

Most of the formulas came from the previous formulations.

Let the location of earth be  $(1, \theta_1)$  and  $(1, \theta_2)$  and  $(r, \delta)$  be position of mars, then

$$\begin{aligned} \text{we have } x - r \sin \theta_1 &= \tan \alpha_1 (y - r \cos \theta_1) \\ y - r \sin \theta_2 &= \tan \alpha_2 (y - r \cos \theta_2). \end{aligned}$$

Now solving these equations

$$\begin{aligned} \text{we get } x &= \left( \frac{-1}{\text{den}} \right) * (\sin(\theta_1) - (\tan \alpha_1 * \cos \theta_1)) + \\ &\quad \left( \frac{1}{\text{den}} \right) * (\sin(\theta_2) - (\tan \alpha_2 * \cos \theta_2)) \end{aligned}$$

$$\text{den} = \tan \alpha_1 - \tan \alpha_2$$

$$\begin{aligned} y &= \left( \frac{-\tan \alpha_2}{\text{den}} \right) * (\sin(\theta_1) - (\tan \alpha_1 * \cos \theta_1)) + \\ &\quad \left( \frac{\tan \alpha_1}{\text{den}} \right) * (\sin(\theta_2) - (\tan \alpha_2 * \cos \theta_2)) \end{aligned}$$

$$\text{Now } r = \sqrt{x^2 + y^2} \quad \text{and } \phi = \tan^{-1} \frac{y}{x}.$$

★ // value of loss and parameters are mentioned in the code as comments.

we get 5 different locations of mars.



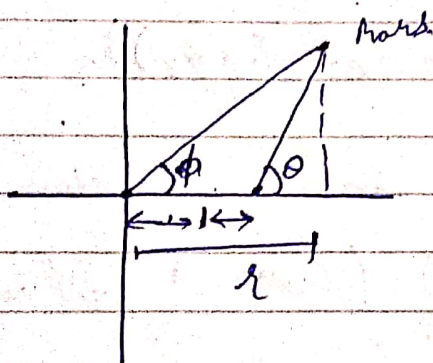
We can use the Concept from Gauss-Newton Approach for developing iterative algorithm.

$$x_{k+1} = x_k - \frac{\text{learning Rate}}{C} (z^T z)^{-1} f'(x_k)$$

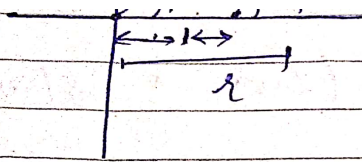
$f'$  :- first order derivative of the function

$f$  :- loss incurred.

$x_k$  :- value at  $k^{\text{th}}$  iteration.



$$\phi = \tan^{-1} \left( \frac{y - \text{mean } y}{x} \right)$$



Equation of the plane:  $ax + by + cz = 0$

loss function is equals  $\left( \frac{ax + by + cz}{\sqrt{a^2 + b^2 + c^2}} \right)^2$

(iv) loss function used is, we try to minimize the sum of distance of a point from each foci for all the points subtended from the length of the major axis because of the property of ellipse.