

समतलीय सतह (Plane Surfaces)

5.1 त्रिभुजको क्षेत्रफल (Area of Triangle)

केही महत्वपूर्ण सुत्रहरू (Some Important Formulae)

- ΔABC को चित्रमा

BC आधारमा = b र यसको उचाई (AD) = h भए

In the figure of ΔABC of base (BC) = b and its height (AD) = h

$$\therefore \text{Area of } \Delta ABC = \frac{1}{2} \text{ base} \times \text{height}$$

$$= \frac{1}{2} bh$$

- दिइएको चित्र ΔABC मा

$BC = a$ $AB = c$ र $AC = b$ भए

$$\text{परिमिति (p)} = a + b + c \text{ र अर्धपरिमिति (S)} = \frac{a + b + c}{2}$$

In the given figure of ΔABC $BC = a$ $AB = c$ and $AC = b$

$$\text{Perimeter (p)} = a + b + c \text{ and semiperimeter (s)} = \frac{a + b + c}{2}$$

$$\text{Area of triangle (A)} = \sqrt{s(s-a)(s-b)(s-c)}$$

- दिएको समबाहु ΔABC मा $AB = BC = AC = a$ भए

$$\text{परिमिति (p)} = 3a \text{ र अर्धपरिमिति (s)} = \frac{3a}{2}$$

$$\text{समबाहु } \Delta BAC \text{ को क्षेत्रफल (A)} = \sqrt{s(s-a)(s-a)(s-a)}$$

OR

$$\text{समबाहु } \Delta ABC \text{ को क्षेत्रफल (A)} = \frac{\sqrt{3}}{4} a^2$$

If in given an equilateral ΔABC $AB = BC = CA = a$, then

$$\text{Perimeter (p)} = 3a \text{ semiperimeter (s)} = \frac{3a}{2}$$

$$\text{Area of an equilateral } \Delta ABC (A) = \sqrt{s(s-a)(s-a)(s-a)}$$

OR

$$\text{Area of an equilateral } \Delta ABC (A) = \frac{\sqrt{3}}{4} a^2$$

- दिइएको समद्विबाहु ΔABC मा $AB = BC = a$ र $AC = b$ भए परिमिति

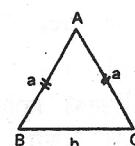
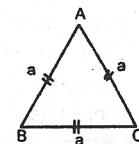
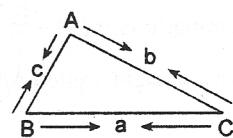
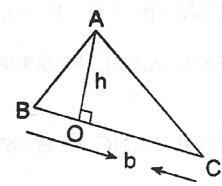
$$(p) = 2a + b \text{ अर्धपरिमिति (s)} = \frac{2a + b}{2}$$

OR

$$\text{समद्विबाहु } \Delta ABC \text{ को क्षेत्रफल (A)} = \sqrt{s(s-a)(s-a)(s-b)}$$

$$\text{समद्विबाहु } \Delta ABC \text{ को क्षेत्रफल} = \frac{b}{4} \sqrt{4a^2 - b^2}$$

In the given in isosceles ΔABC $AB = AC = a$ and $BC = b$



$$\text{Perimeter (p)} = 2a+b, \text{ semiperimeter (s)} = \frac{2a+b}{2}$$

$$\text{Area of an isosceles } \triangle ABC (A) = \sqrt{s(s-a)(s-a)(s-b)}$$

OR

$$\text{Area of an isosceles } \triangle ABC (A) = \frac{b}{4} \sqrt{4a^2 - b^2}$$

- दिइएको समकोण $\triangle ABC$ मा $\angle ABC = 90^\circ$
 $AB = p, BC = b$ भए

$$\text{परिमिति (p)} = h + P + b, \text{ अर्धपरिमिति (s)} = \frac{h + p + b}{2}$$

$$\text{समकोण } \triangle ABC \text{ को क्षेत्रफल (A)} = \sqrt{s(s-h)(s-p)(s-b)}$$

OR

$$\text{समकोण } \triangle ABC \text{ को क्षेत्रफल (A)} = \frac{1}{2}(b \times p)$$

In the right angled $\triangle ABC$ $\angle ABC = 90^\circ$ $AB = p$ and $BC = b$, perimeter (p) = $h + b + p$,
 semiperimeter (S) = $\frac{h + p + b}{2}$

$$\text{Area of right angled } \triangle ABC = \sqrt{s(s-h)(s-p)(s-b)}$$

OR

$$\text{Area of right angled } \triangle ABC = \frac{1}{2}(b \times p)$$

- दिइएको समानान्तर चतुर्भुज ABCD मा आधार (BC) = b र उचाई (AE) = h भए $AB = a$, भए परिमिति (p) = $2(a+b)$

$$\text{स.च. को क्षेत्रफल (A)} = \text{आधार} \times \text{उचाई} = (b \times h)$$

In the given parallelogram ABCD

Base (BC) = b , height (AE) = h and side (AB) = a

Perimeter (p) = $2(a+b)$

$$\text{Area of parallelogram ABCD (A)} = (\text{base} \times \text{height}) = (b \times h)$$

- दिइएको समबाहु चतुर्भुज ABCD मा $AB = BC = CD = AD = a$, विकर्ण (AC) = d_1 , विकर्ण (BD) = d_2 र उचाई (AE) = h

$$\text{समबाहु चतुर्भुजको क्षेत्रफल (A)} = \text{आधार} \times \text{उचाई} = a \times h$$

Or

$$\text{समबाहु चतुर्भुजको क्षेत्रफल (A)} = \frac{1}{2} d_1 \times d_2$$

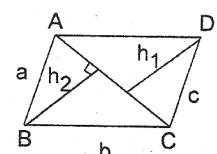
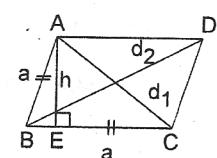
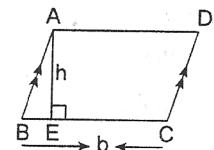
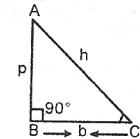
In the given rhombus ABCD $AB = BC = CD = AD = a$ diagonal

(AC) = d_1 and diagonal (BD) = d_2 height = h , perimeter (P) =

$$4a. \text{ Area of rhombus (A)} = a \times h \text{ or area of rhombus (A)} = \frac{1}{2} (d_1 \times d_2)$$

- दिइएको चतुर्भुज ABCD (i) मा $AB = a, BC = b, CD = c, DA = d$
 AC विकर्ण = d र विकर्णसम्म खिचिएको लम्बहरू h_1 र h_2 भए
 परिमिति (p) = $a + b + c + d$

$$\text{चतुर्भुज ABCD को क्षेत्रफल (A)} = \frac{1}{2} \text{ विकर्ण (लम्बहरूको योग)} = \frac{1}{2} d (h_1 + h_2)$$



In the given quadrilateral ABCD, AB = a BC = b CD = c DA = d, AC and diagonal = d, h_1 and h_2 are perpendicular drawn to the diagonal

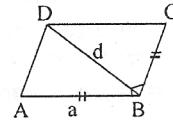
Perimeter (p) = a + b + c + d

Area of quadrilateral (ABCD) (A) = $\frac{1}{2}$ diagonal (Sum of perpendicular = $\frac{1}{2}$ d ($h_1 + h_2$)

- दिइएको चित्र ABCD वर्गमा AB = BC = a र BD विकर्ण d भए
परिमिति (P) = 4a

क्षेत्रफल (A) = $a^2 = \frac{1}{2}d^2$ (In the given figure, in square ABCD AB = BC = a, diagonal (BD) = d,
Perimeter (P) = 4a

Area of square (A) = $a^2 = \frac{1}{2}d^2$

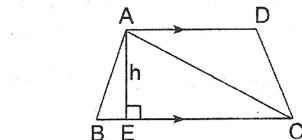


- दिइएको समलम्ब चतुर्भुज ABCD मा AB = a, BC = b, CD = c, DA = d, AD//BC उचाई (AE) = h
परिमिति (p) = a + b + c + d

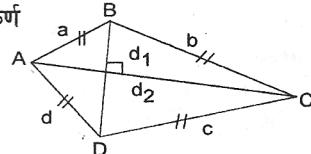
समलम्ब चतुर्भुज ABCD को क्षेत्रफल (A) = $\frac{1}{2}$ उचाई (समानान्तर रेखाहरूको योग) = $\frac{1}{2}$ h(AD + BC)

In the given trapezoid ABCD,
AB = a BC = b CD = c DA = d diagonal AC = d
AD//BC height (AE) = h
Perimeter (p) = a + b + c + d

Area of trapezoid ABCD = $\frac{1}{2}$ height (Sum of parallel lines) = $\frac{1}{2}$ h (AD + BC)



- दिइएको चित्रमा ABCD चक्रमा AB = a, BC = b, CD = c, र DA = d, विकर्ण (AC) = d_1
विकर्ण (BD) = d_2 भए
परिमिति (p) = a + b + c + d = 2(a+b)
चक्रमा ABCD क्षेत्रफल (A) = $\frac{1}{2}$ ($d_1 \times d_2$)



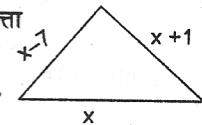
In the given figure ABCD the AB = a BC = b CD = c and DA = d diagonal (AC) = d_1 and diagonal (BD) = d_2 perimeter (p) = a + b + c + d

A = 2 (a + b) area of kite ABCD (a) = $\frac{1}{2}$ ($d_1 \times d_2$)

Very short Questions

- यदि समबाहु त्रिभुजको एउटा भूजाको a एकाई यसको क्षेत्रफल कति हुन्छ ?
If the length of one side of equilateral is a unit, what is its area ?
- यदि एउटा ΔXYZ को भुजाहरूको नाप क्रमशः x, y र z भए क्षेत्रफल कति हुन्छ ?
If measure of ΔXYZ of sides are x, y and z respectively, what is the area of triangle ?
- 6cm लम्बाई भएको समबाहु त्रिभुजको परिमिति कति हुन्छ ?
What is perimeter of equilateral triangle where length is 6cm.
- कुनै त्रिभुजको तीनवटा भुजाहरू क्रमशः a, b र c छ भने त्रिभुजको अधिपरिमिति कति हुन्छ ? लेख्नुहोस्।
If the three sides of a triangle are a, b and c respectively, what is the semi perimeter of the triangle ?
- समद्विबाहु त्रिभुजको क्षेत्रफल कति हुन्छ ? जसका दुई बराबर भूजाको लम्बाई 'a' एकाई र आधार भूजा b एकाई छ ।
What is the area of isosceles triangle, where two equal side is a unit and length of base is 'b'.

6. समकोण समद्विबाहु त्रिभुजमा कर्ण 'h' र वरावर भूजा 'b' एकाई भए प्रमाणित गर्नुहोस् । $h = b\sqrt{2}$
 If in a right angled triangle, hypotenuse 'h' and equal two sides is b unit prove that $h = b\sqrt{2}$.
7. यदि एउटा त्रिभुजको आधारको लम्बाई 20cm र यसको क्षेत्रफल 50 cm^2 छ भने त्रिभुजको उचाई निकाल्नुहोस् ।
 If length base of a triangle is 20cm and its area is 50 cm^2 , find the height of triangle.
8. वर्गको भूजाको लम्बाई कति भए क्षेत्रफल र परिमिति बराबर हुन्छ ?
 How long will be length of a side of square? whose area and perimeter is equal.
9. स.च. को क्षेत्रफल 60 cm^2 र यसको आधार 12 cm भए यसको उचाई कतिहोला ?
 If the area of parallelogram is 60 cm^2 and its base 12 cm , find the height its.
10. दिएको चित्रमा त्रिभुजको प्रत्येक भूजाको लम्बाइहरू $x + 1$, $x - 7$ and x छन् x को मान पत्ता लगाउनुहोस् । जसको परिमिति 30 cm छ ।
 In the given figure of a triangle the length of each sides are $x + 1$, $x - 7$ and x , find the value of x , whose perimeter is 30 cm .
11. यदि समबाहु चतुर्भुजको विकर्णहरू d_1 र d_2 भए यसको क्षेत्रफल कति हुन्छ ?
 If d_1 and d_2 are the diagonal of rhombus find the of its area ?
12. कैनै समद्विबाहु त्रिभुजको क्षेत्रफल $\frac{p}{4} \sqrt{4q^2 - p^2}$ भए कुन दुई भुजाहरू बराबर होला ?
 If the area of Isosceles triangle $\frac{p}{4} \sqrt{4q^2 - p^2}$ which two sides equal ?
13. यदि एउटा वर्गको विकर्णको लम्बाई d भए यसको क्षेत्रफल लाई d को रूपमा लेख्नुहोस् ।
 If d is a diagonal of square , write the its area in terms of d .



Short Questions:

Model 1

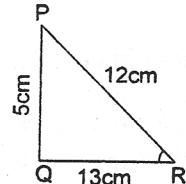
दिएको $\triangle PQR$ को क्षेत्रफल कति हुन्छ ? पत्ता लगाउनुहोस् ।

What is the area of the given $\triangle PQR$, find it .

Solution:

In the given figure of $\triangle PQR$ $PQ = a = 5 \text{ cm}$ $QR = b = 13 \text{ cm}$ and $PR = c = 12 \text{ cm}$

$$\begin{aligned}\text{Semiperimeter (s)} &= \frac{a+b+c}{2} \\ &= \frac{5+13+12 \text{ cm}}{2} = 15 \text{ cm}\end{aligned}$$



Now, area of $\triangle PQR$ (A)

$$\begin{aligned}&= \sqrt{s(s-a)(s-b)(s-c)} \\ &= \sqrt{15 \text{ cm} (15 \text{ cm} - 5 \text{ cm}) (15 \text{ cm} - 13 \text{ cm}) (15 \text{ cm} - 12 \text{ cm})} \\ &= \sqrt{15 \text{ cm} \times 10 \text{ cm} \times 2 \text{ cm} \times 3 \text{ cm}} = \sqrt{900 \text{ cm}^4} = 30 \text{ cm}^2\end{aligned}$$

\therefore Area of $\triangle PQR$ (A) = 30 cm^2

Model 2:

एउटा समबाहु त्रिभुजको क्षेत्रफल $729\sqrt{3} \text{ cm}^2$ छ । यसको भूजाको लम्बाई र परिमिति पत्ता लगाउनुहोस् ।

The area of an equilateral triangle is $729\sqrt{3} \text{ cm}^2$ find its side and perimeter.

Solution:

Here, Area of equilateral triangle (A) = $729\sqrt{3} \text{ cm}^2$

$$\therefore A = \frac{\sqrt{3}}{4} a^2$$

$$\text{or, } 729\sqrt{3} \text{ cm}^2 = \frac{\sqrt{3}}{4} a^2$$

$$\begin{aligned}
 & \text{or, } a^2 = 729 \times 4 \\
 & \text{or, } 729 \sqrt{3} \times 4 \text{ cm}^2 = \sqrt{3} a^2 \\
 & \text{or, } 2916 \text{ cm}^2 = a^2 \\
 & \text{or, } a^2 = (16 \text{ cm})^2 \\
 & \therefore a = 16 \text{ cm} \\
 & \text{Length of sides (a)} = 16 \text{ cm} \\
 & \text{Perimeter (p)} = 4a = 4 \times 16 \text{ cm} = 64 \text{ cm}
 \end{aligned}$$

Model 3:

36cm परिमिति भएको समबाहु त्रिभुजको क्षेत्रफल पत्ता लगाउनुहोस् ।

Find the area of an equilateral triangle of perimeter is 36 cm.

Solution:

Here, Area of equilateral triangle (A) = ?

Its perimeter (p) = 36cm

$$\therefore p = 3a$$

$$\text{or, } 36 \text{ cm} = 3a$$

$$\therefore a = 12 \text{ cm}$$

$$\begin{aligned}
 \text{Area of an equilateral triangle (A)} &= \frac{\sqrt{3}}{4} a^2 = \frac{\sqrt{3}}{4} (12 \text{ cm})^2 = \frac{\sqrt{3} \times 144}{4} \text{ cm}^2 \\
 &= 36\sqrt{3} \text{ cm}^2 = 62.35 \text{ cm}^2
 \end{aligned}$$

$$\therefore \text{Area of an equilateral } \Delta 35.07 \text{ cm}^2$$

Model 4:

एउटा त्रिभुजको परिमिति र दुई भुजाहरूको लम्बाई कमश 36cm 8cm and 12cm छन् । यो त्रिभुजको क्षेत्रफल निकाल्नुहोस् ।

Then perimeter and the length of two sides of a triangle are 36cm, 8cm and 12cm respectively find the area of the triangle.

Solution:

Here, perimeter (P) = 36cm, let two side of triangle be a and b repectively, the a = 8cm and b = 12cm

$$\therefore P = a + b + c$$

$$\text{or, } 36 \text{ cm} = 8 \text{ cm} + 12 \text{ cm} + c$$

$$\text{or, } 36 - 20 \text{ cm} = c$$

$$\text{or, } c = 16 \text{ cm}$$

$$\text{Semiperimeter (s)} = \frac{a + b + c}{2}$$

$$= \frac{36 \text{ cm}}{2} = 18 \text{ cm}$$

$$\begin{aligned}
 \text{Area of triangle (A)} &= \sqrt{s(s-a)(s-b)(s-c)} \\
 &= \sqrt{18 \text{ cm} (18 \text{ cm} - 8 \text{ cm})(18 \text{ cm} - 12 \text{ cm})(18 \text{ cm} - 16 \text{ cm})} \\
 &= \sqrt{18 \times 10 \times 6 \times 2 \text{ cm}^4} = \sqrt{2160 \text{ cm}^4}
 \end{aligned}$$

$$\text{Area of triangle (A)} = 46.48 \text{ cm}^2$$

Model 5 :

एउटा त्रिभुजको भुजाहरूको अनुपात 3:4:5 र परिमिति 12cm छ भने त्रिभुजको क्षेत्रफल पत्ता लगाउनुहोस् ।

The ratio of the sides of a triangle 3:4:5 and its perimeter 12cm find the area of the triangle.

Solution:

Here, let the length of three sides be a, b and c whose ratio are 3:4:5 then a = 3x, b = 4x, c = 5x, and perimeter (P) = 12cm

$$\therefore P = a + b + c$$

$$\text{or, } 12\text{cm} = 3x + 4x + 5x$$

$$\text{or, } 12\text{cm} = 12x$$

$$\therefore x = 1\text{cm}$$

$$a = 3x = 3 \times 1\text{cm} = 3\text{cm}, b = 4x = 4 \times 1\text{cm} = 4\text{cm}, c = 5x = 5 \times 1\text{cm} = 5\text{cm}$$

$$\text{semiperimeter (s)} = \frac{a+b+c}{2} = \frac{12\text{cm}}{2} = 6\text{cm}$$

$$\text{Area of triangle (A)} = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{12\text{cm}(12\text{cm}-3\text{cm})(12\text{cm}-4\text{cm})(12\text{cm}-5\text{cm})}$$

$$= \sqrt{12\text{cm} \times 9\text{cm} \times 8\text{cm} \times 7\text{cm}}$$

$$= \sqrt{6048\text{cm}^4}$$

$$= 77.76\text{cm}^2$$

Model 6:

एउटा समद्विबाहु त्रिभुजको परिमिति र आधारको लम्बाई क्रमशः 25m र 9cm छन् भने सो त्रिभुजको क्षेत्रफल निकाल्नुहोस् ।

The perimeter and the length of the base of an isosceles triangle are 25cm and 9cm respectively calculate the area of the triangle.

Soluton: Here, In the isosceles triangle

$$\text{Perimeter (P)} = 25\text{cm} \text{ and length of base (b)} = 9\text{cm}$$

$$\text{or, } p = 2a + b$$

$$\text{or, } 25\text{cm} = 2a + 9\text{cm}$$

$$\text{or, } (25 - 9)\text{ cm} = 2a$$

$$\text{or, } \frac{16\text{cm}}{2} = a$$

$$\therefore a = 8\text{cm}$$

$$\text{Length of equal sides (a)} = 8\text{cm}$$

$$\text{Area of a isosceles triangle (A)} = \frac{b}{4} \sqrt{4a^2 - b^2} = \frac{9\text{cm}}{4} \sqrt{4 \times 64\text{cm}^2 - (9\text{cm})^2}$$

$$= \frac{9}{4} \text{cm} \sqrt{256\text{cm}^2 - 81\text{cm}^2} = \frac{9 \times 13.23\text{cm}^2}{4} = 29.76\text{cm}^2$$

$$\therefore \text{Area of a isosceles triangle (A)} = 29.76\text{cm}^2$$

Model 7:

यदि एउटा समबाहु चतुर्भुजका विकर्णहरूको लम्बाई क्रमशः 8cm र 10cm भए क्षेत्रफल पत्ता लगाउनुहोस् ।

If the diagonal of a rhombus are 8cm and 10cm respectively, find its area.

Solution:

Here, In a rhombus length of diagonal are 8cm and 10cm

Then $d_1 = 8\text{cm}$ and $d_2 = 10\text{cm}$

$$\text{Area of rhombus (A)} = \frac{1}{2} (d_1 \times d_2) = \frac{1}{2} (8\text{cm} \times 10\text{cm}) = 40\text{cm}^2$$

$$\text{Area of rhombus (A)} = 40\text{cm}^2$$

Model 8:

यदि $\triangle ABC$ मा परिमिति 24cm, $a + b = 18\text{cm}$ $b + c = 14\text{cm}$ भए $\triangle ABC$ को क्षेत्रफल पत्ता लगाउनुहोस् ।

If In $\triangle ABC$, perimeter 24cm, $a + b = 18\text{cm}$ $b + c = 14\text{cm}$ find the area of $\triangle ABC$.

Solution:

Here, perimeter (p) = 24cm $a + b = 18\text{cm}$ $b + c = 14\text{cm}$

Now, $P = a + b + c$

or, $24\text{cm} = 18\text{cm} + c$

$$\text{or, } 24\text{cm} - 18\text{cm} = c$$

$$\therefore c = 6\text{cm}$$

$$\text{Again, } P = a + b + c$$

$$\text{or, } 24\text{cm} = a + 14\text{cm}$$

$$\text{or, } 24\text{cm} - 14\text{cm} = a$$

$$\therefore a = 10\text{cm}$$

$$b + c = 14\text{cm}$$

$$\text{or, } b + 6\text{cm} = 14\text{cm}$$

$$\therefore b = 8\text{cm}$$

$$\text{Semiperimeter (s)} = \frac{P}{2} = \frac{24\text{cm}}{2} = 12\text{cm}$$

$$\begin{aligned}\text{Area of } \triangle ABC (A) &= \sqrt{s(s-a)(s-b)(s-c)} \\ &= \sqrt{12\text{cm}(12\text{cm}-10\text{cm})(12\text{cm}-8\text{cm})(12\text{cm}-6\text{cm})} \\ &= \sqrt{12\text{cm} \times 2\text{cm} \times 4\text{cm} \times 6\text{cm}} = \sqrt{576\text{cm}^4} = 24\text{cm}^2\end{aligned}$$

$$\therefore \text{Area of } \triangle ABC (A) = 24\text{cm}^2$$

Model 9:

दिएको समद्विबाहु $\triangle ABC$ को क्षेत्रफल 672cm^2 भए x को मान पता लगाउनुहोस् ।

The area of $\triangle ABC$ is 672cm^2 , find the value of x .

Solution:

Here, in the given figure of $\triangle ABC$ $AB = BC$ ($a = x$) and BC (b) = 28cm

$$\text{Area of } \triangle ABC = 672\text{cm}^2$$

$$\therefore \text{Area of } \triangle ABC (A) = \frac{b}{4} \sqrt{4a^2 - b^2}$$

$$\text{or, } 672\text{cm}^2 = \frac{28\text{cm}}{4} \sqrt{4x^2 - (28\text{cm})^2}$$

$$\text{or, } 672\text{cm}^2 = 7\text{cm} \sqrt{4x^2 - 784\text{cm}^2}$$

$$\text{or, } \frac{672\text{cm}^2}{7} = \sqrt{4x^2 - 784\text{cm}^2}$$

$$\text{or, } 46\text{cm} = \sqrt{4x^2 - 784\text{cm}^2}$$

Squaring both sides

$$\text{or, } (46\text{cm})^2 = (\sqrt{4x^2 - 784\text{cm}^2})^2$$

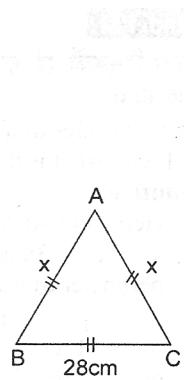
$$\text{or, } 9216\text{cm}^2 = 4x^2 - 784\text{cm}^2$$

$$\text{or, } 10,000\text{cm}^2 = 4x^2$$

$$\text{or, } 2500\text{cm}^2 = 4x^2$$

$$\therefore x = 50\text{cm}$$

$$\text{Value of } x = 50\text{cm}$$



Model 10:

एउटा त्रिभुजको भुजाहरू क्रमशः $3x$, $4x$ $5x$ र क्षेत्रफल 24cm^2 भए x को मान निकालनुहोस् ।

Find the value of x whose side are $3x$, $4x$ $5x$ respectively and area is 24cm^2

Solution: Here, let a , b and c to the side of triangle $3x$, $4x$ and $5x$ respectively.

$$a = 3x \quad b = 4x \quad c = 5x \text{ and area of triangle (A)} = 24\text{cm}^2$$

$$\text{semiperimeter (s)} = \frac{a+b+c}{2} = \frac{3x+4x+5x}{2} = 6x$$

$$\text{Area of triangle (A)} = \sqrt{s(s-a)(s-b)(s-c)}$$

$$\text{or, } 24\text{cm}^2 = \sqrt{6x(6x-3x)(6x-4x)(6x-5x)}$$

$$\text{or, } 24\text{cm}^2 = \sqrt{6x \times 3x \times 2x \times x}$$

$$\text{or, } 24\text{cm}^2 = \sqrt{36x^4}$$

Squaring on the sides

$$\text{or, } (24\text{cm}^2)^2 = (\sqrt{36x^4})^2$$

$$\text{or, } 576\text{cm}^4 = 36x^4$$

$$\text{or, } 16\text{cm}^4 = x^4$$

$$\text{or, } (2\text{cm})^4 = x^4$$

$$\therefore x = 2\text{cm}$$

$$\text{value of } x = 2\text{cm}$$

Model 11:

एउटा त्रिभुजको दुई भूजाको अनुपात 2:3 र तेसी भूजाको लम्बाई 5 cm छ । यदि त्रिभुजको परिमिति 15cm भए क्षेत्रफल कति होला ?

The two sides of a triangle are in the ratio 2:3 and its length of third side is 5cm, if perimeter of triangle is 15cm, what is the area of triangle.

Solution:

Here, let two sides of triangle be a and b whose ratio are 2:3 then.

$$a = 2x \quad b = 3x \quad \text{and } c = 5\text{cm}$$

$$\text{perimeter of triangle (P)} = 15\text{cm}$$

$$\therefore p = a + b + c$$

$$\text{or, } 15\text{cm} = 2x + 3x + 5\text{cm}$$

$$\text{or, } 15\text{cm} = 5x + 5\text{cm}$$

$$\text{or, } (15 - 5)\text{ cm} = 5x$$

$$\text{or, } 10\text{cm} = 5x$$

$$\therefore x = 2\text{cm}$$

$$a = 4\text{cm}, b = 6\text{cm} \text{ and } c = 5\text{cm}$$

$$\text{semiperimeter (s)} = \frac{a+b+c}{2} = \frac{4\text{cm} + 6\text{cm} + 5\text{cm}}{2} = \frac{15\text{cm}}{2} = 7.5\text{cm}$$

$$\text{Area of triangle (A)} = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{7.5\text{cm}(7\text{cm}-4\text{cm}) \times (7.5\text{cm}-6\text{cm}) \times (7.5\text{cm}-5\text{cm})}$$

$$= \sqrt{7.5\text{cm} \times 3.5\text{cm} \times 1.5\text{cm} \times 2.5\text{cm}} = \sqrt{98.4375\text{cm}^4} = 9.92\text{cm}^2$$

$$\text{Area of triangle (A)} = 9.92\text{cm}^2$$

Model 12:

चित्रमा दिइएको ABCD समबाहु चतुर्भुजको क्षेत्रफल निकाल्नुहोस् ।

In given figure of find area of rhombus ABCD.

Solution: Here, in the given figure rhombus ABCD

$$\text{diagonal (AC)} = 16\text{cm}$$

$$OC = \frac{1}{2} AC = \frac{1}{2} 16\text{cm} = 8\text{cm}$$

$$AB = 10\text{cm}$$

\therefore Pythagoras theorem

$$\text{or, } AB^2 = OC^2 + OB^2$$

$$\text{or, } (10\text{cm})^2 = (8\text{cm})^2 + OB^2$$

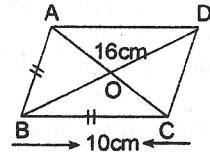
$$\text{or, } 100\text{cm}^2 = 64\text{cm}^2 + OB^2$$

$$\text{or, } (100 - 64)\text{cm}^2 = OB^2$$

$$\therefore OB = 6\text{cm}$$

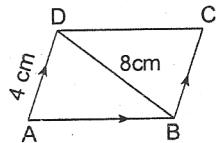
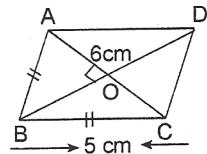
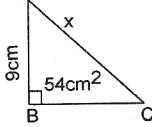
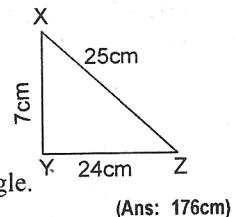
$$\text{Diagonal (BD)} = 2 \times OB = 2 \times 6\text{cm} = 12\text{cm}$$

$$\text{Area of rhombus ABCD (A)} = \frac{1}{2} \text{product of diagonal} = \frac{1}{2} 16\text{cm} \times 12\text{cm} = 96\text{cm}^2$$



Practice Yourself

1. दिएको चित्र ΔXYZ मा , ΔXYZ को क्षेत्रफल कति हुन्छ ?
In the given figure ΔXYZ , what is the area of ΔXYZ . (Ans: 84cm^2)
2. एउटा समबाहु त्रिभुजको क्षेत्रफल $484\sqrt{3}\text{ cm}^2$ छ । त्रिभुजको परिमिति पत्ता लगाउनुहोस् ।
The area of an equilateral triangle is $484\sqrt{3}\text{ cm}^2$ find the perimeter of triangle. (Ans: 176cm)
3. यदि एउटा समबाहु त्रिभुजको तीन वटा भुजाहरूको योगफल 18cm भए सो त्रिभुजको क्षेत्रफल पत्ता लगाउनुहोस् ।
If the length of the sum of three sides of an equilateral triangle is 18cm find the area of triangle. (Ans: $9\sqrt{3}\text{ cm}^2$)
4. एउटा त्रिभुजको परिमिति र दुई भुजाहरूको लम्बाई क्रमशः 60cm , 10m र 26m भए त्रिभुजको क्षेत्रफल निकाल्नुहोस् ।
The perimeter of and length of two sides of a triangle are 60cm , 10m and 26m respectively. Find the area of triangle. (Ans: 120m^2)
5. एउटा त्रिभुजका भुजाहरू $5:12:13$ को अनुपातमा छन् । यदि सो त्रिभुजको क्षेत्रफल 480cm^2 भए भुजाहरूको नाप निकाल्नुहोस् ।
The sides of a triangle are in the ratio of $5:12:13$. If the area of the triangle is 480cm^2 find the measure of sides. (Ans: 5cm , 12cm and 13cm)
6. एउटा त्रिभुजको भुजाहरूको अनुपात $6:8:10$ र परिमिति 48cm भए उक्त त्रिभुजको क्षेत्रफल पत्ता लगाउनुहोस् ।
If the ratio of the sides of triangle are $6:8:10$ and the perimeter is 48cm . find the area of triangle. (Ans: 96cm^2)
7. एउटा समद्विबाहु त्रिभुजको क्षेत्रफल 12cm^2 र आधारभुजा 8cm भए बराबर भुजाको लम्बाई पत्ता लगाउनुहोस् ।
The area of a isosceles triangle is 12cm^2 base is 8cm , then find the length of equal sides. (Ans: 5cm)
8. दिइएको चित्रमा ΔABC को क्षेत्रफल 54cm^2 छ x को मान कति होला ? In the given figure, area of ΔABC is 54m^2 , find the value of x .
(Ans: $-3\sqrt{10}\text{ cm}$)
9. दिएको समबाहु चतुर्भुज ABCD का विकर्ण (AC) = 6cm र भुजा (BC) = 5cm भए समबाहु चतुर्भुज ABCD को क्षेत्रफल निकाल्नुहोस् ।
In the given figure rhombus ABCD diagonal (AC) = 6cm side BC = 5cm , find the area of rhombus ABCD.
(Ans: 24cm^2)
10. दिएको स.च. ABCD को क्षेत्रफल पत्ता लगाउनुहोस् । जहाँ AD = 4cm , BD = 8cm र CD = 6cm छ ।
In the given ABCD, find area of parallelogram ABCD where AD = 4cm BD = 8cm , CD = 6cm .
(Ans. 23.23cm^2)
11. आधार भुजा लम्बाई 10m भएको समदिवाहु त्रिभुजकार जग्गाको क्षेत्रफल 80m^2 भए जग्गाको बाँकी भुजाको नाप पत्ता लगाउनुहोस् ।
The area of an isosceles triangular and whose base side 10m is 60m^2 . Find the measure of its remaining sides)



Long Questions

- आधार भुजा लम्बाई 10cm भएको समदिवाहु त्रिभुजकार जग्गाको क्षेत्रफल 80cm^2 भए जग्गाको बाँकी भुजाको नाप पत्ता लगाउनुहोस्।
The area of an isosceles triangular and whose base side 10m is 60m^2 . Find the measure of its remaining sides.
- एउटा त्रिभुजाकार जग्गाको भुजाहरू 2:3:4 को अनुपातमा छन्। यदि यसको परिमिति 900 पिटर भए सो जग्गाको क्षेत्रफल कति होला ? पत्ता लगाउनुहोस्।
The sides of triangular field are in the ratio of 2:3:4. If its perimeter is 900m what is the area of that land? Find it.
- एउटा भुइमा 20 ओटा त्रिभुजकार टायलहरू प्रयोग गरी डिजाइन गरिएको छ। एउटा त्रिभुजाकार टायलको भुजाहरू 8cm, 8cm र 10cm भए भने सो टायलहरूलाई प्रति वर्ग मी रु. 15 का दरले मानिस लगाउन लाग्ने जम्मा खर्च पत्ता लगाउनुहोस्।
A floral design an floor is made up of 20 tiles which are triangular, the sides of triangle being 6cm , 8cm and 10cm . Find the cost of polishing that tiles at the rate os Rs. ·15 prefer square cm.
- क्षेत्रफल 336 वर्ग मि. र परिमिति 84 मिटर भएको एउटा त्रिभुजाकार गजगगाको एउटा किनाराको लम्बाई 26 मिटर छ। उक्त जग्गाको बाँकी दुई भुजाको किनाराको नाप निकान्दनुहोस्।
A triangular land having area 336cm^2 and perimeter 84 m has length of edge 26m. Find the measure of remaining two sides.