

# Diarization of overlapping speech: Methods and ensembles

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**ISCA SIG-ML Seminar**  
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# Overview

- A brief **background in diarization**:
  - The task and its applications
  - A traditional solution, and the problem of overlapping speech
- **Methods**:
  - Overlap-aware clustering
  - Separate then diarize
- **Ensemble**: An approach for combining overlap-aware diarization systems

# Background

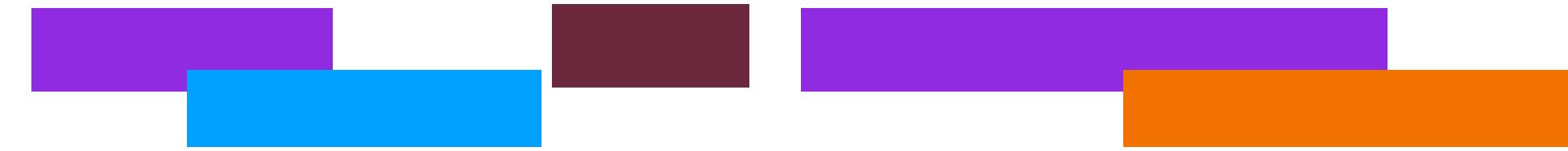
## What is speaker diarization?

# Task of “who spoke when”

# **Input: recording containing multiple speakers**



# **Output: *homogeneous speaker segments***



Xavier Anguera Miro et al., “Speaker diarization: A review of recent research,” IEEE Transactions on Audio, Speech, and Language Processing, 2012.

# Background

## Applications of Diarization



Psychotherapy and human interaction



Child language acquisition



Collaborative learning



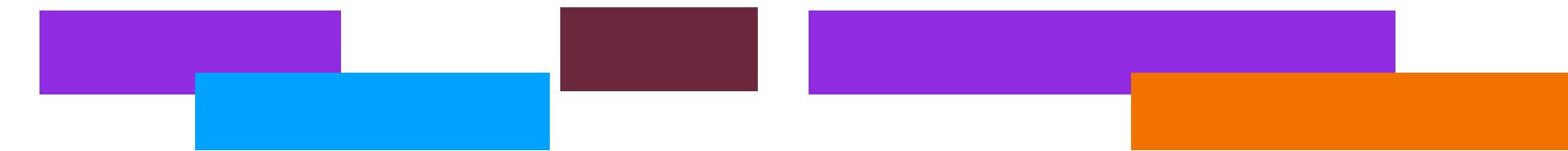
Meeting transcription



Cocktail party problem

# Background

## What makes Diarization difficult?



**Input: recording containing multiple speakers**

**Output: homogeneous speaker segments**

1. The recording may be very long with arbitrary silences/noise.
2. Number of speakers may be unknown.
3. Overlapping speech may be present.

**Example from CHiME-6 challenge  
(best system achieved >30% error rate)**

# The traditional solution

## “Clustering-based” systems

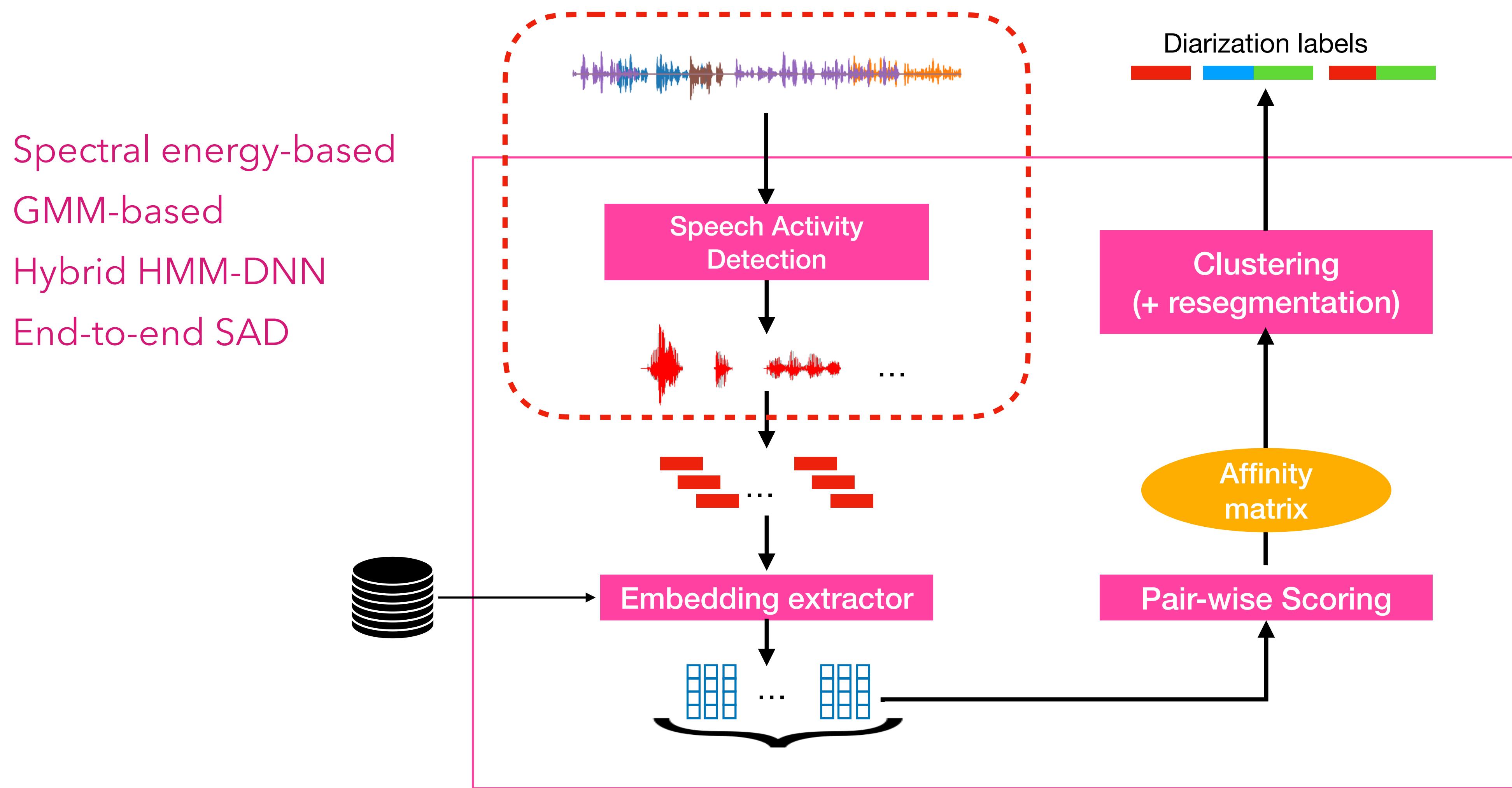
- **Key idea:** formulate Diarization as a clustering problem
- Cluster small segments of audio
- Each cluster represents a distinct speaker

Basu, J., Khan, S., Roy, R., Pal, M., Basu, T., Bepari, M.S., & Basu, T.K. (2016). An overview of speaker diarization: Approaches, resources and challenges.

Tranter, S., & Reynolds, D. (2006). An overview of automatic speaker diarization systems. *IEEE Transactions on Audio, Speech, and Language Processing*.

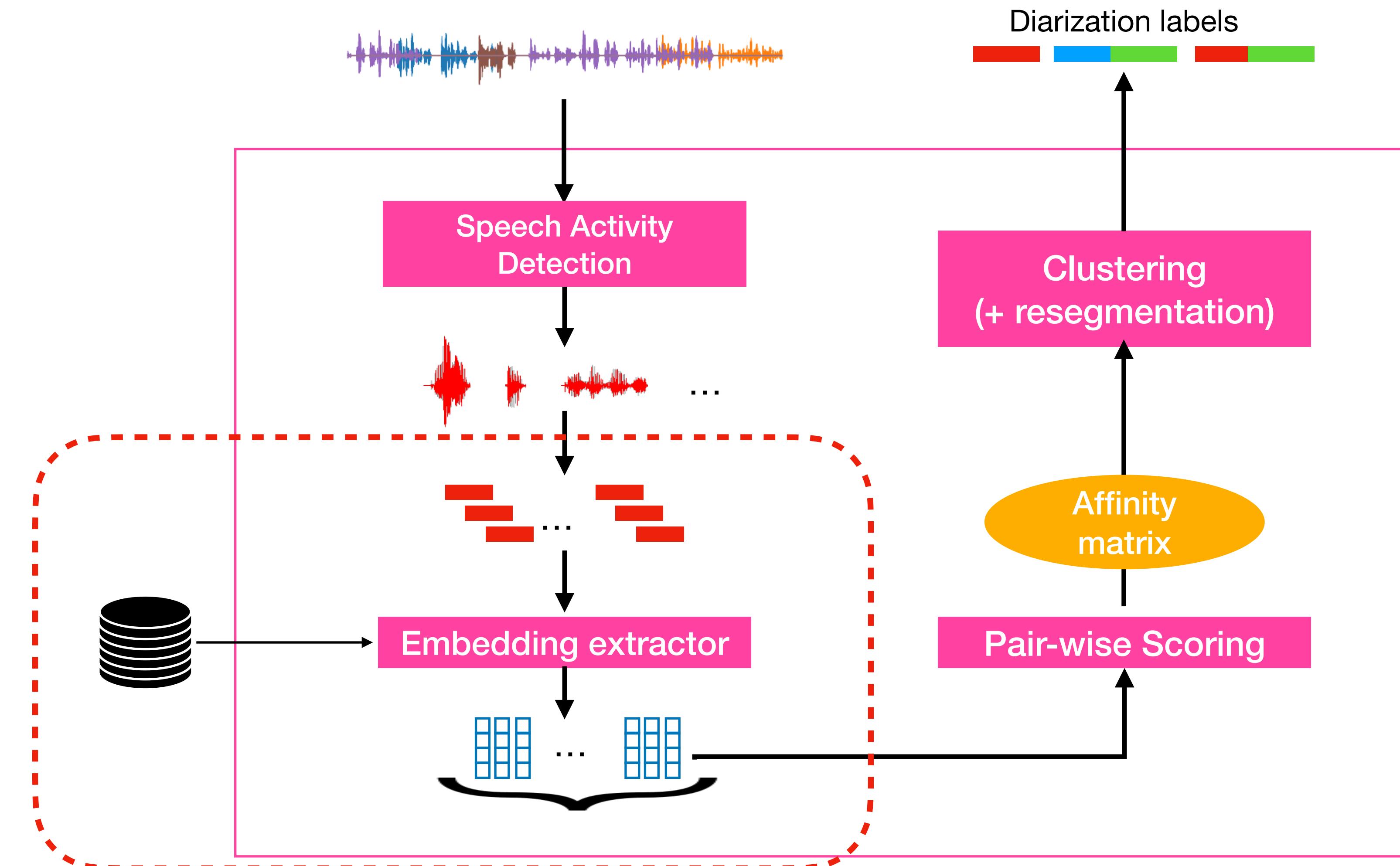
# Clustering-based diarization

SAD extracts speech segments from recordings



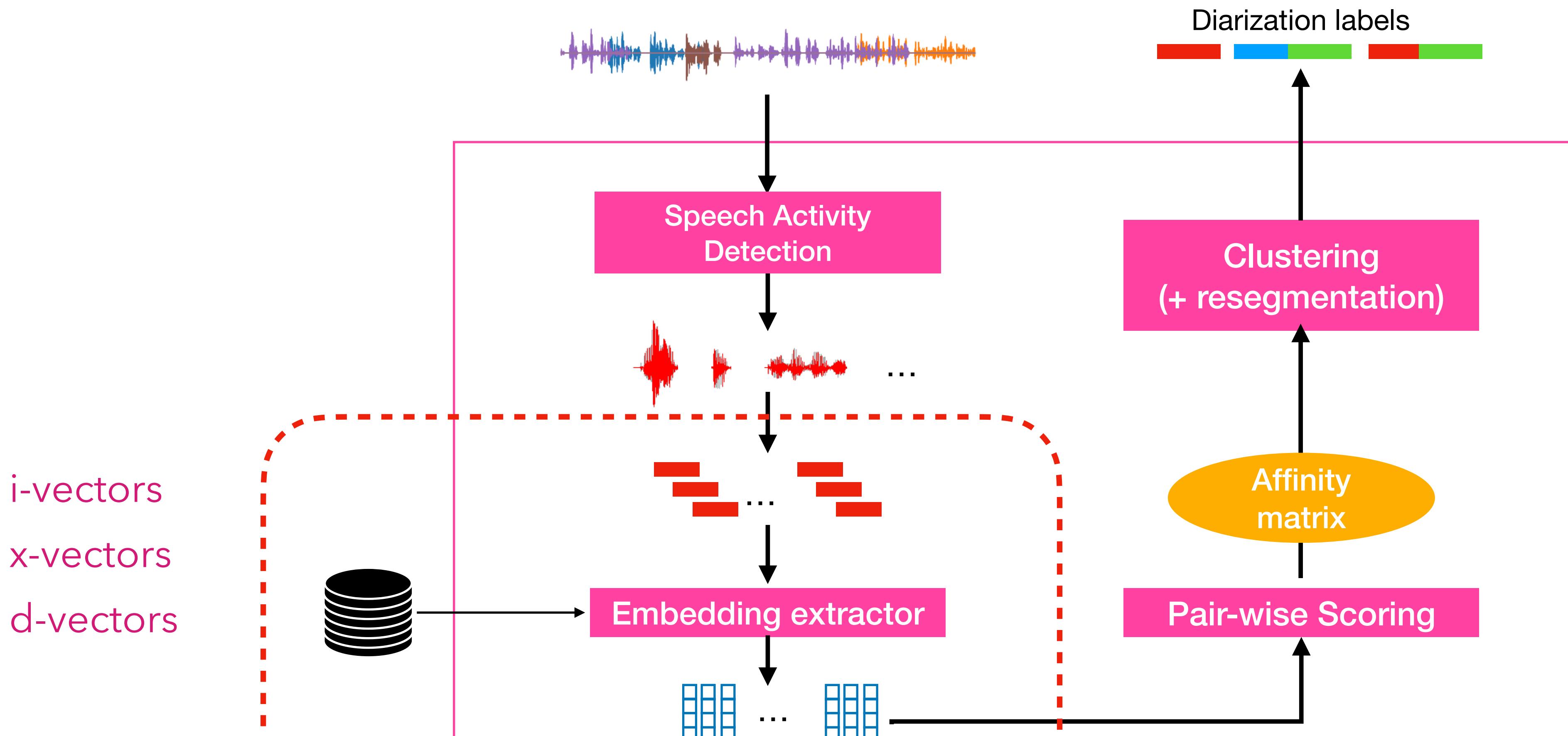
# Clustering-based diarization

Embeddings extracted for small subsegments



# Clustering-based diarization

## Embeddings extracted for small subsegments



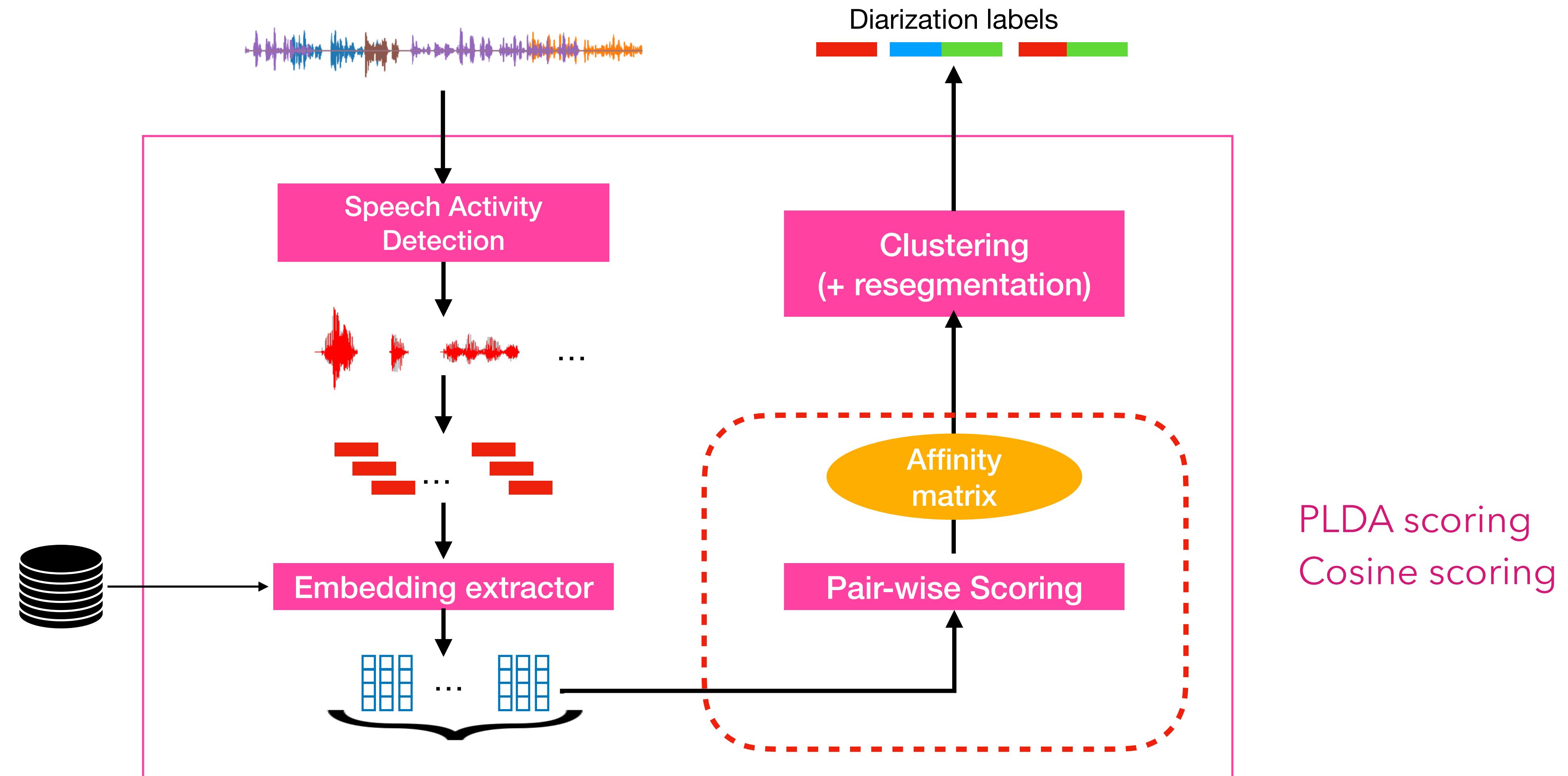
Dehak, N., et al (2011). Front-End Factor Analysis for Speaker Verification. *IEEE Transactions on Audio, Speech, and Language Processing*.

Snyder, D., et al. (2018). X-Vectors: Robust DNN Embeddings for Speaker Recognition. 2018 IEEE ICASSP.

Variani, E., et al. (2014). Deep neural networks for small footprint text-dependent speaker verification. 2014 IEEE ICASSP.

# Clustering-based diarization

## Pair-wise scoring of subsegments



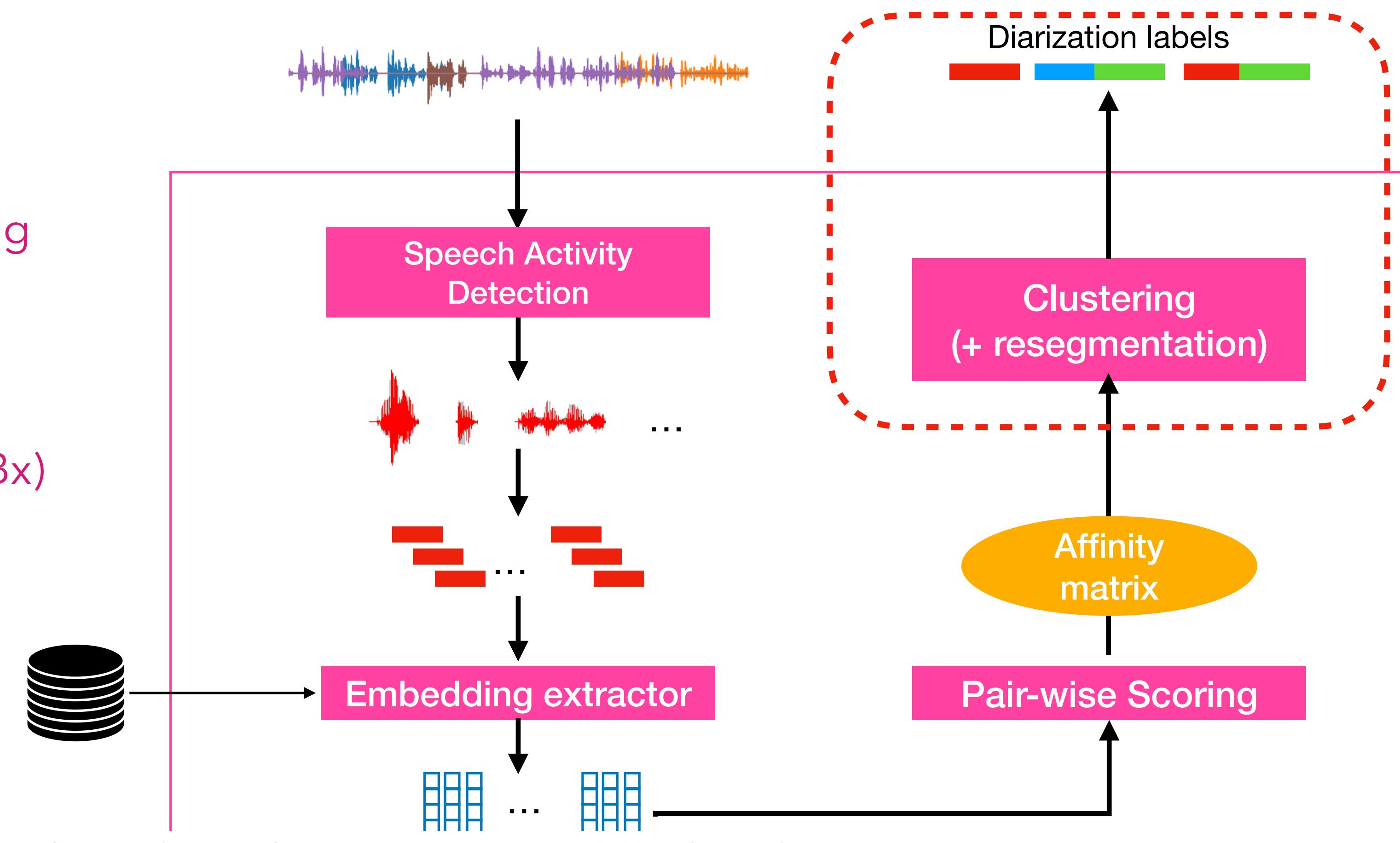
# Clustering-based diarization

Clustering based on the affinity matrix, followed by optional resegmentation

Agglomerative  
hierarchical clustering

Spectral clustering

Variational Bayes (VBx)



Daniel Garcia-Romero, David Snyder, Gregory Sell, Daniel Povey, and Alan McCree, "Speaker diarization using deep neural network embeddings," ICASSP 2017.  
Mireia Díez, Lukas Burget, and Pavel Matejka, "Speaker diarization based on Bayesian HMM with eigenvoice priors," Odyssey 2018.

# Clustering-based diarization

## How well does it perform?

- **Winning system in DIHARD I (2018) and II (2019)**
- DIHARD contains “hard” Diarization evaluation with recordings from several domains
- But **Diarization error rates (DER) still high**: 37% in DIHARD I and 27% in DIHARD II

$$\text{DER} = \frac{\text{Missed speech} + \text{False alarm} + \text{Speaker error}}{\text{Total speaking time}}$$

Sell, G., et al. (2018). Diarization is Hard: Some Experiences and Lessons Learned for the JHU Team in the Inaugural DIHARD Challenge. *INTERSPEECH 2018*.

Landini, F., et al. (2020). BUT System for the Second Dihard Speech Diarization Challenge. *IEEE ICASSP 2020*.

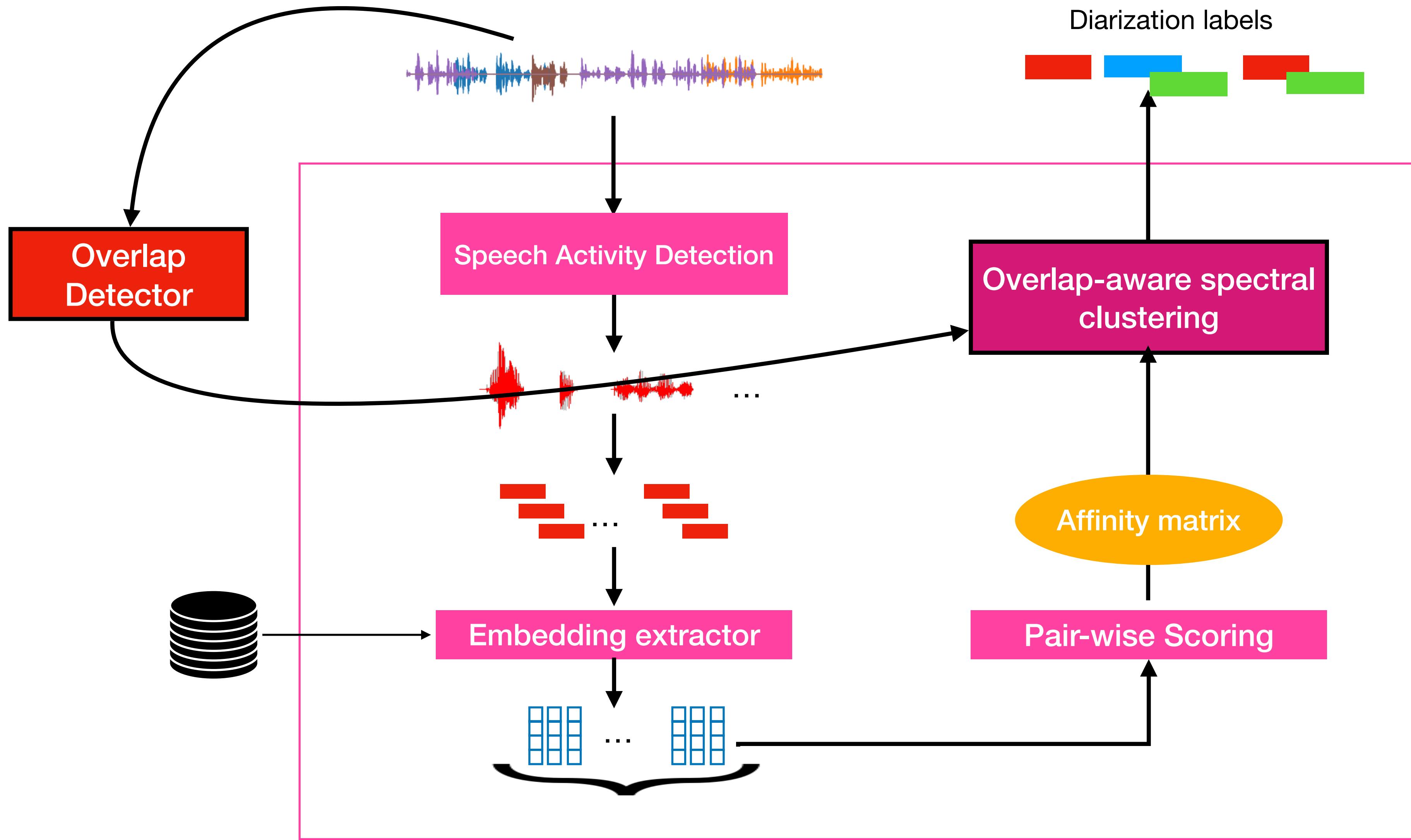
# Clustering paradigm assumes single-speaker segments

So overlapping speakers are completely ignored!

"Roughly 8% of the absolute error in our systems was from overlapping speech ... it will likely require a complete rethinking of the diarization process ... This is an important direction, but could not be addressed ..." - JHU team (2018)

"Given the current performance of the systems, the overlapped speech gains more relevance ... more than 50% of the DER in our best systems ... has to be addressed in the future ..." - BUT team (2019)

# Overlap-aware spectral clustering



Raj, D., Huang, Z., & Khudanpur, S. (2021). Multi-class Spectral Clustering with Overlaps for Speaker Diarization. *IEEE SLT 2021*.

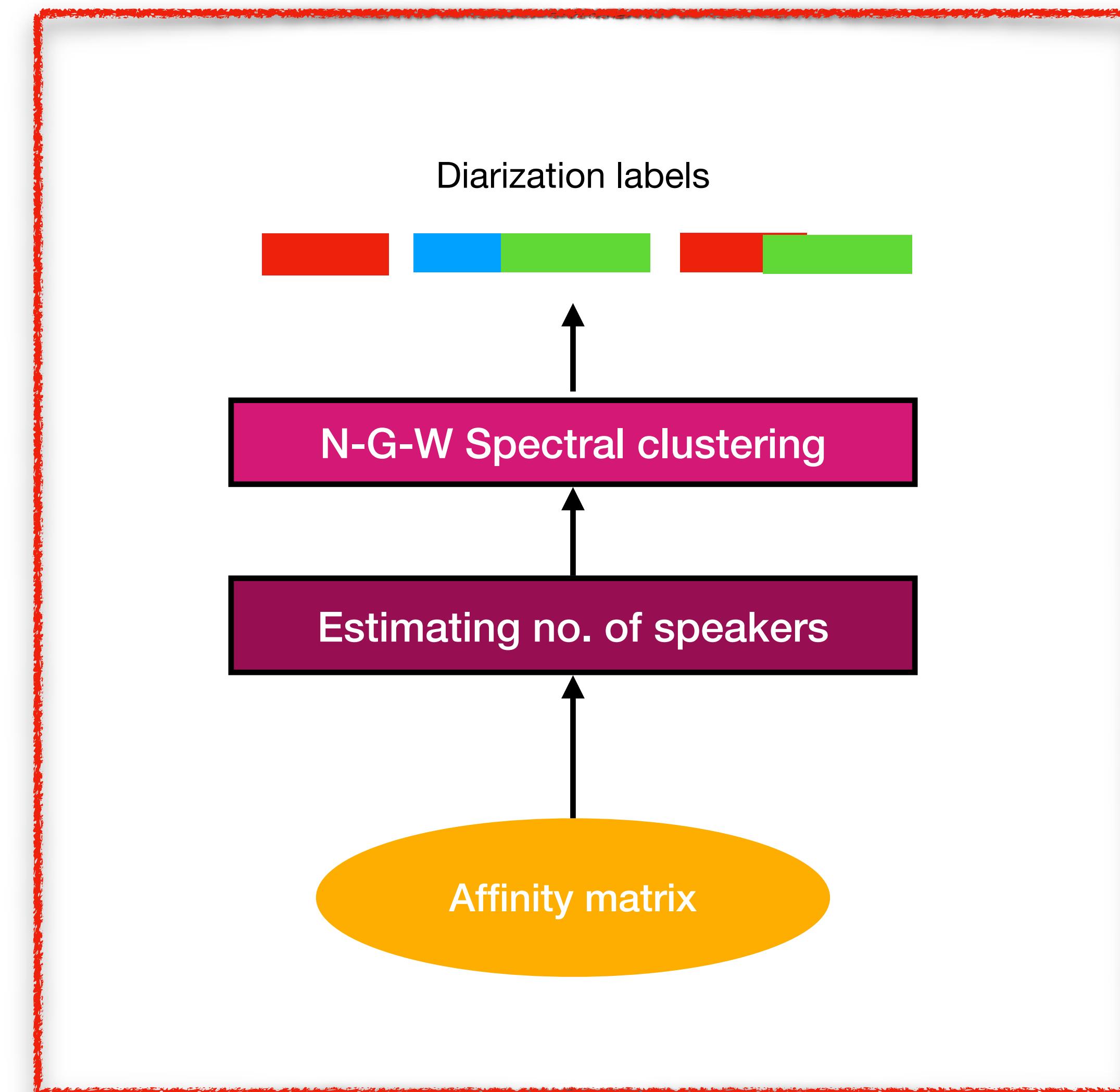
# Overlap-aware spectral clustering

## Overview of differences

### Regular spectral clustering

#### (Ng-Jordan-Weiss algorithm):

- Estimate number of speakers (say,  $K$ )
- Compute Laplacian  $L$  of affinity matrix
- Apply K-means clustering on first  $K$  eigenvectors of  $L$



Andrew Y. Ng, Michael I. Jordan, and Yair Weiss, “On spectral clustering: Analysis and an algorithm,” NIPS, 2001

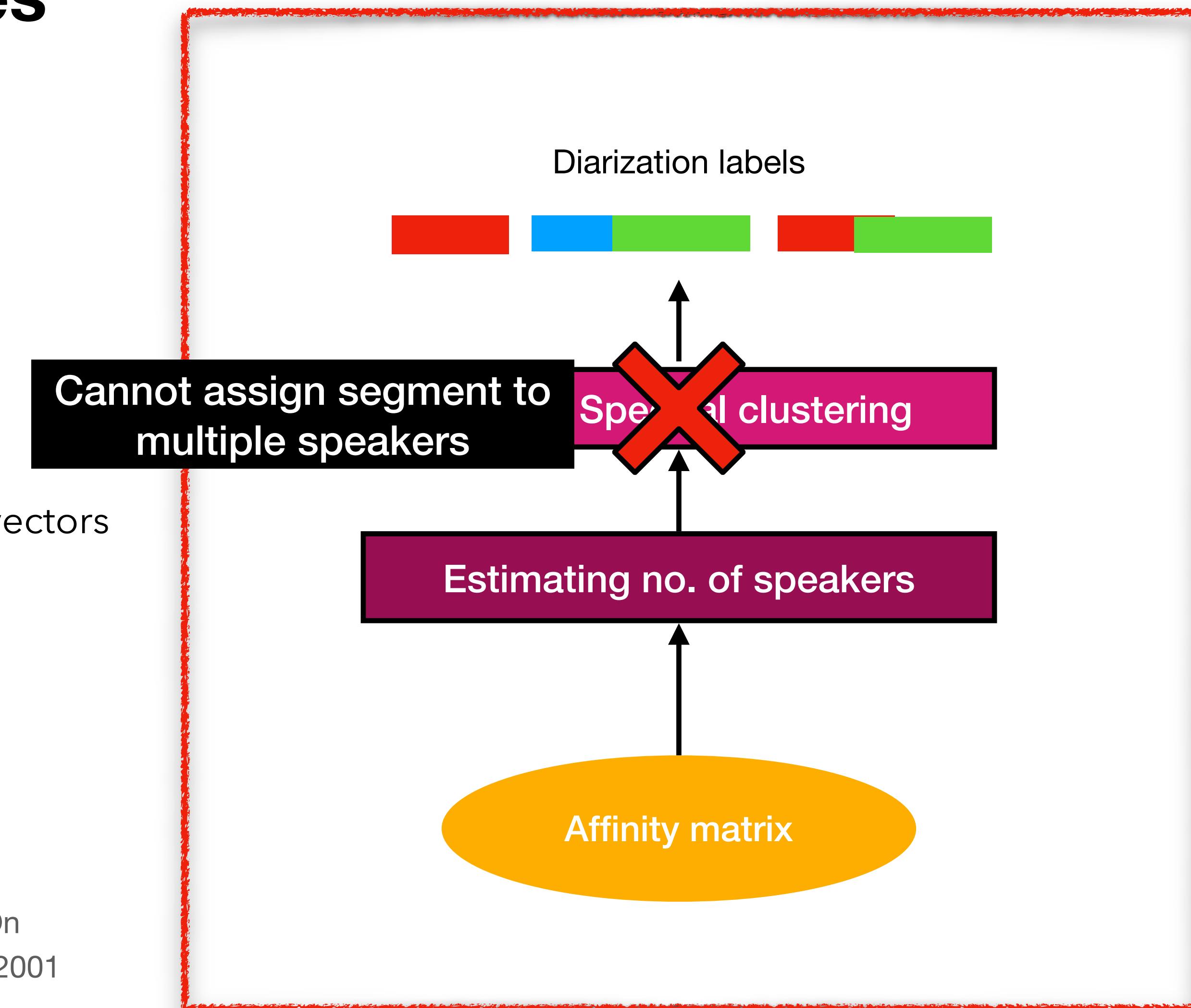
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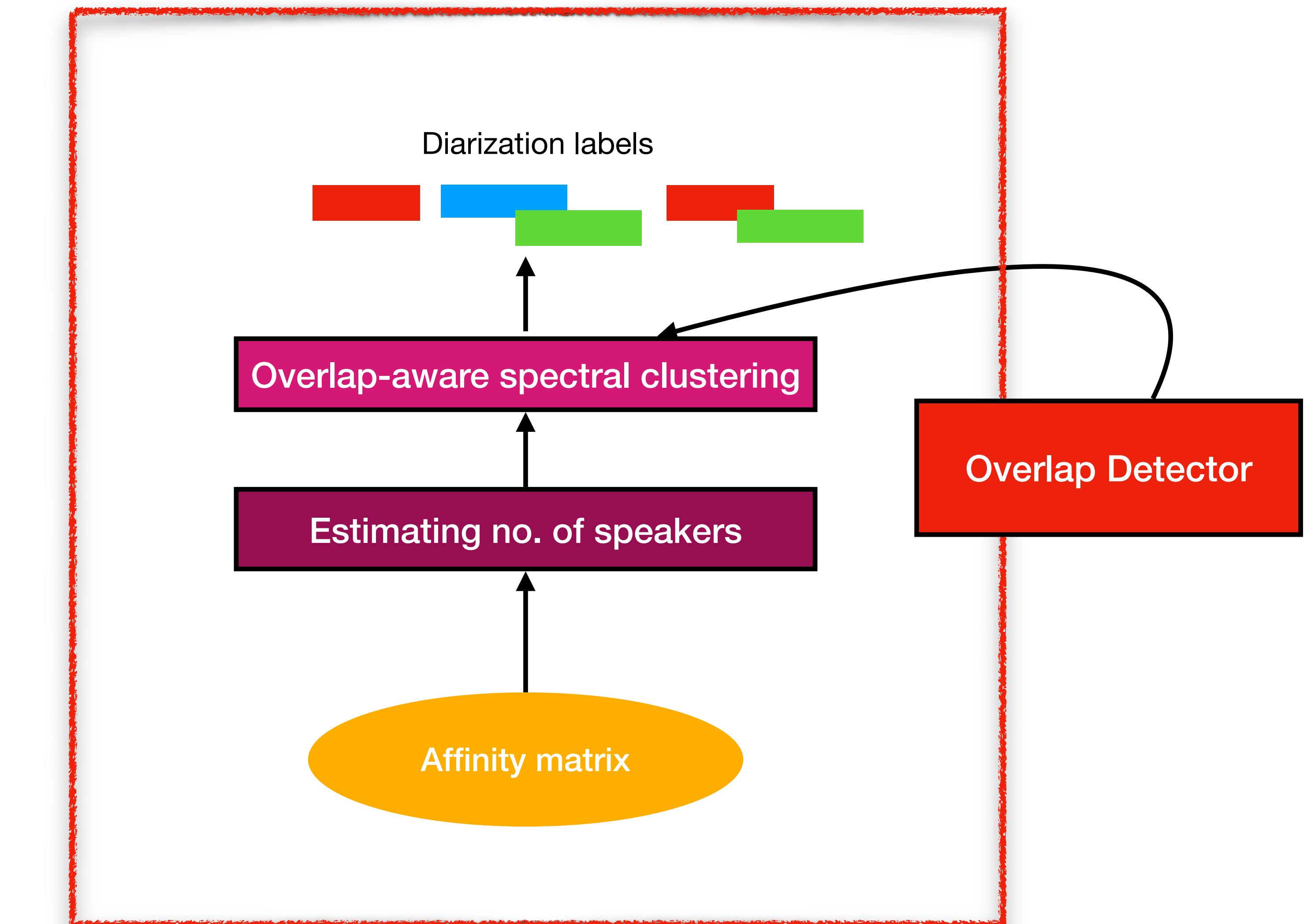


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# Overlap-aware spectral clustering

## Overview of differences

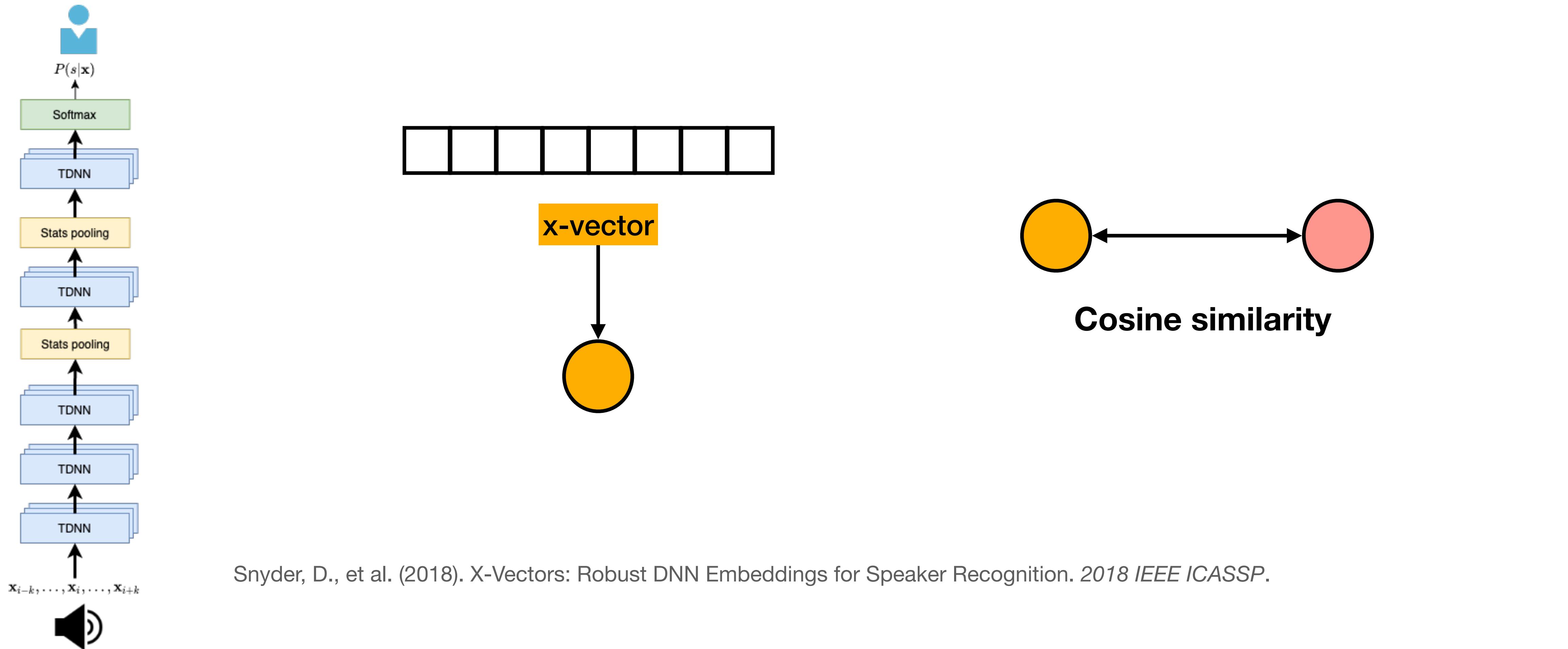
**Alternative formulation:**  
**multi-class spectral clustering**



Yu, S., & Shi, J. Multiclass spectral clustering. ICCV 2003.

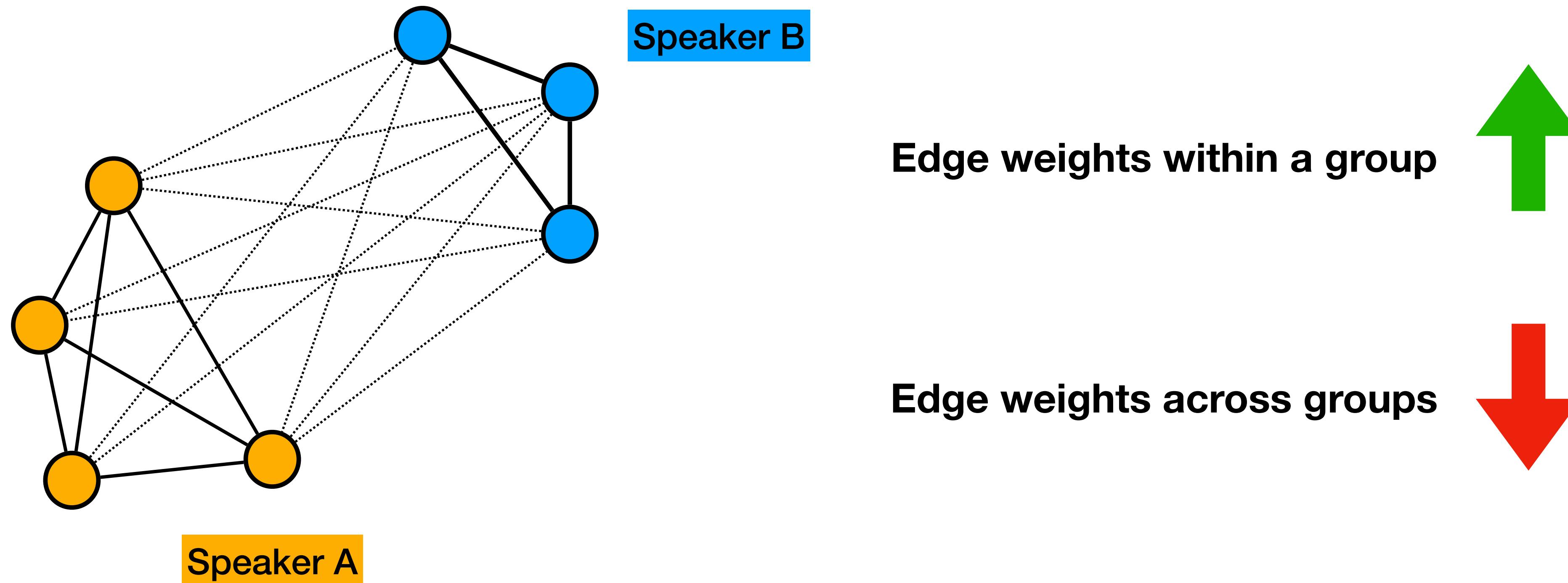
# New formulation for spectral clustering

## The basic clustering problem: a graph view



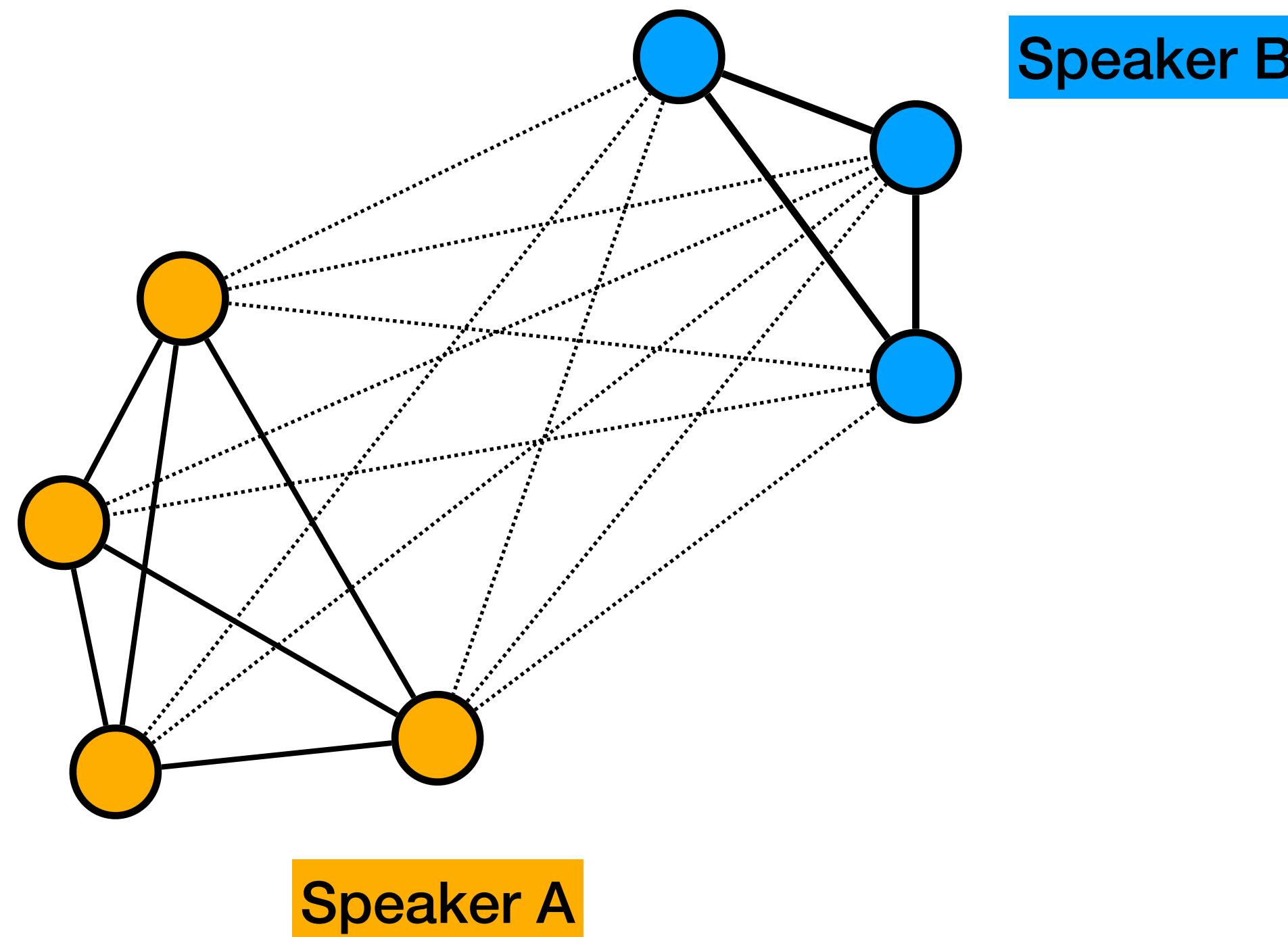
# New formulation for spectral clustering

The basic clustering problem: a graph view



# New formulation for spectral clustering

The basic clustering problem: a graph view



*maximize*

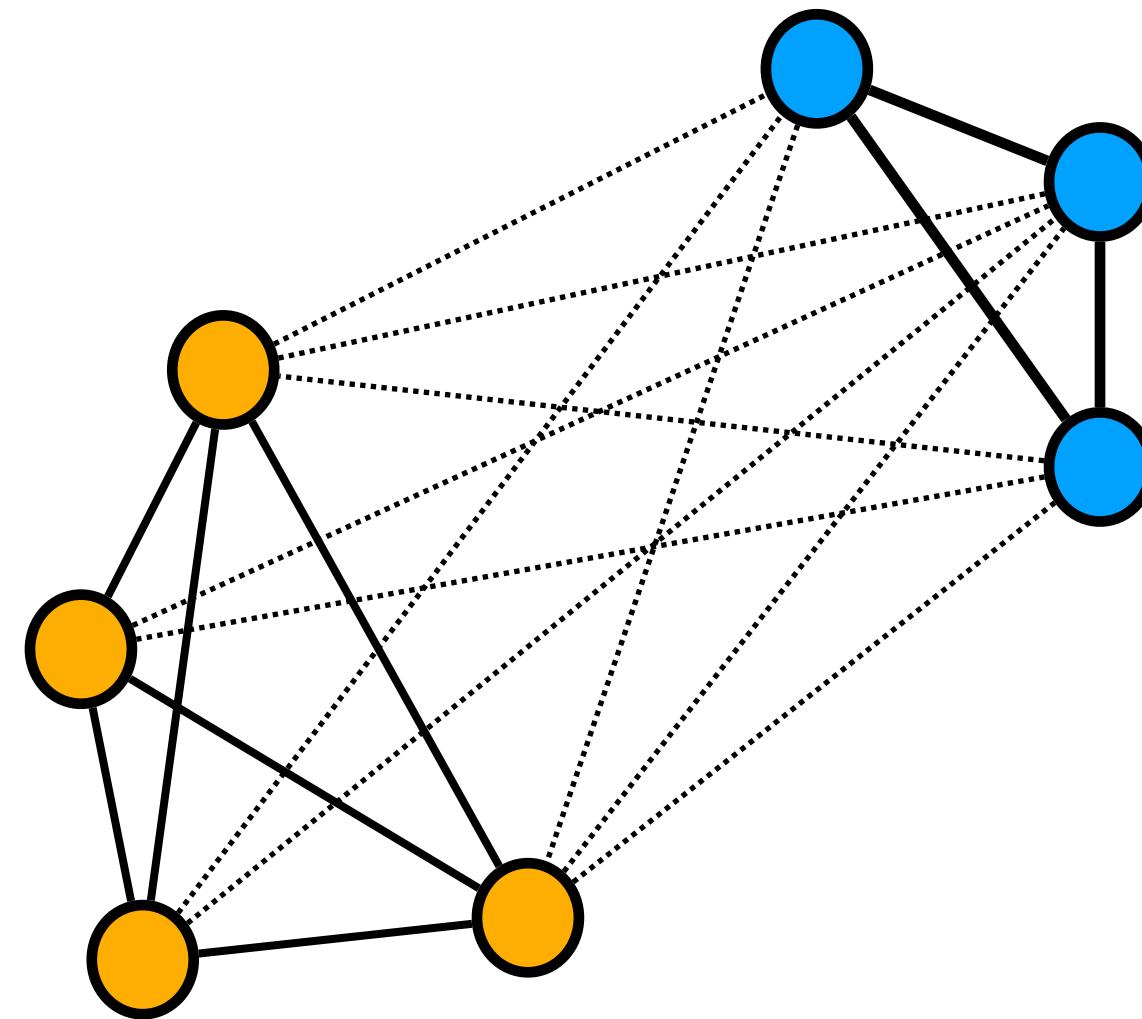
**Edge weights within a group**

---

**Edge weights across groups**

# New formulation for spectral clustering

The basic clustering problem: a graph view



*maximize*

Edge weights within a group

Edge weights across groups

maximize

$$\epsilon(X) = \frac{1}{K} \sum_{k=1}^K \frac{X_k^T \mathbf{A} X_k}{X_k^T \mathbf{D} X_k}$$

subject to

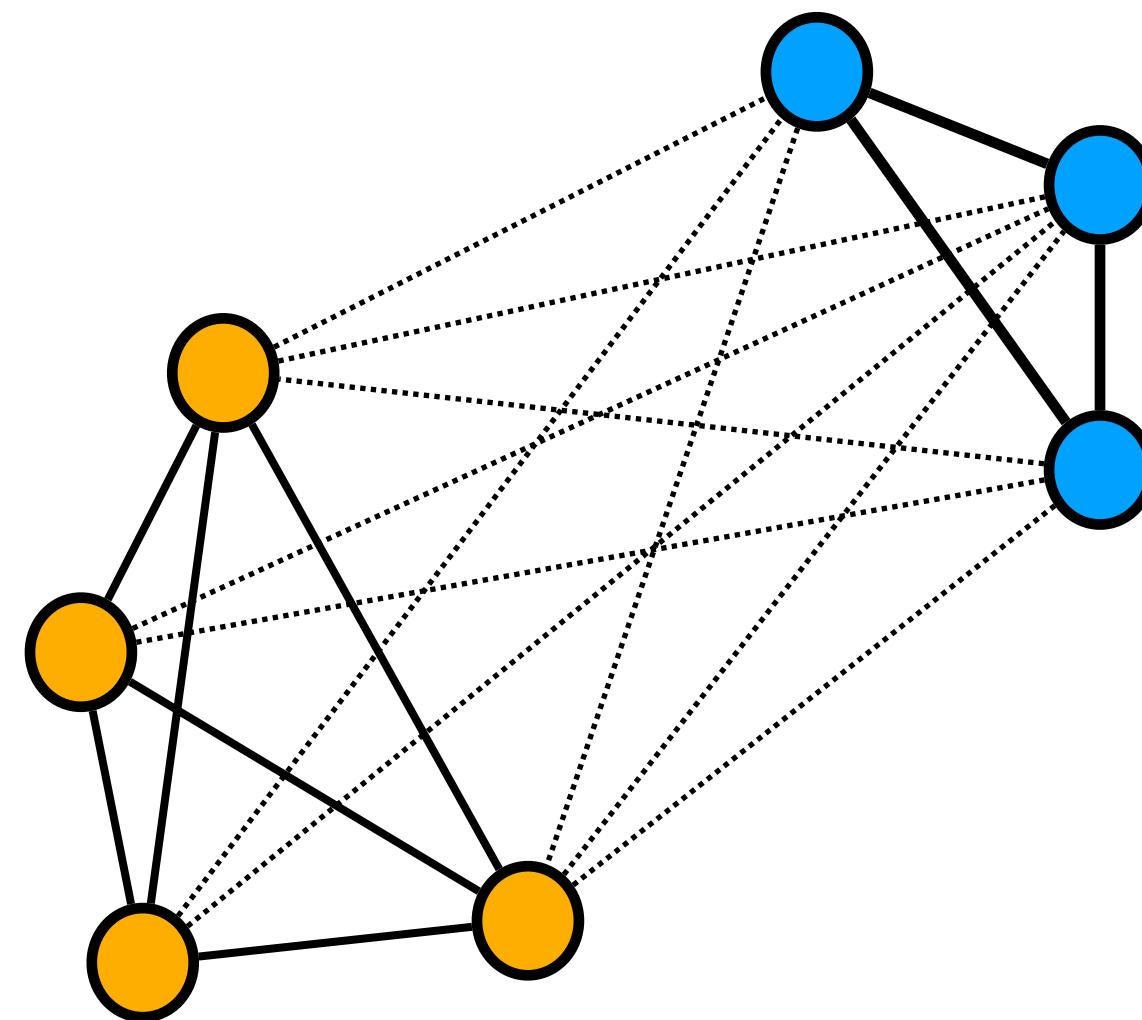
$$X \in \{0,1\}^{N \times K},$$

$$X\mathbf{1}_K = \mathbf{1}_N.$$

**K** speakers, **N** segments

# New formulation for spectral clustering

The basic clustering problem: a graph view



*maximize*

*maximize*

*subject to*

**Edge weights within a group**

**Edge weights across groups**

$$\epsilon(X) = \frac{1}{K} \sum_{k=1}^K \frac{X_k^T \mathbf{A} X_k}{X_k^T \mathbf{D} X_k}$$

$$X \in \{0,1\}^{N \times K},$$

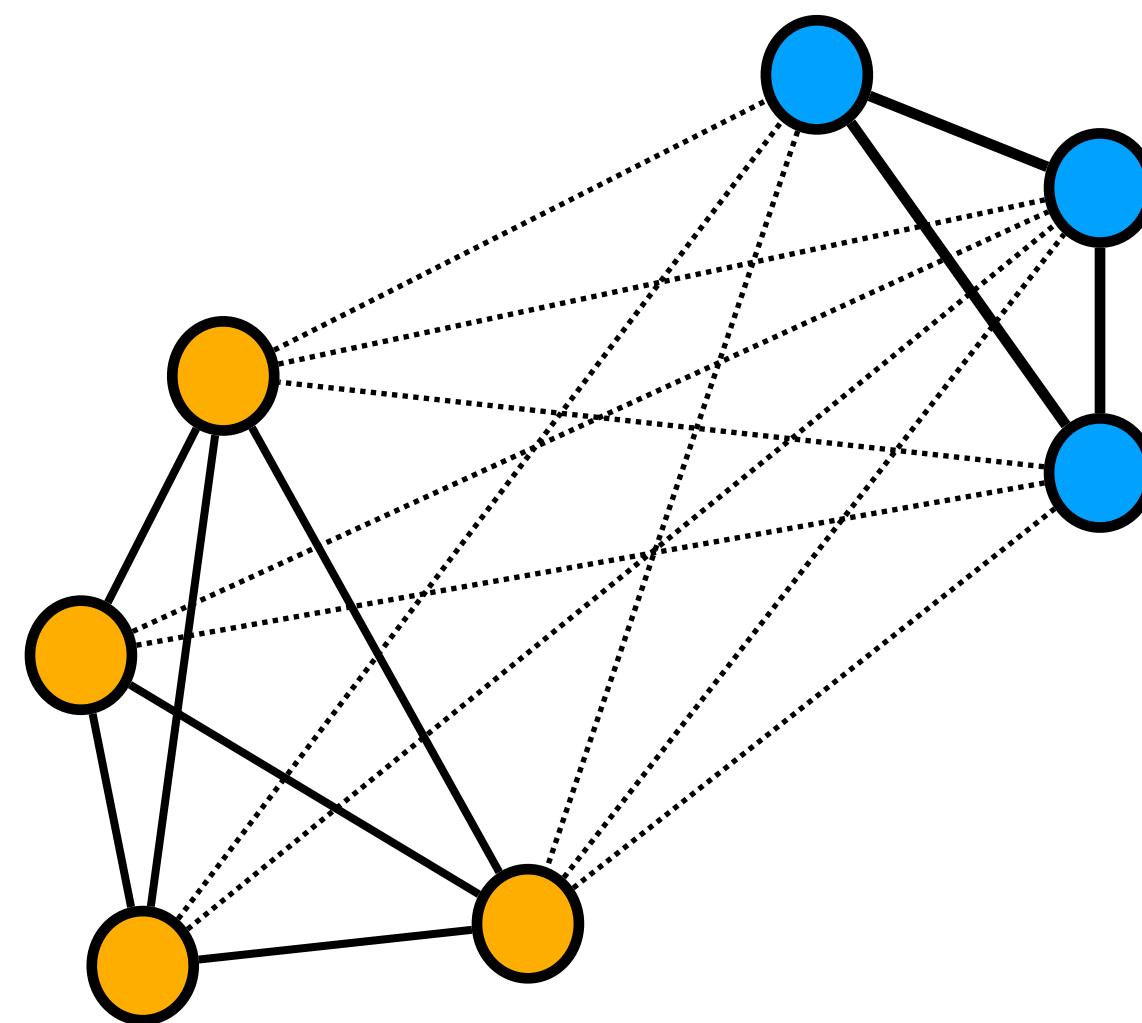
$$X\mathbf{1}_K = \mathbf{1}_N.$$

Affinity  
matrix

Diagonal matrix containing  
degree of nodes

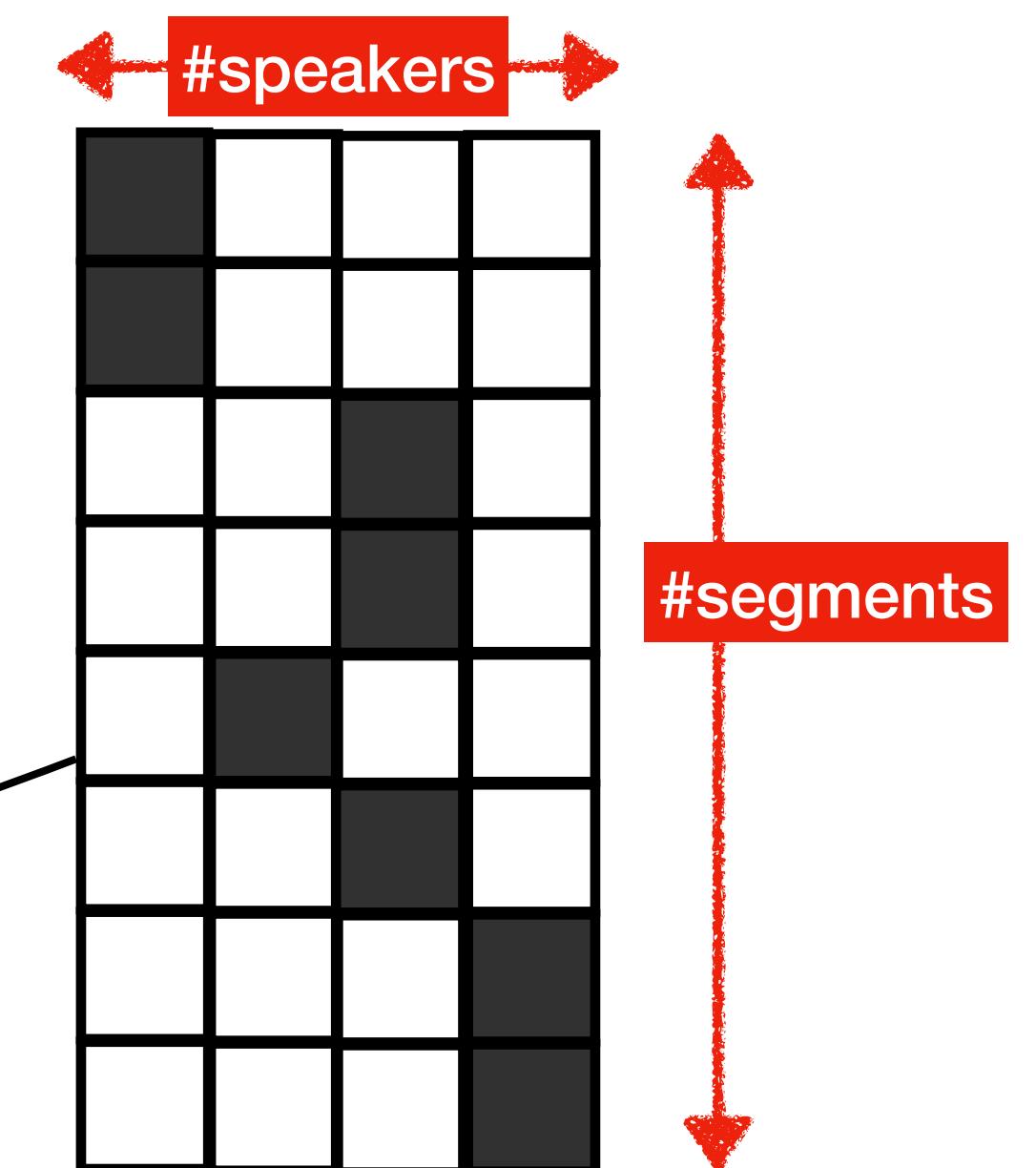
# New formulation for spectral clustering

The basic clustering problem: a graph view



$$\begin{aligned}
 & \text{maximize} && \epsilon(X) = \frac{1}{K} \sum_{k=1}^K \frac{X_k^T A X_k}{X_k^T D X_k} \\
 & \text{subject to} && X \in \{0,1\}^{N \times K}, \\
 & && X \mathbf{1}_K = \mathbf{1}_N.
 \end{aligned}$$

Final cluster assignment matrix



# New formulation for spectral clustering

This problem is NP-hard!

$$\begin{aligned}
 & \text{maximize} && \epsilon(X) = \frac{1}{K} \sum_{k=1}^K \frac{X_k^T \mathbf{A} X_k}{X_k^T \mathbf{D} X_k} \\
 & \text{subject to} && X \in \{0,1\}^{N \times K}, \\
 & && X \mathbf{1}_K \in \mathbb{R}^N.
 \end{aligned}$$

**Remove the discrete constraints** to make the problem solvable

# New formulation for spectral clustering

Relaxed problem has a set of solutions

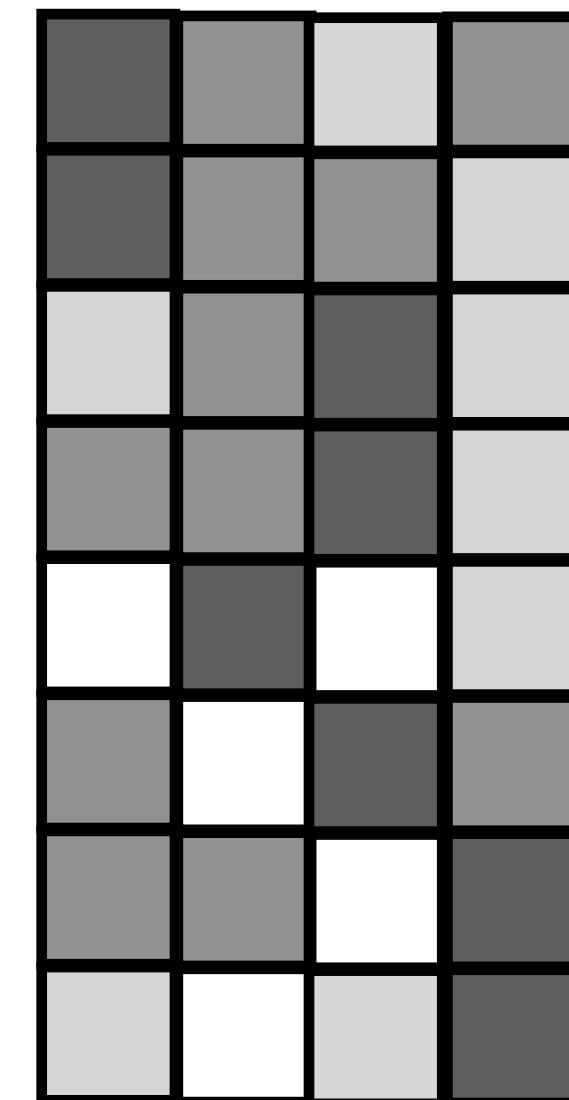
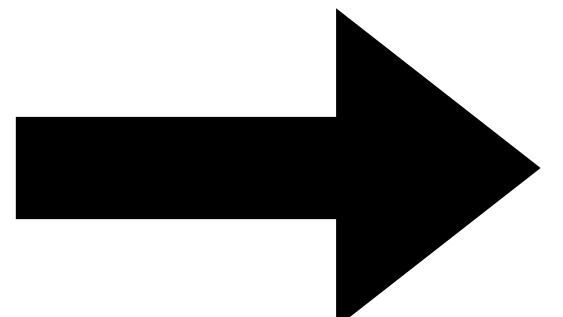
$$\text{maximize } \epsilon(X) = \frac{1}{K} \sum_{k=1}^K \frac{X_k^T \mathbf{A} X_k}{X_k^T \mathbf{D} X_k}$$

subject to

$$X \in \{-1, 1\}^{N \times K},$$

$$X \mathbf{1}_K = \mathbf{1}_N.$$

**Taking the Eigen-decomposition of  $\mathbf{D}^{-1}\mathbf{A}$**

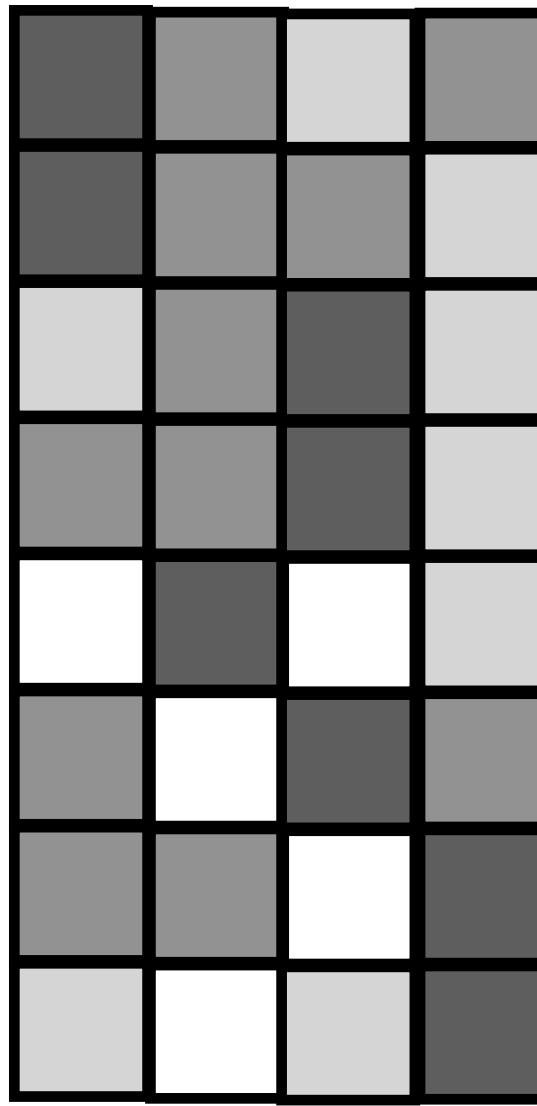


and its orthonormal transforms

**Set of solutions** to the **relaxed** problem

# New formulation for spectral clustering

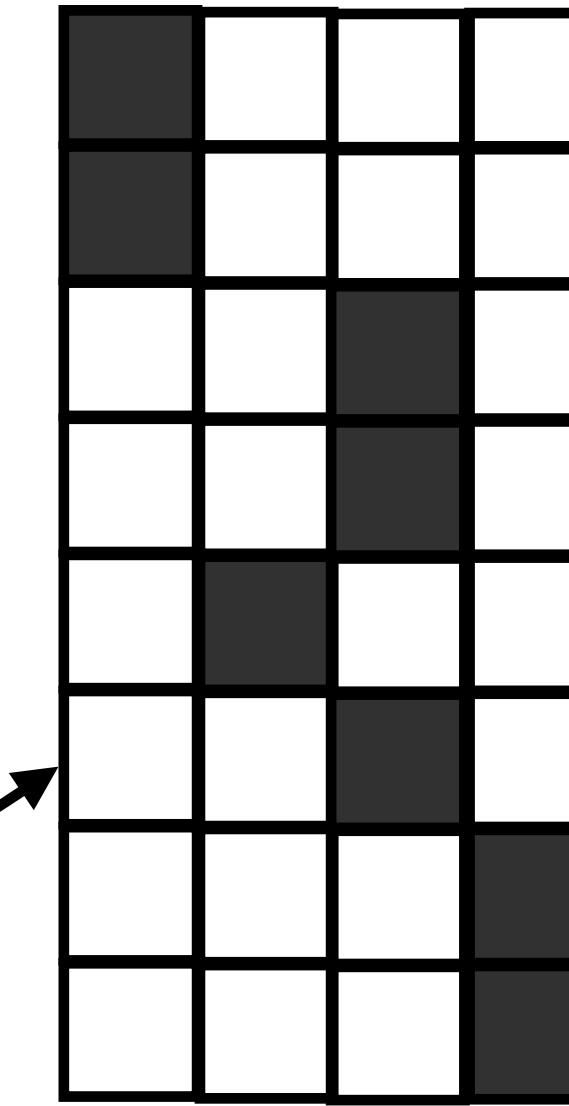
Now we need to **discretize** this solution!



and its orthonormal  
transforms

subject to

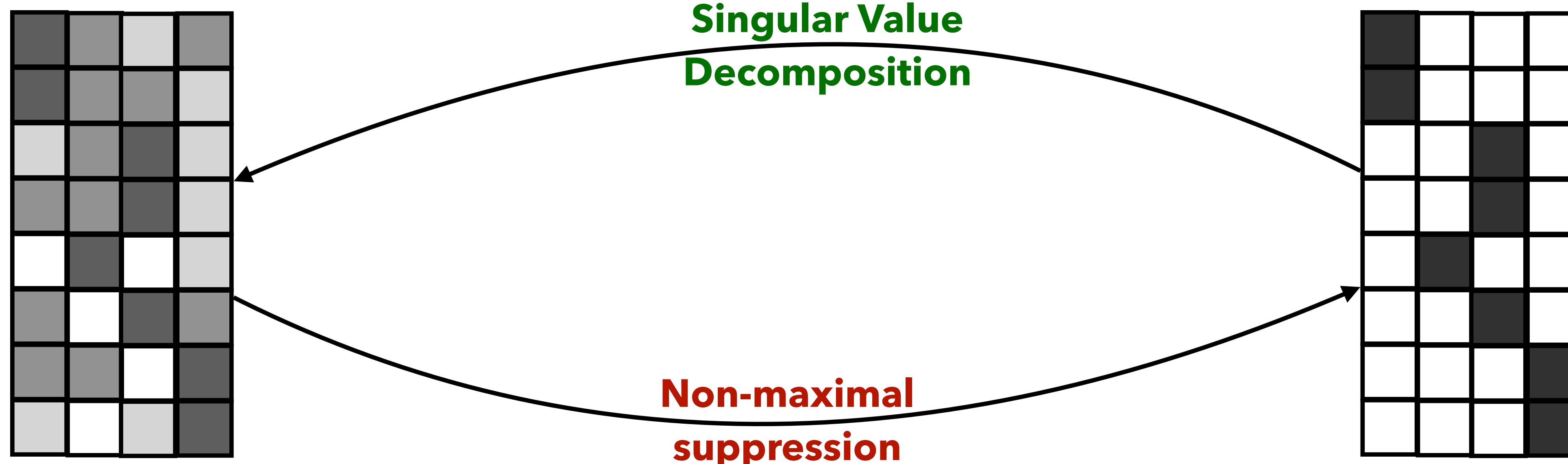
$$X \in \{0,1\}^{N \times K}, \\ X\mathbf{1}_K = \mathbf{1}_N.$$



Find a matrix which is **discrete** and also close  
to any one of the **orthonormal**  
**transformations** of the relaxed solution

# New formulation for spectral clustering

Now we need to **discretize** this solution!



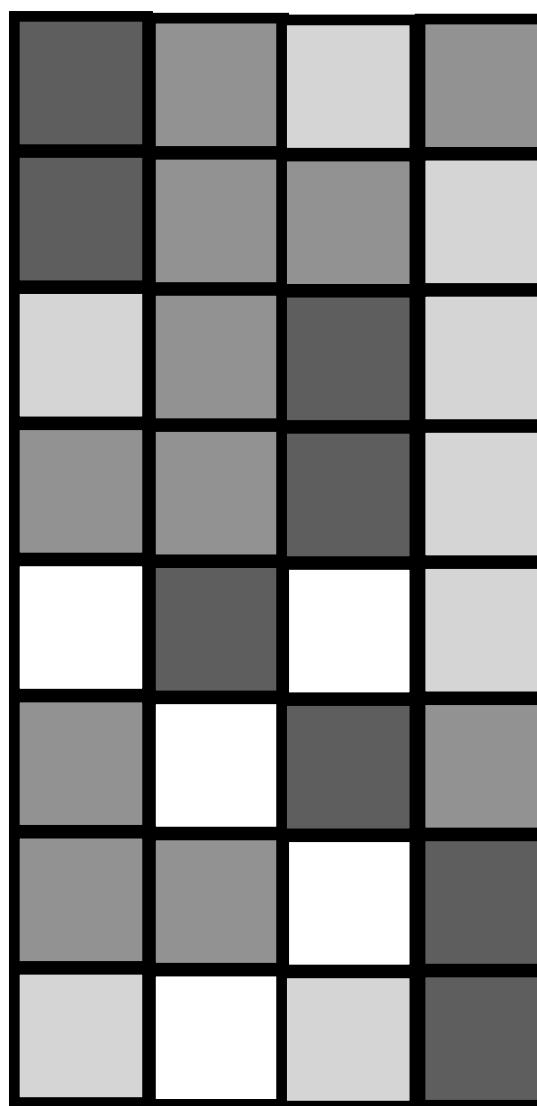
and its orthonormal  
transforms

**Iterate until convergence**

# Let us now make it overlap-aware

Suppose we have

$$v_{OL}$$



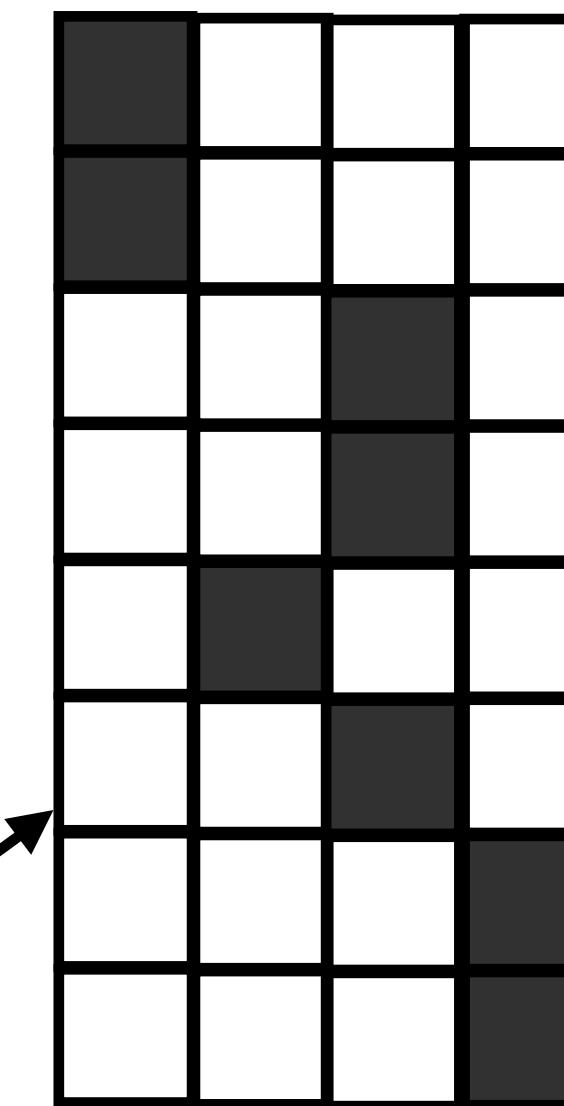
and its orthonormal  
transforms



subject to

$$X \in \{0,1\}^{N \times K},$$

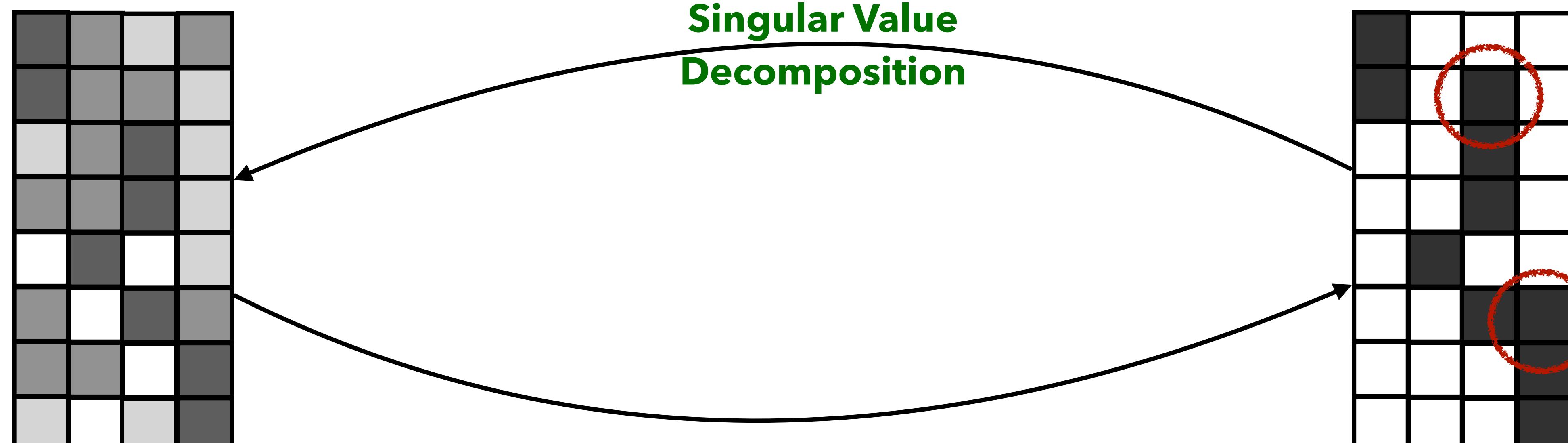
$$X\mathbf{1}_K = \mathbf{1}_N + v_{OL}.$$



**Discrete constraint is modified to include  
overlap detector output**

# Let us now make it overlap-aware

## Modify non-maximal suppression to pick top 2 speakers

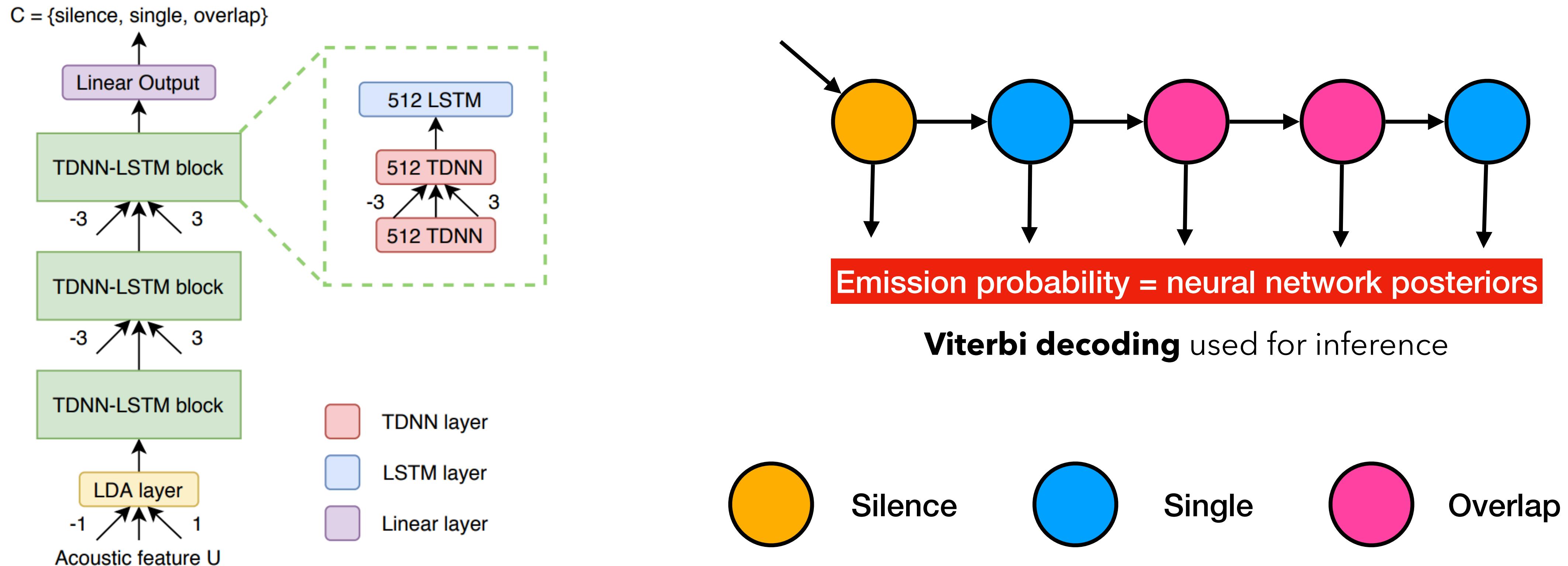


and its orthonormal  
transforms

**Iterate until convergence**

# Hybrid HMM-DNN overlap detector

(Can also use other methods, e.g. end-to-end)



# Results on AMI Mix-Headset eval

**12.0% relative improvement over spectral clustering baseline**

System	DER
<b>Spectral clustering</b>	26.9
<b>AHC</b>	28.3
<b>VBx</b>	26.2
<b>Overlap-aware SC</b>	<b>24.0</b>

Park et al., “Auto-tuning spectral clustering for speaker diarization using normalized maximum eigengap,” IEEE Signal Processing Letters, 2020.

Garcia-Romero et al., “Speaker diarization using deep neural network embeddings,” ICASSP 2017.

Díez et al., “Speaker diarization based on Bayesian HMM with eigenvoice priors,” Odyssey 2018.

AMI data contains **4-speaker meetings**

# Results on AMI Mix-Headset eval

## Comparable with other overlap-aware diarization methods

System	DER
<b>VB-based overlap assignment</b>	23.8
<b>Region proposal networks</b>	25.5
<b>Overlap-aware SC</b>	<b>24.0</b>

Bullock, et al., “Overlap-aware diarization: resegmentation using neural end-to-end overlapped speech detection,” ICASSP 2020.

Huang et al., “Speaker diarization with region proposal network,” ICASSP 2020.

Does not require **matching training data** or **initialization** with other diarization systems.

# Results: DER breakdown on AMI eval

System	Missed speech	False alarm	Speaker conf.	DER
AHC/PLDA	19.9	0.0	8.4	26.9
Spectral/cosine	19.9	0.0	7.0	28.3
VBx	19.9	0.0	6.3	26.2
VB-based overlap assignment	13.0	3.6	7.2	23.8
RPN	9.5	7.7	8.3	25.5
Overlap-aware SC	11.3	2.2	10.5	24.0

# Results: DER breakdown on AMI eval

Missed speech decreases significantly



System	Missed speech	False alarm	Speaker conf.	DER
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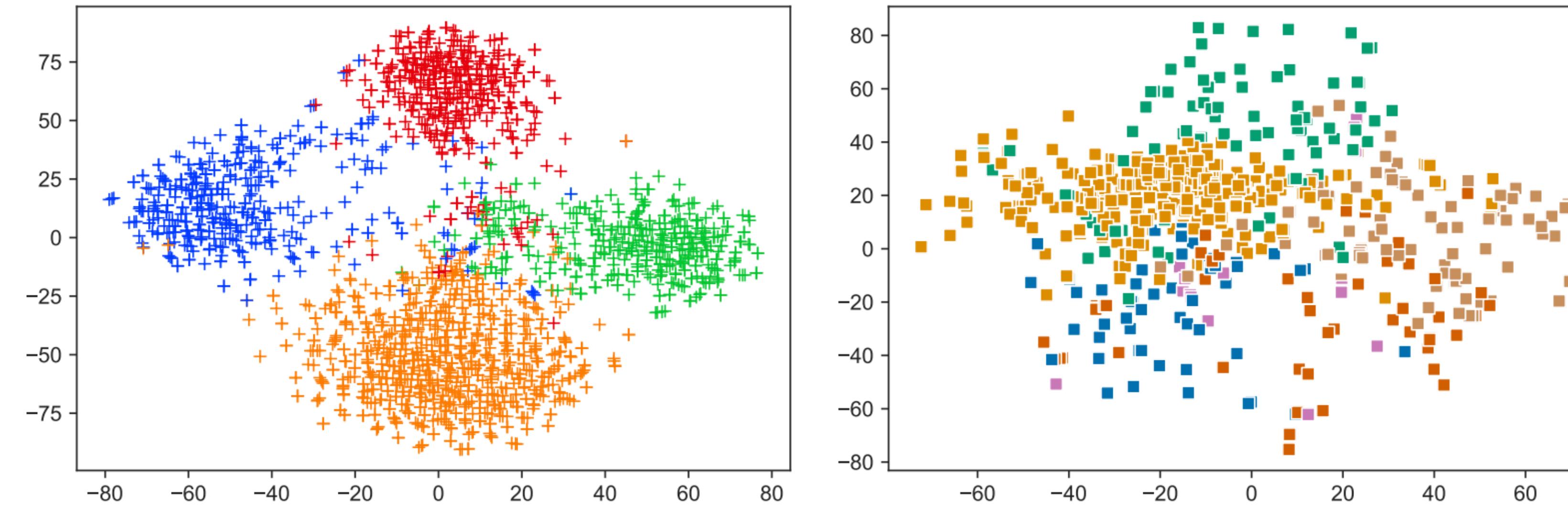
# Results: DER breakdown on AMI eval

## Speaker confusion increases



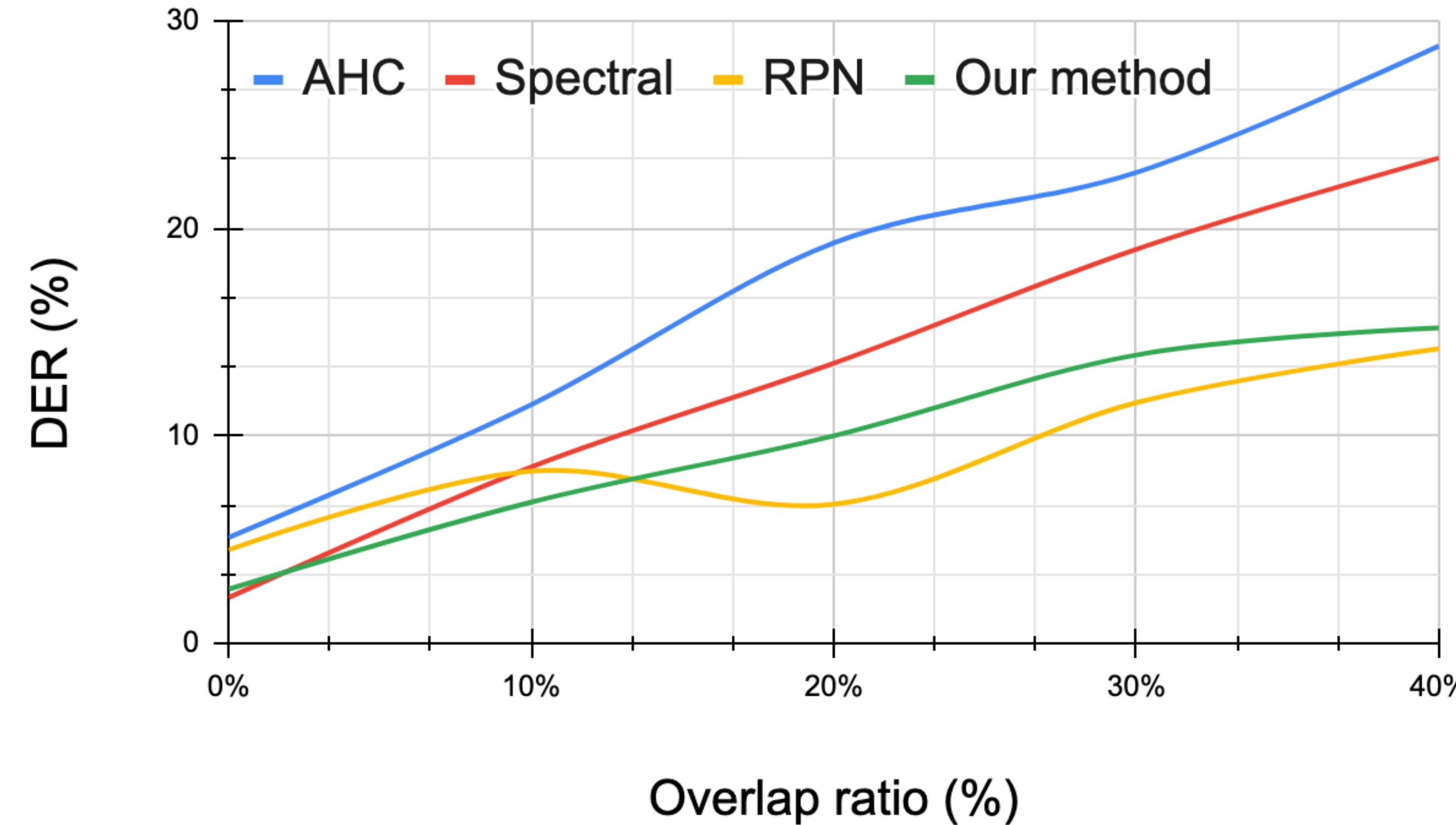
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# Need more robust x-vector extractors



**T-SNE plot** of x-vector embeddings

# More results: DER on LibriCSS



# Overlap-aware Diarization

## Several new methods proposed recently

Bullock, et al., “Overlap-aware diarization: **resegmentation** using neural end-to-end overlapped speech detection,” ICASSP 2020.

Fujita et al. “**End-to-end neural diarization**: Reformulating speaker diarization as simple multi-label classification,” ArXiv, 2020.

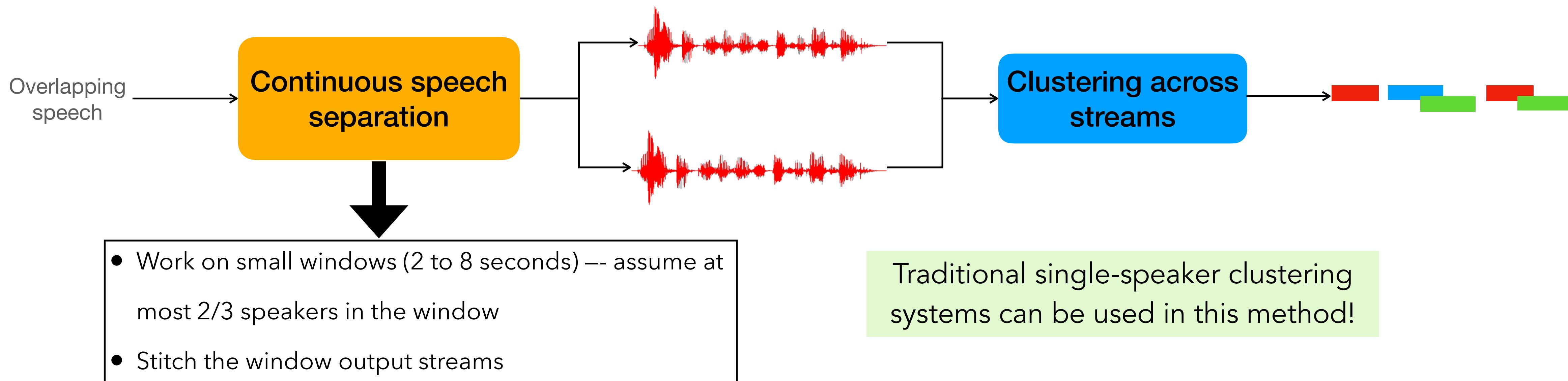
Huang et al., “Speaker diarization with **region proposal network**,” ICASSP 2020.

Kinoshita, et al. **Integrating** end-to-end neural and clustering-based diarization: Getting the best of both worlds. ArXiv, 2020.

Medennikov, et al. “**Target speaker voice activity detection**: a novel approach for multispeaker diarization in a dinner party scenario,” Interspeech 2020.

# A different paradigm

## Separate, then diarize



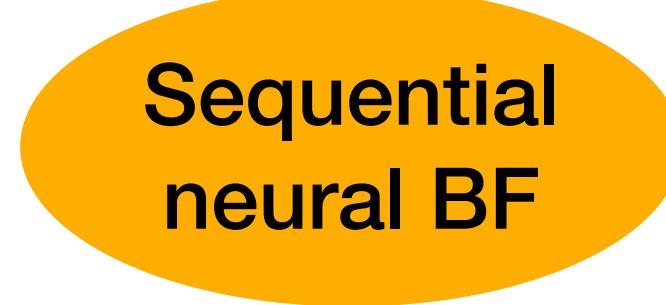
Raj, D., Denisov, P., Chen, Z., Erdogan, H., Huang, Z., He, M., Watanabe, S., Du, J., Yoshioka, T., Luo, Y., Kanda, N., Li, J., Wisdom, S., & Hershey, J. Integration of Speech Separation, Diarization, and Recognition for Multi-Speaker Meetings: System Description, Comparison, and Analysis. *IEEE SLT 2021*.

# Results on LibriCSS data

## Using 2 different continuous speech separation methods



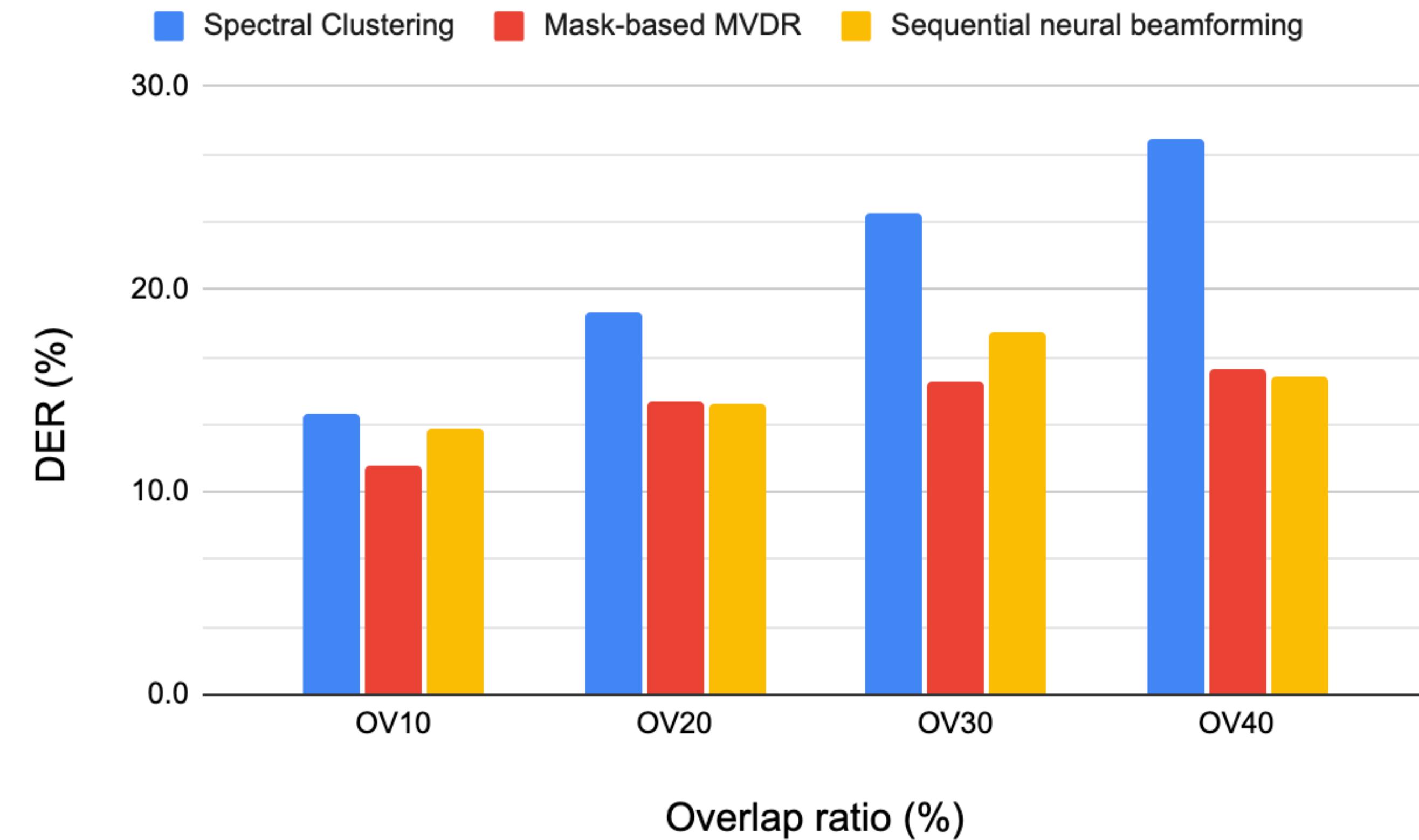
Takuya Yoshioka, Hakan Erdogan, Zhuo Chen, and Fil Alleva, "Multi-microphone neural speech separation for far-field multi-talker speech recognition," ICASSP 2018



Zhong-Qiu Wang, Hakan Erdogan, Scott Wisdom, Kevin Wilson, Desh Raj, Shinji Watanabe, Zhuo Chen, and John R. Hershey, "Sequential multi-frame neural beamforming for speech separation and enhancement," IEEE SLT 2021.

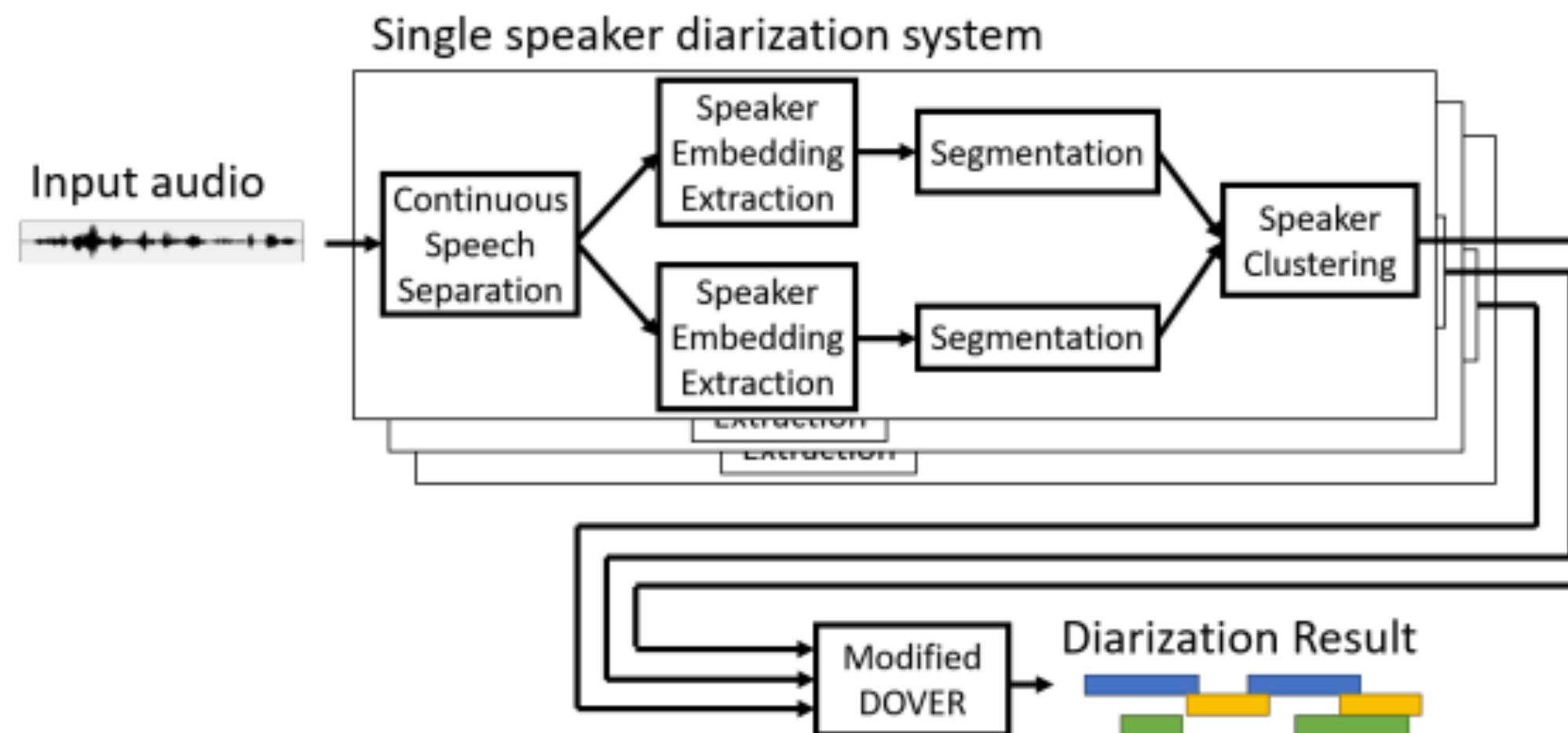
2.4s chunks; 2 streams

10s chunks; 3 streams



# Works well in practice

## Winner of VoxSRC Track 4 (Diarization)



**Fig. 1.** System Diagram

Team	Method	DER (%)
Huawei	VBx	9.5
Sugou	VB-based overlap assignment	7.2
DKU-DukeECE	VB-based overlap assignment	6.5*
BUT	VBx + overlap handling	4.0
Microsoft	CSS + spectral clustering	3.7

# Machine learning tasks benefit from an **ensemble** of systems.

For example, ROVER is a popular combination method for ASR systems.

Jonathan G. Fiscus, “A post-processing system to yield reduced word error rates: Recognizer output voting error reduction (ROVER),” IEEE ASRU 1997.

# Problem

## Why is it hard to combine diarization systems?

- System outputs may have different number of speaker estimates.
- System outputs are usually in different label space.
- There may not be agreement on whether a region contains overlap.

# Solution

## DOVER-Lap performs “map and vote”

- System outputs may have different number of speaker estimates.
- System outputs are usually in different label space.
- There may not be agreement on whether a region contains overlap.

**Label mapping:** Maximal matching algorithm based on a global cost tensor



Raj, D., García-Perera, L.P., Huang, Z., Watanabe, S., Povey, D., Stolcke, A., & Khudanpur, S. DOVER-Lap: A Method for Combining Overlap-aware Diarization Outputs. *IEEE SLT 2021*.

# Solution

## DOVER-Lap performs “map and vote”

- System outputs may have different number of speaker estimates.
- System outputs are usually in different label space.
- There may not be agreement on whether a region contains overlap.

**Label voting:** Weighted majority voting considers speaker count in region

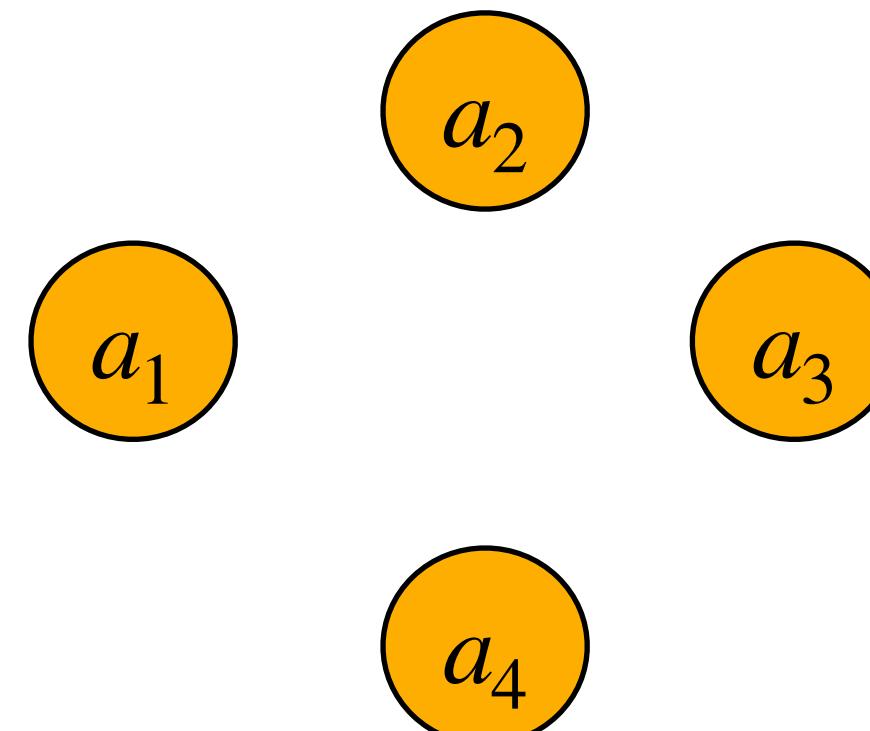


Raj, D., García-Perera, L.P., Huang, Z., Watanabe, S., Povey, D., Stolcke, A., & Khudanpur, S. DOVER-Lap: A Method for Combining Overlap-aware Diarization Outputs. *IEEE SLT 2021*.

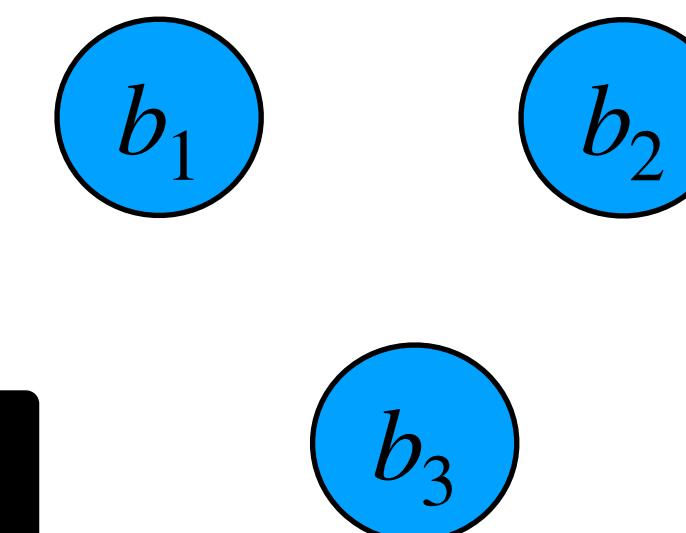
# DOVER-Lap extends DOVER

## Diarization Output Voting Error Reduction

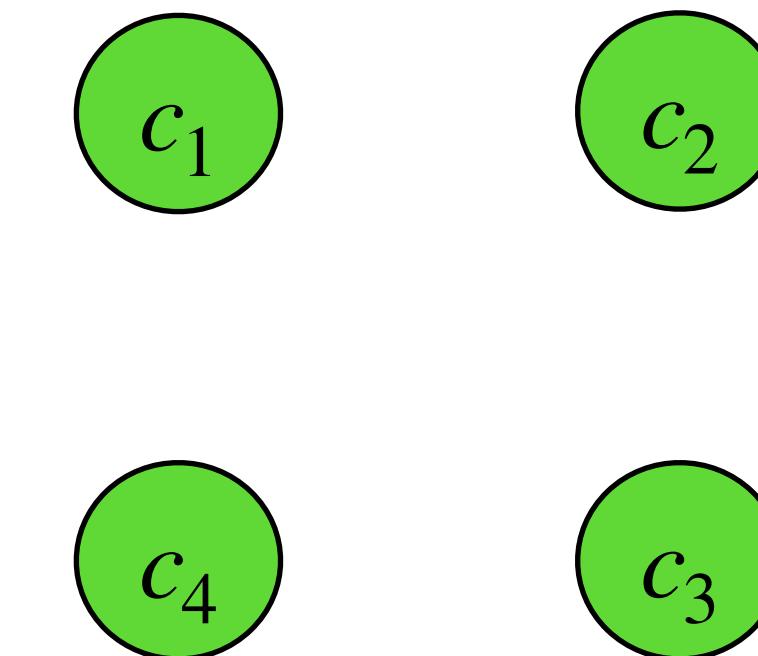
**Hypothesis A** e.g. AHC



**Hypothesis B** e.g. SC



**Hypothesis C** e.g. VBx



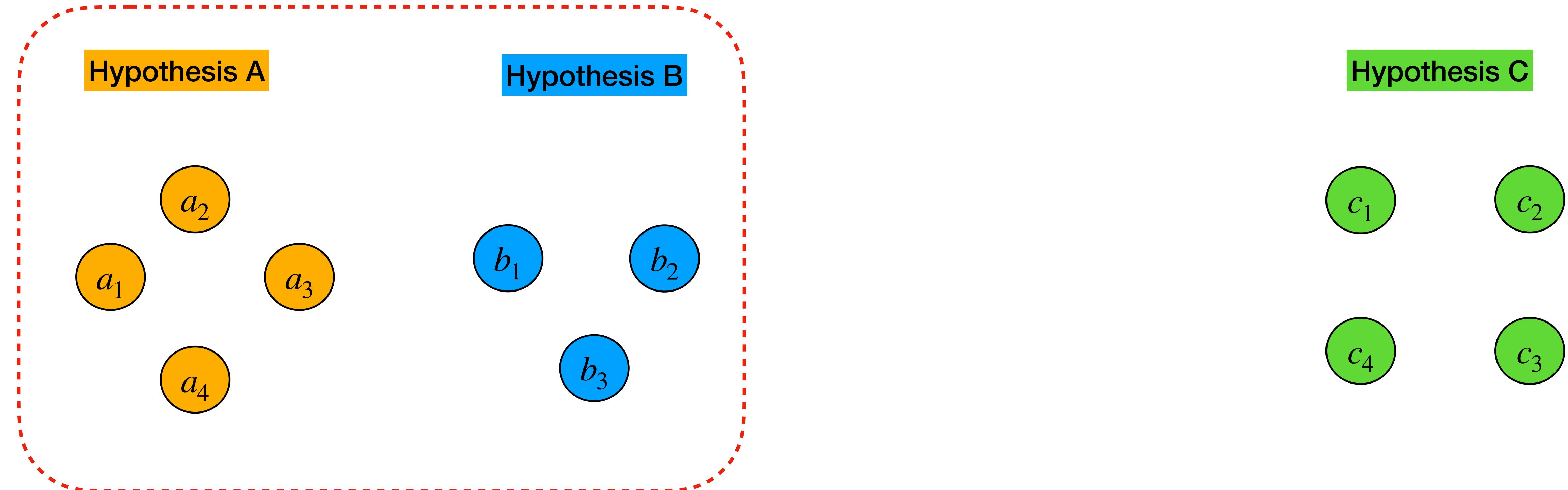
Diarization  
system output

**Assumption:** The input hypotheses do not contain overlapping segments.

Andreas Stolcke and Takuya Yoshioka, "DOVER: A method for combining diarization outputs," IEEE ASRU 2019.

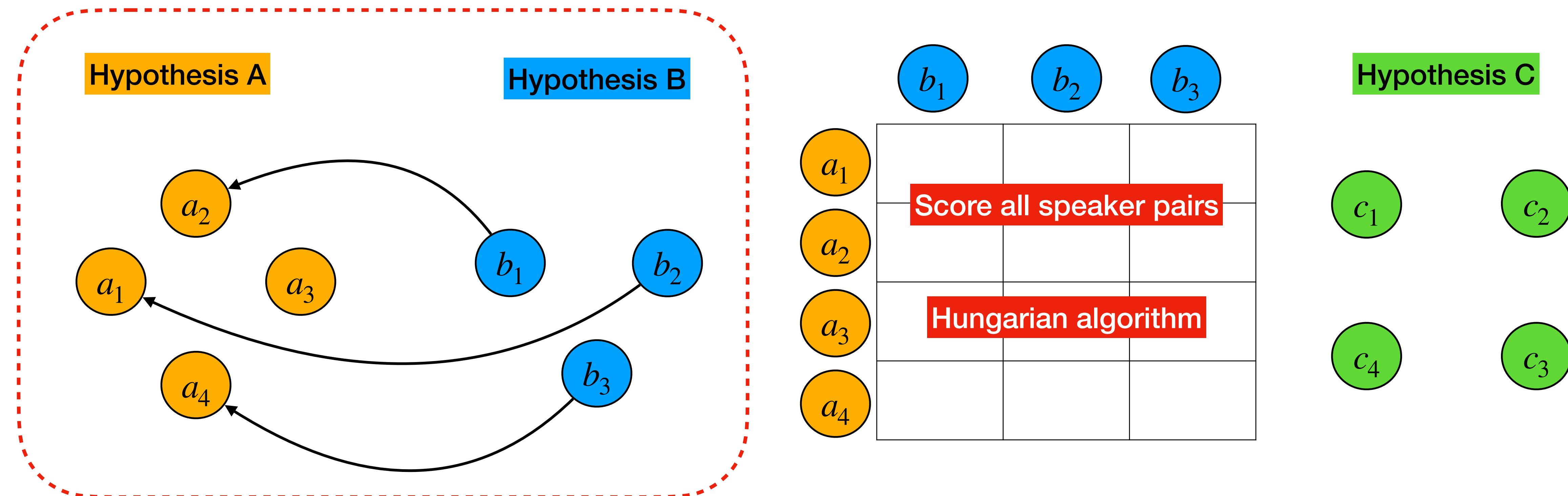
# Preliminary: how DOVER works

## Pair-wise incremental label mapping



# Preliminary: how DOVER works

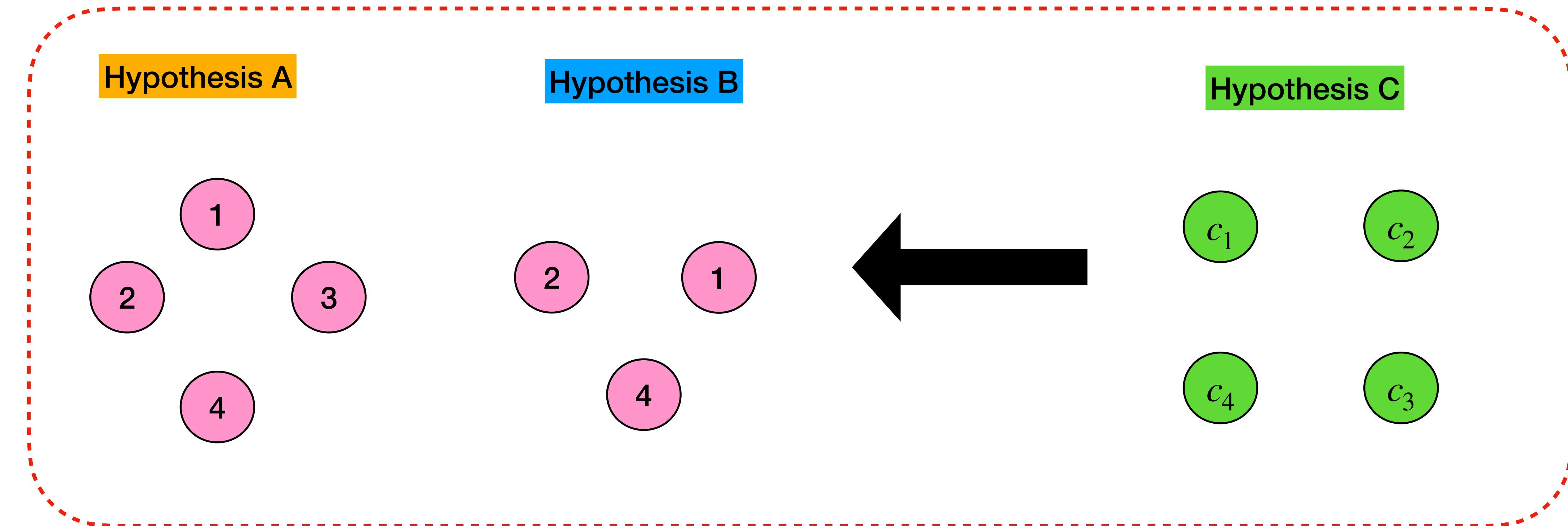
## Pair-wise incremental label mapping



This is the same algorithm that is used to map hypothesis to reference for DER computation.

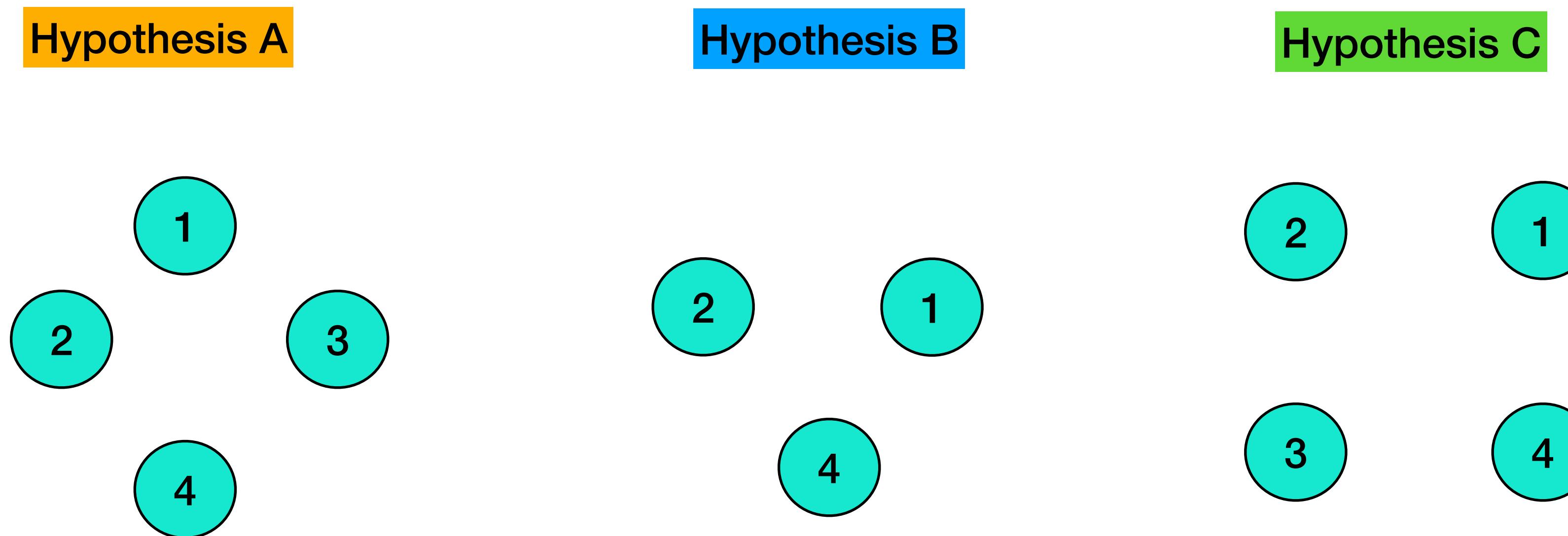
# Preliminary: how DOVER works

## Pair-wise incremental label mapping



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## Pair-wise incremental label mapping



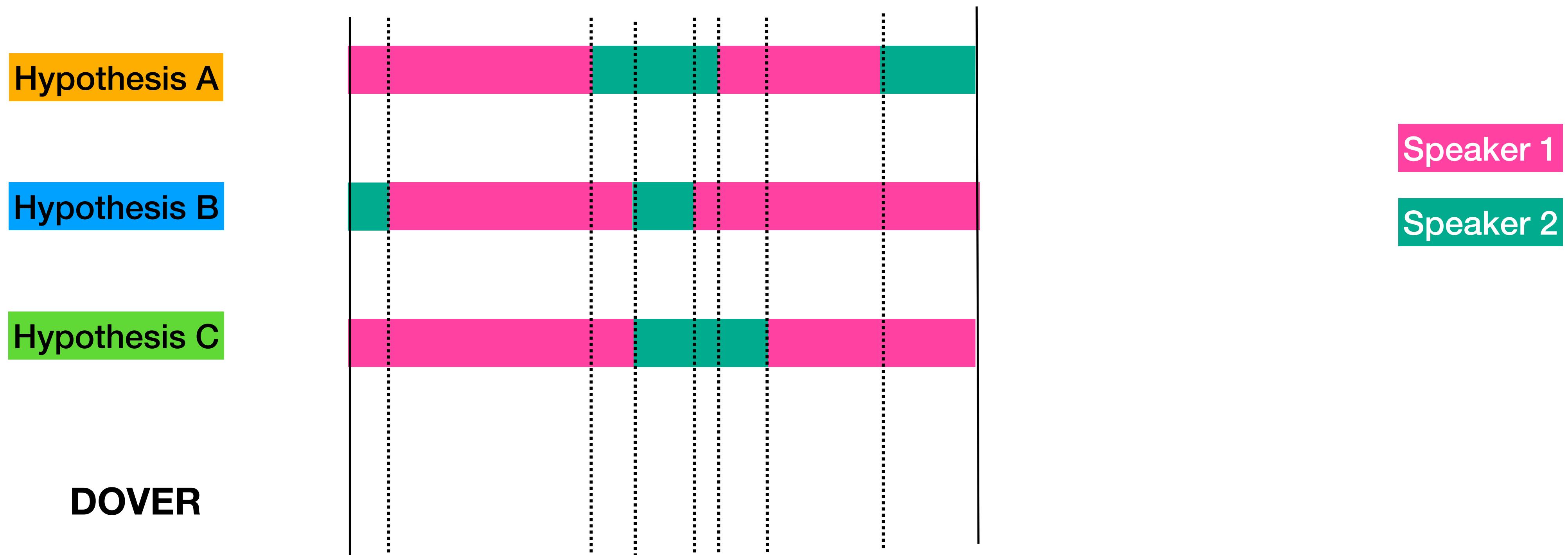
# Preliminary: how DOVER works

## Label voting using rank-weighting



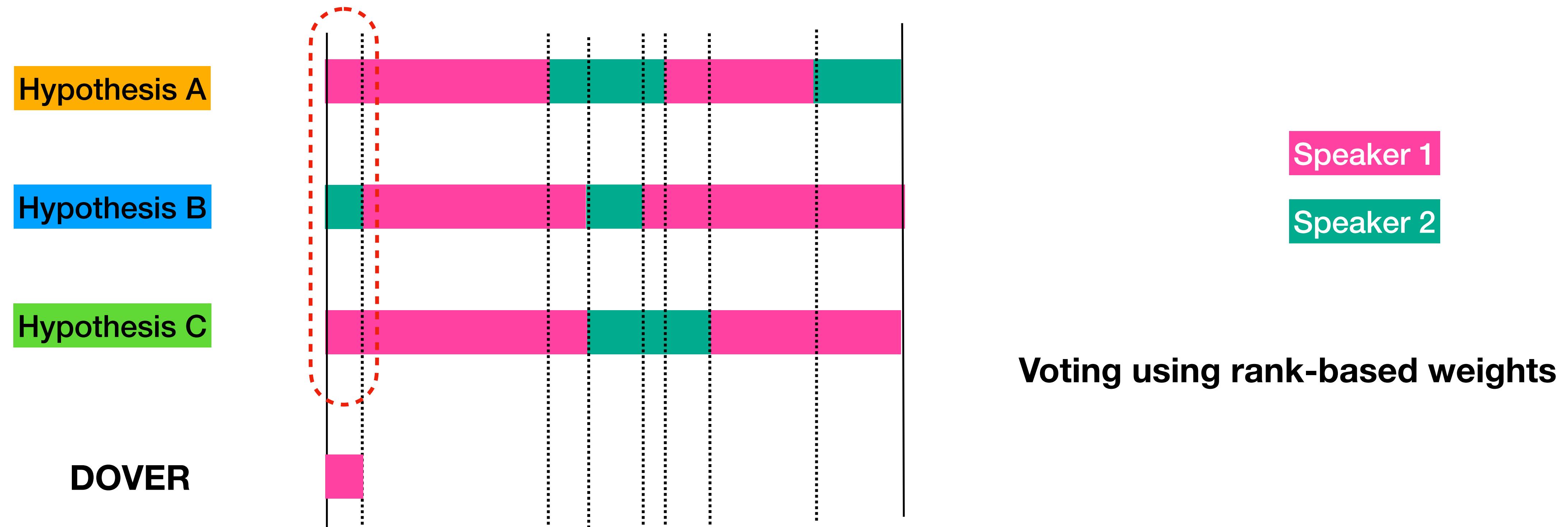
# Preliminary: how DOVER works

## Label voting using rank-weighting



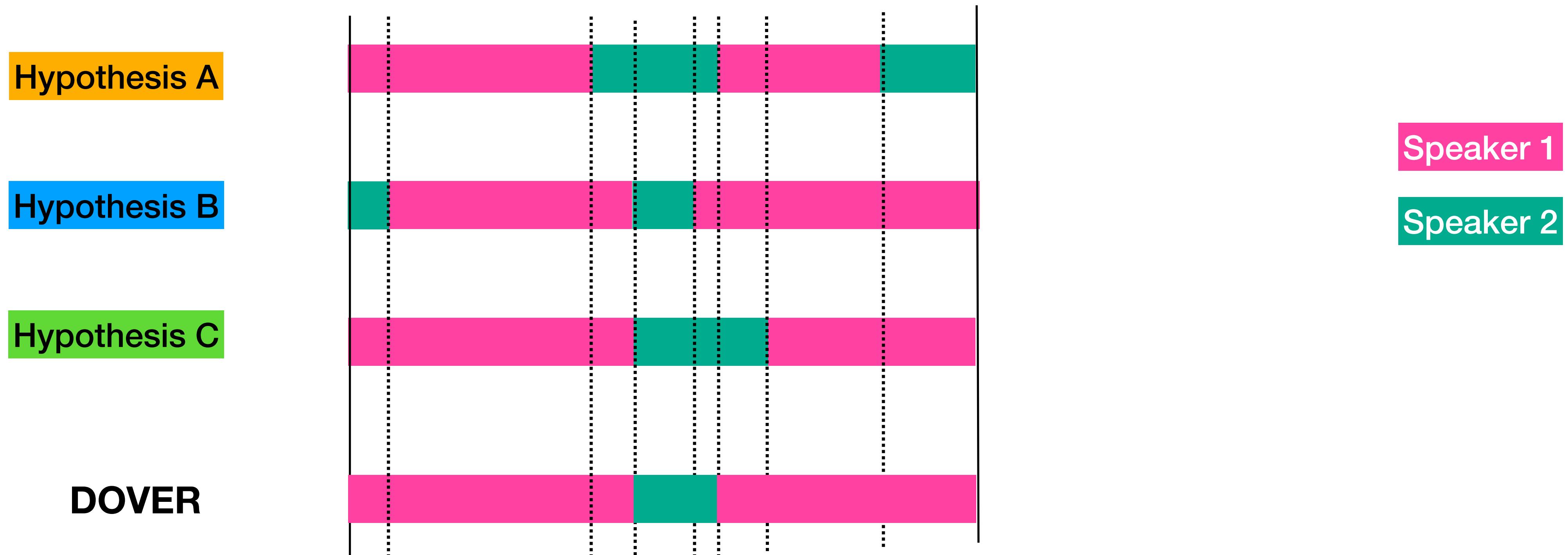
# Preliminary: how DOVER works

## Label voting using rank-weighting



# Preliminary: how DOVER works

## Label voting using rank-weighting

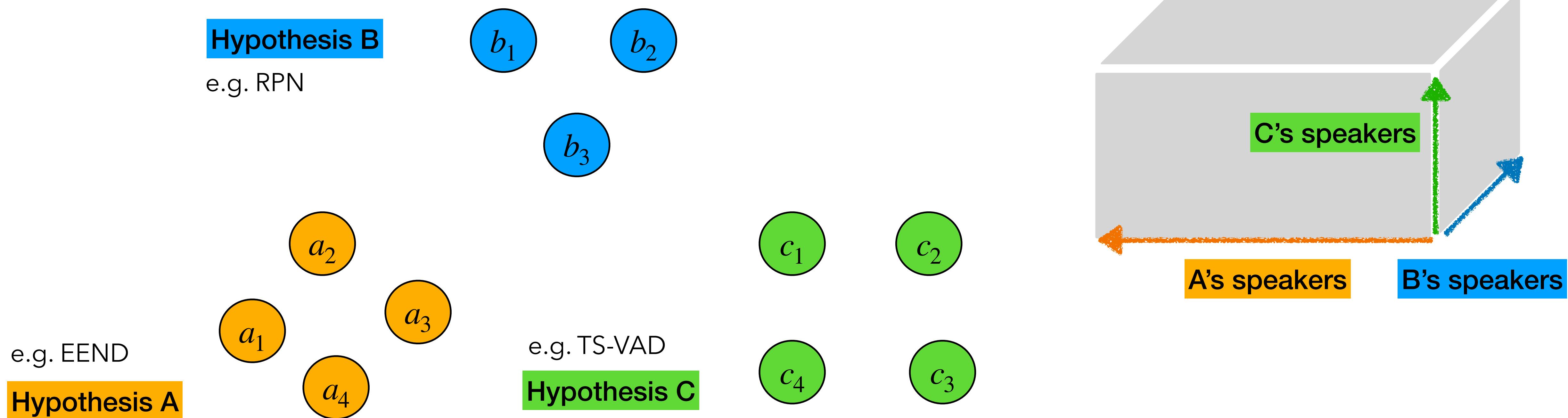


# 2 limitations of DOVER

1. Incremental pair-wise label assignment does not give **optimal mapping**
2. Voting method does not handle **overlapping speaker segments**

# DOVER-Lap label mapping

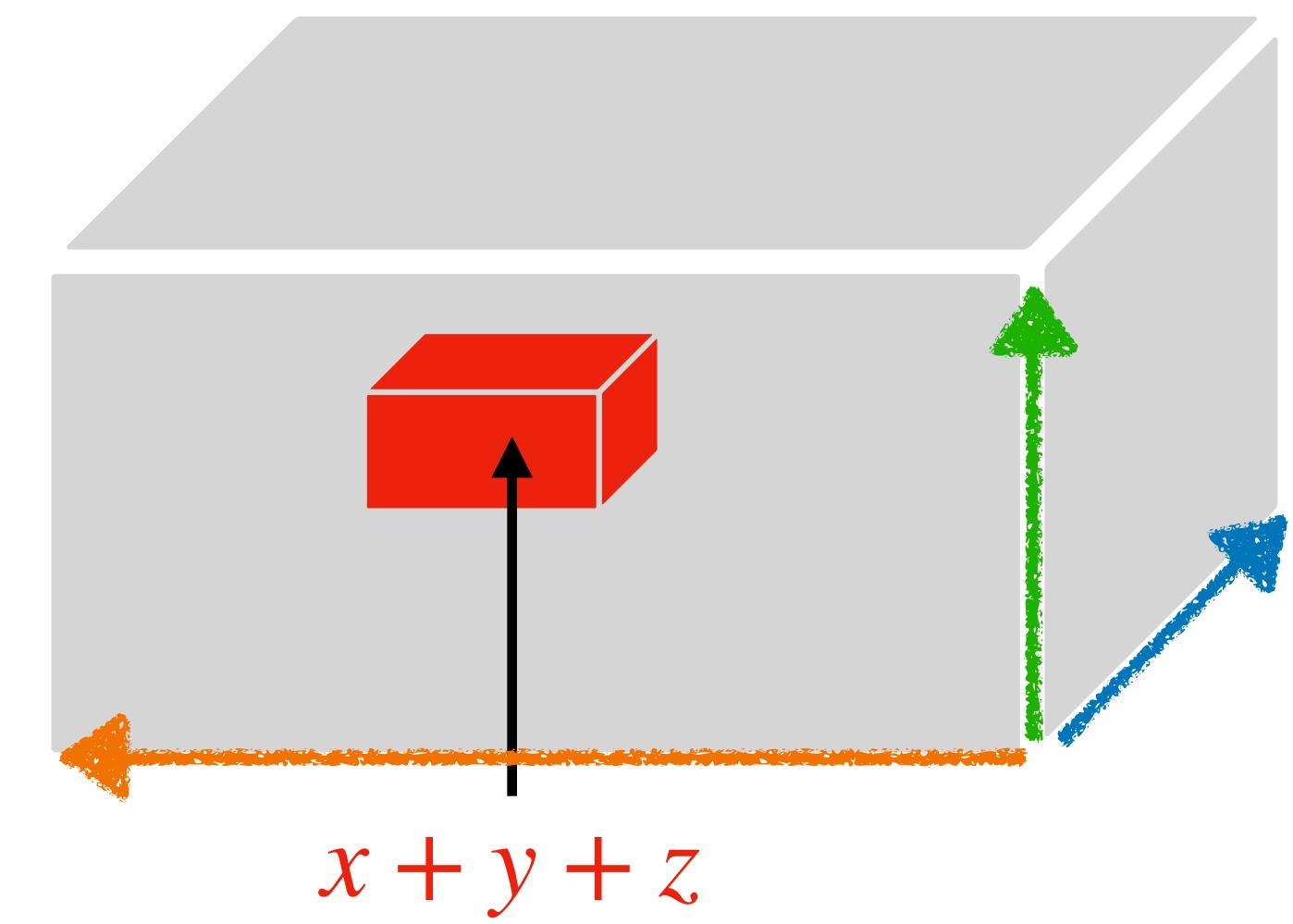
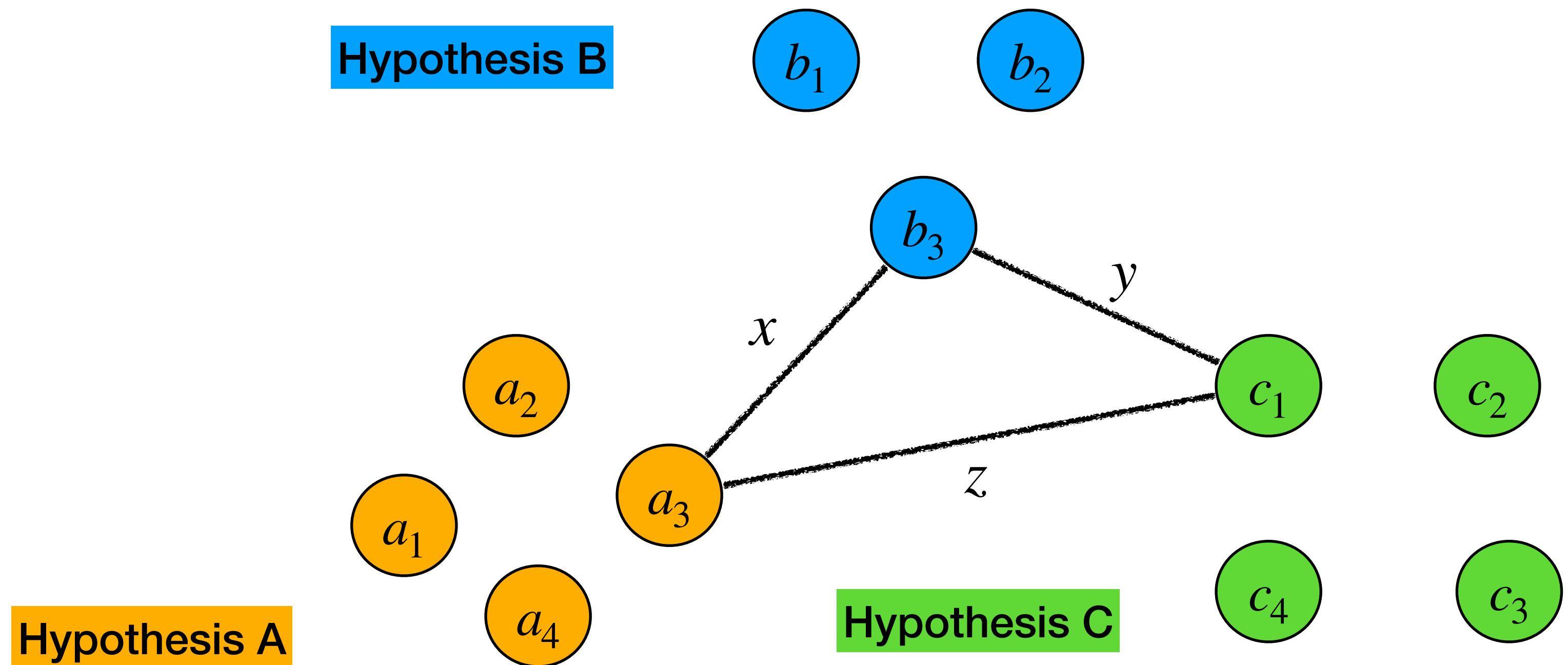
## Change incremental method to global



**Hypotheses can contain overlapping segments.**

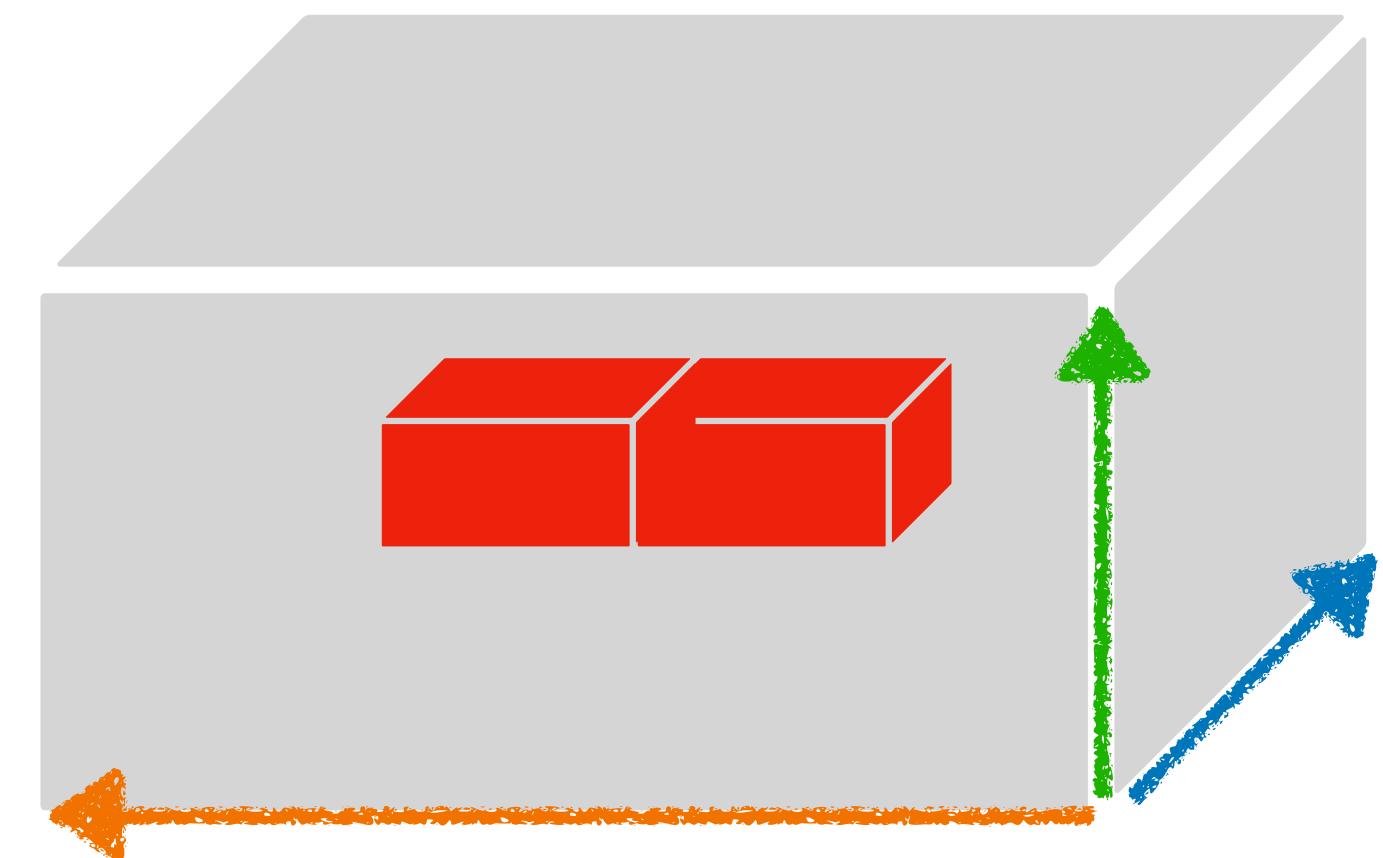
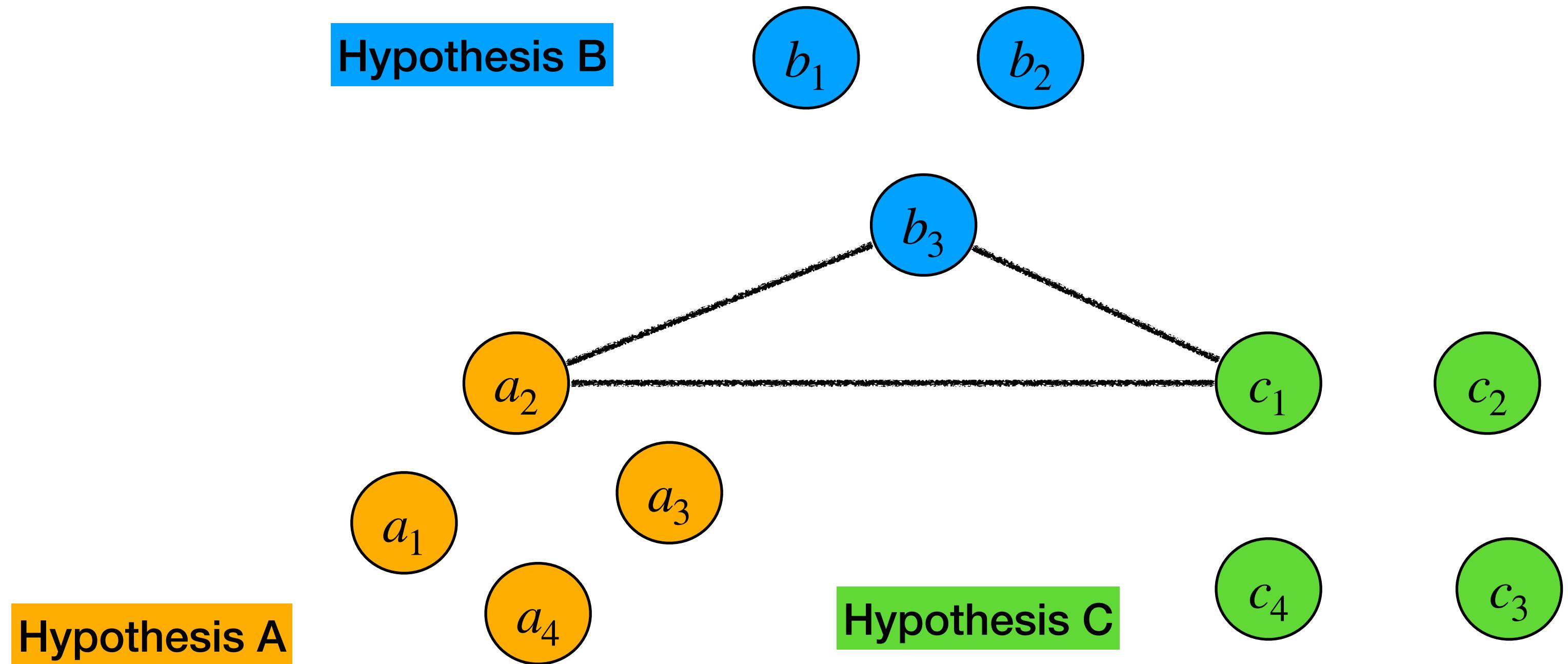
# DOVER-Lap label mapping

## Compute “tuple costs” for all tuples



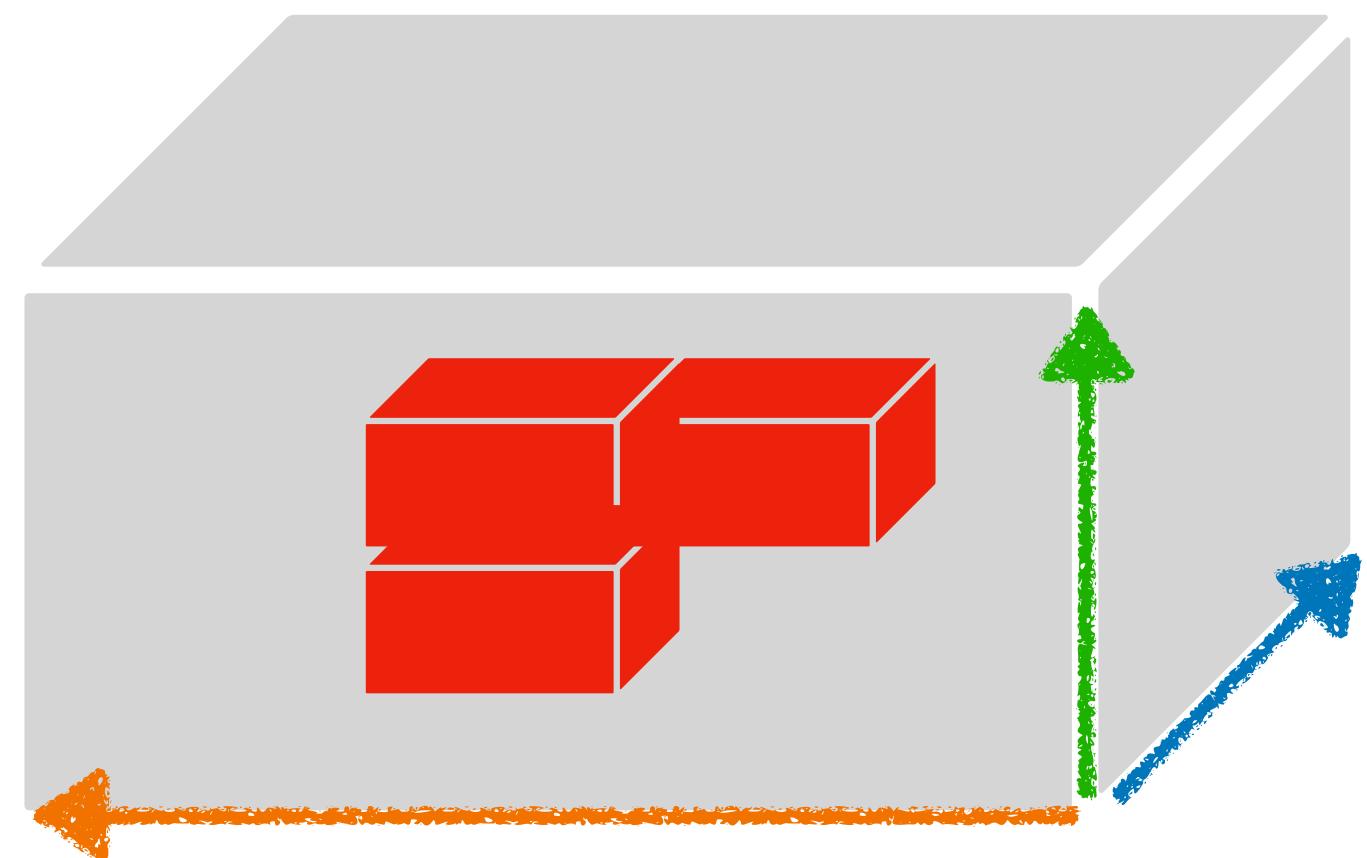
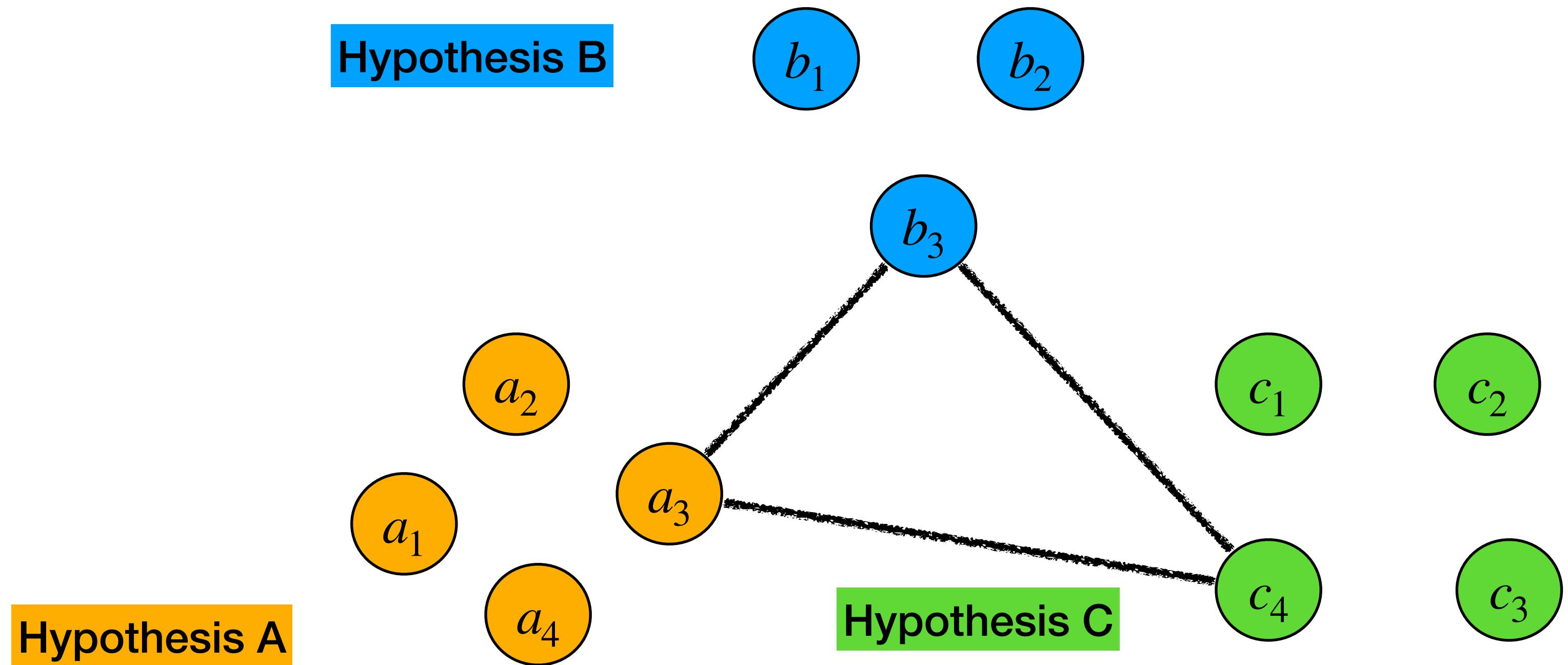
# DOVER-Lap label mapping

Compute “tuple costs” for all tuples



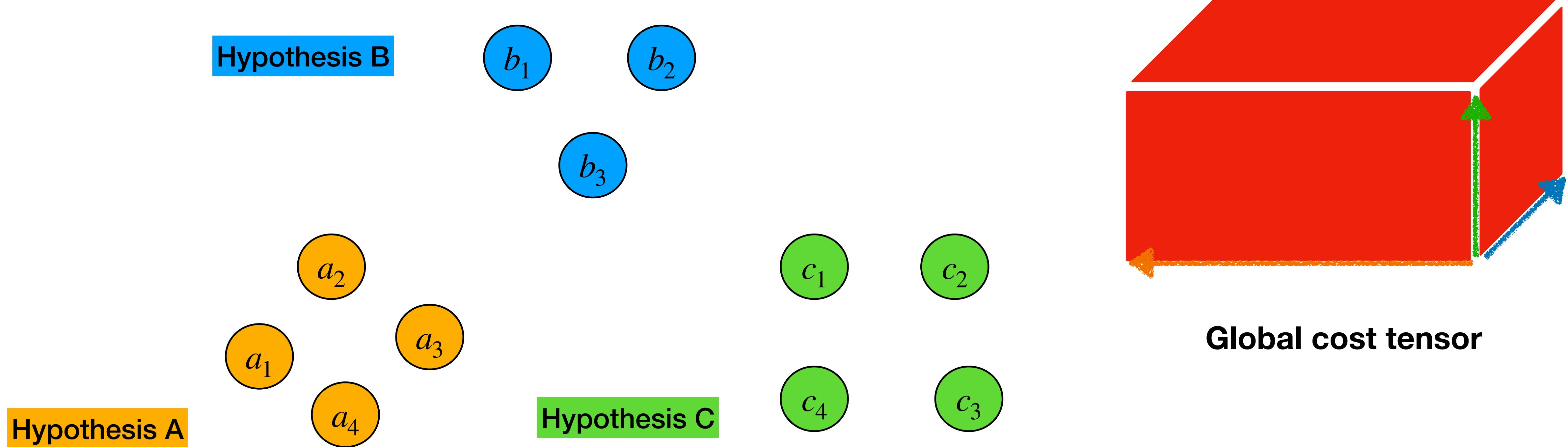
# DOVER-Lap label mapping

## Compute “tuple costs” for all tuples



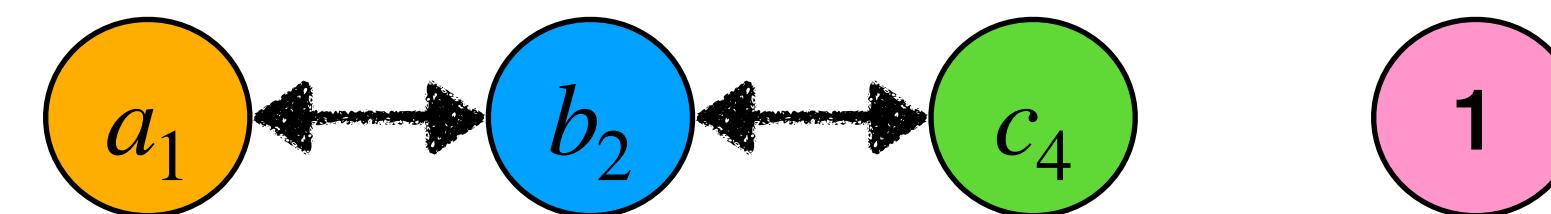
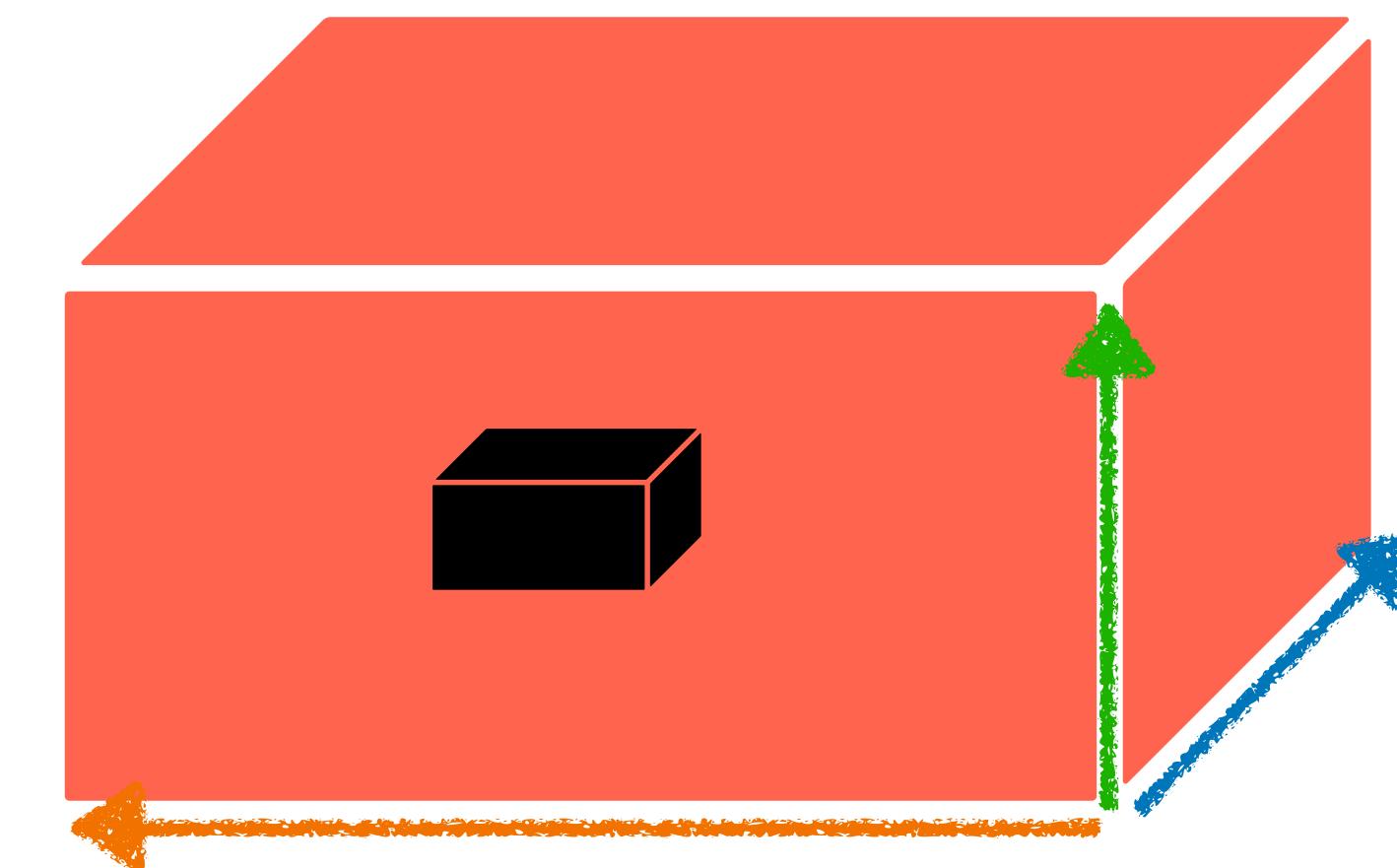
# DOVER-Lap label mapping

This gives us a “global” cost tensor



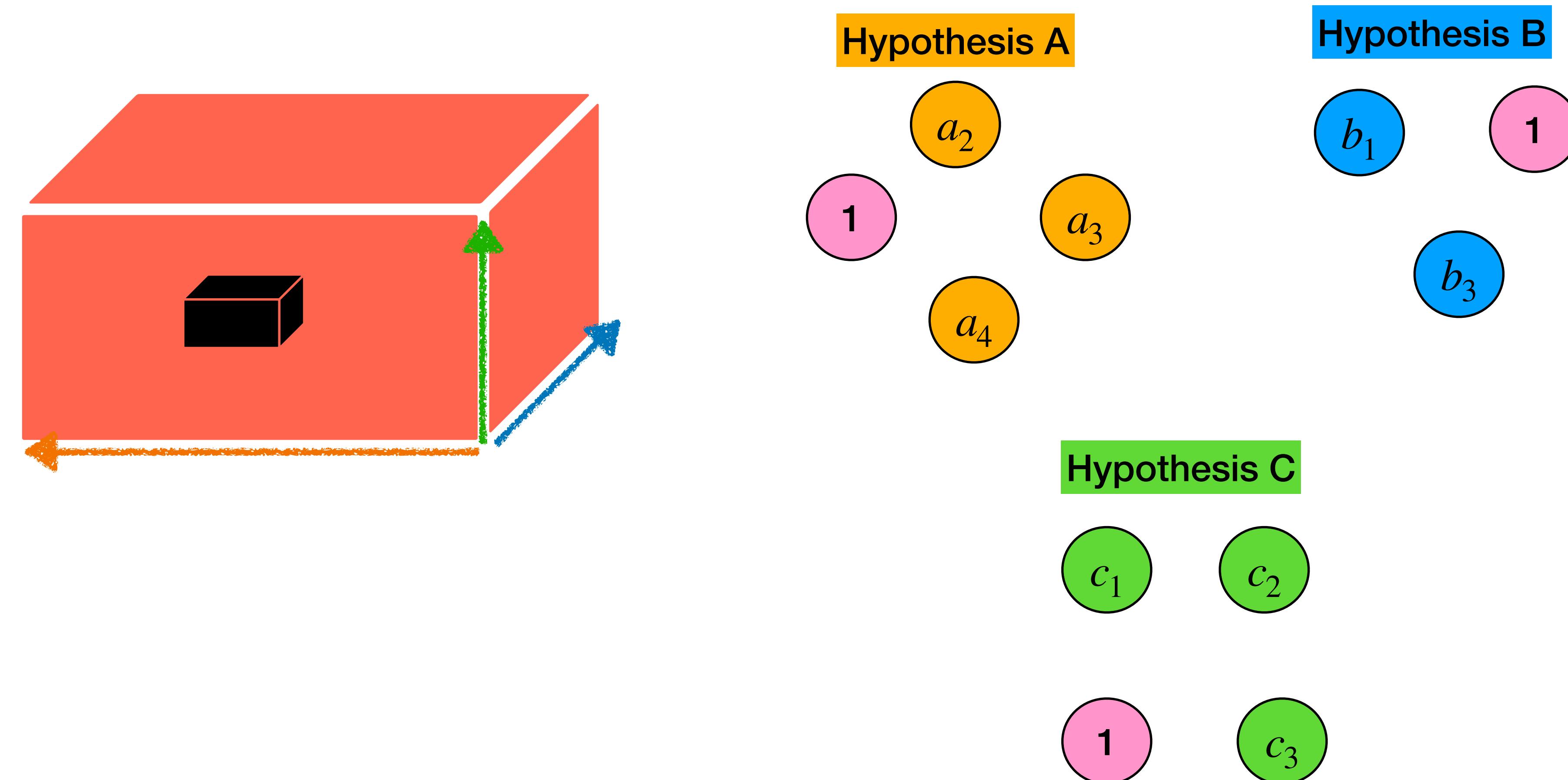
# DOVER-Lap label mapping

Pick tuple with the lowest cost and assign them same label



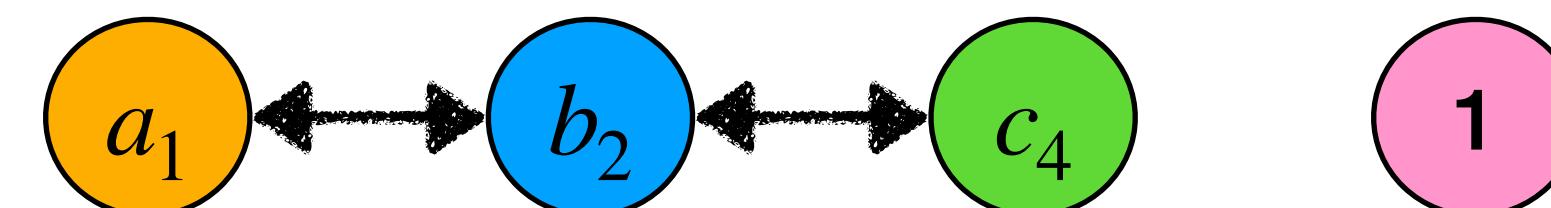
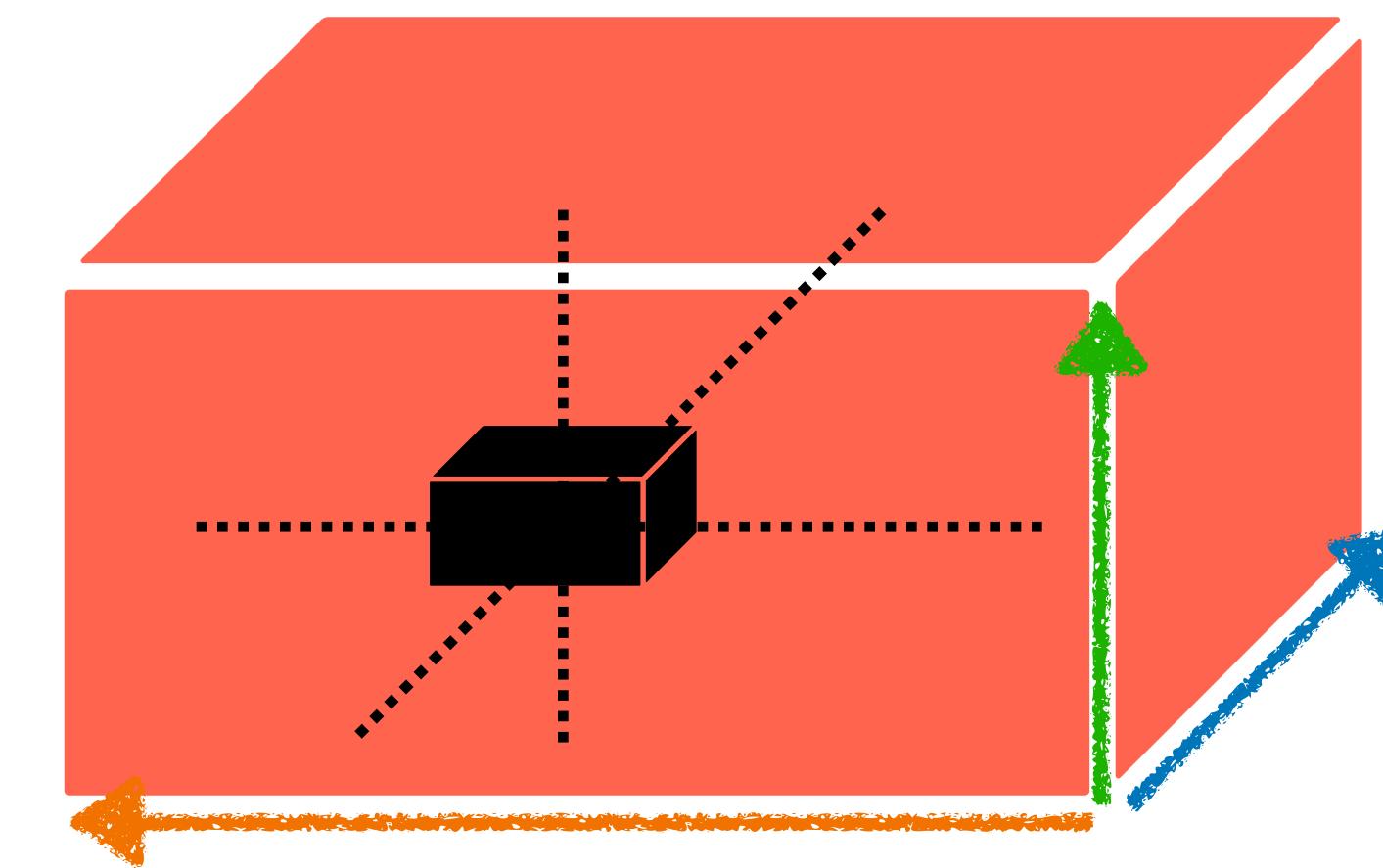
# DOVER-Lap label mapping

Pick tuple with the lowest cost and assign them same label



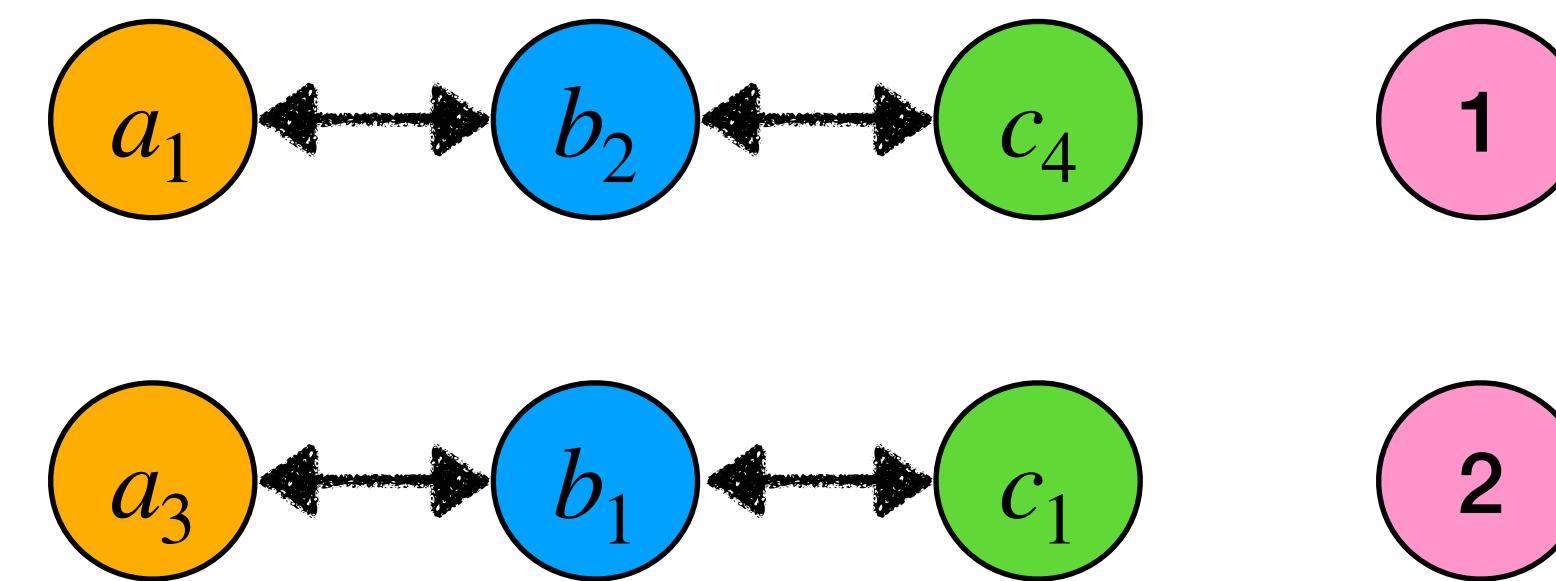
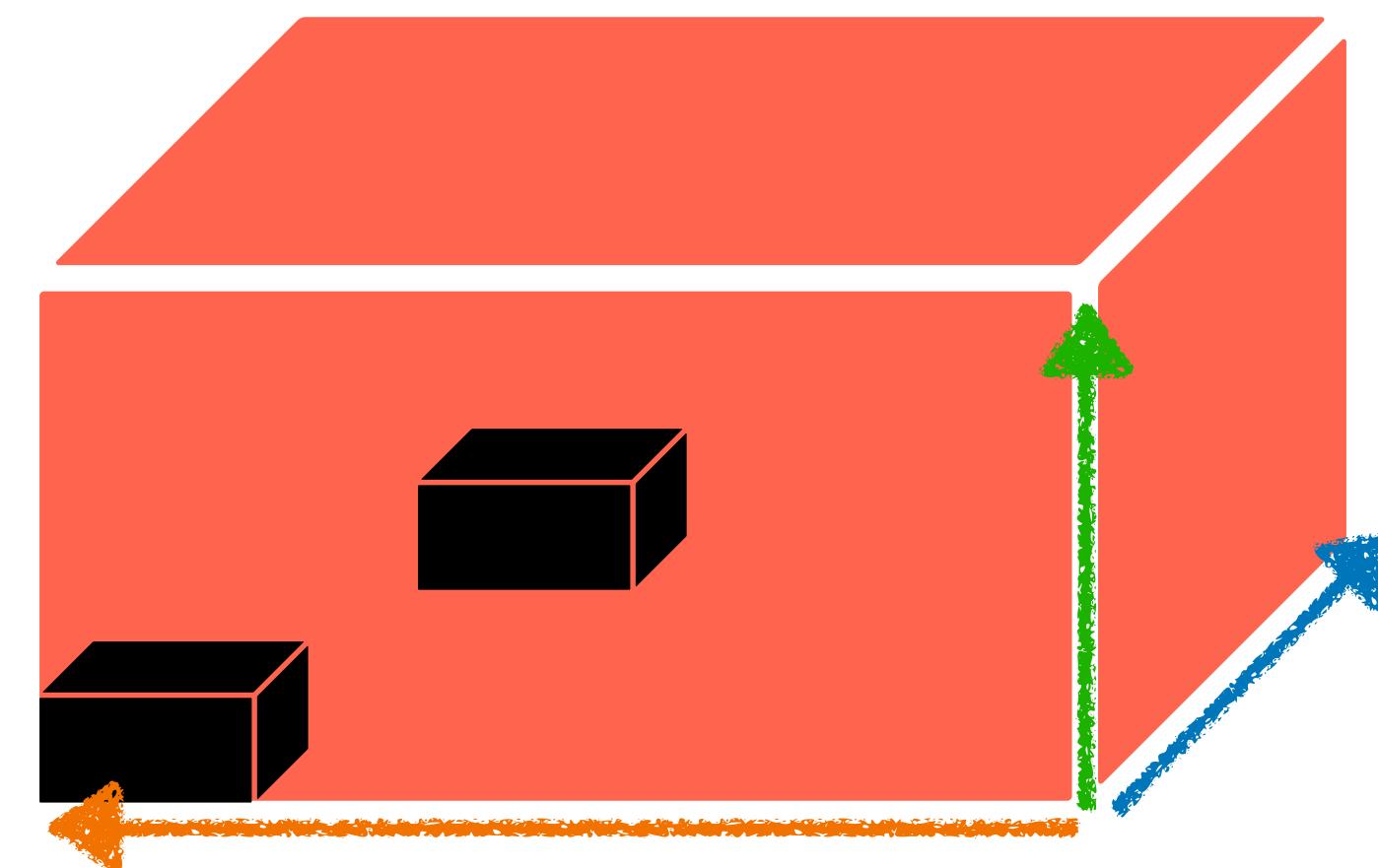
# DOVER-Lap label mapping

Discard all tuples containing these labels



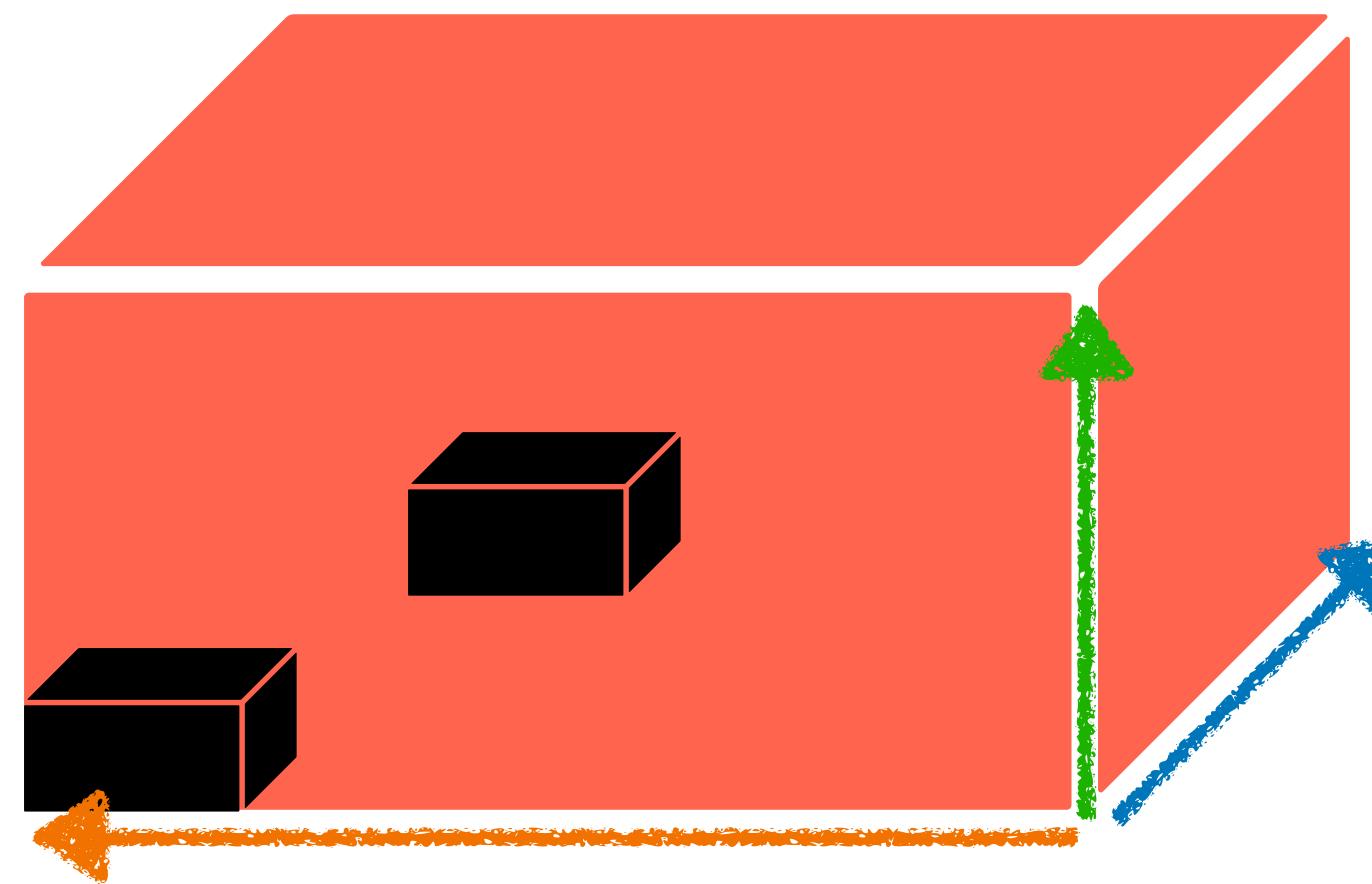
# DOVER-Lap label mapping

Pick tuple with lowest cost in remaining tensor

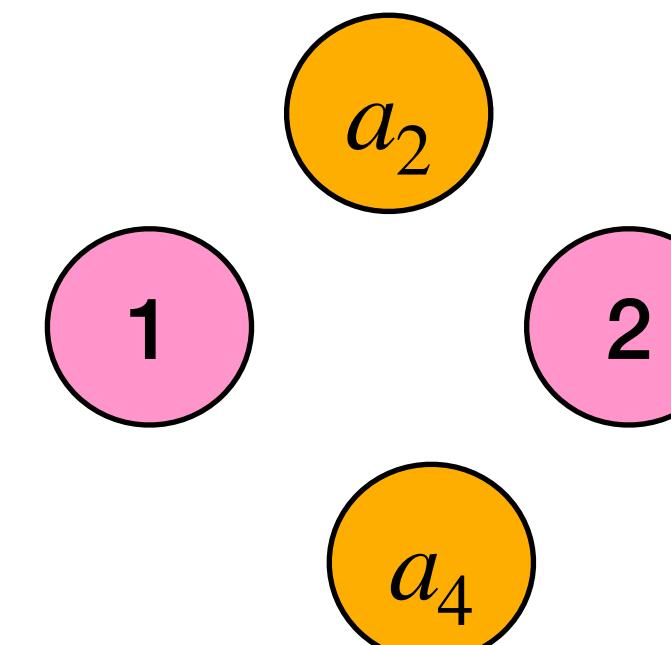


# DOVER-Lap label mapping

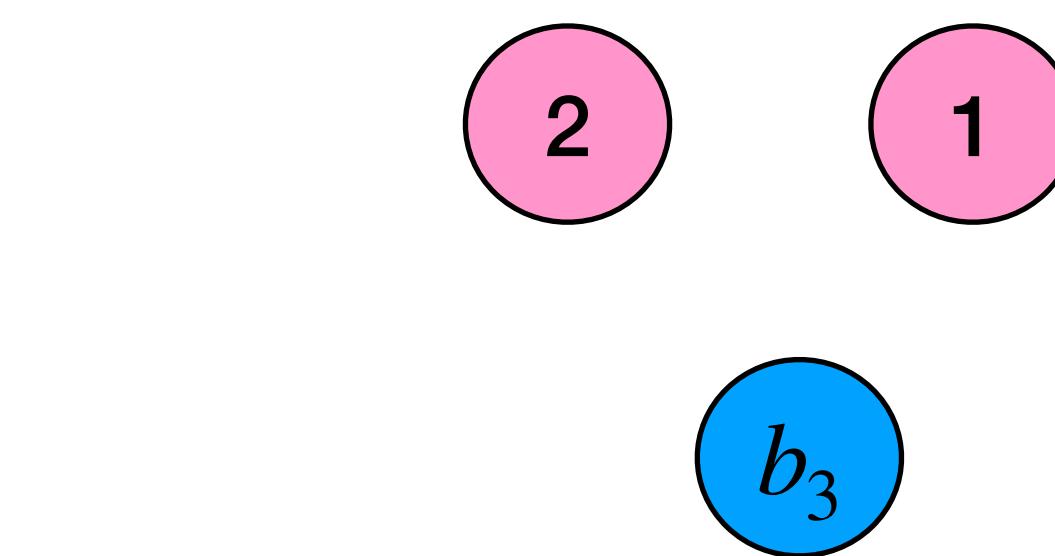
Pick tuple with lowest cost in remaining tensor



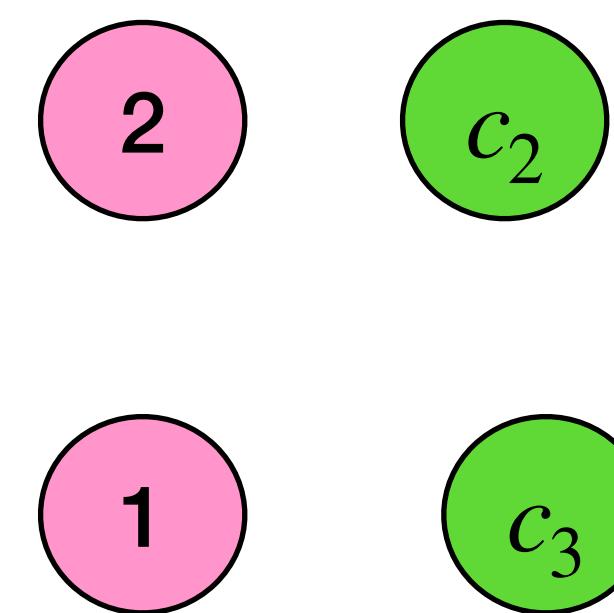
Hypothesis A



Hypothesis B

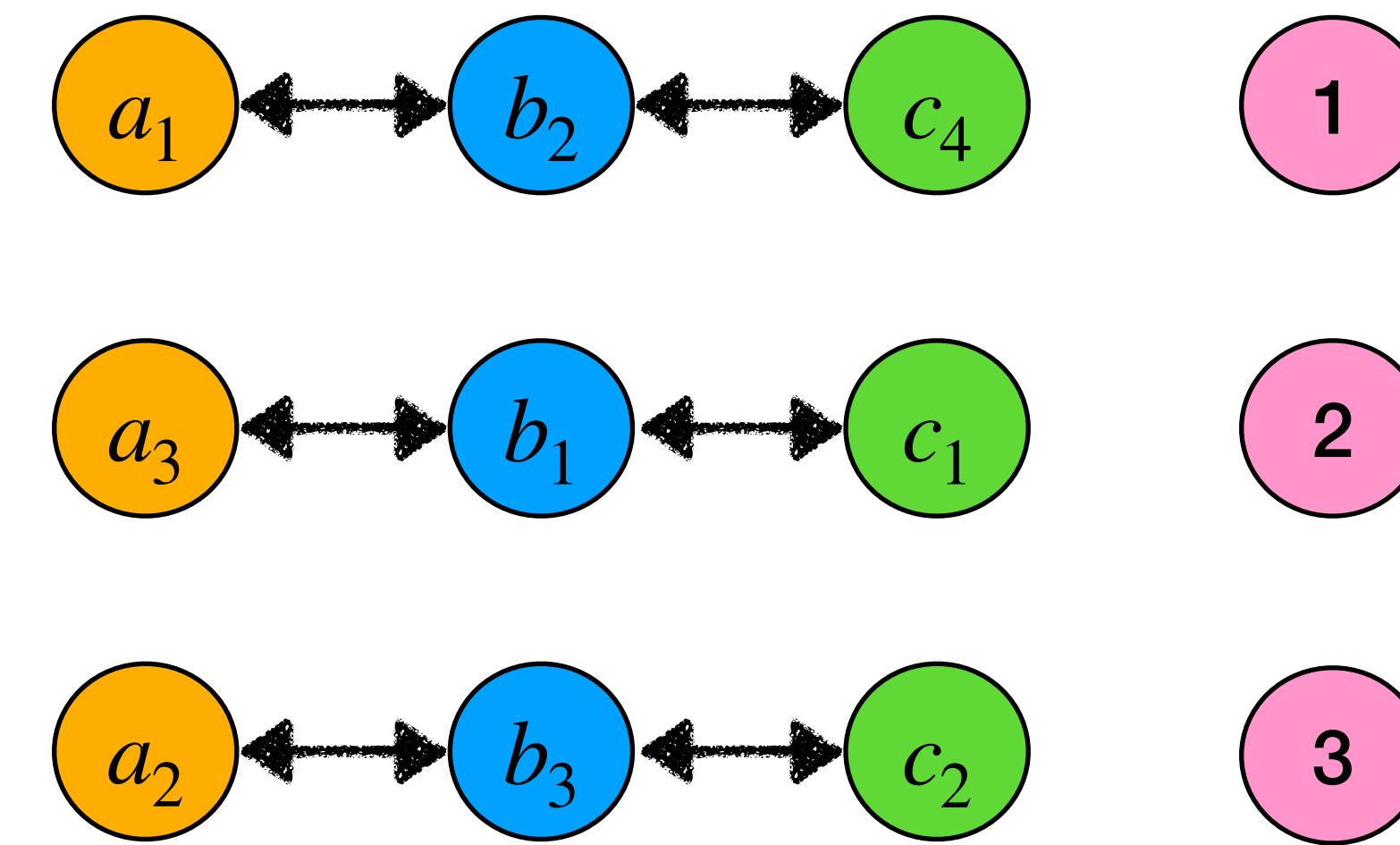
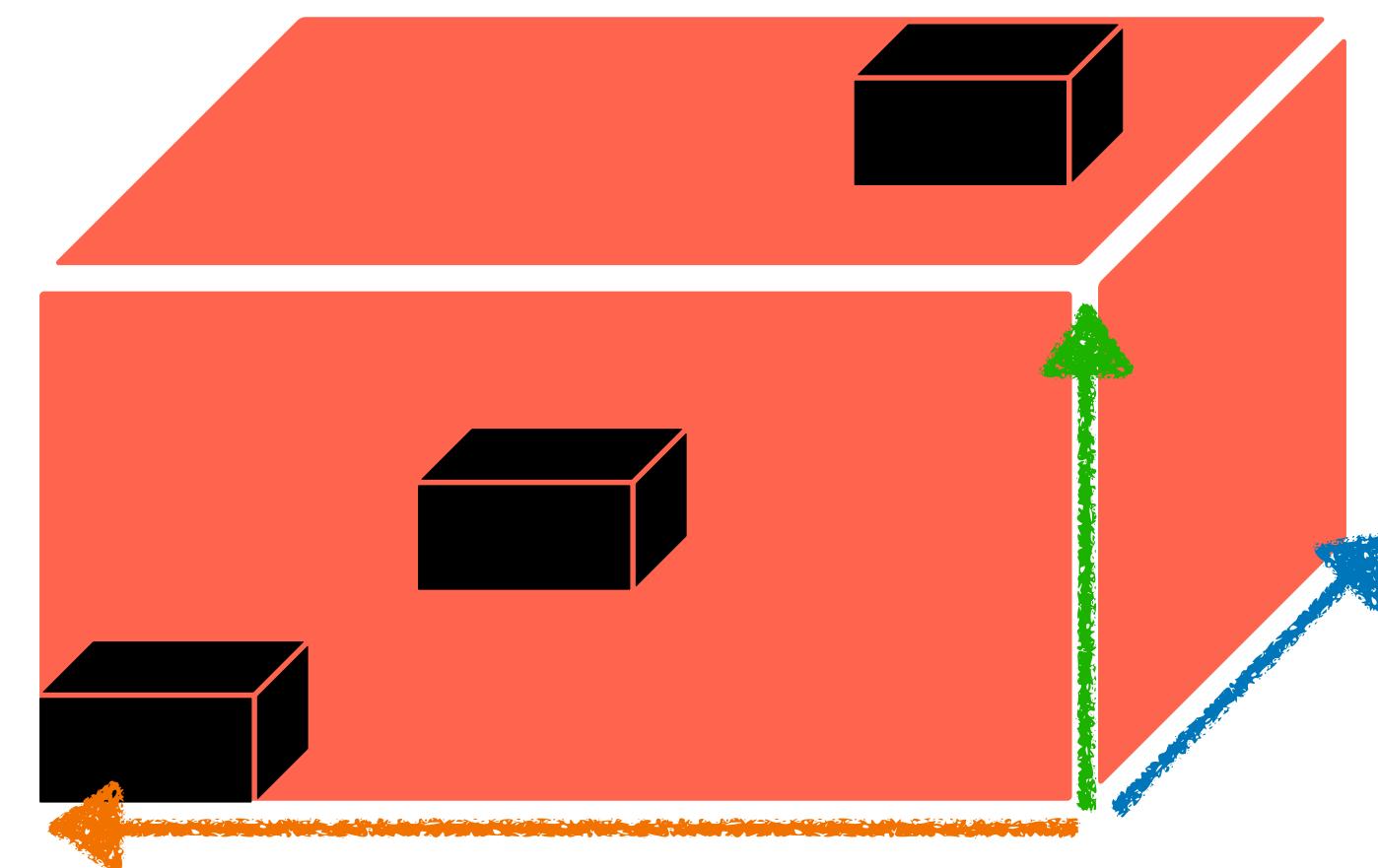


Hypothesis C



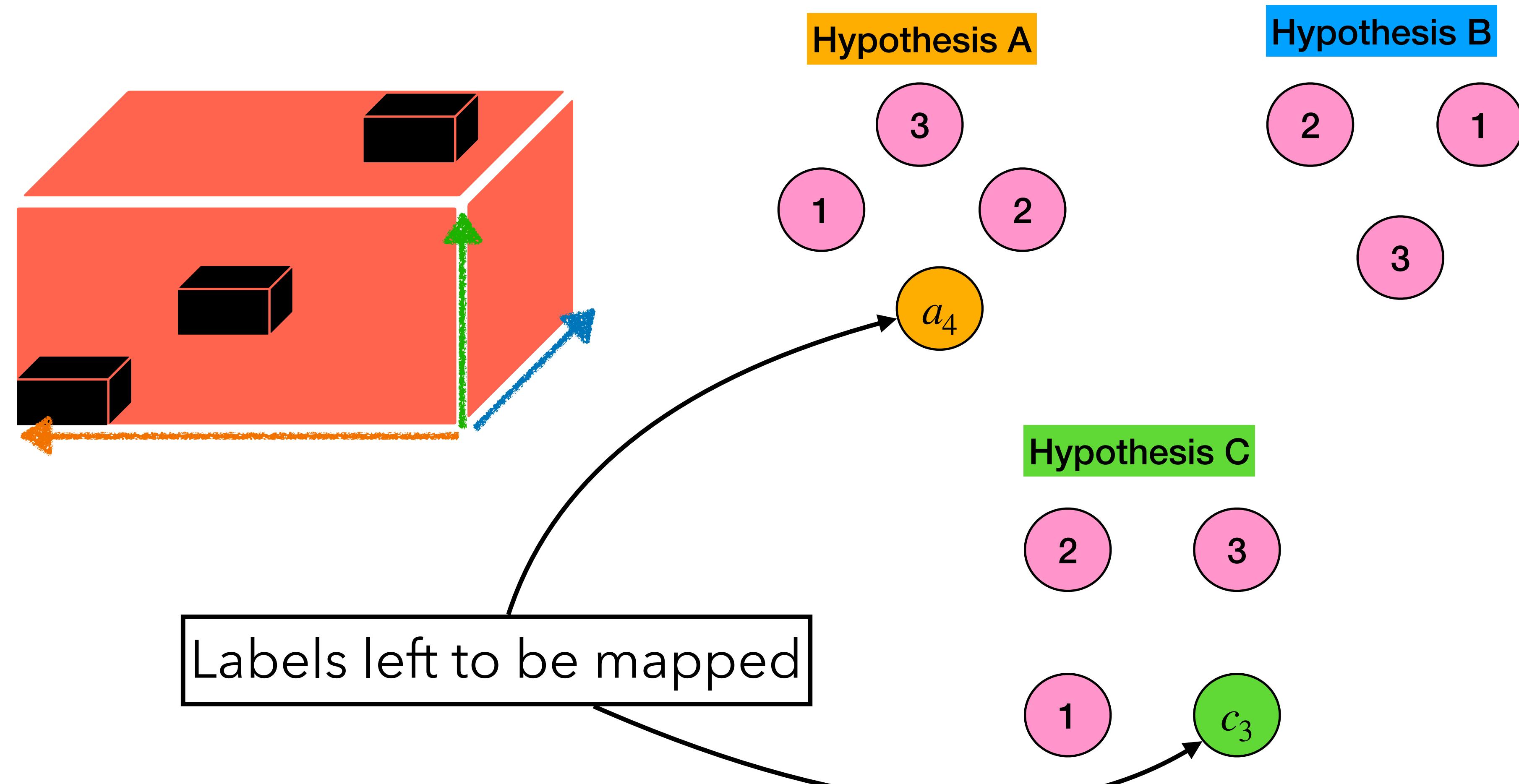
# DOVER-Lap label mapping

Repeat until no tuples are remaining



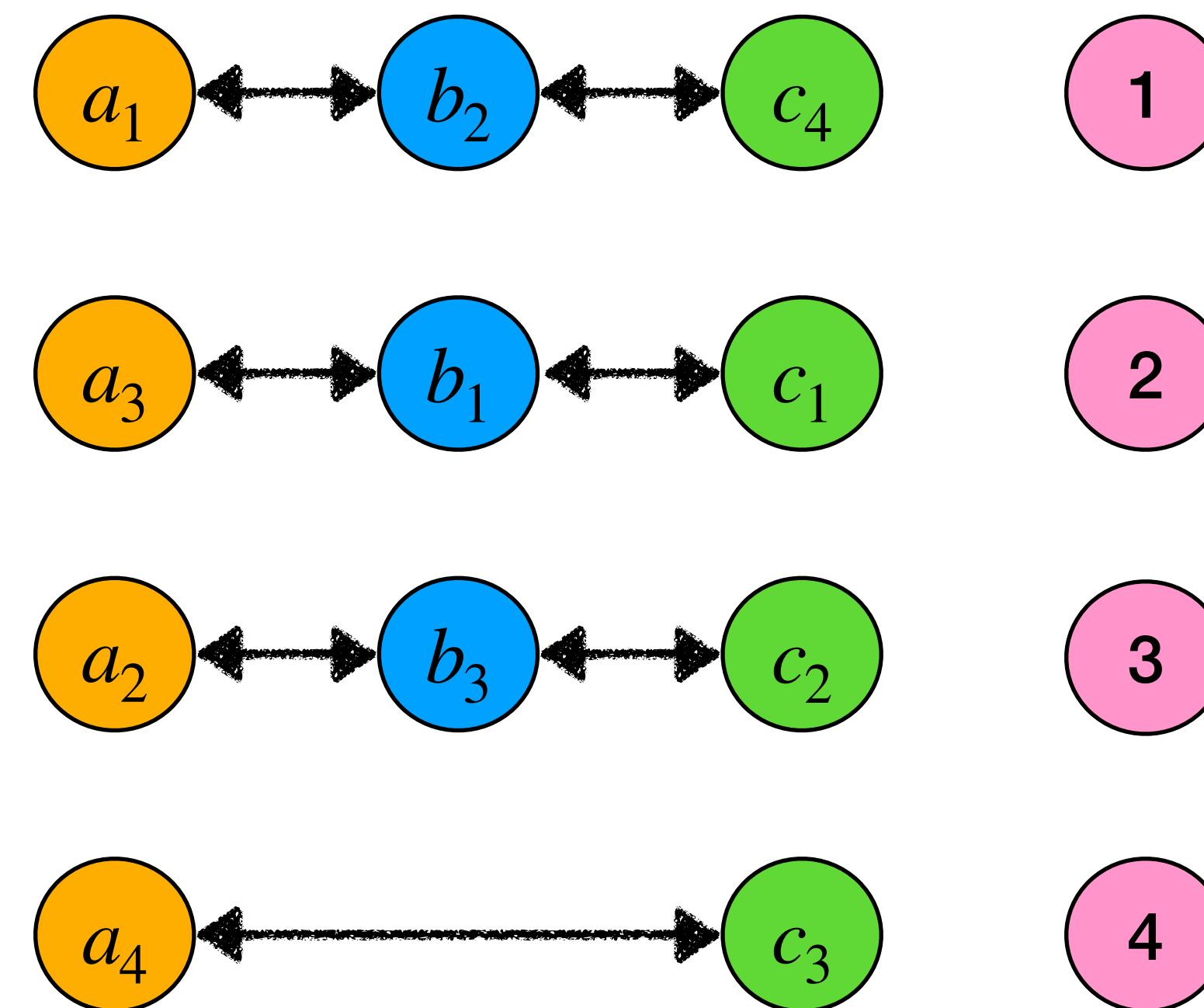
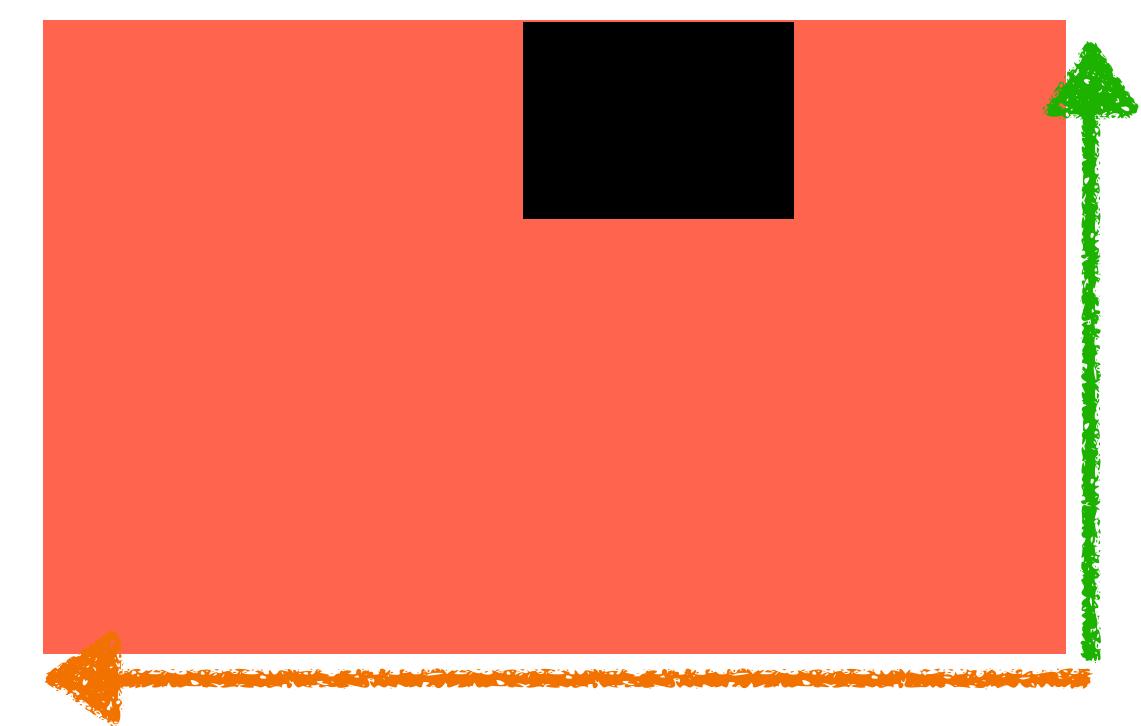
# DOVER-Lap label mapping

Repeat until no tuples are remaining



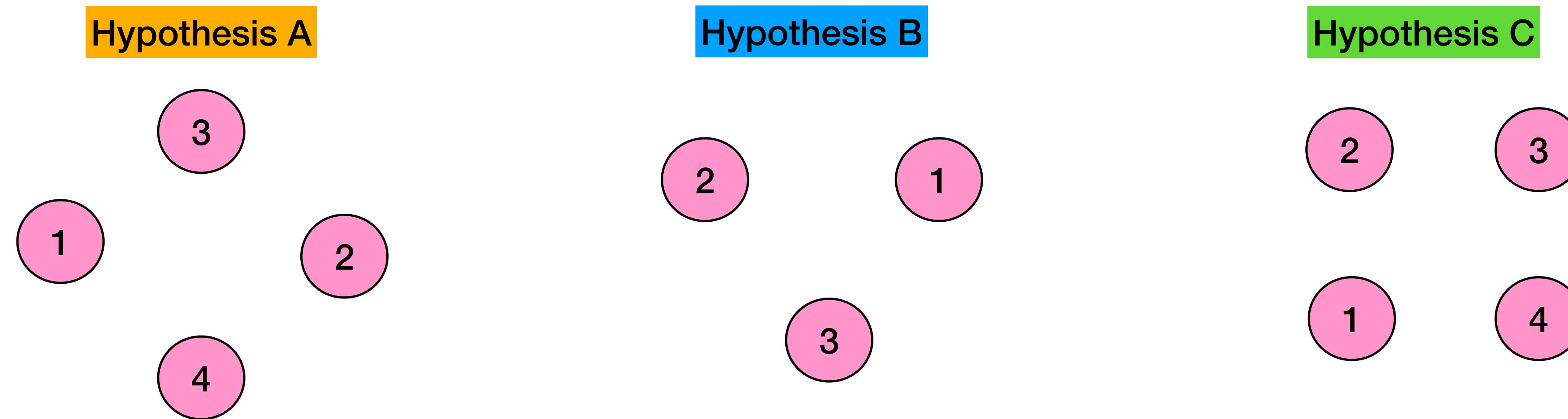
# DOVER-Lap label mapping

If no tuples remaining but labels left to be mapped, remove filled dimensions and repeat



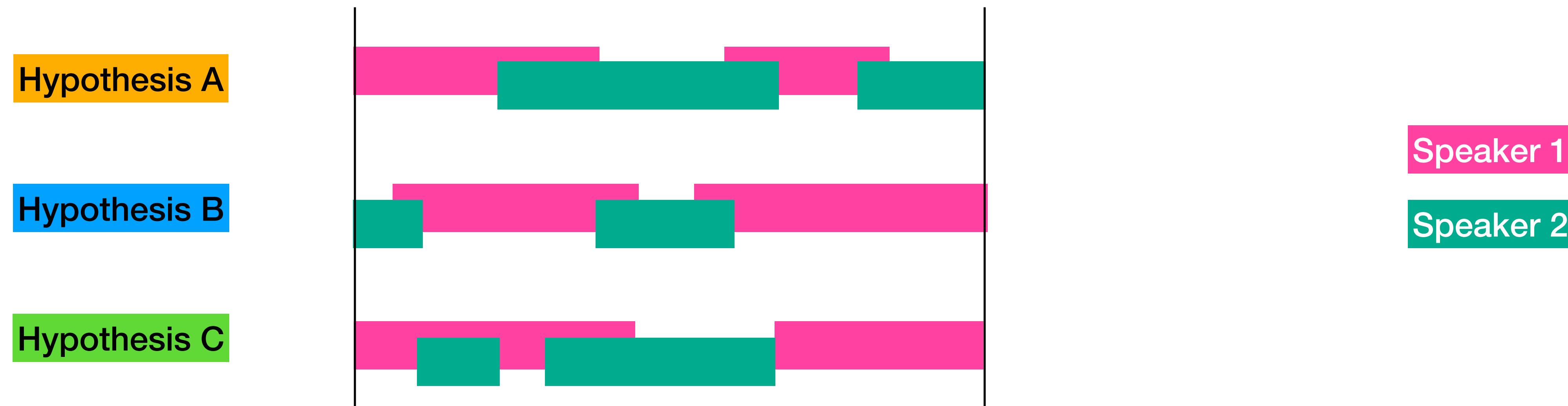
# DOVER-Lap label mapping

## Final mapped labels



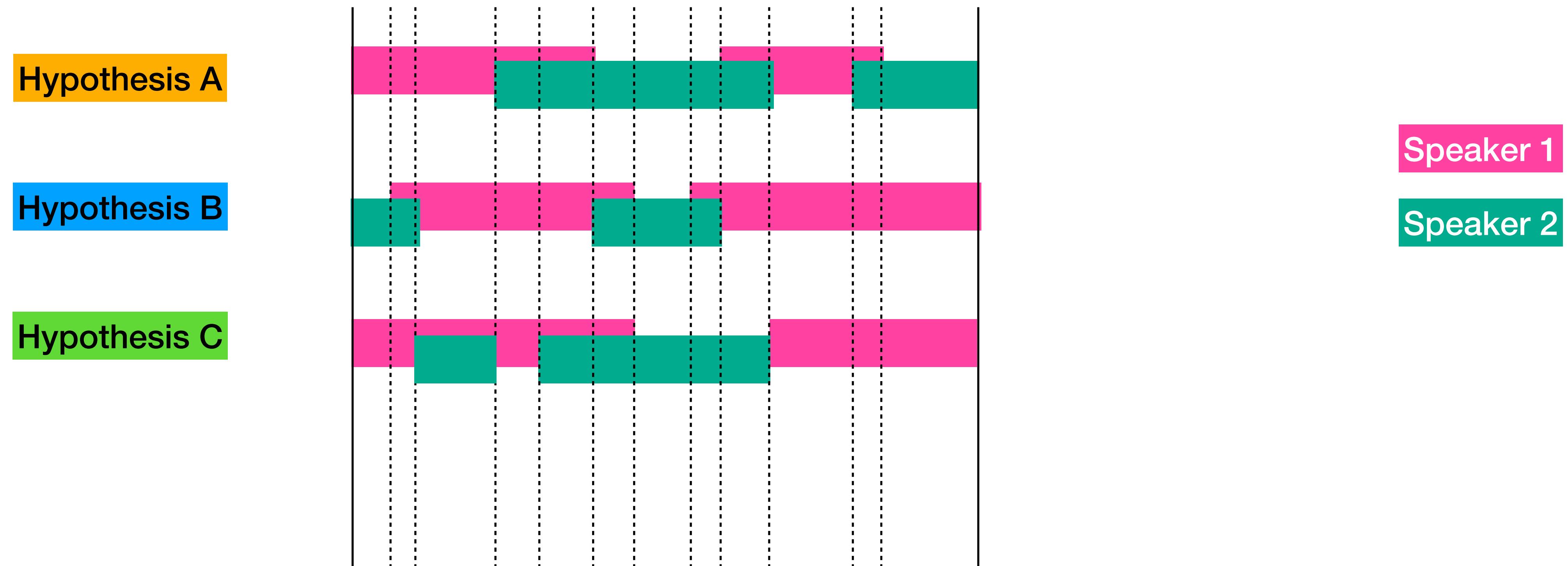
# DOVER-Lap label voting

Consider 3 hypotheses from overlap-aware diarization systems



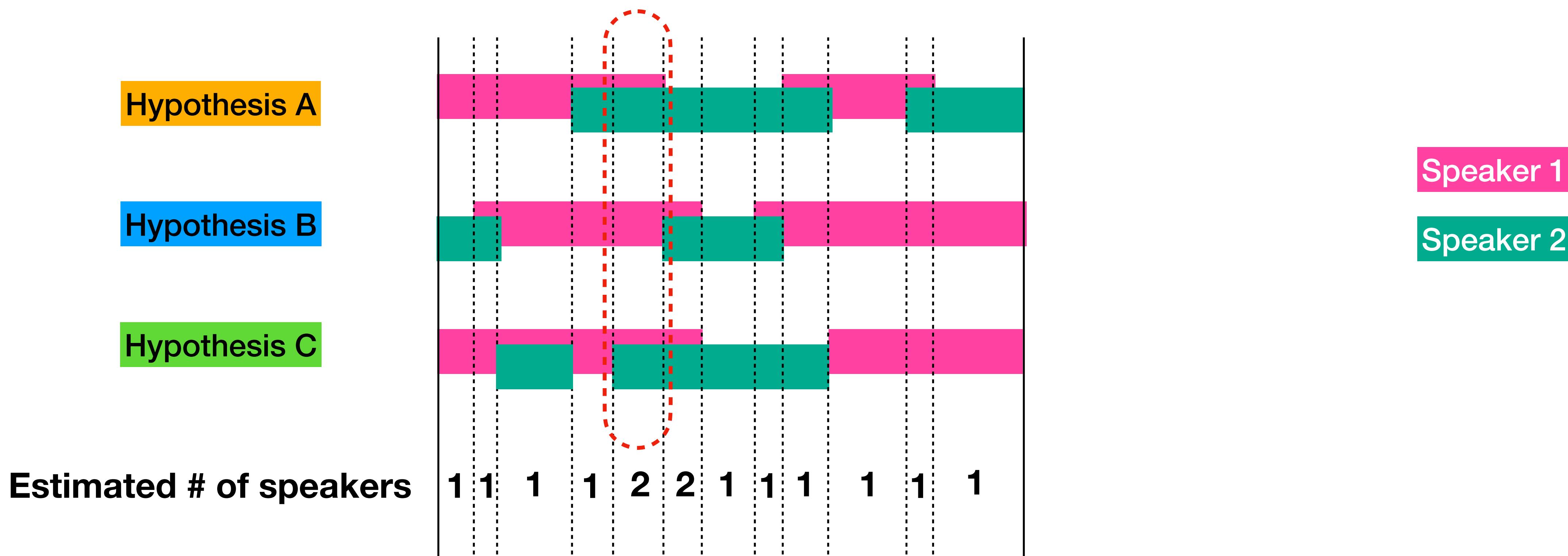
# DOVER-Lap label voting

## Divide into regions (similar to DOVER)



# DOVER-Lap label voting

## Estimate number of speakers in each region

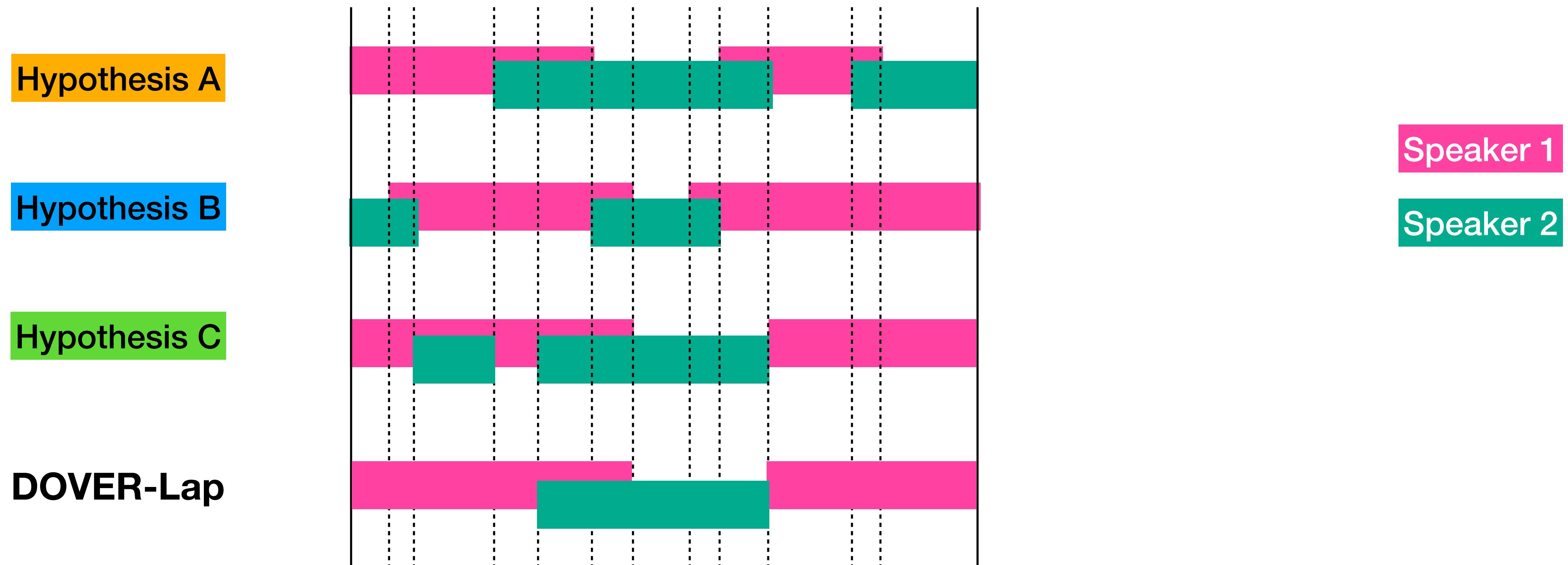


**# speakers** = weighted mean of # speakers in hypotheses

**Weights** -> obtained by ranking hypotheses by **total cost**

# DOVER-Lap label voting

Assign highest weighted N speakers in each region



# DOVER-Lap results: AMI

## Effect of global label mapping algorithm

System	Spk. conf.	DER
Overlap-aware SC	10.1	23.6
VB-based overlap assignment*	9.6	21.5
Region proposal network	8.3	25.5
Average	9.3	23.5
<b>DOVER</b>	10.6	30.5
<b>+ global label mapping</b>	5.1	25.0

AMI data contains **4-speaker meetings**

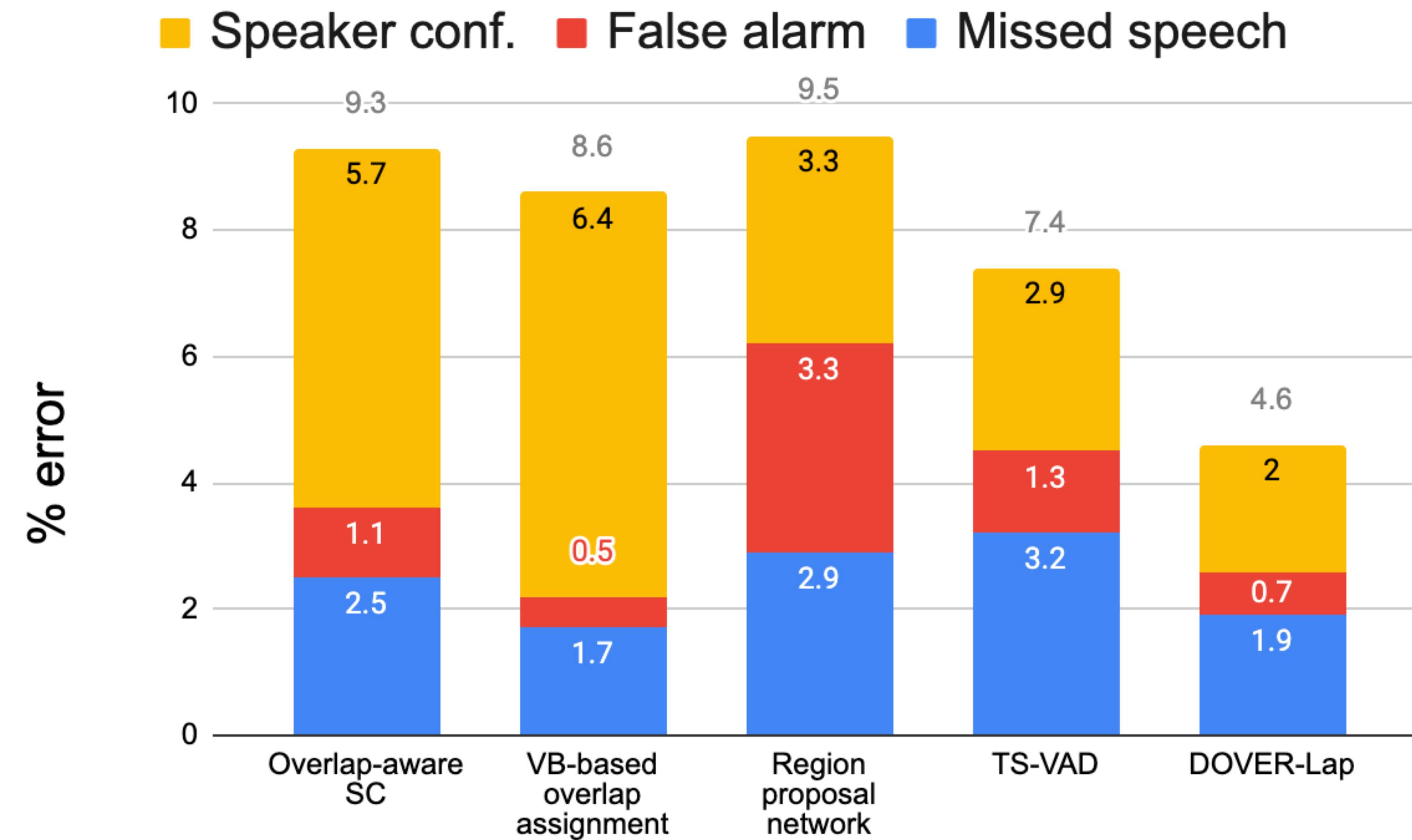
# DOVER-Lap results: AMI

## Effect of rank-weighted majority voting

System	Spk. conf.	DER
Overlap-aware SC	10.1	23.6
VB-based overlap assignment*	9.6	21.5
Region proposal network	8.3	25.5
Average	9.3	23.5
<b>DOVER</b>	10.6	30.5
+ global label mapping	5.1	25.0
<b>DOVER-Lap</b>	7.6	<b>20.3</b>

# Results: Breakdown on LibriCSS

## Effectively combines complementary strengths



LibriCSS data contains **8-speaker meetings**

# Results from DIHARD-3

Top 2 teams used DOVER-Lap for system fusion in DIHARD-3

#1: **USTC team** combined clustering, separation-based, and TS-VAD systems

#2: **Hitachi-JHU team** combined VB-based and EEND-based systems

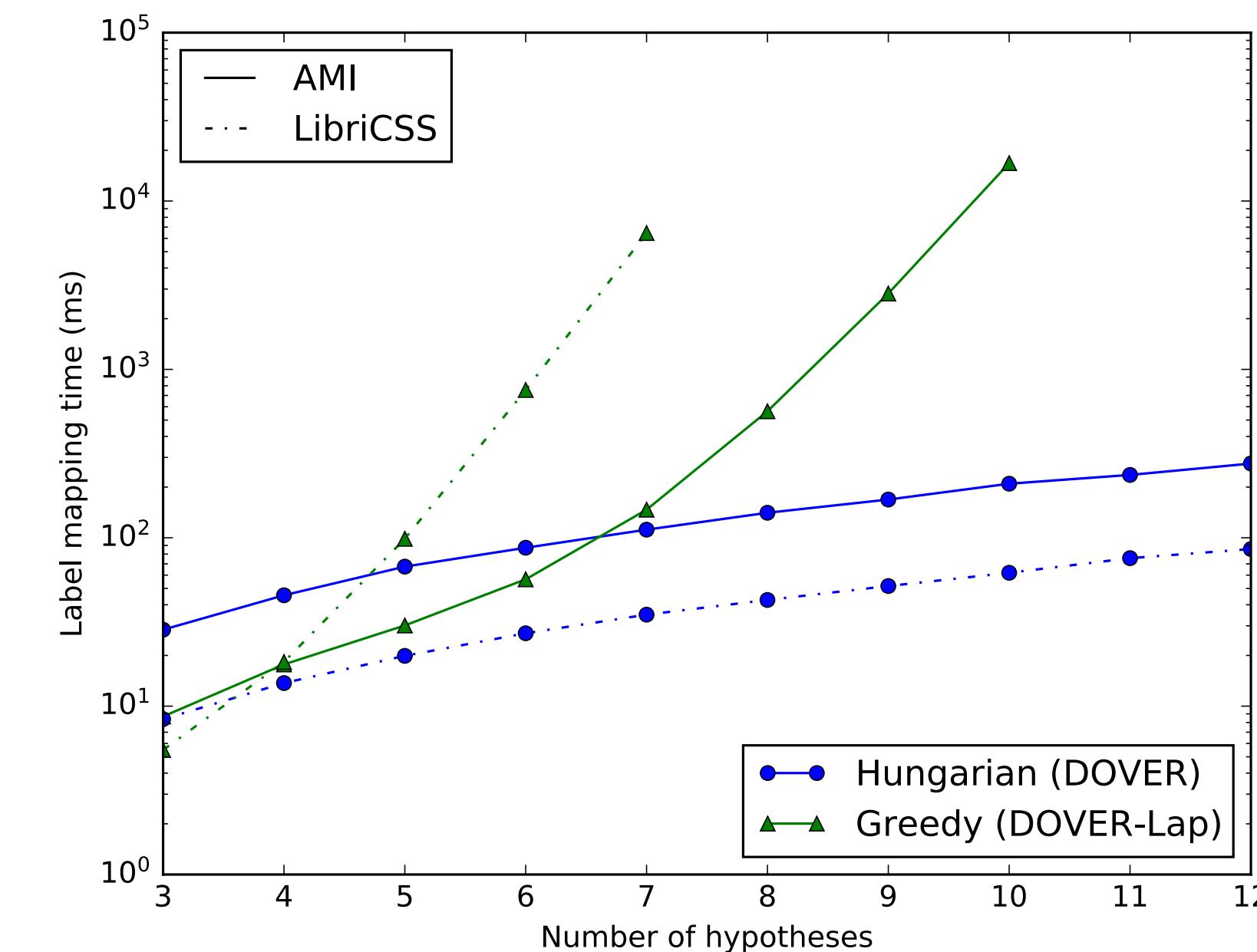
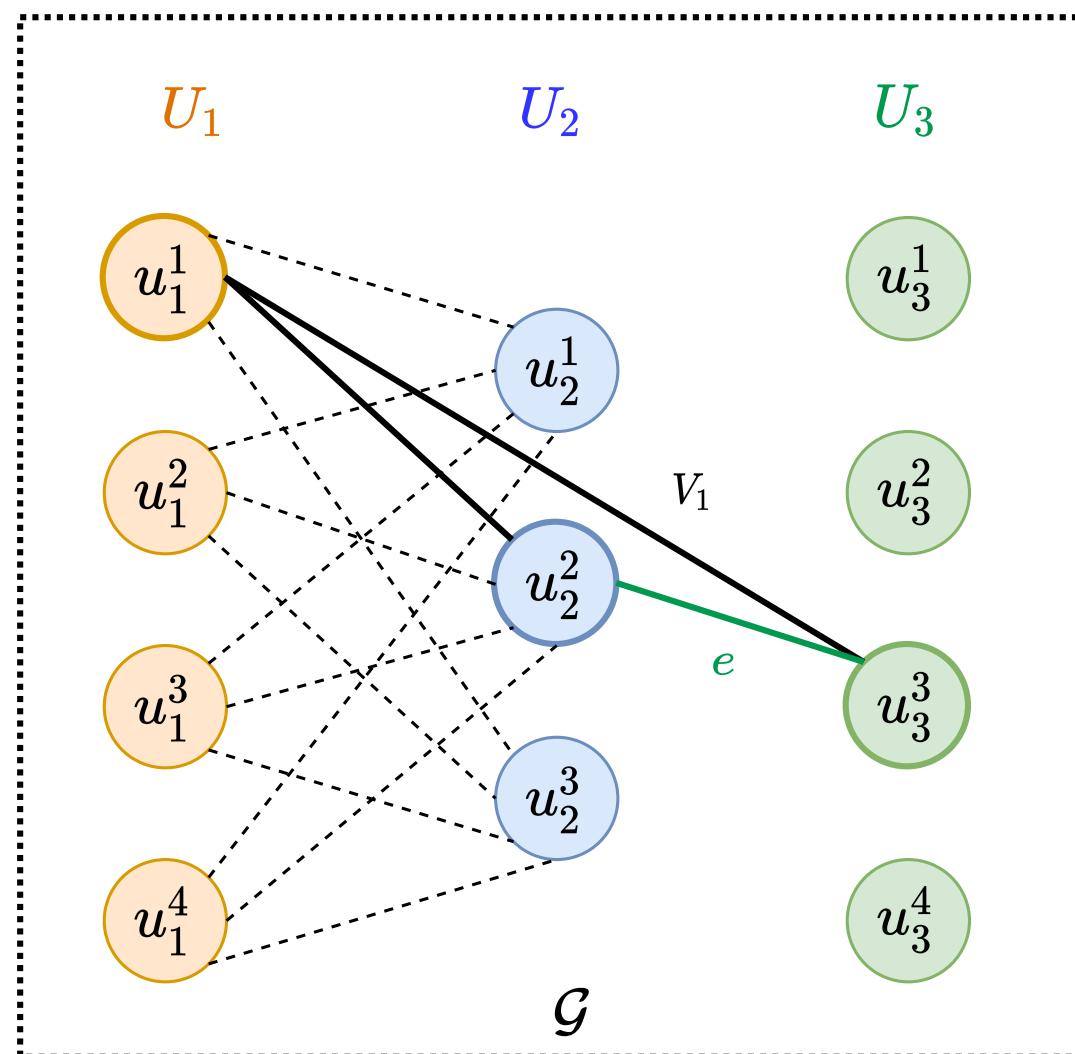


Wang, Y., et al. USTC-NELSLIP System Description for DIHARD-III Challenge. ArXiv, abs/2103.10661.

Horiguchi, S., et al. The Hitachi-JHU DIHARD III System: Competitive End-to-End Neural Diarization and X-Vector Clustering Systems Combined by DOVER-Lap. ArXiv, abs/2102.01363.

# New analysis

**Label mapping is a graph partitioning problem,  
DOVER-Lap algorithm is exponential!**



Raj, D., & Khudanpur, S. (2021). Reformulating DOVER-Lap Label Mapping as a Graph Partitioning Problem. ArXiv, abs/2104.01954.

# New analysis

## Modified Hungarian algorithm is fast and accurate

System	Spk. conf.	DER
Agglomerative Hierarchical	10.1	23.6
VB-based overlap assignment*	9.6	21.5
Region proposal network	8.3	25.5
Average	9.3	23.5
DOVER-Lap	7.6	<b>20.3</b>
<b>Hungarian (modified)</b>	8.2	<b>20.9</b>

Raj, D., & Khudanpur, S. (2021). Reformulating DOVER-Lap Label Mapping as a Graph Partitioning Problem. ArXiv, abs/2104.01954.

# A word on evaluation

<https://github.com/desh2608/spyder>

- 4-5x faster than [md-eval.pl](#) and dscore
- Use from Python or as CLI tool
- Selectively evaluate on single-speaker or overlapping regions
- Other metrics (JER) coming soon...

```
import spyder

# reference (ground truth)
ref = [("A", 0.0, 2.0), # (speaker, start, end)
       ("B", 1.5, 3.5),
       ("A", 4.0, 5.1)]

# hypothesis (diarization result from your algorithm)
hyp = [("1", 0.0, 0.8),
       ("2", 0.6, 2.3),
       ("3", 2.1, 3.9),
       ("1", 3.8, 5.2)]

metrics = spyder.DER(ref, hyp)
print(metrics)
# DERMetrics(duration=5.10,miss=9.80%,falarm=21.57%,conf=25.49%,der=56.86%)
```

# Summary

**Diarization** is a useful but difficult task.

**Clustering-based systems** fall short on handling overlapping speech, but small modifications inspired from mathematical insights can change this.

**Continuous Speech Separation (CSS)** works well with clustering-based systems, but well-trained separation module is required.

**Ensembles** work. Use **DOVER-Lap** for your challenge submissions.

# Collaborators

**Overlap-aware spectral clustering:** Zili Huang, Sanjeev Khudanpur

**CSS-based diarization:** Zhuo Chen, Hakan Erdogan, Maokui He, Zili Huang, Shinji Watanabe

**DOVER-Lap:** Paola Garcia, Zili Huang, Shinji Watanabe, Dan Povey, Andreas Stolcke, Sanjeev Khudanpur

# Acknowledgments

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Special thanks to:

**Takuya Yoshioka** (Microsoft), for providing data simulation scripts.

**Shota Horiguchi** (Hitachi) for suggesting a modification for DOVER-Lap.