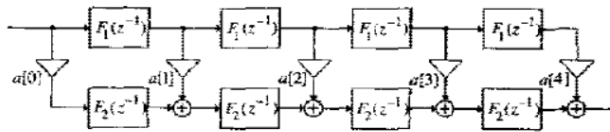
By using the relation

$$z^t + z^{-t} = 2T_t\left(\frac{z + z^{-1}}{2}\right).$$

where  $T_\ell(x)$  is the  $\ell$ th-order Chebyshev polynomial<sup>10</sup> in  $x$ , express  $H(z)$  in the form

$$H(z) = z^{-M} \sum_{n=0}^M a[n] \left( \frac{z + z^{-1}}{2} \right)^n. \quad (6.131)$$

Determine the relation between  $a[n]$  and  $h[n]$ . Develop a realization of  $H(z)$  based on Eq. (6.131) in the form of Figure P6.9, where  $F_1(z^{-1})$  and  $F_2(z^{-1})$  are causal structures. Determine the form of  $F_1(z^{-1})$  and  $F_2(z^{-1})$ . The structure of Figure P6.9 is called the *Taylor structure* for linear-phase FIR filters [Sch72].



**Figure P6.9** The Taylor structure shown for  $M = 4$ .

## 2 SU2

- |        |        |        |        |        |
|--------|--------|--------|--------|--------|
| • 7.5  | • 7.23 | • 7.34 | • 7.47 | • 7.80 |
| • 7.6  | • 7.26 | • 7.39 | • 7.49 |        |
| • 7.12 | • 7.27 | • 7.40 | • 7.57 | • 7.83 |
| • 7.20 | • 7.30 | • 7.41 | • 7.60 |        |
| • 7.22 | • 7.33 | • 7.42 | • 7.62 | • 7.92 |

### 3 SU3

- 8.1            • 8.6            • 8.14            • 8.18            • 8.25  
 • 8.5            • 8.13            • 8.17            • 8.24            • 8.26

- 8.28
- 8.31
- 8.37
- 8.50
- 8.52
- 8.60

## 4 SU4

- 9.1
- 9.2
- 9.4
- 9.9
- 9.11
- 9.20
- 9.27
- 9.29
- 9.33

## 5 SU5

- 10.1
- 10.2
- 10.3
- 10.5
- 10.8
- 10.17