



Access Control Matrix

Chapter 2



Overview

- Access Control Matrix Model
 - Boolean Expression Evaluation
 - History
- Protection State Transitions
 - Commands
 - Conditional Commands
- Special Rights
 - Principle of Attenuation of Privilege

Section 2.1

A subject is an active entity



Description

| | | objects (entities) | | | | | |
|----------|-------|--------------------|-----|-------|-------|-----|-------|
| | | o_1 | ... | o_m | s_1 | ... | s_n |
| subjects | s_1 | | | | | | |
| | s_2 | | | | | | |
| | ... | | | | | | |
| | s_n | | | | | | |

- Subjects $S = \{ s_1, \dots, s_n \}$
- Objects $O = \{ o_1, \dots, o_m \}$
- Rights $R = \{ r_1, \dots, r_k \}$
- Entries $A[s_i, o_j] \subseteq R$
- $A[s_i, o_j] = \{ r_x, \dots, r_y \}$ means subject s_i has rights r_x, \dots, r_y over object o_j

Section 2.2

Note the way “object” is used here; it means “any entity”, not a “passive entity” as is usually the case. An object that is passive cannot take any actions, of course.



Example 1

- Processes p, q
- Files f, g
- Rights r, w, x, a, o

| | f | g | p | q |
|-----|-------|------|--------|--------|
| p | rwo | r | $rwxo$ | w |
| q | a | ro | r | $rwxo$ |

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Figure 2-1, slightly redone

The change here is to use the letters r, w, o, x, a to mean read, write, own, execute, and append respectively (Figure 2-1 spells them out)

Own is often treated specially, though (it can alter rights in the column, not row, in which it lies)

Note interpretation of rights is not relevant here; “ x ” can mean execute (as with a UNIX file) or “search” (as with a UNIX directory)



Example 2

- Host names *telegraph*, *nob*, *toadflax*
- Rights *own*, *ftp*, *nfs*, *mail*

| | <i>telegraph</i> | <i>nob</i> | <i>toadflax</i> |
|------------------|------------------|----------------------------|----------------------------|
| <i>telegraph</i> | <i>own</i> | <i>ftp</i> | <i>ftp</i> |
| <i>nob</i> | | <i>ftp, mail, nfs, own</i> | <i>ftp, nfs, mail</i> |
| <i>toadflax</i> | | <i>ftp, mail</i> | <i>ftp, mail, nfs, own</i> |

Figure 2-3

This is a data module to increment and decrement a counter

Note manager can call itself, so it's recursive



Example 3

- Procedures *inc_ctr*, *dec_ctr*, *manage*
- Variable *counter*
- Rights *+*, *-*, *call*

| | <i>counter</i> | <i>inc_ctr</i> | <i>dec_ctr</i> | <i>manage</i> |
|----------------|----------------|----------------|----------------|---------------|
| <i>inc_ctr</i> | <i>+</i> | | | |
| <i>dec_ctr</i> | <i>-</i> | | | |
| <i>manager</i> | | <i>call</i> | <i>call</i> | <i>call</i> |

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Figure 2-3

This is a data module to increment and decrement a counter

Note manager can call itself, so it's recursive



Boolean Expression Evaluation

- ACM controls access to database fields
 - Subjects have attributes
 - Verbs define type of access
 - Rules associated with objects, verb pair
- Subject attempts to access object
 - Rule for object, verb evaluated, grants or denies access

Section 2.2.1



Example

- Subject annie
 - Attributes *role* (artist), *group* (creative)
- Verb paint
 - Default 0 (deny unless explicitly granted)
- Object picture
 - Rule:
paint: 'artist' in subject.role and
'creative' in subject.groups and
time.hour ≥ 0 and time.hour ≤ 4

The next two slides are similar to the example in Section 2.2.1, but use painting rather than a file



ACM at 3AM and 10AM

At 3AM, time condition met
ACM is:

| | | |
|-----------------|-------|--|
| ... picture ... | | |
| ... annie ... | | |
| | paint | |
| | | |

At 10AM, time condition not met
ACM is:

| | | |
|-----------------|--|--|
| ... picture ... | | |
| ... annie ... | | |
| | | |
| | | |



History

- Problem: what a process has accessed may affect what it can access now
- Example: procedure in a web applet can access other procedures depending on what procedures it has already accessed
 - S set of *static rights* associated with procedure
 - C set of current rights associated with each executing process
 - When process calls procedure, rights are $S \cap C$



Example Program

```
// This routine has no filesystem access rights  
// beyond those in a limited, temporary area
```

```
procedure helper_proc()  
    return sys_kernel_file
```

```
// But this has the right to delete files
```

```
program main()  
    sys_load_file(helper_proc)  
    tmp_file = helper_proc()  
    sys_delete_file(tmp_file)
```

- *sys_kernel_file* contains system kernel
- *tmp_file* is in limited area that *helper_proc()* can access



Before *helper_proc* Called

- Static rights of program

| | <i>sys_kernel_file</i> | <i>tmp_file</i> |
|--------------------|------------------------|-----------------|
| <i>main</i> | delete | delete |
| <i>helper_proc</i> | | delete |

- When program starts, current rights:

| | <i>sys_kernel_file</i> | <i>tmp_file</i> |
|--------------------|------------------------|-----------------|
| <i>main</i> | delete | delete |
| <i>helper_proc</i> | | delete |
| <i>process</i> | delete | delete |

In “current rights”, *helper_proc()* is not yet loaded



After *helper_proc* Called

- Process rights are intersection of static, previous “current” rights:

| | <i>sys_kernel_file</i> | <i>tmp_file</i> |
|--------------------|------------------------|-----------------|
| <i>main</i> | delete | delete |
| <i>helper_proc</i> | | delete |
| <i>process</i> | | delete |

In “current rights”, *helper_proc()* is not yet loaded



State Transitions

- Change the protection state of system
- $| -$ represents transition
 - $X_i | -_{\tau} X_{i+1}$: command τ moves system from state X_i to X_{i+1}
 - $X_i | -^* Y$: a sequence of commands moves system from state X_i to Y
- Commands often called *transformation procedures*

Section 2.3

State is the triple (S, O, A) , where O here means the set of entities, not the set of passive entities (so $O \subseteq S$)



Primitive Operations

- **create subject s ; create object o**
 - Creates new row, column in ACM; creates new column in ACM
- **destroy subject s ; destroy object o**
 - Deletes row, column from ACM; deletes column from ACM
- **enter r into $A[s, o]$**
 - Adds r rights for subject s over object o
- **delete r from $A[s, o]$**
 - Removes r rights from subject s over object o



Create Subject

- Precondition: $s \notin S$
- Primitive command: **create subject** s
- Postconditions:
 - $S' = S \cup \{s\}$, $O' = O \cup \{s\}$
 - $(\forall y \in O') [A'[s, y] = \emptyset]$, $(\forall x \in S') [A'[x, s] = \emptyset]$
 - $(\forall x \in S)(\forall y \in O) [A'[x, y] = A[x, y]]$



Create Object

- Precondition: $o \notin O$
- Primitive command: **create object** o
- Postconditions:
 - $S' = S, O' = O \cup \{o\}$
 - $(\forall x \in S') [A'[x, o] = \emptyset]$
 - $(\forall x \in S)(\forall y \in O) [A'[x, y] = A[x, y]]$



Add Right

- Precondition: $s \in S, o \in O$
- Primitive command: **enter r into $A[s, o]$**
- Postconditions:
 - $S' = S, O' = O$
 - $A'[s, o] = A[s, o] \cup \{ r \}$
 - $(\forall x \in S')(\forall y \in O' - \{ o \}) [A'[x, y] = A[x, y]]$
 - $(\forall x \in S' - \{ s \})(\forall y \in O') [A'[x, y] = A[x, y]]$



Delete Right

- Precondition: $s \in S, o \in O$
- Primitive command: **delete** r from $A[s, o]$
- Postconditions:
 - $S' = S, O' = O$
 - $A'[s, o] = A[s, o] - \{ r \}$
 - $(\forall x \in S')(\forall y \in O' - \{ o \}) [A'[x, y] = A[x, y]]$
 - $(\forall x \in S' - \{ s \})(\forall y \in O') [A'[x, y] = A[x, y]]$



Destroy Subject

- Precondition: $s \in S$
- Primitive command: **destroy subject s**
- Postconditions:
 - $S' = S - \{ s \}, O' = O - \{ s \}$
 - $(\forall y \in O') [A'[s, y] = \emptyset], (\forall x \in S') [A'[x, s] = \emptyset]$
 - $(\forall x \in S')(\forall y \in O') [A'[x, y] = A[x, y]]$



Destroy Object

- Precondition: $o \in O$
- Primitive command: **destroy object o**
- Postconditions:
 - $S' = S, O' = O - \{ o \}$
 - $(\forall x \in S') [A'[x, o] = \emptyset]$
 - $(\forall x \in S')(\forall y \in O') [A'[x, y] = A[x, y]]$

Creating File

- Process p creates file f with r and w permission

```
command create•file( $p$ ,  $f$ )  
    create object  $f$ ;  
    enter own into  $A[p, f]$ ;  
    enter  $r$  into  $A[p, f]$ ;  
    enter  $w$  into  $A[p, f]$ ;  
end
```



Mono-Operational Commands

- Make process p the owner of file g
command *make-owner*(p, g)
 enter own into $A[p, g]$;
end
- Mono-operational command
 - Single primitive operation in this command



Conditional Commands

- Let p give q r rights over f , if p owns f
`command grant•read•file•1(p, f, q)`
 `if own in $A[p, f]$`
 `then`
 `enter r into $A[q, f]$;`
 `end`
- Mono-conditional command
 - Single condition in this command



Multiple Conditions

- Let p give q r and w rights over f , if p owns f and p has c rights over q

```
command grant•read•file•2( $p, f, q$ )  
  if own in  $A[p, f]$  and  $c$  in  $A[p, q]$   
  then  
    enter  $r$  into  $A[q, f]$ ;  
    enter  $w$  into  $A[q, f]$ ;  
end
```



Copy Flag and Right

- Allows possessor to give rights to another
- Often attached to a right (called a *flag*), so only applies to that right
 - r is read right that cannot be copied
 - rc is read right that can be copied
- Is copy flag copied when giving r rights?
 - Depends on model, instantiation of model



Own Right

- Usually allows possessor to change entries in ACM column
 - So owner of object can add, delete rights for others
- May depend on what system allows
 - Can't give rights to specific (set of) users
 - Can't pass copy flag to specific (set of) users



Attenuation of Privilege

- Principle says you can't increase your rights, or give rights you do not possess
 - Restricts addition of rights within a system
 - Usually *ignored* for owner
 - Why? Owner gives herself rights, gives them to others, deletes her rights.



Key Points

- Access control matrix simplest abstraction mechanism for representing protection state
- Transitions alter protection state
- 6 primitive operations alter matrix
 - Transitions can be expressed as commands composed of these operations and, possibly, conditions