# Homework Assignment N°1

AML3
Thibault Douzon
Georgios Lioutas
November 30th, 2018

## Contents

1	$\mathbf{E}\mathbf{x}\mathbf{e}$	rcise 1																	3
	1.1	Part a																	3
	1.2	Part b																	3
	1.3	Part c																	3

### 1 Exercise 1

#### 1.1 Part a

From the topology of the graph, we deduce that:

$$P(S) = \sum_{c} P(D|C=c) \sum_{d} P(I|D=d) \sum_{i} P(S|I=i) \sum_{g} P(G=g|D=d,I=i)$$

Because P(G|D=d,I=i) is a probability distribution,  $\sum_g P(G|D=d,I=i)=1$ . Our final formula is the following:

$$P(S) = \sum_{c} P(D|C = c) \sum_{d} P(I|D = d) \sum_{i} P(S|I = i)$$
$$P(S) = [s_0, s_1] = [0.516, 0.484]$$

#### 1.2 Part b

From the graph we know that

$$P(G, I = i_0) = \sum_{c} P(D|C = c) \sum_{d} P(I|D = d) P(G|D = d, I = i_0) \sum_{s} P(S|I = i_0)$$

Once again,  $P(S|I=i_0)$  is a probability distribution, then

$$P(G, I = i_0) = \sum_{c} P(D|C = c) \sum_{d} P(I|D = d) P(G|D = d, I = i_0)$$

$$P(G, I = i_0) = [p(g_0|i_0), p(g_1|i_0), p(g_2|i_0)] = [0.1384, 0.2272, 0.2024]$$

Because it is not a probability distribution, its sum is not 1. From Bayes rule we know that by dividing by  $P(I=i_0)$  we would obtain  $P(G|I=i_0)$  which is a distribution.

$$P(G|I=i_0) = \frac{P(G,I=i_0)}{P(I=i_0)} = \frac{P(G,I=i_0)}{\sum_g P(G,I=i_0)} = \frac{P(G,I=i_0)}{0.568}$$

$$P(G|I=i_0) = [0.244, 0.4, 0.356]$$

Which adds up to 1 accordingly.

#### 1.3 Part c

Same process as before:

$$P(S, G = g_0) = \sum_{c} P(D|C = c) \sum_{d} P(I|D = d) \sum_{i} P(G = g_0|D = d, I = i) P(S|I = i)$$

$$P(S, G = g_0) = [p(s_0|g_0), p(s_1|g_0)] = [0.245, 0.148]$$

Because it is not a probability distribution, its sum is not 1. From Bayes rule we know that by dividing by  $P(G=g_0)$  we would obtain  $P(S|G=g_0)$  which is a distribution.

$$P(S|G = g_0) = \frac{P(S, G = g_0)}{P(G = g_0)} = \frac{P(S, G = g_0)}{\sum_{s} P(S, G = g_0)} = \frac{P(S, G = g_0)}{0.393}$$
$$P(S|G = g_0) = [0.624, 0.376]$$

Which adds up to 1 accordingly.