

7.1e) $H(z) = \frac{z - p^{-1}}{z - p}$ represents an all pass filter.

$H(z) = \frac{z}{z - p}$, if p is +ve, it is high pass.
if p is -ve, it is low pass.

7.1d) Two diff. impulse responses are possible.
One is causal & another is non-causal.
The one which is generated is causal.

7.2 a) $H(z) = \frac{z}{z^2 - (2r \cos \theta)z + r^2}$

zeros = 0

poles: $z^2 - (2r \cos \theta)z + r^2 = 0$

$$\frac{2r \cos \theta \pm \sqrt{4r^2 \cos^2 \theta - 4r^2}}{2}$$

$$= r \cos \theta \pm j r \sin \theta$$

$$7.3 a) y[n] = 2.5 y[n-1] - y[n-2] + x[n] - 5x[n-1] + 6x[n-2]$$

Applying z-transform

$$z(Y[n-p]) = \sum_{n=-\infty}^{\infty} y[n-p] z^{-n}$$

$$= z^{-p} \sum y[n-p] z^{-(n-p)}$$

$$= z^{-p} Y(z)$$

$$Y(z) = 2.5 z^{-1} Y(z) - Y(z) z^{-1} + X(z) - 5 z^{-1} X(z) + 6 z^{-2} X(z)$$

$$Y(1 - 2.5 z^{-1} + z^{-2}) = X(1 - 5 z^{-1} + 6 z^{-2})$$

$$\frac{Y}{X} = H = \frac{1 - 5z^{-1} + 6z^{-2}}{1 - 2.5z^{-1} + z^{-2}}$$

Poles: $z = 2, z = \frac{1}{2}$

Zeros: $z = 2, z = 3$

$$H = \frac{(1 - 2z^{-1})(1 - 3z^{-1})}{(1 - 2z^{-1})(1 - \frac{1}{2}z^{-1})} = \frac{1 - 3z^{-1}}{1 - \frac{z^{-1}}{2}}$$

$$\frac{Y}{X} = \frac{1 - 3z^{-1}}{1 - \frac{z^{-1}}{2}}$$

$$Y(1 - \frac{z^{-1}}{2}) = X(1 - 3z^{-1})$$

7.3 b)

Applying inverse

$$y[n] - \frac{y[n-1]}{2} = x[n] - 3x[n-1]$$

This is the reduced eqⁿ because of concatenation.

$$H = \frac{1 - 3z^{-1}}{1 - \frac{z^{-1}}{2}}$$

$$7.3c) H(z) = \frac{1}{1 - \frac{z^{-1}}{2}} - \frac{3z^{-1}}{1 - \frac{z^{-1}}{2}}$$

Inverse of this

$$h[n] = \left(\frac{1}{2}\right)^n u[n] - 3 \left(\frac{1}{2}\right)^{n-1} u[n-1]$$

This is a Causal system