

Computer Science 112

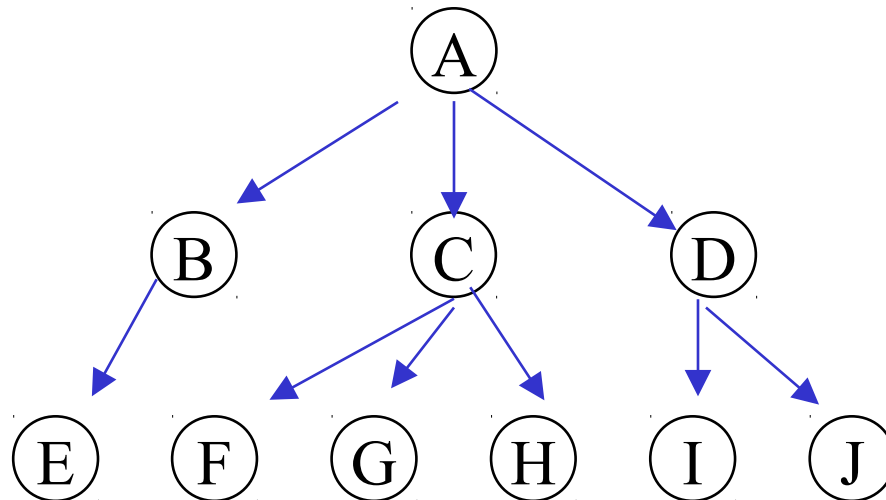
Data Structures

Lecture 15:

Huffman coding

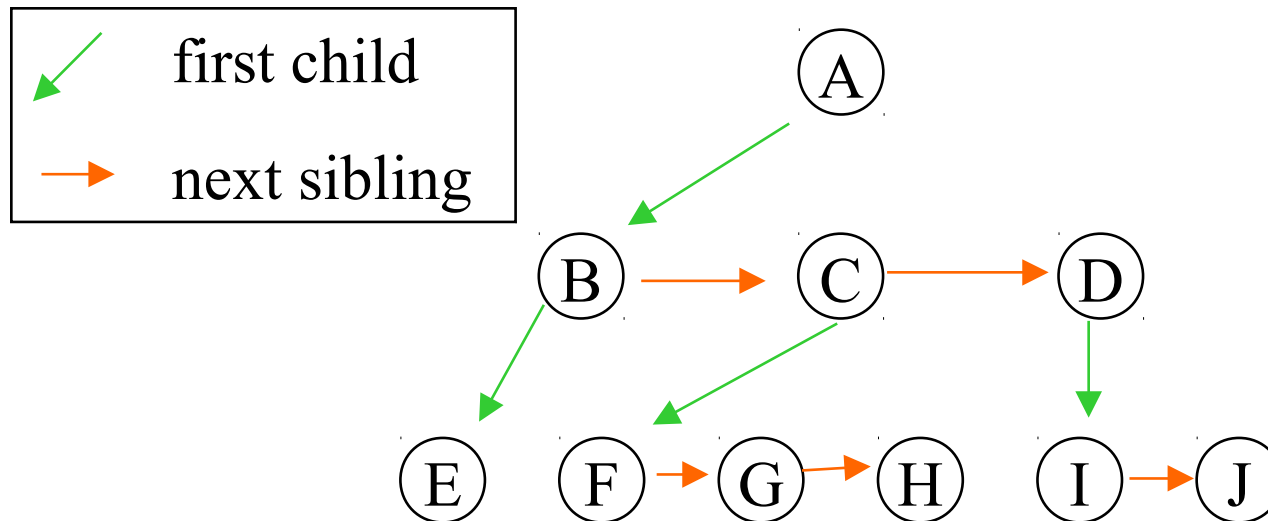
General Trees

- **How do you represent a node when it can have any number of children?**



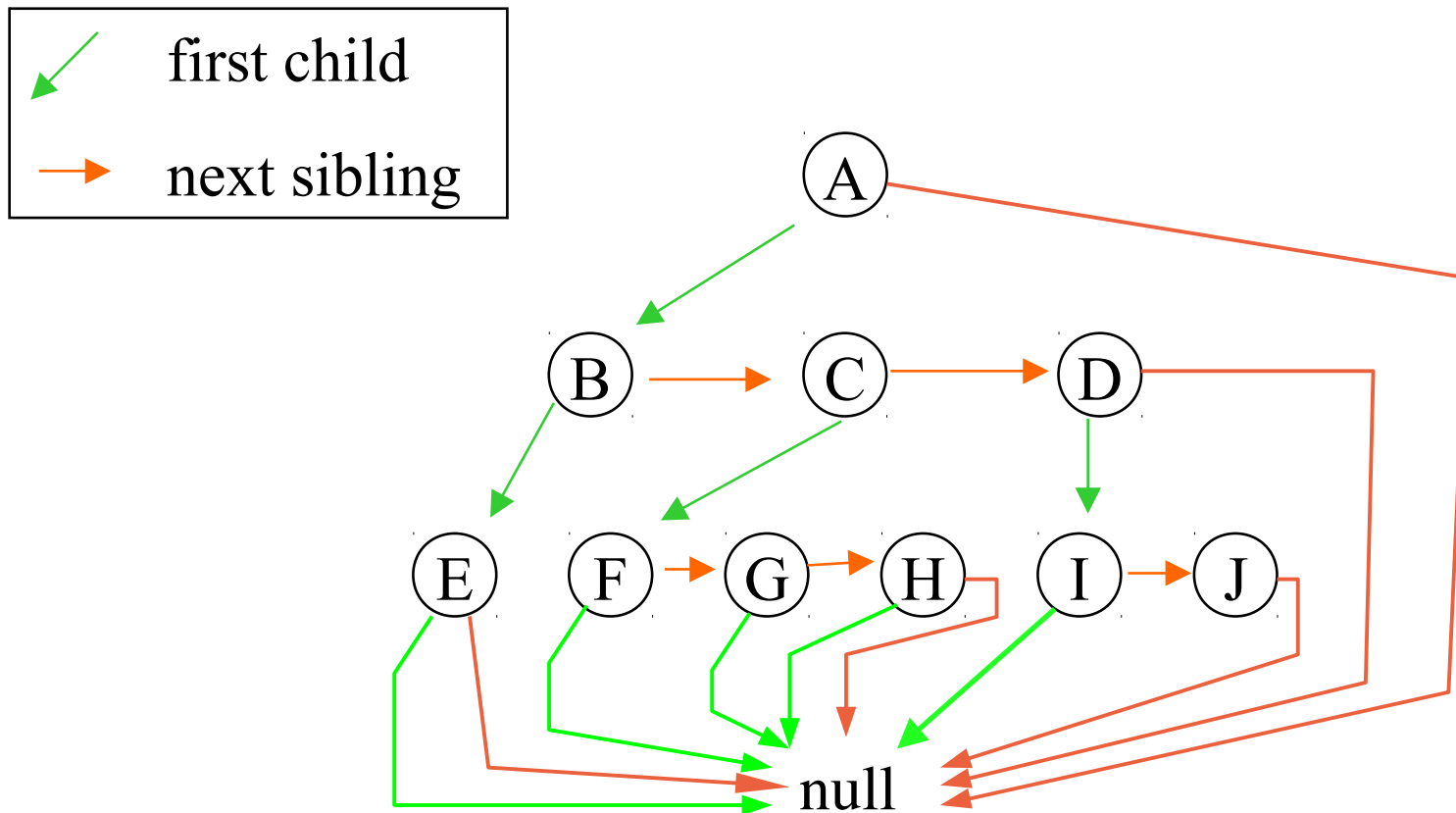
General Trees

- **Solution: linked list of children**



General Trees

- **Solution: linked list of children**



DOM tree in assignment

<html>

<body>

<p>

this is a line

</p>

<p>

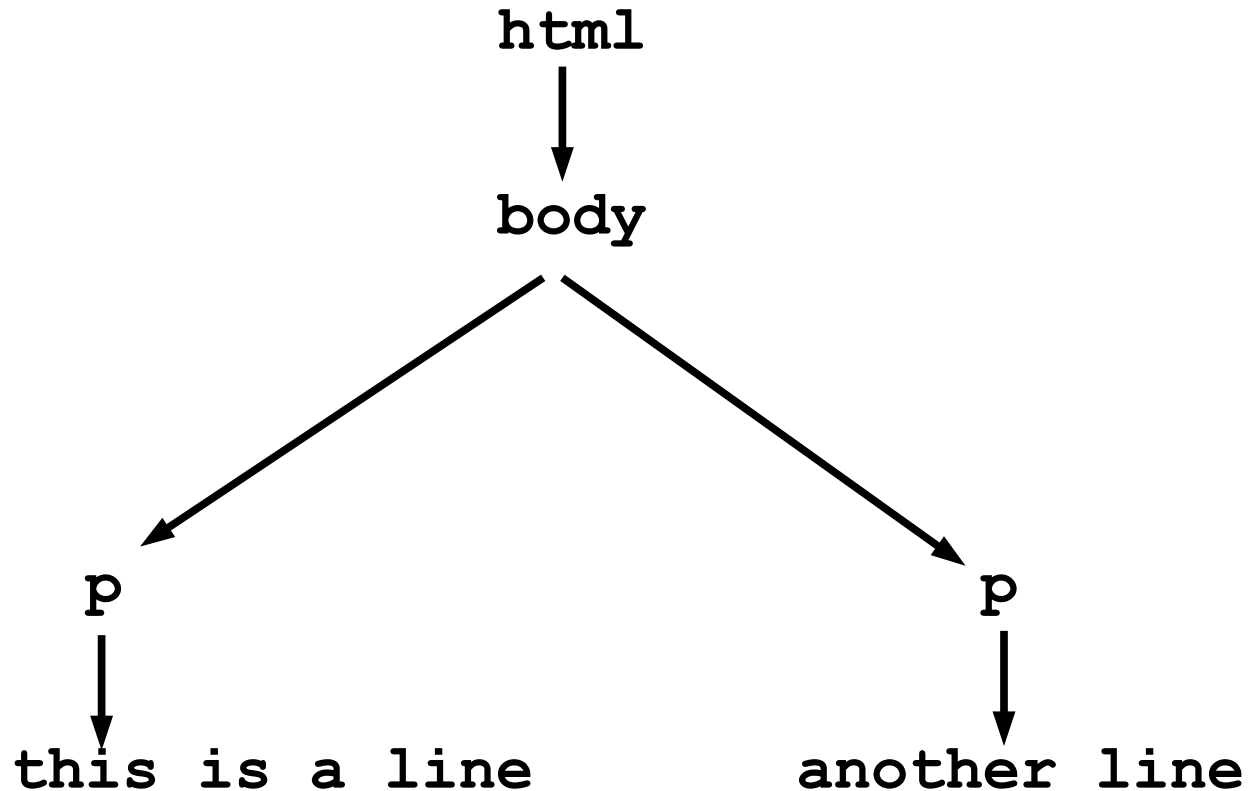
another line

</p>

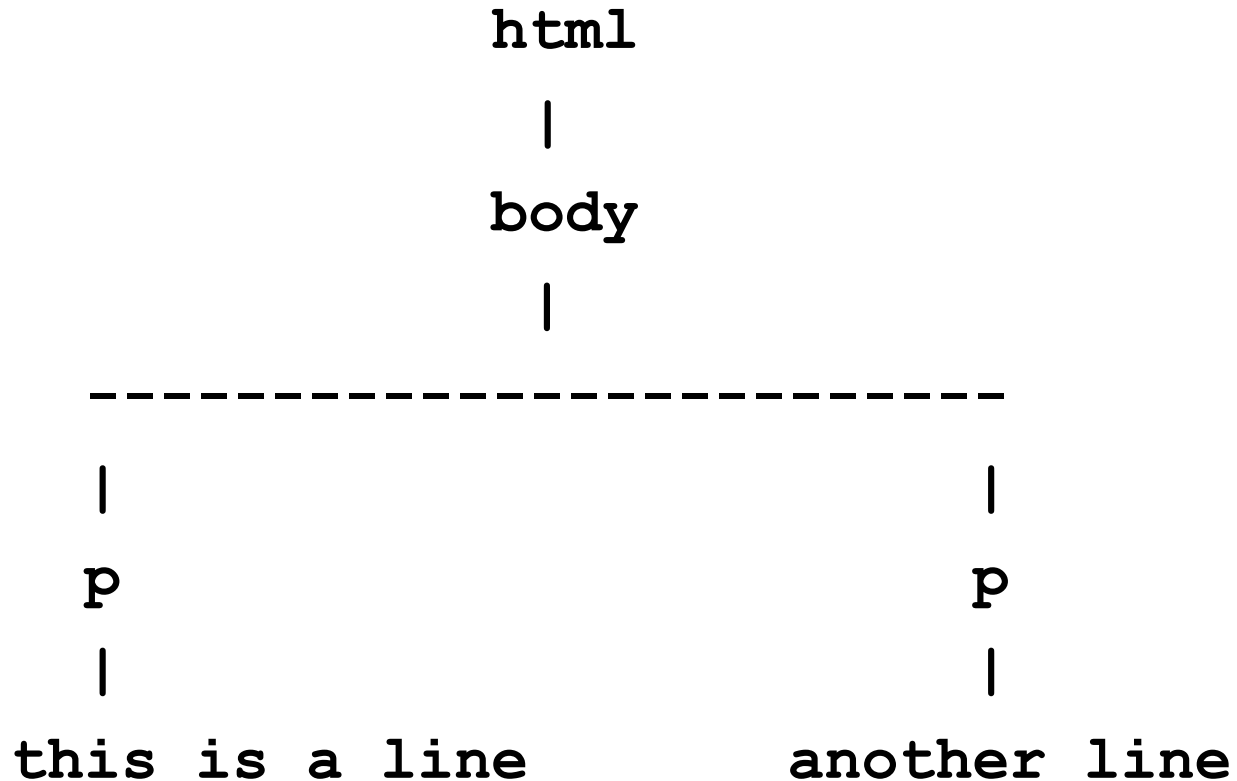
</body>

</html>

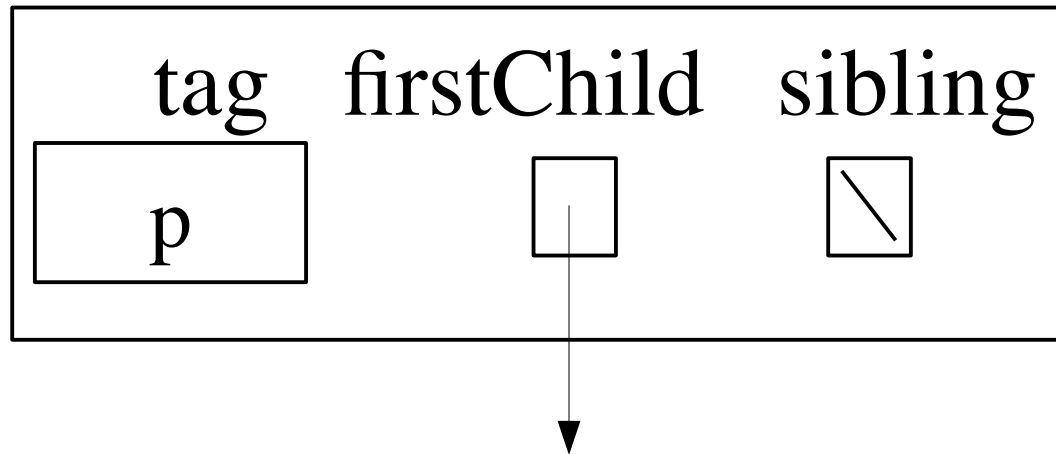
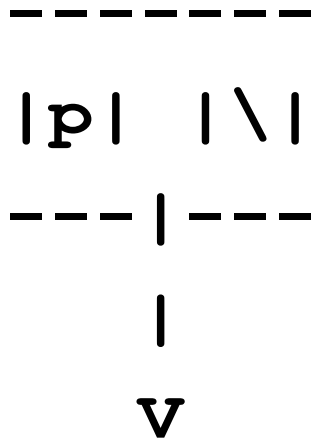
The tree as we think about it



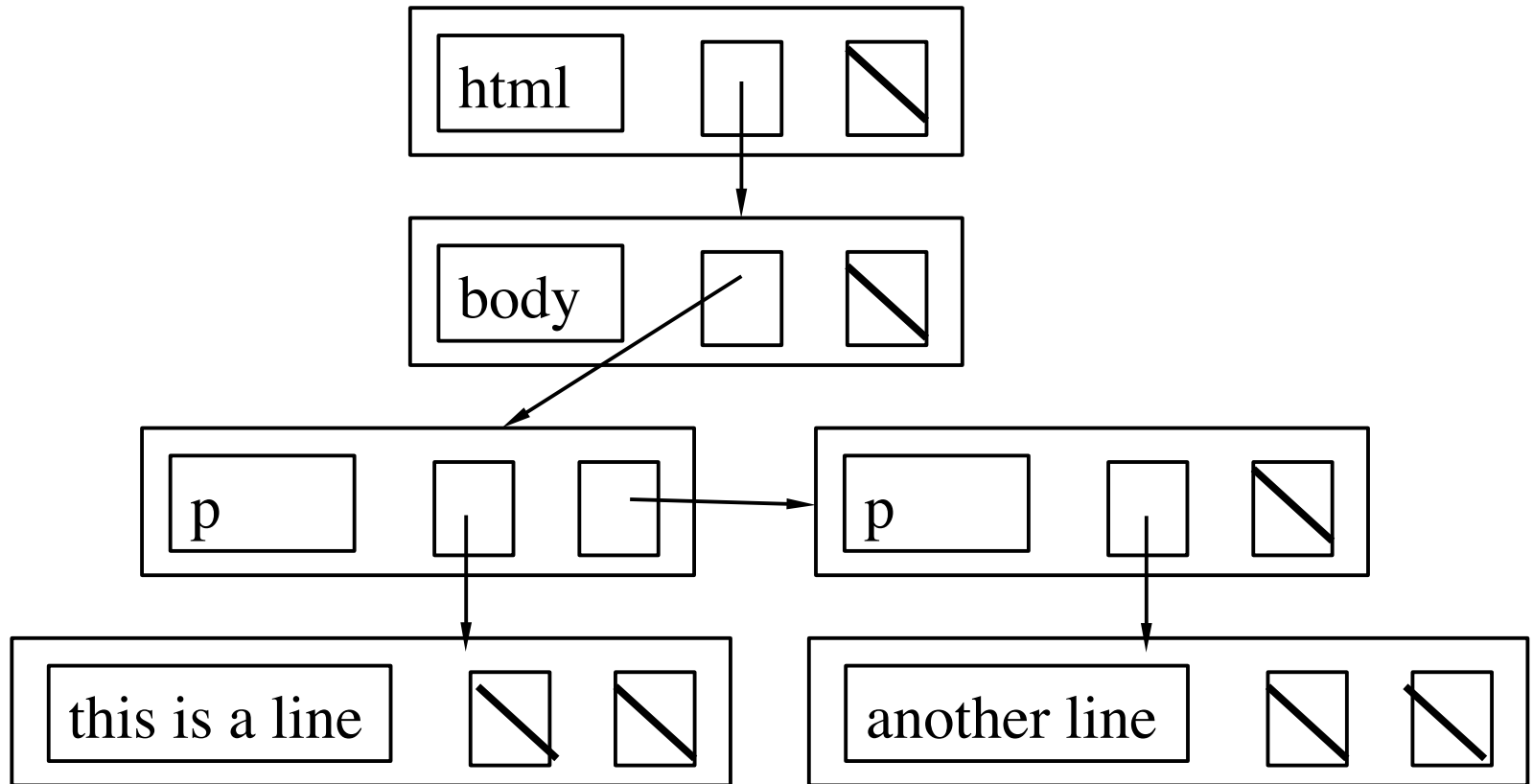
The tree as we drew it



TagNodes



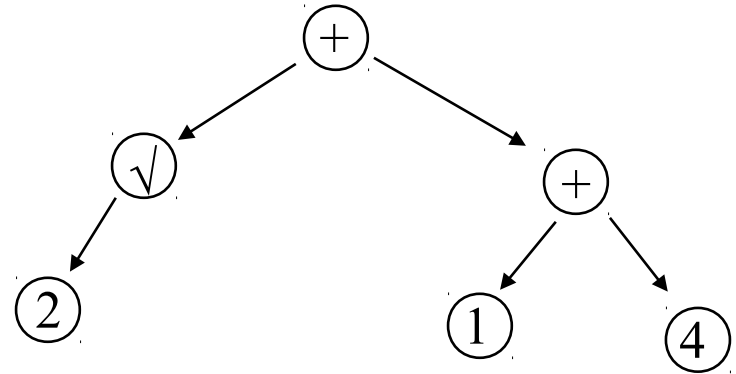
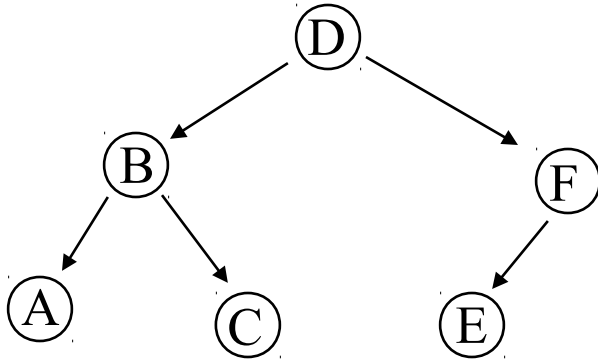
Tree as TagNodes



Tree Traversals

- **“Visit” each node in the tree**
 - **“visit” = do something, e.g. print**
- **In some systematic order**
 - **eg “inorder”:**
 - visit all nodes in left subtree**
 - then visit node**
 - then visit all nodes in right subtree**

Traversals



InOrder A B C D E F

$2 \sqrt{1 + 4}$

See `TreeNode.java`

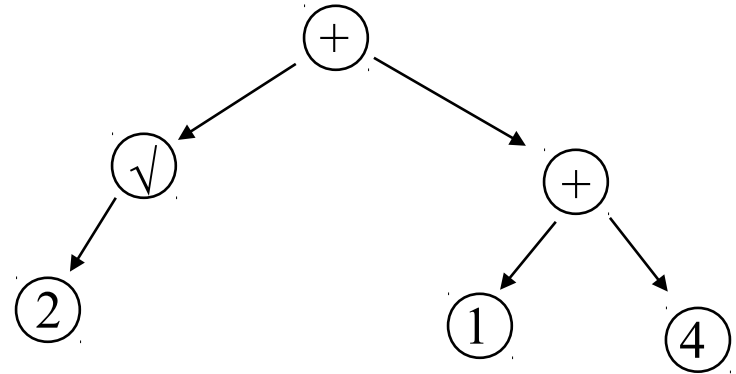
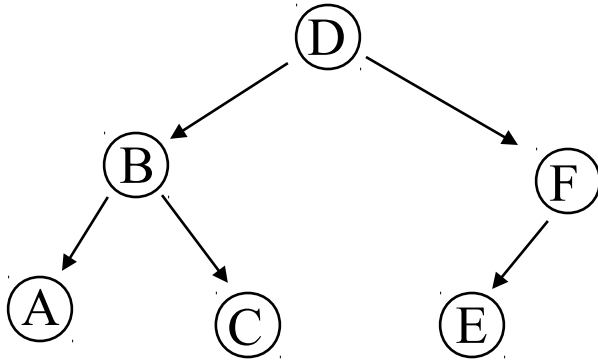
Recursive Traversals

```
inOrderPrint(tree):  
    if (tree == null)  
        return  
    inOrderPrint(tree.lst)  
    print(tree.node)  
    inOrderPrint(tree.rst)
```

```
preOrderPrint(tree):  
    if (tree == null)  
        return  
    print(tree.node)  
    preOrderPrint(tree.left)  
    preOrderPrint(tree.right)
```

```
postOrderPrint(tree):  
    if (tree == null)  
        return  
    postOrderPrint(tree.lst)  
    postOrderPrint(tree.rst)  
    print(tree.node)
```

Traversals



InOrder A B C D E F

2 √ + 1 + 4

PreOrder D B A C F E

+ √ 2 + 1 4

PostOrder A C B E F D

2 √ 1 4 + +

Depth vs Breadth first

- **Depth first**
 - when you start a node, do its whole subtree before anything else
 - recursion or stack
- **Breadth first**
 - do all at same level before anything else
 - queue

New: Huffman Encoding

Data Compression:

- **In most data some symbols appear more often than others**
 - **Eg English text ‘e’ appears more often than ‘q’**
- **Can we make use of this to reduce the average number of bits in a message?**

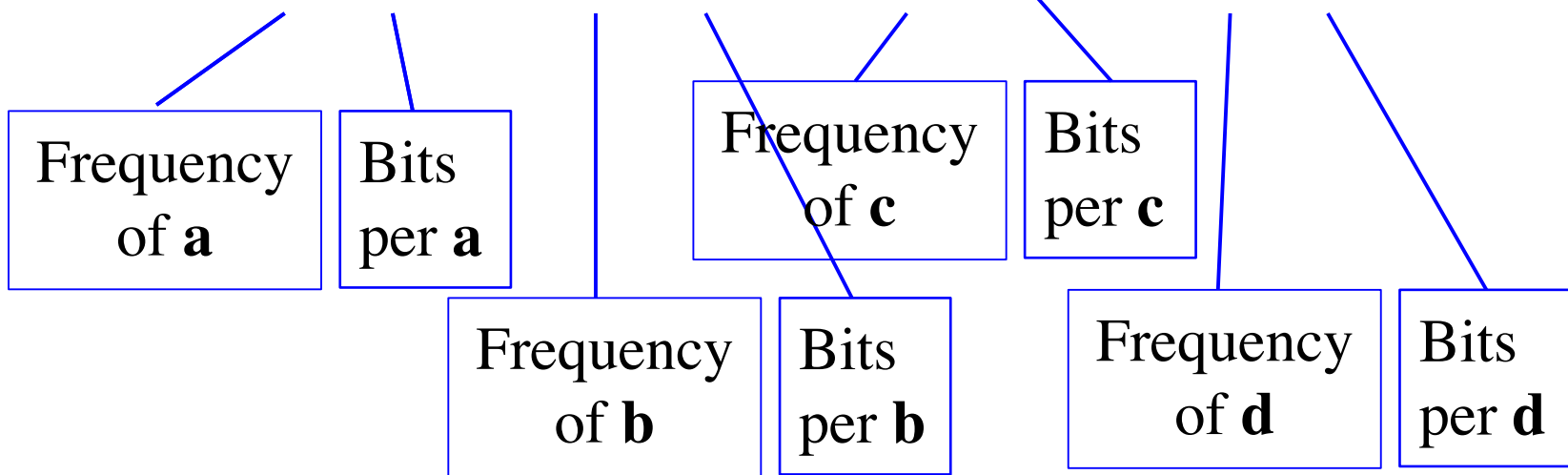
Fixed-length Code

- **EG 4 symbols: a, b, c, d with frequencies:**
 - **a: 50%, b: 30%, c: 10%, d:10%**
- **Fixed length code: 2 bits / character**
 - **e.g: 00 = a, 01 = b, 10 = c, 11 = d**
 - **aabcbaa = 00000110010000**
 - **14 bits / 7 characters = 2 bits/character**
- **Decode: 00010010 = abac**

Fixed-length Code

- **EG 4 symbols: a, b, c, d with frequencies:**
 - **a: 50%, b: 30%, c: 10%, d:10%**
- **Fixed length code: 2 bits / character**
- **Average bits per character:**

$$0.5*2 + 0.3*2 + 0.1*2 + 0.1*2 = 2$$



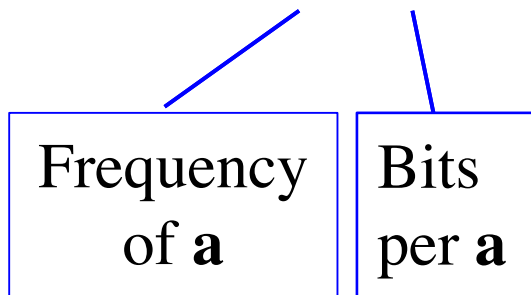
Variable Length Code

- **EG 4 symbols: a, b, c, d with different frequencies:**
 - **a: 50% , b: 30% , c: 10% , d:10%**
- **Variable length code: 1, 2, or 3 bits / character**
 - **e.g: 0 = a, 10 = b, 110 = c, 111 = d**
 - **aabcbaa = 00101101000**
 - **11 bits / 7 characters = 1.6 bits/character**
- **Decode: 0100110 = 'abac'**

Variable Length Code

- **EG 4 symbols: a, b, c, d with different frequencies:**
 - **a: 50% , b: 30% , c: 10% , d:10%**
- **Variable length code: 1, 2, or 3 bits / character**
 - **e.g: 0 = a, 10 = b, 110 = c, 111 = d**
- **Average bits per character:**

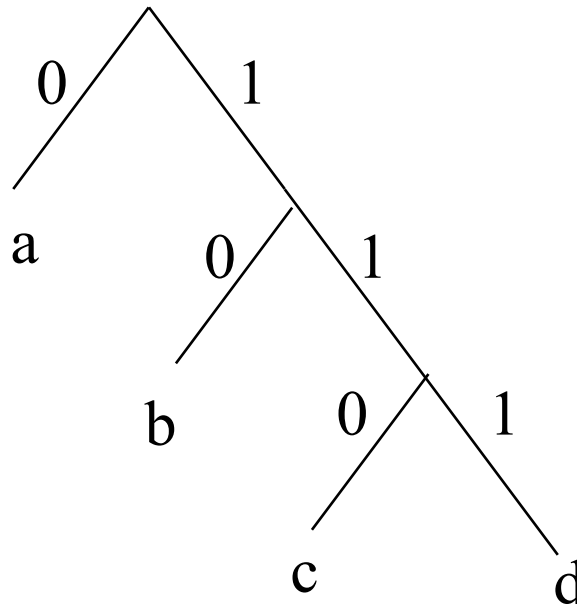
$$0.5*1 + 0.3*2 + 0.1*3 + 0.1*3 = 1.7$$



Variable Length Code

- Suppose code was
 1 = a, 10 = b, 110 = c, 111 = d
- Decode 1111 as 'ad', as 'da', or as 'aaaa'?
- No character's code can be prefix of another

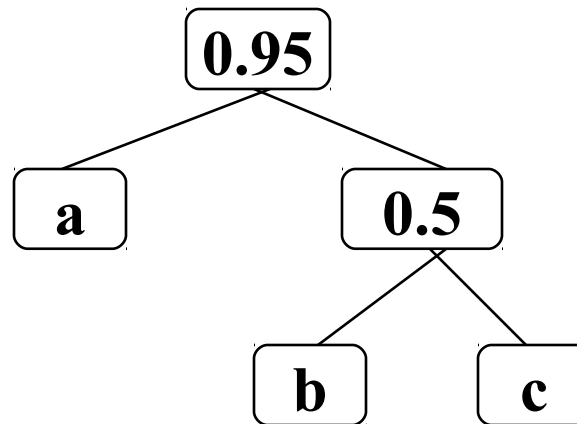
Huffman Code as a Tree



Symbols only at leaves

Algorithm

- **2 queues: S, T**
- **Contents of each queue: Tree**
 - A leaf node stores (an index of) a symbol
 - A non-leaf node stores total frequency of all symbols at leaves under this node
- **E.g., for frequencies a: 0.45, b: 0.3, c: 0.2:**



Algorithm

- **2 queues:**
 - **S initially holds 1-node trees for all symbols, least likely first**
 - **T empty**

while not (S empty and T length == 1)

find two least-weight trees in S, T and dequeue them

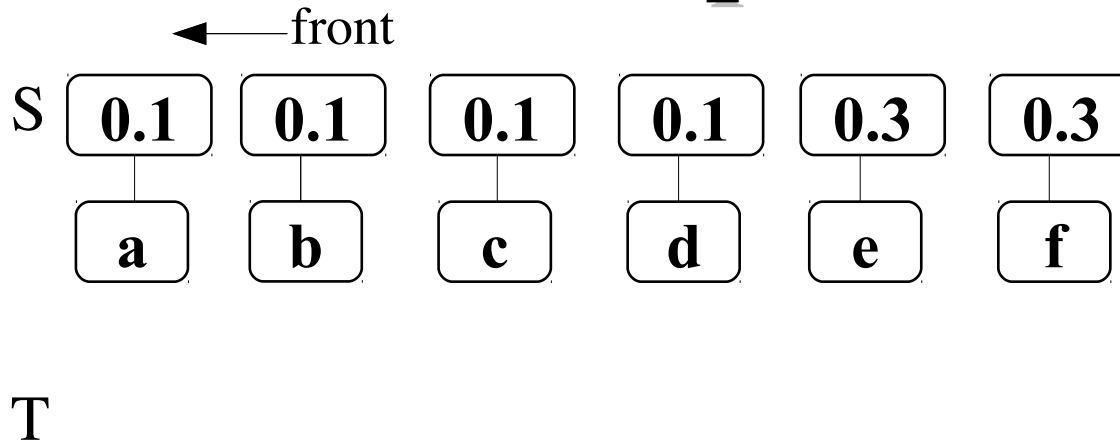
make a tree with these two as subtrees

enqueue this tree on T

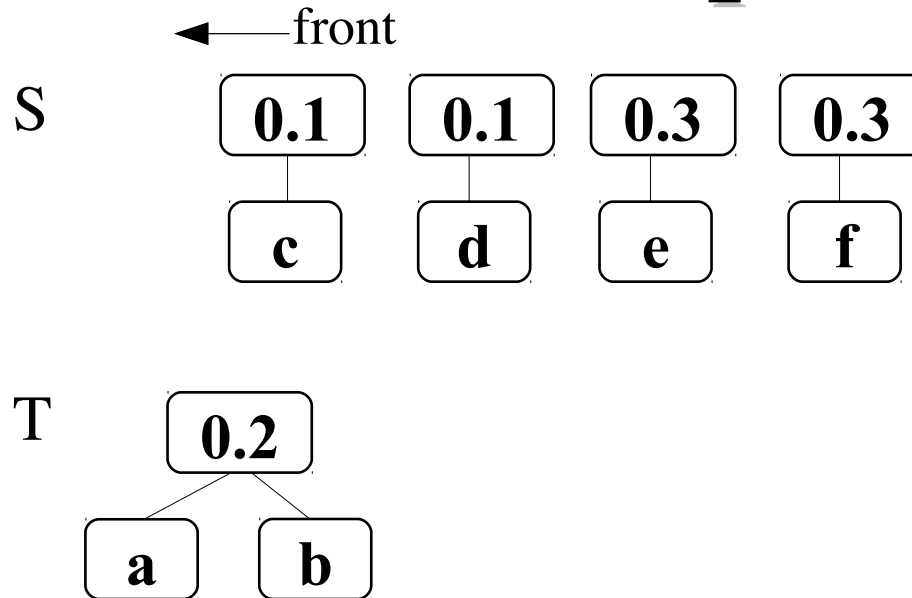
Example

A	.1
B	.1
C	.1
D	.1
E	.3
F	.3

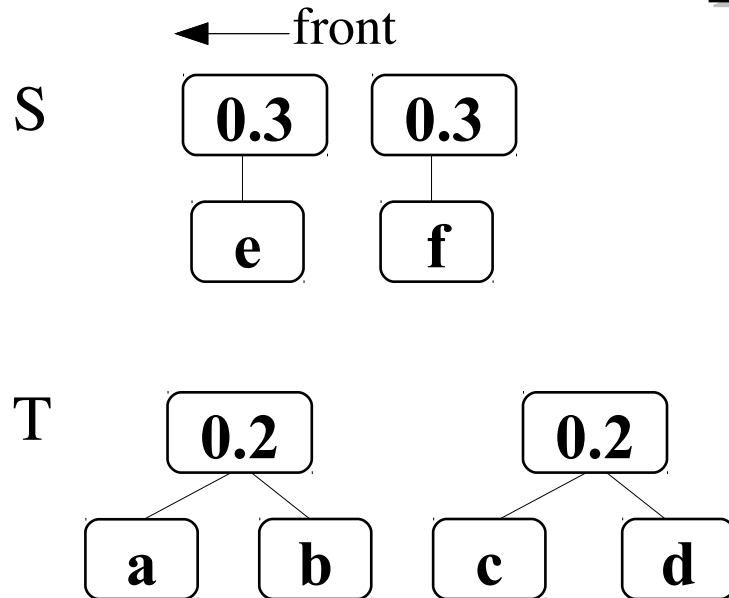
Example



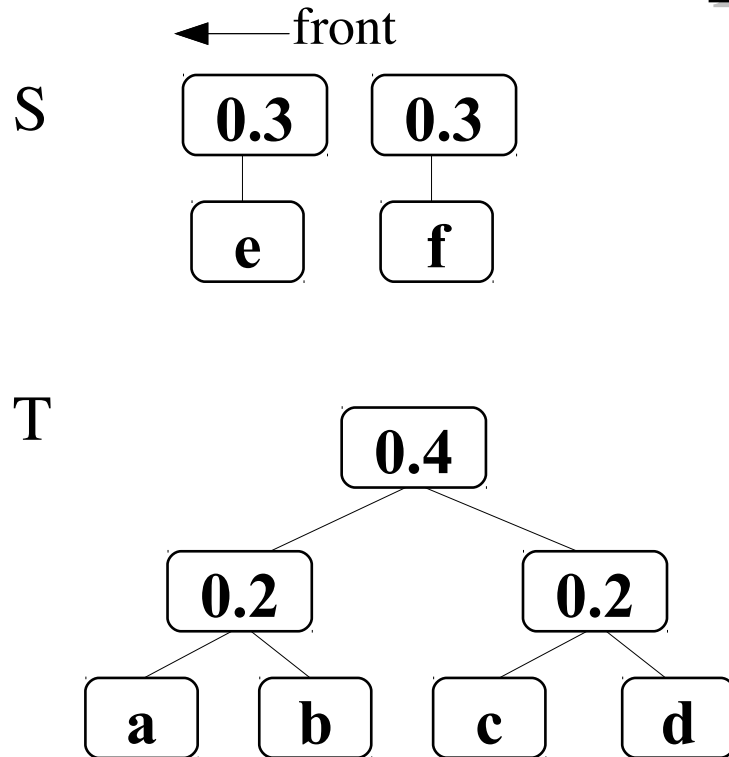
Example



Example



Example

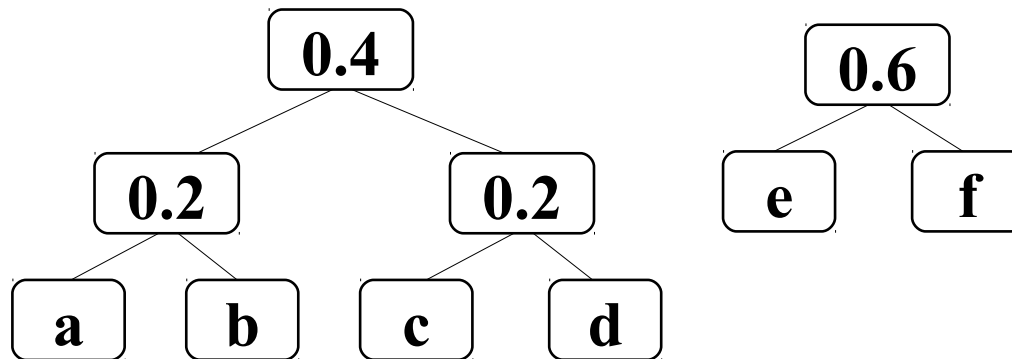


Example

← front

S

T

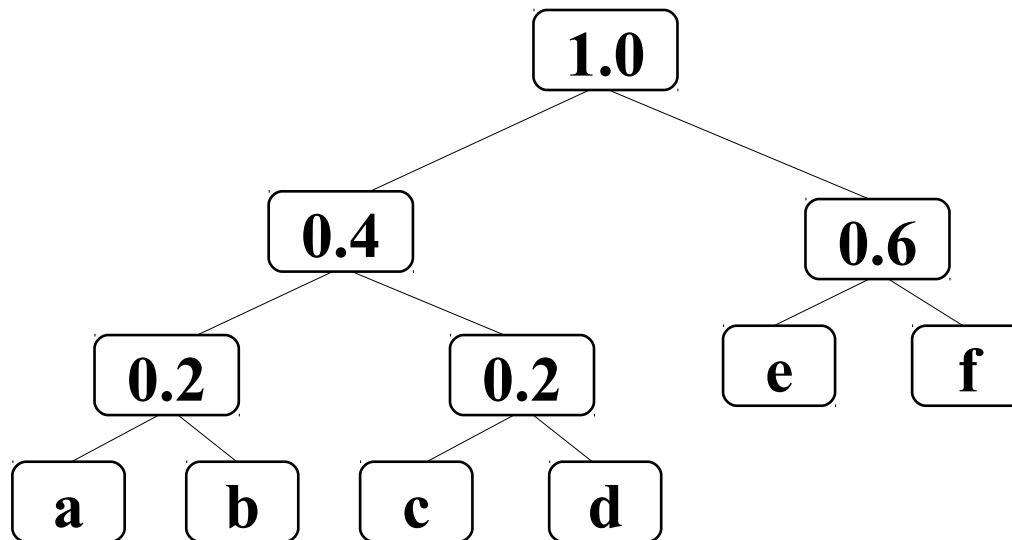


Example

← front

S

T



Book code

- See **Huffman.java** and **HuffmanDriver.java** in **dsoi.progs.src.zip** in **apps/tree/**