



Hao Ren &lt;renhao.szu@gmail.com&gt;

**(无主题)**

Hao Ren <renhao.szu@gmail.com>  
草稿

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MRL's paper is confusing, it's better to read the source code.

There is a new output we want to make a "range proof".

$$C = aG + 10H$$

10 is the amount,  $a$  is the secret key.  $G$  and  $H$  are different base point.

We split it in four, we get:

$$C_0 = a_0G + 0 \times 1H$$

$$C_1 = a_1G + 1 \times 2H$$

$$C_2 = a_2G + 0 \times 4H$$

$$C_3 = a_3G + 1 \times 8H$$

because  $2 + 8 = 10$ .  $a_i$  is random.

For the first line, we get  $(C_0, C_0 - 1 \times 1H)$  these two points.

We know:

1. The first point's secret key is  $a_0$ .
2. We can't compute the second point's secret key.
3. The difference between the tow points is  $1H$ .

We sign a ring signature on these two points, a ring contains only two points.

$$L_0 = \alpha G$$

$\alpha$  is random.

$$q_1 = H(L_0)$$

$H()$  is a hash function to covert a point to scalar.

$$L_1 = s_1G + q_1P_1$$

$s_1$  is random,  $P_1$  is the second point.

$$q_0 = H(L_1)$$

$$s_0 = \alpha - q_0a_0 \text{ since } L_0 = \alpha G = s_0G + q_0P_0 = (\alpha G - q_0a_0)G + q_0P_0$$

It's easy to verify this signature because:

$$L_0 + L_1 = (s_0 + s_1)G + (q_0 + q_1)H$$

The second line is similar but we should change the order of  $(P_0, P_1)$  because we only know the second point's secret key.

At last we make four range proof.

In practice, the code is a little different for space-saving.