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UNIVERSITY

PCT COLLABORATION DOCUMENTATION

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## DATA ACQUISITION/PROCESSING AND IMAGE RECONSTRUCTION SOFTWARE: THEORY AND IMPLEMENTATION DETAILS

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BLAKE EDWARD SCHULTZE

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The logo for Baylor University Engineering & Computer Science. It features a green circle at the top, a large orange swoosh on the left, and the text 'Baylor University Engineering & Computer Science' in a serif font. A large, faint 'E' is visible in the background.

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# Part I

## Image Reconstruction



## **1.1 : INITIAL ITERATE**

## **1.2 : ITERATIVE PROJECTION ALGORITHMS**

### **1.2.1 SEQUENTIAL PROJECTION ALGORITHMS**

## 1.2.2 BLOCK-ITERATIVE PROJECTION ALGORITHMS

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### Block-Iterative Algorithms: Notation

- $m$  : total # of proton histories
- $n$  : total # of image vector voxels
- $B$  : total # of BIP blocks
- $\{a:b\} = \{i \mid i \in [a,b]\}$  : interval of indices
- $A_{*,j}$  : Column vector composed of all  $*$  = 1: $m$  rows of the  $j$ -th column of the matrix  $A$
- $A_{i,*}$  : Row vector composed of all  $*$  = 1: $n$  columns of the  $i$ -th row of the matrix  $A$
- $A_{\{a:b\},j}$  : Column vector composed of the interval  $a:b$  of rows of the  $j$ -th column of the matrix  $A$
- $A_{i,\{a:b\}}$  : Row vector composed of the interval  $a:b$  of columns of the  $i$ -th row of the matrix  $A$
- $x_{(k)}$  : Image vector  $x$  at iteration  $k$
- $\mathcal{J} = \{1, 2, 3, \dots, m\}$  : the sequentially ordered set of all proton history indices
- $\mathcal{B}_{(k)} = \{1, 2, 3, \dots, B_{(k)}\}$  : the sequentially ordered set of all BIP block indices, where the # of BIP blocks  $B_{(k)}$  may vary as a function of iteration  $k$ .
- $f_{(k)} : \mathcal{J} \rightarrow \mathcal{B}_{(k)} = \left\{ f_{(k)}(1), f_{(k)}(2), f_{(k)}(3), \dots, f_{(k)}(m) \mid f_{(k)}(i) = b \in \mathcal{B}_{(k)}, i \in \mathcal{J} \right\}$  : function  $f_{(k)}$  mapping each of the  $m$  proton histories to one of the  $B_{(k)}$  BIP blocks, which may vary as a function of  $k$ , thereby establishing the # of histories in each block and the order they are processed.
- $\mathcal{M}_{b(k)} = \left\{ i \in \mathcal{J} \mid f_{(k)}(i) = b, \bigcup_{b \in \mathcal{B}_{(k)}} \mathcal{M}_{b(k)} = \mathcal{J} \right\}$  : the ordered set of proton history indices within the  $b$ -th BIP block during iteration  $k$ , assigned according to the function  $f_{(k)}$
- $\mathcal{M}_{(k)} = \left\{ \left\{ \mathcal{M}_{b(k)} \right\}_{b \in \mathcal{B}_{(k)}} \right\} = \left\{ \mathcal{M}_{1(k)}, \mathcal{M}_{2(k)}, \dots, \mathcal{M}_{B(k)} \right\}$  : the ordered family of sets of BIP blocks of proton history indices for iteration  $k$ , assigned according to the function  $f_{(k)}$
- $H_i = \left\{ x \in \mathbb{R}^n \mid \langle A_{i,*}, x \rangle = b_i, i \in \mathcal{J} \right\}$  : the hyperplanes corresponding to the  $i$ th row of the  $m \times n$  linear system  $Ax = b$  upon which the image vector  $x_{(k)}$  is projected

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