

## Introduction

# Deprecated prior art with "tilted loss function":

<https://towardsdatascience.com/deep-quantile-regression-c85481548b5a>

## Configuration

# Eager

```
import tensorflow as tf
tf.enable_eager_execution()
```

```
/databricks/python/lib/python3.7/site-packages/botocore/vendored/requests/packages/urllib3/_collections.py:1: DeprecationWarning: Using or importing the ABCs from 'collections' instead of from 'collections.abc' is deprecated, and in 3.8 it will stop working
from collections import Mapping, MutableMapping
```

# fix random seed for reproducibility

```
import random
import scipy
import numpy as np
import keras
```

```
RANDOM_SEED = 0
random.seed(RANDOM_SEED)
np.random.seed(RANDOM_SEED)
tf.set_random_seed(RANDOM_SEED)
```

```
tf.logging.set_verbosity(tf.logging.ERROR)
```

Using TensorFlow backend.

```
# Versioning
print("SCIPY=", scipy.__version__)
print("NUMPY=", np.__version__)
print("TENSORFLOW=", tf.__version__)
print("KERAS=", keras.__version__)
```

```
SCIPY= 1.2.1
NUMPY= 1.16.2
TENSORFLOW= 1.15.0
KERAS= 2.2.5
```

## Credentials

```
# Get credential to read
key=dbutils.secrets.get(scope="application-secrets", key="enterprisedatalakeprodsas")

container_list = [
    'customer',
    'customerorder',
    'foundation',
    'pricing',
    'sales',
    'cdaworkspace'
]

# Setup access to read from any container in container list
for container in container_list:
    spark.conf.set(
        "fs.azure.sas.
{container}.enterprisedatalakeprod.blob.core.windows.net".format(container=container),
        key
    )

from pyspark.sql import SparkSession

# Create sparkContext
spark = SparkSession.builder.master("local[*]").getOrCreate()
sc = spark.sparkContext
sc._jsc.hadoopConfiguration().set("fs.azure.sas.cdaworkspace.enterprisedatalakeprod.bl
ob.core.windows.net", key)
```

## Read

```
import json

def view_avro(view_name, file_location):
```

```
df = spark.read.format('avro').option("inferSchema", "true").load(file_location)
df.createOrReplaceTempView(view_name)
shape = (df.count(), len(df.columns))
print("DATAFRAME_SHAPE=", shape)
return df, shape

def view_orc(view_name, file_location):
    df = spark.read.format('orc').option("inferSchema", "true").load(file_location)
    df.createOrReplaceTempView(view_name)
    shape = (df.count(), len(df.columns))
    print("DATAFRAME_SHAPE=", shape)
    return df, shape

def view_header_csv(view_name, file_location):
    df = spark.read.format('csv').option("inferSchema", "true").option("header",
'true').load(file_location)
    df.createOrReplaceTempView(view_name)
    shape = (df.count(), len(df.columns))
    print("DATAFRAME_SHAPE=", shape)
    return df, shape

def view_blob_csv(view_name, file_name):
    file_path =
'wasbs://cdaworkspace@enterprisedatalakeprod.blob.core.windows.net/cda/prod/'
    df = spark.read.format('csv').option("inferSchema", "true").option("header",
'true').load(file_path+file_name)
    df.createOrReplaceTempView(view_name)
    shape = (df.count(), len(df.columns))
    print("DATAFRAME_SHAPE=", shape)
    return df, shape

def view_schema_csv(view_name, file_location, table_schema):
    df = spark.read.format('csv').schema(table_schema).load(file_location)
    df.createOrReplaceTempView(view_name)
    shape = (df.count(), len(df.columns))
    print("DATAFRAME_SHAPE=", shape)
    return df, shape

def view_file(file_name):
    file_path =
'wasbs://cdaworkspace@enterprisedatalakeprod.blob.core.windows.net/cda/prod/'
    text_rdd = sc.textFile(file_path+file_name)
    return text_rdd
```

```
%fs ls
```

path
dbfs:/FileStore/
dbfs:/databricks/
dbfs:/databricks-datasets/
dbfs:/databricks-results/
dbfs:/delta/
dbfs:/ml/
dbfs:/mnt/
dbfs:/tmp/
dbfs:/user/



# Training Dataset

## Purchase

```
purchase_regression_df, purchase_regression_shape =
view_blob_csv('purchase_regression_view', 'LTV_BF_US_Regression_sales.csv')
```

```
DATAFRAME_SHAPE= (6492696, 102)
```

```
purchase_regression_df.printSchema()
```

```
root
|-- customer_key: decimal(9,0) (nullable = true)
|-- spend_6mo_sls: double (nullable = true)
|-- repeat_spend_6mo_sls: double (nullable = true)
|-- item_qty_6mo_sls: string (nullable = true)
|-- spend_12mo_sls: double (nullable = true)
|-- repeat_spend_12mo_sls: double (nullable = true)
|-- item_qty_12mo_sls: string (nullable = true)
|-- spend_24mo_sls: double (nullable = true)
|-- repeat_spend_24mo_sls: double (nullable = true)
```

```
|-- item_qty_24mo_sls: string (nullable = true)
|-- onsale_qty_6mo_sls: string (nullable = true)
|-- onsale_qty_12mo_sls: string (nullable = true)
|-- onsale_qty_24mo_sls: string (nullable = true)
|-- num_txns_6mo_sls: string (nullable = true)
|-- num_txns_12mo_sls: string (nullable = true)
|-- num_txns_24mo_sls: string (nullable = true)
|-- repeat_num_txns_6mo_sls: string (nullable = true)
|-- repeat_num_txns_12mo_sls: string (nullable = true)
|-- repeat_num_txns_24mo_sls: string (nullable = true)
```

```
display(purchase_regression_df.describe())
```

summary ▼	customer_key ▼	spend_6mo_sls ▼	repeat_spend_6mo_sls ▼	item_qty_6mo_sls
count	6492696	6492696	6492696	6492696
mean	195510649.6123	47.991817372949725	2.3076863278369153	5.68607292861858
stddev	1.0857491852506673E8	108.26365583092777	40.53191933238156	9.12364537997196
min	115	-15.49	-3116.7099999999994	1
max	395764197	48379.44000000747	11595.8299999999876	NA



## Return

```
return_regression_df, return_regression_shape =
view_blob_csv('return_regression_view', 'LTV_BF_US_Regression_return.csv')
```

```
DATAFRAME_SHAPE= (6492696, 46)
```

```
return_regression_df.printSchema()
```

```
root
|-- customer_key: decimal(9,0) (nullable = true)
|-- spend_6mo_rtn: double (nullable = true)
|-- item_qty_6mo_rtn: string (nullable = true)
|-- spend_12mo_rtn: double (nullable = true)
|-- item_qty_12mo_rtn: string (nullable = true)
|-- spend_24mo_rtn: double (nullable = true)
```

```
|-- item_qty_24mo_rtn: string (nullable = true)
|-- onsale_qty_6mo_rtn: string (nullable = true)
|-- onsale_qty_12mo_rtn: string (nullable = true)
|-- onsale_qty_24mo_rtn: string (nullable = true)
|-- num_txns_6mo_rtn: string (nullable = true)
|-- num_txns_12mo_rtn: string (nullable = true)
|-- num_txns_24mo_rtn: string (nullable = true)
|-- spend_6mo_men_rtn: double (nullable = true)
|-- item_qty_6mo_men_rtn: string (nullable = true)
|-- spend_6mo_women_rtn: double (nullable = true)
|-- item_qty_6mo_women_rtn: string (nullable = true)
|-- spend_6mo_accessories_rtn: double (nullable = true)
|-- item_qty_6mo_accessories_rtn: string (nullable = true)
```

```
display(return_regression_df.describe())
```

summary ▼	customer_key ▼	spend_6mo_rtn ▼	item_qty_6mo_rtn ▼	spend_12mo_rtn ▼	item_qty_12mo_rtn ▼
count	6492696	6492696	6492696	6492696	6492696
mean	195510649.6123	4.708404126731888	-2.980244666635949	8.40134604177409	-3.30134604177409
stddev	1.0857491852506663E8	29.0342673897853	3.9007880112960986	43.00482727367231	4.9007880112960986
min	115	0.0	-1	0.0	-1
max	395764197	6640.1799999999973	NA	9865.579999999996	NA



## Labels

```
ground_truth_col_names = ['validation_spend_sls', 'validation_num_txns_sls',
                           'validation_item_qty_sls',
                           'validation_spend_rtn', 'validation_num_txns_rtn',
                           'validation_item_qty_rtn',
                           'net_txn_amt']
purchase_label_name = 'validation_spend_sls'
return_label_name = 'validation_spend_rtn'
```

## Join Purchase and Return

```
to_join_cols = ['customer_key', return_label_name]
return_regression_select_df = return_regression_df.select(*to_join_cols)
```

```
overall_df = purchase_regression_df.join(return_regression_select_df,
on='customer_key', how='inner')
```

```
overall_df.printSchema()
```

```
root
|-- customer_key: decimal(9,0) (nullable = true)
|-- spend_6mo_sls: double (nullable = true)
|-- repeat_spend_6mo_sls: double (nullable = true)
|-- item_qty_6mo_sls: string (nullable = true)
|-- spend_12mo_sls: double (nullable = true)
|-- repeat_spend_12mo_sls: double (nullable = true)
|-- item_qty_12mo_sls: string (nullable = true)
|-- spend_24mo_sls: double (nullable = true)
|-- repeat_spend_24mo_sls: double (nullable = true)
|-- item_qty_24mo_sls: string (nullable = true)
|-- onsale_qty_6mo_sls: string (nullable = true)
|-- onsale_qty_12mo_sls: string (nullable = true)
|-- onsale_qty_24mo_sls: string (nullable = true)
|-- num_txns_6mo_sls: string (nullable = true)
|-- num_txns_12mo_sls: string (nullable = true)
|-- num_txns_24mo_sls: string (nullable = true)
|-- repeat_num_txns_6mo_sls: string (nullable = true)
|-- repeat_num_txns_12mo_sls: string (nullable = true)
|-- repeat_num_txns_24mo_sls: string (nullable = true)
|-- spend_6mo_men_sls: double (nullable = true)
```

```
display(overall_df)
```

customer_key ▼	spend_6mo_sls ▼	repeat_spend_6mo_sls ▼	item_qty_6mo_sls ▼	spend_12mo_sls
8440	73.77999999999999	0	4	73.77999999999999
13248	0	0	NA	0
31156	23.39	0	2	23.39
32912	171.78000000000003	0	8	267.2500000000
33013	0	0	NA	0

39473	16	0	1	16
40436	0	0	NA	0
55474	16.88	0	0	16.88

Showing the first 1000 rows.



# Model Training



```
import warnings
warnings.filterwarnings('ignore')

# General libraries
import sys,os,time
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
import seaborn as sns
import seaborn as sb
from statistics import median

# ML libraries
from sklearn.model_selection import train_test_split
from sklearn.preprocessing import LabelEncoder
from sklearn.preprocessing import StandardScaler
from sklearn.preprocessing import RobustScaler
from sklearn.pipeline import Pipeline
from sklearn.utils import resample
from sklearn.ensemble import RandomForestRegressor as rfr
from keras import layers
import tensorflow as tf
from keras import backend as K
from keras.models import Sequential
from keras.layers import Dense
from keras.wrappers.scikit_learn import KerasClassifier
from sklearn.model_selection import StratifiedKFold
from sklearn.model_selection import cross_val_score
from sklearn import preprocessing
from keras import regularizers
from keras.layers import Dropout
from sklearn.metrics import roc_auc_score
from sklearn.metrics import accuracy_score
from keras.constraints import max_norm
from keras.models import model_from_json
from keras.layers.advanced_activations import LeakyReLU
from keras.callbacks import ModelCheckpoint
from sklearn.metrics import mean_absolute_error
from sklearn.metrics import median_absolute_error
from sklearn.preprocessing import MinMaxScaler
import keras.backend as K
```

```

from pyspark.sql.types import DoubleType
import pyspark.sql.functions as F

```

```
CAST_COLUMN_TAG = '_'
```

```

def na_and_fill(df):
    return df \
        .dropna()
        # TODO: revisit this assumption vs fillna(0)?

```

```

def cast_column(df):
    for col_name in df.in.columns:
        cast_col_name = col_name + CAST_COLUMN_TAG
        df = df \
            .withColumn(cast_col_name, df[col_name].cast(DoubleType())) \
            .drop(col_name)
    return df

```

```

def drop_null(df):
    null_counts = df.select([F.count(F.when(F.col(c).isNull(), c)).alias(c) for c in
df.columns]) \
        .collect()[0] \
        .asDict()
    to_drop = [k for k, v in null_counts.items() if v > 0]
    df = df.drop(*to_drop)

    return df, to_drop

```

```
# TODO: Cap outliers?
```

```

def filter_negative(df):
    for col_name in ground_truth_col_names:
        try:
            df = df.filter(df[col_name] > 0)
        except:
            pass
    return df

```

```
df_in = overall_df.drop('customer_key')
```

```
df = na_and_fill(df_in)
```

```
df = cast_column(df)
```

```
df = filter_negative(df)
```

```
df_final, to_drop = drop_null(df)
```

```
print("COLUMN_TO_DROP=", to_drop)
```

```
assert df_final.count() > 0, "DATAFRAME_LENGTH_ERROR"
```

```
COLUMN_TO_DROP= ['item_qty_6mo_sls_', 'item_qty_12mo_sls_', 'item_qty_24mo_sls_', 'onsale_qty_6mo_sls_', 'onsale_qty_12mo_sls_', 'onsale_qty_24mo_sls_', 'num_txns_6mo_sls_', 'num_txns_12mo_sls_', 'num_txns_24mo_sls_', 'repeat_num_txns_6mo_sls_', 'repeat_num_txns_12mo_sls_', 'repeat_num_txns_24mo_sls_', 'item_qty_6mo_men_sls_', 'item_qty_6mo_women_sls_', 'item_qty_6mo_accessories_sls_', 'item_qty_6mo_plcb_sls_', 'item_qty_12mo_plcb_sls_', 'item_qty_24mo_plcb_sls_', 'num_plcb_txns_6mo_sls_', 'num_plcb_txns_12mo_sls_', 'num_plcb_txns_24mo_sls_', 'item_qty_6mo_sls_sb_', 'item_qty_12mo_sls_sb_', 'item_qty_24mo_sls_sb_', 'onsale_qty_6mo_sls_sb_', 'onsale_qty_12mo_sls_sb_', 'onsale_qty_24mo_sls_sb_', 'num_txns_6mo_sls_sb_', 'num_txns_12mo_sls_sb_', 'num_txns_24mo_sls_sb_', 'item_qty_plcb_6mo_sls_sb_', 'item_qty_plcb_12mo_sls_sb_', 'item_qty_plcb_24mo_sls_sb_', 'num_plcb_txns_6mo_sls_sb_', 'num_plcb_txns_12mo_sls_sb_', 'num_plcb_txns_24mo_sls_sb_', 'item_qty_6mo_onl_sls_', 'item_qty_12mo_onl_sls_', 'item_qty_24mo_onl_sls_', 'num_txns_6mo_onl_sls_', 'num_txns_12mo_onl_sls_', 'num_txns_24mo_onl_sls_', 'item_qty_6mo_rtl_sls_', 'item_qty_12mo_rtl_sls_', 'item_qty_24mo_rtl_sls_', 'num_txns_6mo_rtl_sls_', 'num_txns_12mo_rtl_sls_', 'num_txns_24mo_rtl_sls_', 'stores_shopped_6mo_sls_', 'stores_shopped_12mo_sls_', 'stores_shopped_24mo_sls_', 'customer_duration_sb_', 'days_first_pur_sb_', 'days_last_pur_sb_', 'customer_duration_sb_onl_', 'days_first_pur_sb_onl_', 'days_last_pur_sb_onl_', 'customer_duration_sb_rtl_', 'days_first_pur_sb_rtl_', 'days_last_pur_sb_rtl_', 'customer_duration_', 'days_first_pur_', 'days_last_pur_', 'customer_duration_onl_', 'days_first_pur_onl_', 'days_last_pur_onl_', 'customer_duration_rtl_', 'days_first_pur_rtl_', 'days_last_pur_rtl_', 'days_on_books_', 'card_status_', 'mapped_source_', 'validation_item_qty_sls_', 'validation_num_txns_sls_', 'segment_flags_']
```

```
train_df, test_df, val_df = df_final.randomSplit([.7, .25, .05])
```

```
train_df.cache()
```

```
test_df.cache()
```

```
val_df.cache()
```

```
train_df.count(), test_df.count(), val_df.count()
```

```
Out[21]: (4544001, 1623432, 325263)
```

```
display(train_df)
```

spend_6mo_sls_ ▼	repeat_spend_6mo_sls_ ▼	spend_12mo_sls_ ▼	repeat_spend_12mo_sls_ ▼	spen
0	-16.4500000000000017	0	-16.4500000000000017	0
0	0	0	0	0
0	0	0	0	0
0	0	0	0	0
0	0	0	0	0
0	0	0	0	0
0	0	0	0	0
0	0	0	0	0

Showing the first 1000 rows.



## Ground truth columns renamed

```
ground_truth_col_renamed = [x+CAST_COLUMN_TAG for x in ground_truth_col_names]
purchase_label_renamed = purchase_label_name + CAST_COLUMN_TAG
return_label_renamed = return_label_name + CAST_COLUMN_TAG
```

## Input pipeline

```
# https://dwgeek.com/python-pyspark-iterator-how-to-create-and-use.html/
def get_dict_iter(df):
    return df.rdd.map(lambda r: r.asDict()).toLocalIterator()

# test
sample_iter = get_dict_iter(val_df)
```

```

def get_df_batch(df_iter, batch_size=100):
    batch = []
    for i in range(batch_size):
        try:
            next_is = next(df_iter)
            batch.append(next_is)
            # print(next_is)
        except:
            pass
    return batch

def get_tf_dataset_batch(df_iter, batch_size):
    batch_dict = get_df_batch(df_iter, batch_size)
    batch_pd = pd.DataFrame.from_dict(batch_dict)

    purchase_label_col = batch_pd.pop(purchase_label_renamed)
    return_label_col = batch_pd.pop(return_label_renamed)
    net_label_col = purchase_label_col - return_label_col
    dict_labels = (dict(batch_pd), net_label_col)

    tf_dataset = tf.data.Dataset.from_tensor_slices(dict_labels)
    return tf_dataset.batch(batch_size), batch_pd

```

```

# test
sample_ds, sample_pd = get_tf_dataset_batch(sample_iter, batch_size=1)

```

```

for feature_batch, label_batch in sample_ds.take(1):
    print('EVERY_FEATURE=', list(feature_batch.keys()))
    print('FEATURE_BATCH repeat_spend_12mo_sls=',
feature_batch['repeat_spend_12mo_sls_'])
    print('TARGET_BATCH=', label_batch )

```

```

EVERY_FEATURE= ['net_txn_amt_', 'repeat_spend_12mo_sls_', 'repeat_spend_24mo_sls_', 'r
epeat_spend_6mo_sls_', 'spend_12mo_onl_sls_', 'spend_12mo_plcb_sls_', 'spend_12mo_plcb
_sls_sb_', 'spend_12mo_rtl_sls_', 'spend_12mo_sls_', 'spend_12mo_sls_sb_', 'spend_24mo
_onl_sls_', 'spend_24mo_plcb_sls_', 'spend_24mo_plcb_sls_sb_', 'spend_24mo_rtl_sls_',
'spend_24mo_sls_', 'spend_24mo_sls_sb_', 'spend_6mo_accessories_sls_', 'spend_6mo_men_
sls_', 'spend_6mo_onl_sls_', 'spend_6mo_plcb_sls_', 'spend_6mo_plcb_sls_sb_', 'spend_6
mo_rtl_sls_', 'spend_6mo_sls_', 'spend_6mo_sls_sb_', 'spend_6mo_women_sls_']
FEATURE_BATCH repeat_spend_12mo_sls_ = tf.Tensor([0.], shape=(1,), dtype=float64)
TARGET_BATCH= tf.Tensor([0.], shape=(1,), dtype=float64)

```

```

# test
from tensorflow import feature_column

sample_batch = next(iter(sample_ds))[0]
col = feature_column.numeric_column('repeat_spend_12mo_sls_')
sample_layer = tf.keras.layers.DenseFeatures(col)
layer_numpy = sample_layer(sample_batch).numpy()

print("layer_numpy=", layer_numpy)
assert len(layer_numpy)>0, "BATCHING_FAILED"

layer_numpy= [[0.]]

from tensorflow.keras.layers import Layer

def avoid_snooping_truth(xy_pd):
    x_pd = xy_pd

    for col in ground_truth_col_renamed:
        try:
            x_pd.drop(col)
        except:
            pass

    return x_pd

def get_numeric_features(x_pd):
    feature_columns = []
    numeric_columns = x_pd.select_dtypes(include=['float64']).columns
    for header in numeric_columns:
        feature_columns.append(feature_column.numeric_column(header))
    return feature_columns

def get_features(xy_pd):
    x_pd = avoid_snooping_truth(xy_pd)

    feature_columns = []
    feature_columns += get_numeric_features(x_pd)
    # feature_columns += get_indicator_features(x_pd)

    feature_layer = tf.keras.layers.DenseFeatures(feature_columns)
    # print("feature_columns", feature_columns)

```

```

return feature_layer

def get_indicator_features(x_pd):
    feature_columns = []
    indicator_columns = x_pd.select_dtypes(include=['object']).columns

    for col in indicator_columns:
        category_feature = feature_column.categorical_column_with_vocabulary_list(col,
indicator_columns)
        onehot_feature = feature_column.indicator_column(category_feature)
        feature_columns.append(onehot_feature)
    return feature_columns

# test
sample_layer = get_features(sample_pd)

sample_layer

Out[30]: <tensorflow.python.feature_column.dense_features.DenseFeatures at 0x7efd0e118
5f8>

def neural_net_model(input_layer,
                        hidden_layer_neuron_count=256, num_hidden_layers=4):
    layers = [input_layer]
    for i in range(num_hidden_layers):
        layers.append(tf.keras.layers.Dense(hidden_layer_neuron_count,
kernel_initializer='normal', activation='relu'))
        layers.append(tf.keras.layers.Dense(1, kernel_initializer='normal',
activation='linear'))
    model = tf.keras.Sequential(layers)
    return model

from collections import defaultdict

from keras.callbacks import History
from keras.callbacks import EarlyStopping

def train_model(model_key,
                  loss_function,

```

```

        train_df, test_df,
        learning_rate,
        layer_neurons_nonlinear, num_layers_nonlinear,
        whole_epochs=1, epoch_per_batch=1000 # relies on EarlyStopping
    ):

num_batches = 10
batch_size = int(train_df.count()/num_batches)

test_iter = get_dict_iter(test_df)
test_ds, test_pd = get_tf_dataset_batch(test_iter, batch_size)
feature_layer = get_features(test_pd)

training_model = neural_net_model(feature_layer, layer_neurons_nonlinear,
num_layers_nonlinear)
# keras_wrapper = keras.wrappers.scikit_learn.KerasRegressor(training_model)
training_model.compile(loss=loss_function,
                        optimizer=tf.keras.optimizers.SGD(learning_rate=learning_rate),
                        metrics=[loss_function, 'mean_absolute_error'])

training_history = []

while whole_epochs > 0:
    train_iter = get_dict_iter(train_df) # .orderBy(rand())

    while num_batches > 0:
        print("\n\n*****\n",
              "MODEL_KEY=", model_key,
              "REMAINING_EPOCHS=", whole_epochs,
              "REMAINING_BATCHES=", num_batches,
              "\n\n*****\n")

        train_ds, train_pd = get_tf_dataset_batch(train_iter, batch_size)

        history = History()
        training_model.fit(train_ds,
                           validation_data=test_ds,
                           shuffle=True,
                           epochs=epoch_per_batch,
                           callbacks=[history,
                                     EarlyStopping(monitor='val_loss', mode='auto',
patience=5)]) # min_delta=1
        training_history.append(history)

        num_batches-=1

```



```

whole_epochs=1

return training_model, training_history

def train_models(hyper_params):
    param_model = {}
    param_history = {}

    for loss in hyper_params['loss_function']:
        for height in hyper_params['layer_neurons_nonlinear']:
            for depth in hyper_params['num_layers_nonlinear']:
                for rate in hyper_params['learning_rate']:
                    for whole_epochs in hyper_params['whole_dataset_epochs']:
                        for epoch_per_batch in hyper_params['epoch_per_batch']:
                            try:
                                model_key = '-' + 'depth=' + str(depth) + '-' + 'height=' +
str(height) + \
                                '-' + 'whole_epochs=' + str(whole_epochs) + '-' + 'epoch_per_batch='
+ str(epoch_per_batch) + \
                                '-' + 'loss=' + loss + '-' + 'rate=' + str(rate)
                                model, history = train_model(model_key,
                                                                loss,
                                                                train_df, test_df,
                                                                rate,
                                                                layer_neurons_nonlinear=height,
                                                                num_layers_nonlinear=depth,
                                                                whole_epochs=whole_epochs,
                                                                epoch_per_batch=epoch_per_batch)
                                param_model[model_key] = model
                                param_history[model_key] = history
                            except Exception as e:
                                print("TRAINING_EXCEPTION", model_key, e)

    return param_model, param_history

```

```

def choose_model(param_model, param_history):
    COMPARISON_BATCH_SIZE = 250000
    test_iter = get_dict_iter(test_df)
    test_ds, test_pd = get_tf_dataset_batch(test_iter, batch_size=COMPARISON_BATCH_SIZE)

    chosen_key = None
    chosen_model = None
    chosen_test_loss = None
    chosen_test_error = None
    for model_key, model in param_model.items():
        try:
            test_evaluation = model.evaluate(test_ds)
            test_loss = test_evaluation[0]
            test_objective_error = test_evaluation[1]
            print("MODEL_EVALUATED=", model_key, "TRAIN_LOSS=", test_loss, "TRAIN_ERROR=",
test_objective_error)
            if chosen_model == None or (test_loss < chosen_test_loss):
                chosen_key = model_key
                chosen_model = model
                chosen_test_loss = test_loss
                chosen_test_error = test_objective_error
                print("MODEL_SELECTED=", model_key)
        except Exception as e:
            print(model_key, "FAILED_SELECTION", e)
        pass
    return chosen_key, chosen_model, chosen_test_loss, chosen_test_error

def measure_model_performance(chosen_key, chosen_model):
    try:
        MEASUREMENT_BATCH_SIZE = 50000
        val_iter = get_dict_iter(val_df)
        val_ds, val_pd = get_tf_dataset_batch(val_iter, batch_size=MEASUREMENT_BATCH_SIZE)

        val_evaluation = chosen_model.evaluate(val_ds)
        loss = val_evaluation[0]
        error = val_evaluation[1]
        print("CHOSEN_MODEL=", chosen_key, "VALIDATION_ERROR=", error)
    except Exception as e:
        print(e)
    pass

```

# Run Model Training and Selection

## Loss = mean\_absolute\_percentage\_error

```
hyper_params = {}
hyper_params['loss_function'] = ['mean_absolute_percentage_error'] #
'mean_squared_error', mean_absolute_error, mean_squared_logarithmic_error,
cosine_similarity, huber_loss, log_cosh
hyper_params['num_layers_nonlinear'] = [1, 2, 3]
hyper_params['layer_neurons_nonlinear'] = [6, 12, 18]
hyper_params['learning_rate'] = [10**-12]

hyper_params['whole_dataset_epochs'] = [1] # 10
hyper_params['epoch_per_batch'] = [5]
```

```
param_model, param_history = train_models(hyper_params)
```

```
*****
MODEL_KEY= -depth=1-height=6-whole_epochs=1-epoch_per_batch=5-loss=mean_absolute_per
centage_error-rate=1e-12 REMAINING_EPOCHS= 1 REMAINING_BATCHES= 10
*****

Epoch 1/5

1/Unknown - 18s 18s/step - loss: 1945880192.0000 - mean_absolute_percentage_err
or: 1945880192.0000 - mean_absolute_error: 49.3841
1/1 [=====] - 35s 35s/step - loss: 1945880192.0000 - mean_ab
solute_percentage_error: 1945880192.0000 - mean_absolute_error: 49.3841 - val_loss: 0
.0000e+00 - val_mean_absolute_percentage_error: 0.0000e+00 - val_mean_absolute_error:
0.0000e+00
Epoch 2/5

1/1 [=====] - 32s 32s/step - loss: 262421216.0000 - mean_abs
olute_percentage_error: 262421216.0000 - mean_absolute_error: 46.2176 - val_loss: 330
273888.0000 - val_mean_absolute_percentage_error: 330273888.0000 - val_mean_absolute_
error: 45.5441
```

```
chosen_key, chosen_model, chosen_test_loss, chosen_test_error =
choose_model(param_model, param_history)
```

```
1/1 [=====] - 32s 32s/step - loss: 8739077.0000 - mean_absolute_percentage_error: 8739077.0000 - mean_absolute_error: 45.5943
MODEL_EVALUATED= -depth=1-height=6-whole_epochs=1-epoch_per_batch=5-loss=mean_absolute_percentage_error-rate=1e-12 TRAIN_LOSS= 8739077.0 TRAIN_ERROR= 8739077.0
MODEL_SELECTED= -depth=1-height=6-whole_epochs=1-epoch_per_batch=5-loss=mean_absolute_percentage_error-rate=1e-12
```

```
1/1 [=====] - 9s 9s/step - loss: 8143327.0000 - mean_absolute_percentage_error: 8143327.0000 - mean_absolute_error: 45.6253
MODEL_EVALUATED= -depth=2-height=6-whole_epochs=1-epoch_per_batch=5-loss=mean_absolute_percentage_error-rate=1e-12 TRAIN_LOSS= 8143327.0 TRAIN_ERROR= 8143327.0
MODEL_SELECTED= -depth=2-height=6-whole_epochs=1-epoch_per_batch=5-loss=mean_absolute_percentage_error-rate=1e-12
```

```
1/1 [=====] - 8s 8s/step - loss: 3672998.5000 - mean_absolute_percentage_error: 3672998.5000 - mean_absolute_error: 45.6250
MODEL_EVALUATED= -depth=3-height=6-whole_epochs=1-epoch_per_batch=5-loss=mean_absolute_percentage_error-rate=1e-12 TRAIN_LOSS= 3672998.5 TRAIN_ERROR= 3672998.5
MODEL_SELECTED= -depth=3-height=6-whole_epochs=1-epoch_per_batch=5-loss=mean_absolute_percentage_error-rate=1e-12
```

```
1/1 [=====] - 9s 9s/step - loss: 72781640.0000 - mean_absolute_percentage_error: 72781640.0000 - mean_absolute_error: 45.7747
MODEL_EVALUATED= -depth=1-height=12-whole_epochs=1-epoch_per_batch=5-loss=mean_absolute_percentage_error-rate=1e-12 TRAIN_LOSS= 72781640.0 TRAIN_ERROR= 72781640.0
```

```
1/1 [=====] - 8s 8s/step - loss: 10194882.0000 - mean_absolute_percentage_error: 10194882.0000 - mean_absolute_error: 45.6218
MODEL_EVALUATED= -depth=2-height=12-whole_epochs=1-epoch_per_batch=5-loss=mean_absolute_percentage_error-rate=1e-12 TRAIN_LOSS= 10194882.0 TRAIN_ERROR= 10194882.0
```

```
1/1 [=====] - 9s 9s/step - loss: 6754391.0000 - mean_absolute_percentage_error: 6754391.0000 - mean_absolute_error: 45.6325
MODEL_EVALUATED= -depth=3-height=12-whole_epochs=1-epoch_per_batch=5-loss=mean_absolute_percentage_error-rate=1e-12 TRAIN_LOSS= 6754391.0 TRAIN_ERROR= 6754391.0
```

```
1/1 [=====] - 9s 9s/step - loss: 132566992.0000 - mean_absolute_percentage_error: 132566992.0000 - mean_absolute_error: 45.5887
MODEL_EVALUATED= -depth=1-height=18-whole_epochs=1-epoch_per_batch=5-loss=mean_absolute_percentage_error-rate=1e-12 TRAIN_LOSS= 132566992.0 TRAIN_ERROR= 132566990.0
```

```
1/1 [=====] - 9s 9s/step - loss: 42452596.0000 - mean_absolut
e_percentage_error: 42452596.0000 - mean_absolute_error: 45.6428
MODEL_EVALUATED= -depth=2-height=18-whole_epochs=1-epoch_per_batch=5-loss=mean_absolut
e_percentage_error-rate=1e-12 TRAIN_LOSS= 42452596.0 TRAIN_ERROR= 42452596.0
```

```
1/1 [=====] - 9s 9s/step - loss: 11508606.0000 - mean_absolut
e_percentage_error: 11508606.0000 - mean_absolute_error: 45.6334
MODEL_EVALUATED= -depth=3-height=18-whole_epochs=1-epoch_per_batch=5-loss=mean_absolut
e_percentage_error-rate=1e-12 TRAIN_LOSS= 11508606.0 TRAIN_ERROR= 11508606.0
```

```
measure_model_performance(chosen_key, chosen_model)
```

```
1/1 [=====] - 2s 2s/step - loss: 3666583.2500 - mean_absolute
_percentage_error: 3666583.2500 - mean_absolute_error: 46.6171
CHOSEN_MODEL= -depth=3-height=6-whole_epochs=1-epoch_per_batch=5-loss=mean_absolute_pe
rcentage_error-rate=1e-12 VALIDATION_ERROR= 3666583.2
```

## Plot

## Plot Helper Classes

```

from collections import defaultdict

class model_history():

    def __init__(self):
        self.loss_history = defaultdict(list)
        self.error_history = defaultdict(list)
        self.percentage_error_history = defaultdict(list)

    def add(self, key, values):
        if key in ["loss", "val_loss"]:
            self.loss_history[key].extend(values)
        if key in ["mean_absolute_error", "val_mean_absolute_error"]:
            self.error_history[key].extend(values)
        if key in ["mean_absolute_percentage_error",
"val_mean_absolute_percentage_error"]:
            self.percentage_error_history[key].extend(values)

# test
h = model_history()
h.add('loss', [1,2,3])
h.add('loss', [3,2,1])
h.loss_history

Out[40]: defaultdict(list, {'loss': [1, 2, 3, 3, 2, 1]})

model_train_history = {}

for model_key in param_history.keys():
    try:
        history_arr = param_history[model_key]
        for batch_id in range(len(history_arr)):
            history_batch = history_arr[batch_id]
            # print(history_batch.history.keys())
            for metric_name, metric_history in history_batch.history.items():
                if model_key not in model_train_history:
                    this_history = model_history()
                else:
                    this_history = model_train_history[model_key]
                this_history.add(metric_name, metric_history)
            model_train_history[model_key] = this_history
    except:
        pass

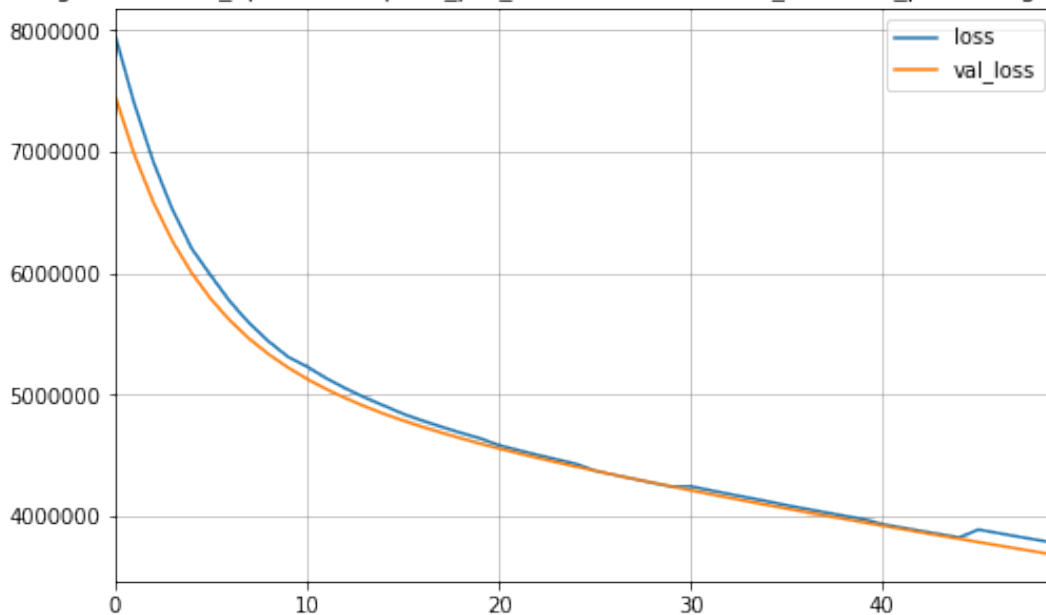
```

```
def plot_learning_curves(model_key, train_history):
    try:
        print("model_key=", model_key)
        pd.DataFrame(train_history).plot(figsize=(8, 5), title=model_key)
        plt.grid(True)
        # plt.gca().set_ylim(0, 1)
        # plt.show()
    except:
        pass
```

## Plot the Selected Model

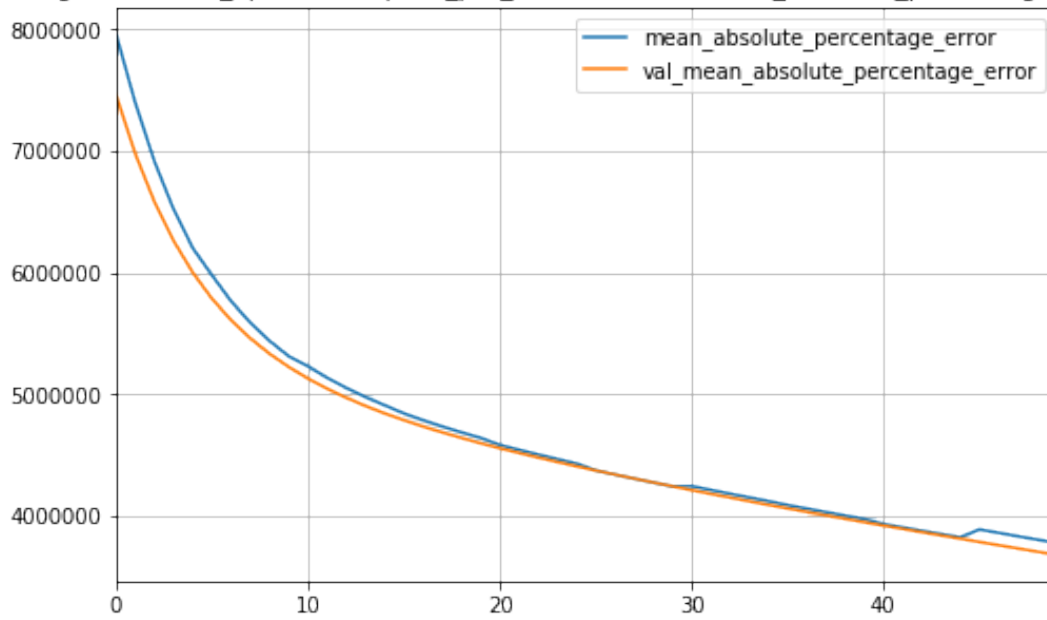
```
plot_learning_curves(chosen_key, model_train_history[chosen_key].loss_history)
```

-depth=3-height=6-whole\_epochs=1-epoch\_per\_batch=5-loss=mean\_absolute\_percentage\_error-rate=1e-12



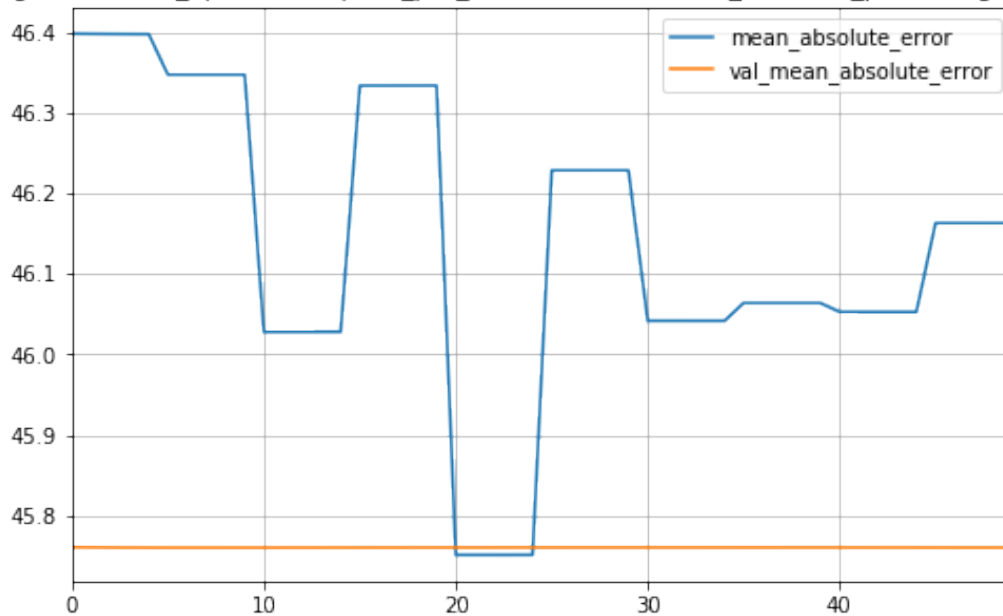
```
plot_learning_curves(chosen_key,
model_train_history[chosen_key].percentage_error_history)
```

-depth=3-height=6-whole\_epochs=1-epoch\_per\_batch=5-loss=mean\_absolute\_percentage\_error-rate=1e-12



```
plot_learning_curves(chosen_key, model_train_history[chosen_key].error_history)
```

-depth=3-height=6-whole\_epochs=1-epoch\_per\_batch=5-loss=mean\_absolute\_percentage\_error-rate=1e-12

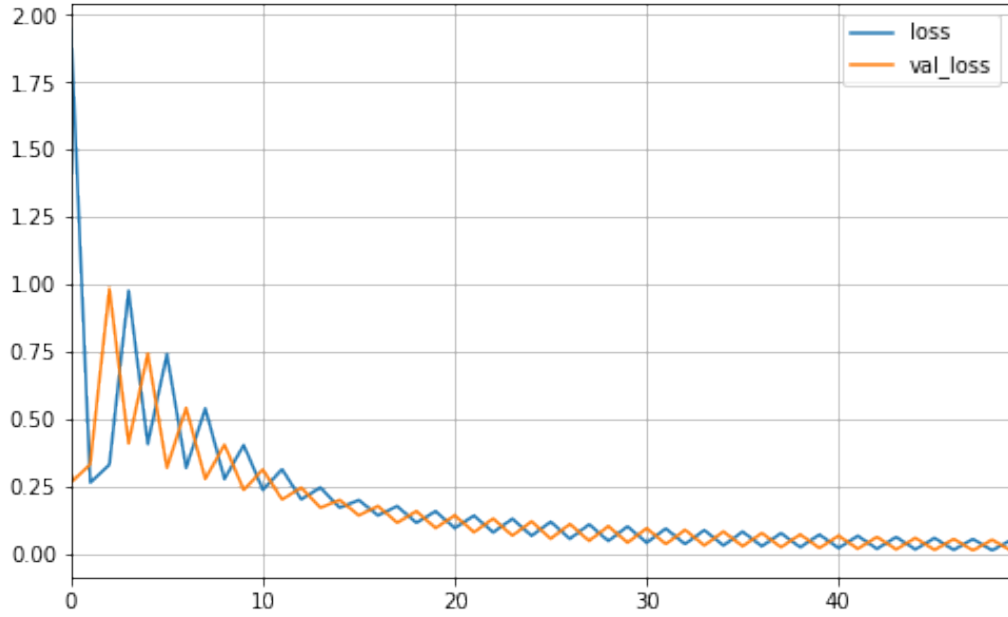


## Plot All Models

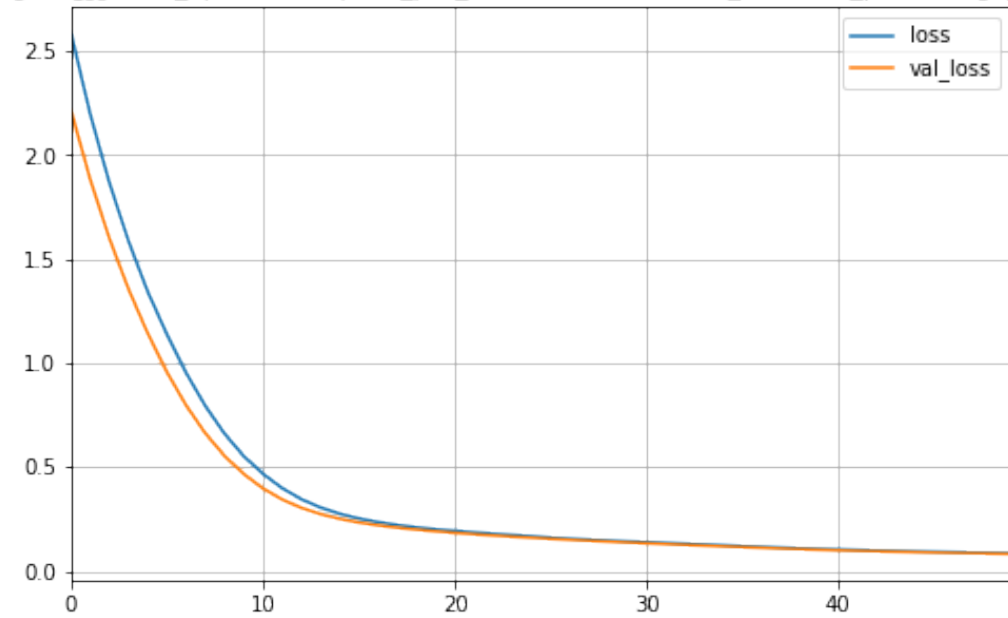
```
for key in model_train_history.keys():
    plot_learning_curves(key, model_train_history[key].loss_history)
```



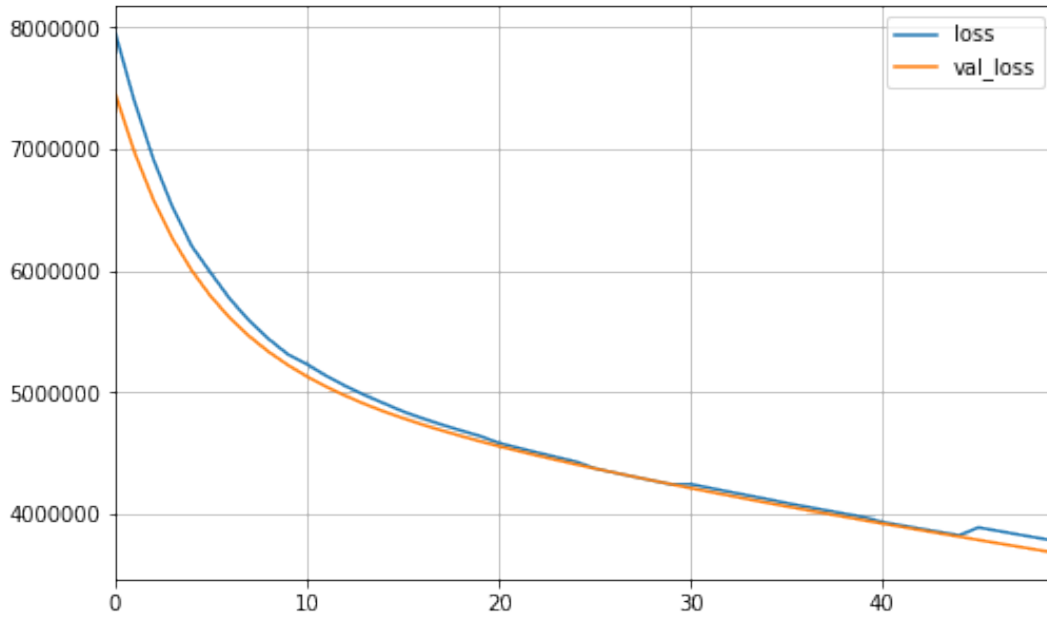
-depth=1-height=6-whole\_epochs=1-epoch\_per\_batch=5-loss=mean\_absolute\_percentage\_error-rate=1e-12



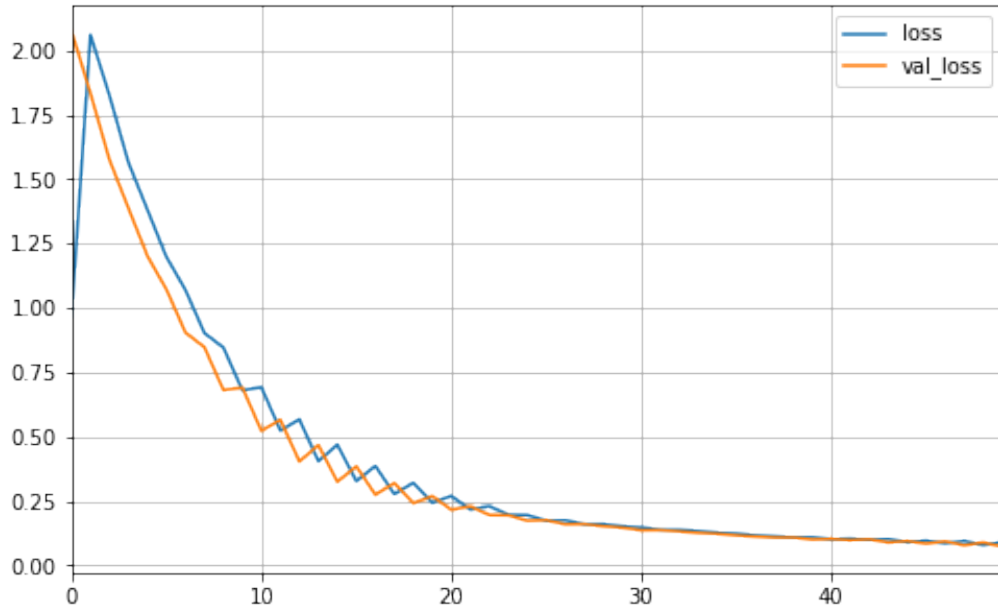
-depth=2-height=6-whole\_epochs=1-epoch\_per\_batch=5-loss=mean\_absolute\_percentage\_error-rate=1e-12



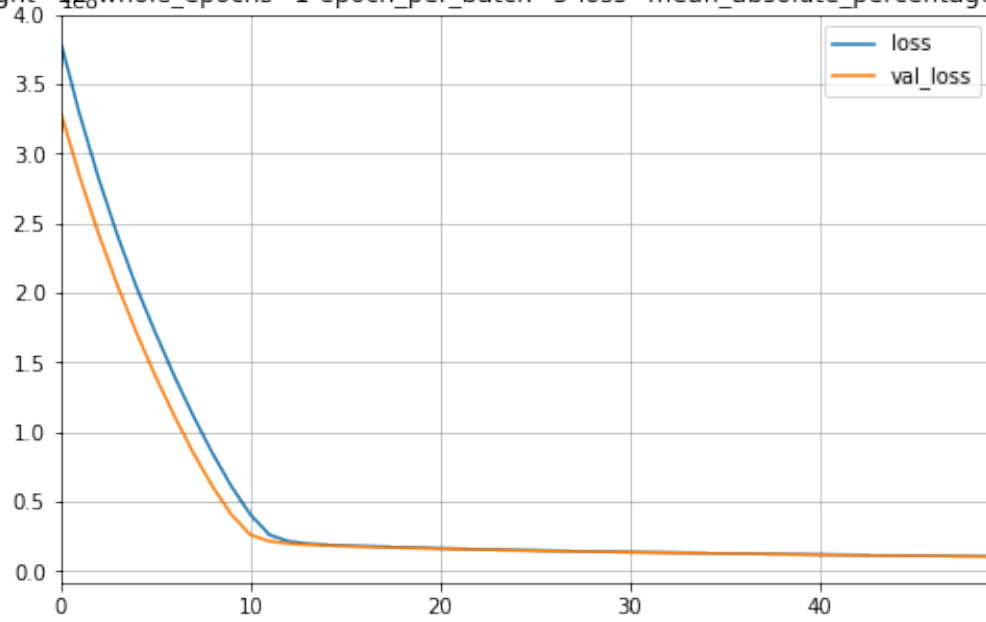
-depth=3-height=6-whole\_epochs=1-epoch\_per\_batch=5-loss=mean\_absolute\_percentage\_error-rate=1e-12



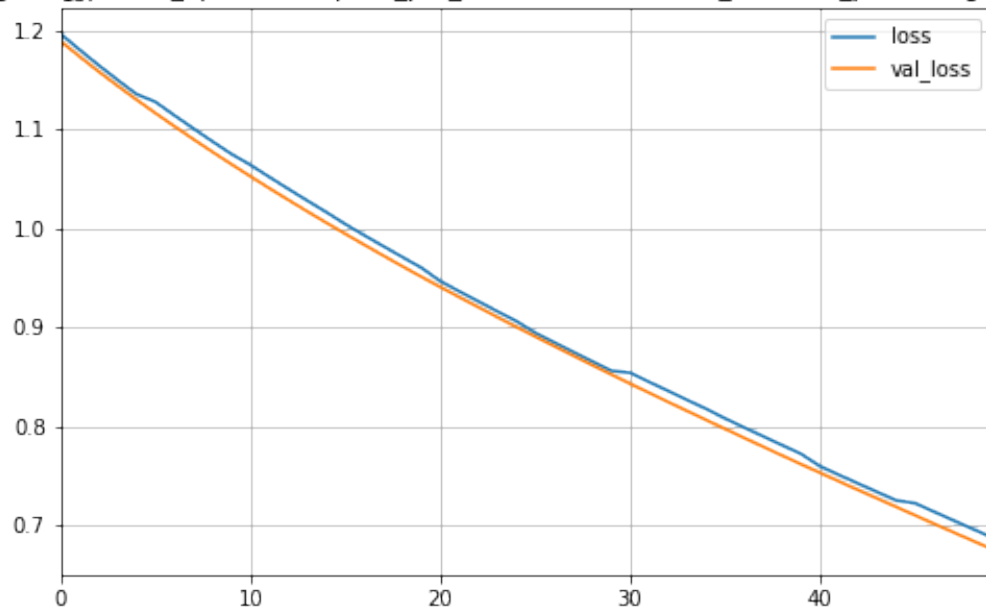
-depth=1-height=12-whole\_epochs=1-epoch\_per\_batch=5-loss=mean\_absolute\_percentage\_error-rate=1e-12



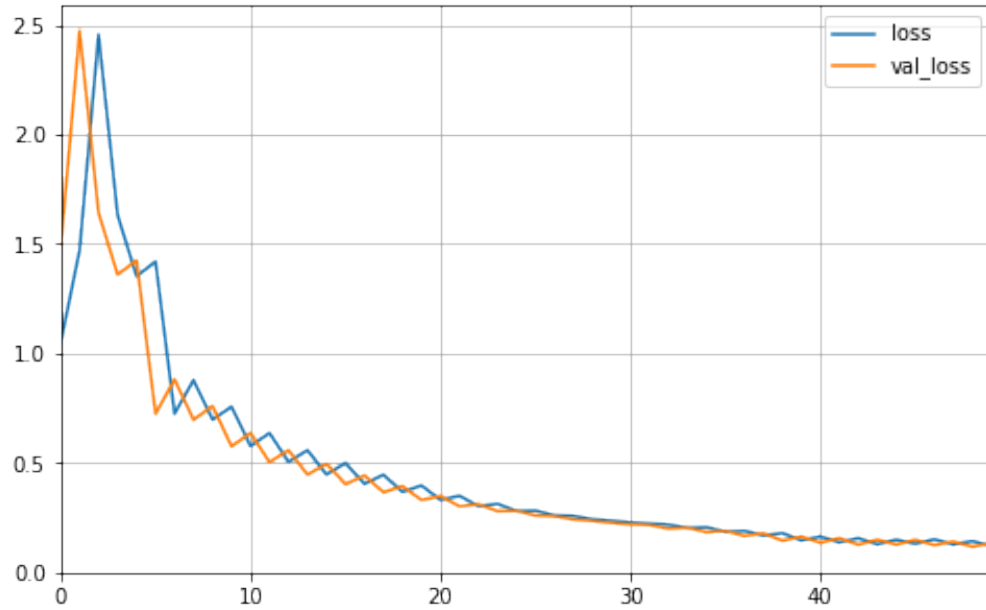
-depth=2-height=12-whole\_epochs=1-epoch\_per\_batch=5-loss=mean\_absolute\_percentage\_error-rate=1e-12



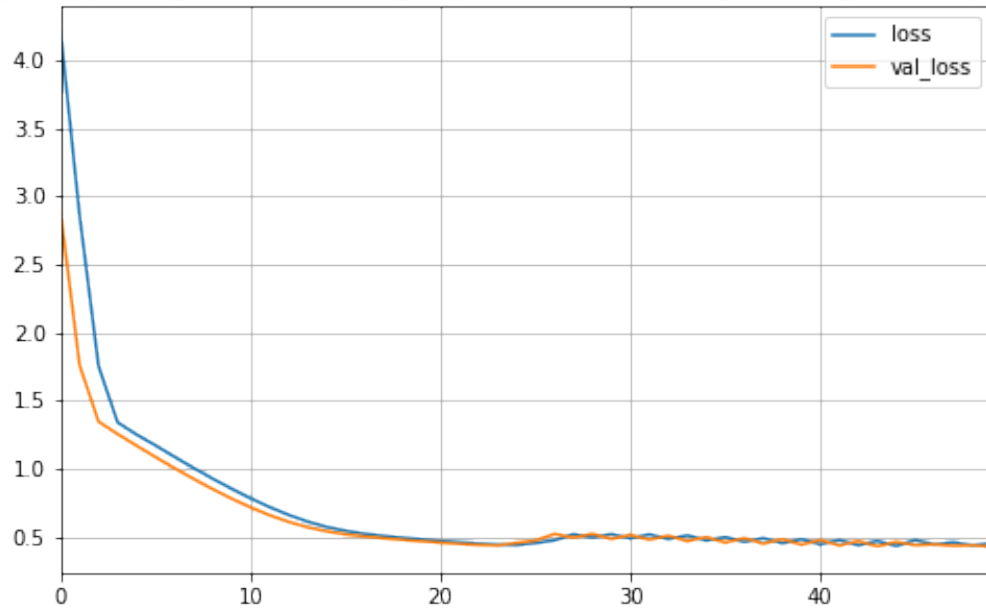
-depth=3-height=12-whole\_epochs=1-epoch\_per\_batch=5-loss=mean\_absolute\_percentage\_error-rate=1e-12



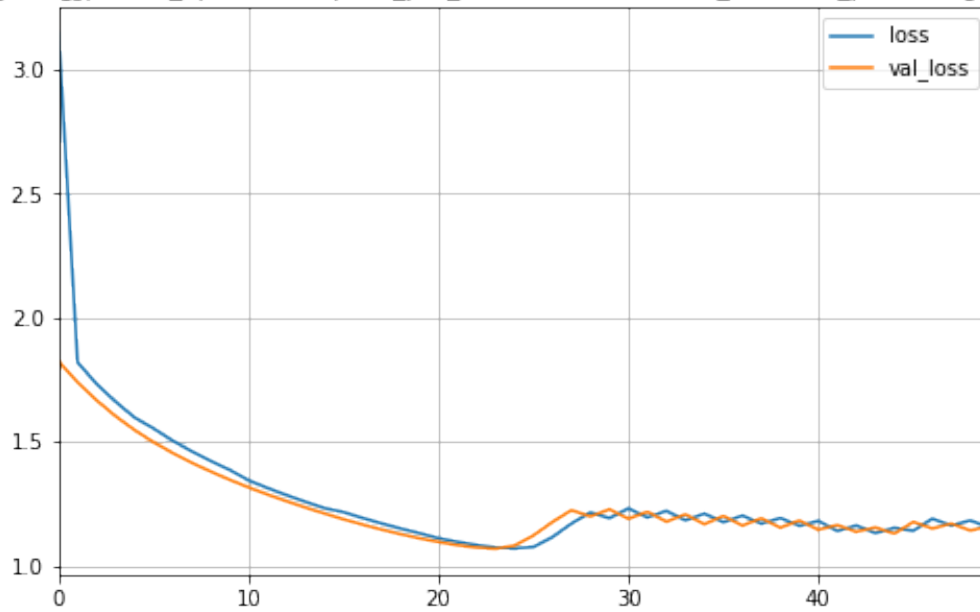
-depth=1-height=18-whole\_epochs=1-epoch\_per\_batch=5-loss=mean\_absolute\_percentage\_error-rate=1e-12



-depth=2-height=18-whole\_epochs=1-epoch\_per\_batch=5-loss=mean\_absolute\_percentage\_error-rate=1e-12

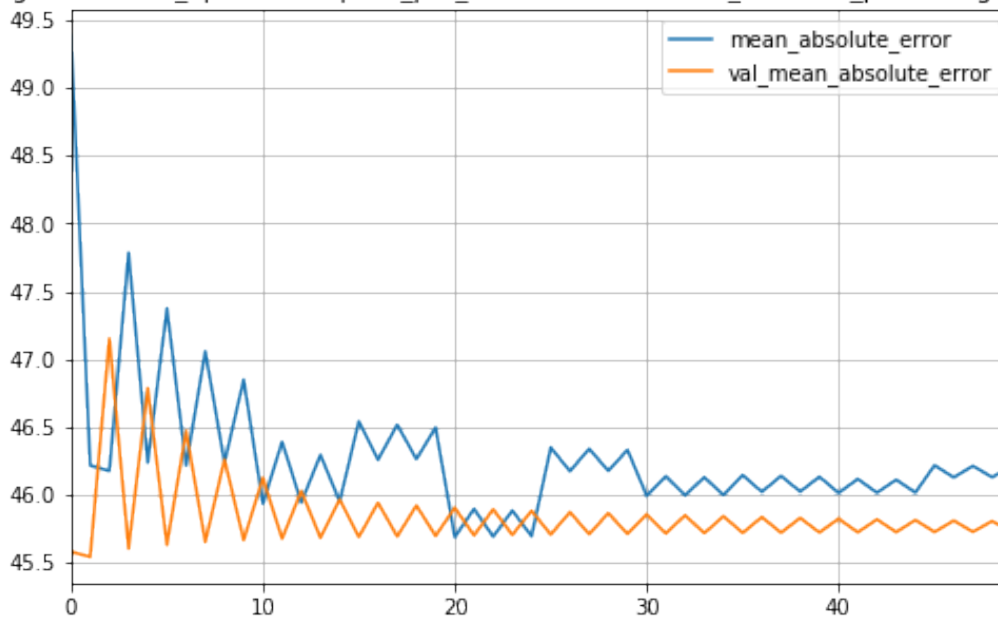


-depth=3-height=18-whole\_epochs=1-epoch\_per\_batch=5-loss=mean\_absolute\_percentage\_error-rate=1e-12

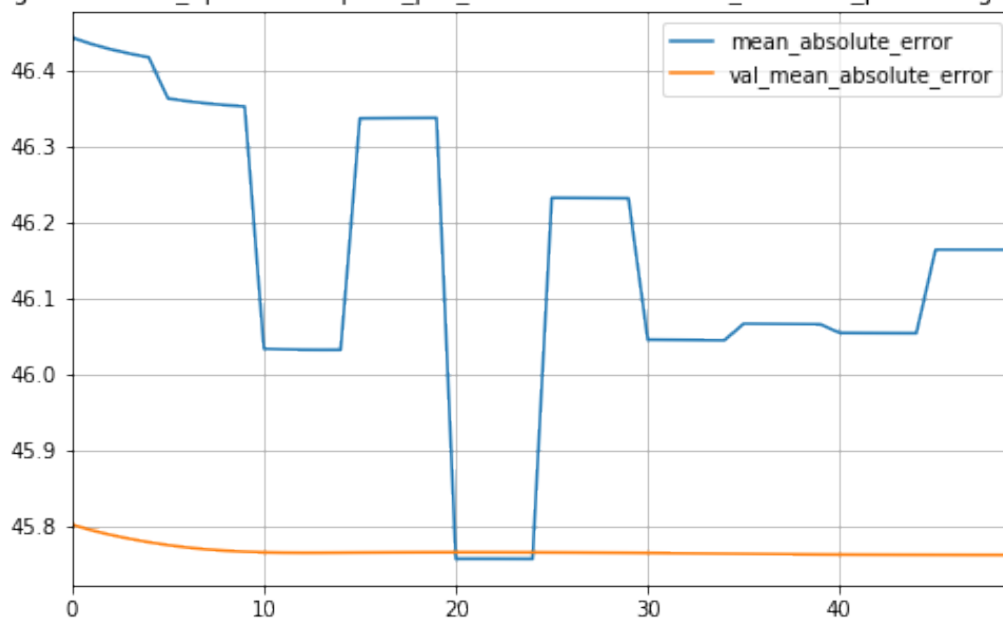


```
for key in model_train_history.keys():
    plot_learning_curves(key, model_train_history[key].error_history)
```

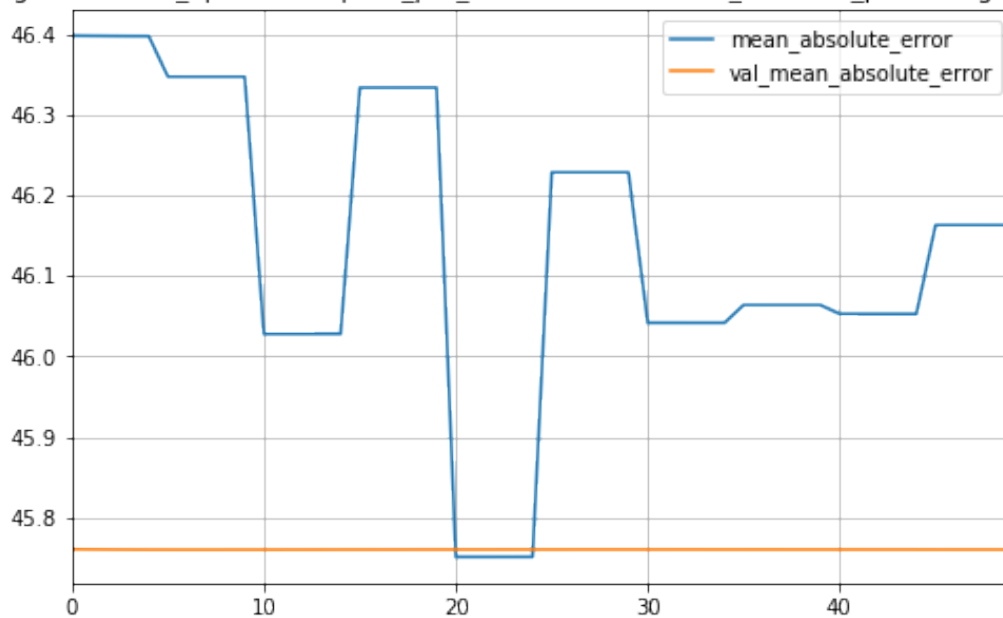
-depth=1-height=6-whole\_epochs=1-epoch\_per\_batch=5-loss=mean\_absolute\_percentage\_error-rate=1e-12



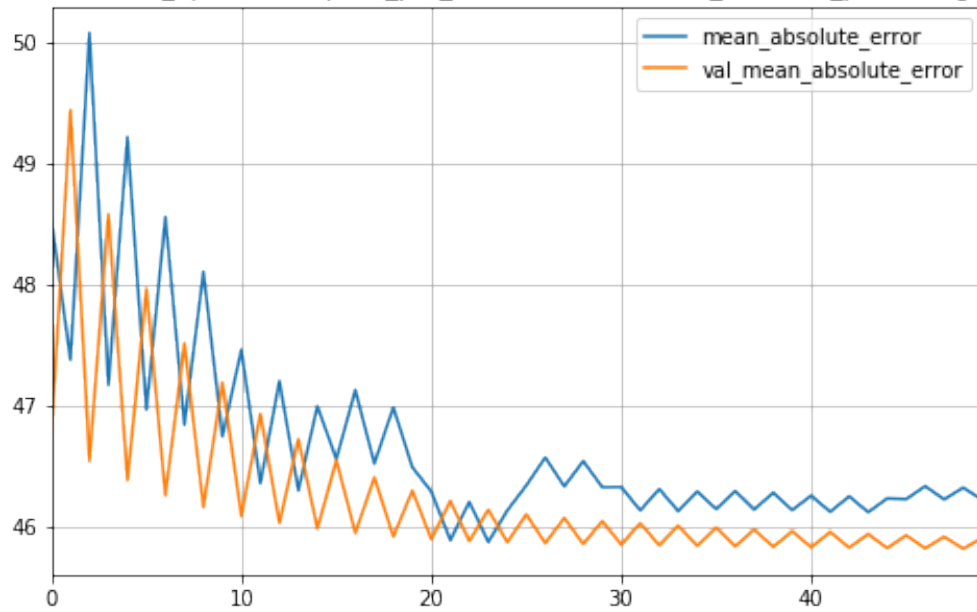
-depth=2-height=6-whole\_epochs=1-epoch\_per\_batch=5-loss=mean\_absolute\_percentage\_error-rate=1e-12



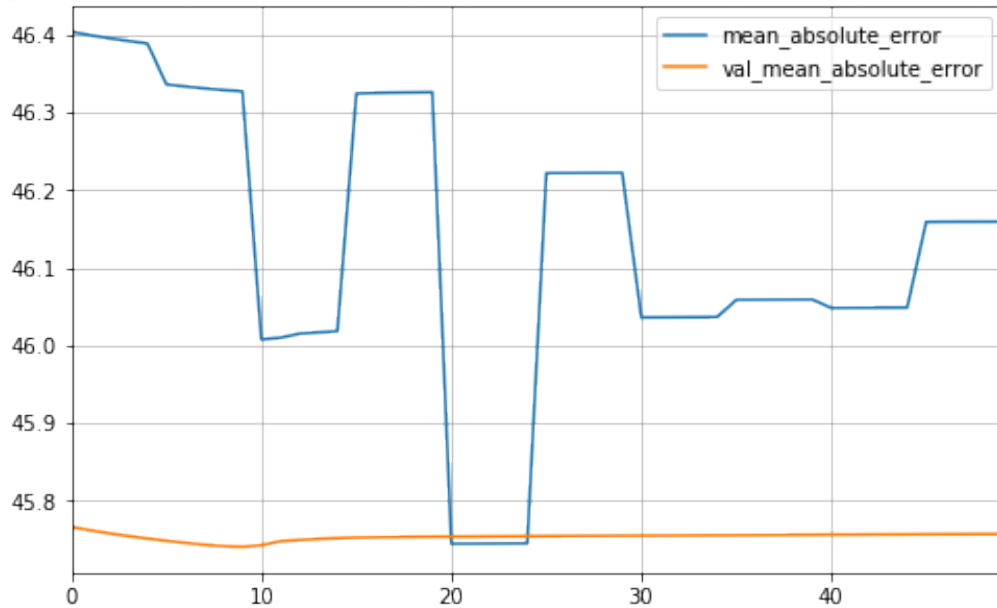
-depth=3-height=6-whole\_epochs=1-epoch\_per\_batch=5-loss=mean\_absolute\_percentage\_error-rate=1e-12



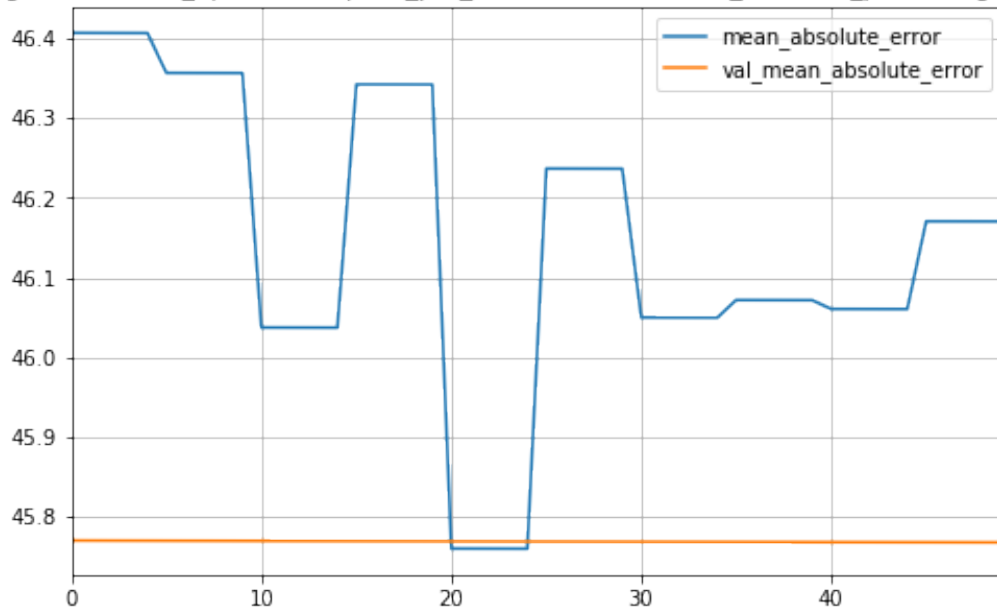
-depth=1-height=12-whole\_epochs=1-epoch\_per\_batch=5-loss=mean\_absolute\_percentage\_error-rate=1e-12



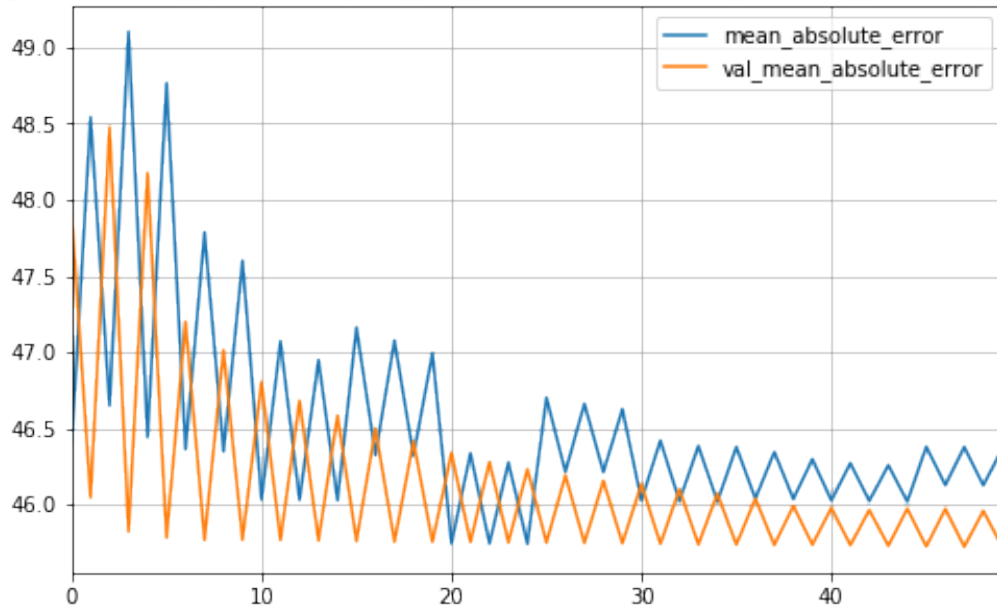
-depth=2-height=12-whole\_epochs=1-epoch\_per\_batch=5-loss=mean\_absolute\_percentage\_error-rate=1e-12



-depth=3-height=12-whole\_epochs=1-epoch\_per\_batch=5-loss=mean\_absolute\_percentage\_error-rate=1e-12

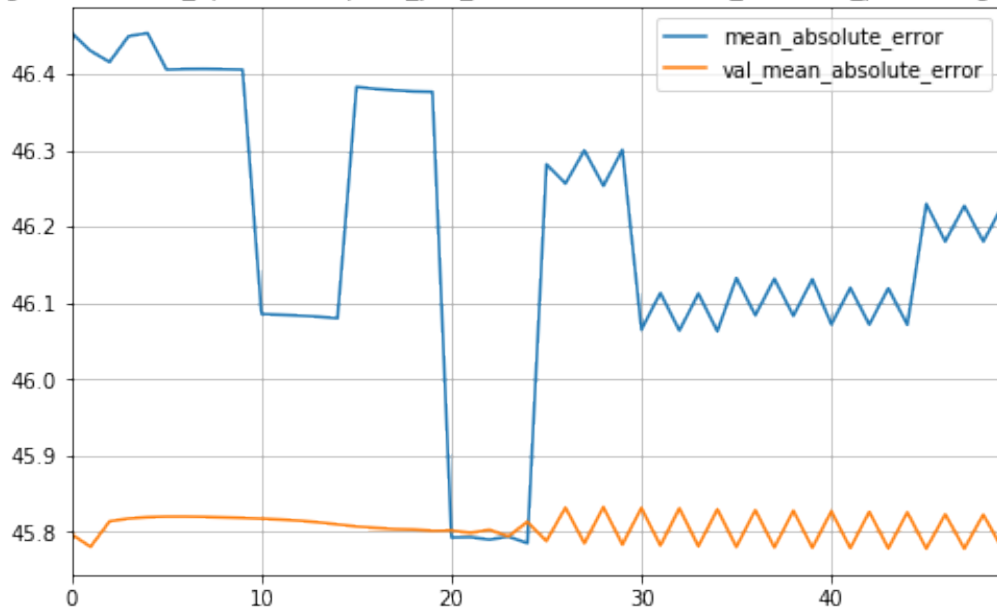


-depth=1-height=18-whole\_epochs=1-epoch\_per\_batch=5-loss=mean\_absolute\_percentage\_error-rate=1e-12

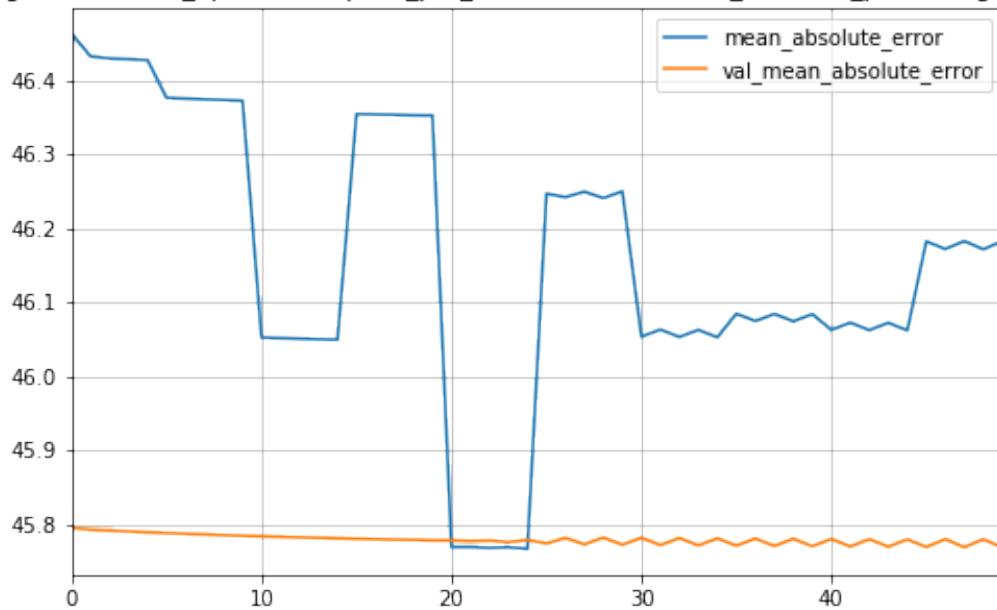




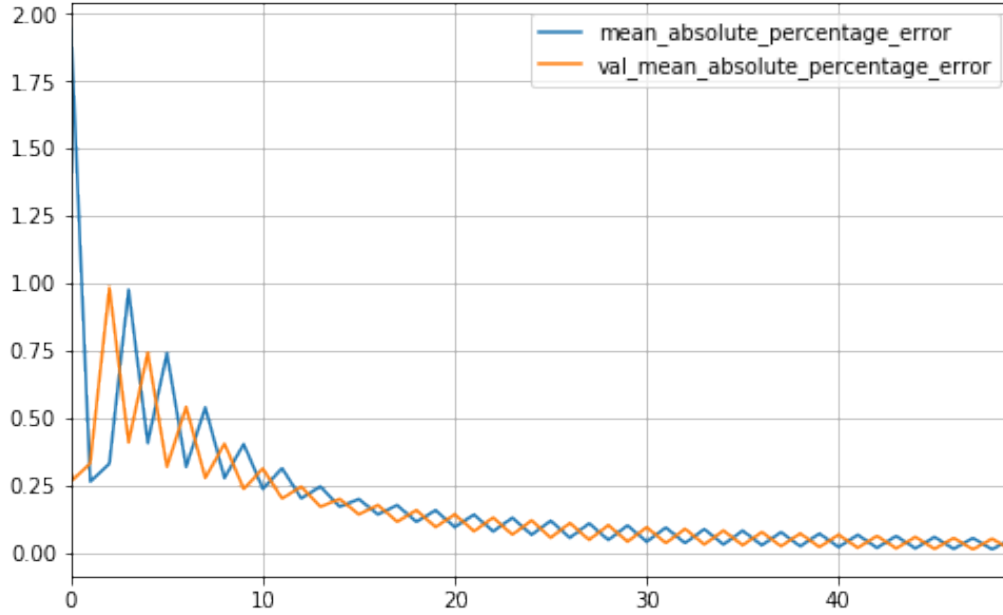
-depth=2-height=18-whole\_epochs=1-epoch\_per\_batch=5-loss=mean\_absolute\_percentage\_error-rate=1e-12



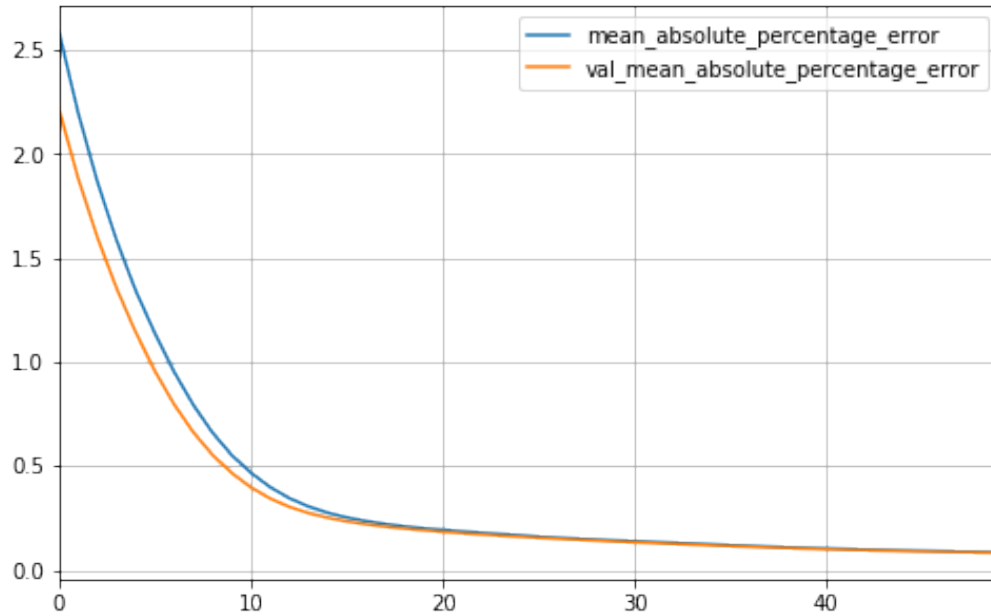
-depth=3-height=18-whole\_epochs=1-epoch\_per\_batch=5-loss=mean\_absolute\_percentage\_error-rate=1e-12



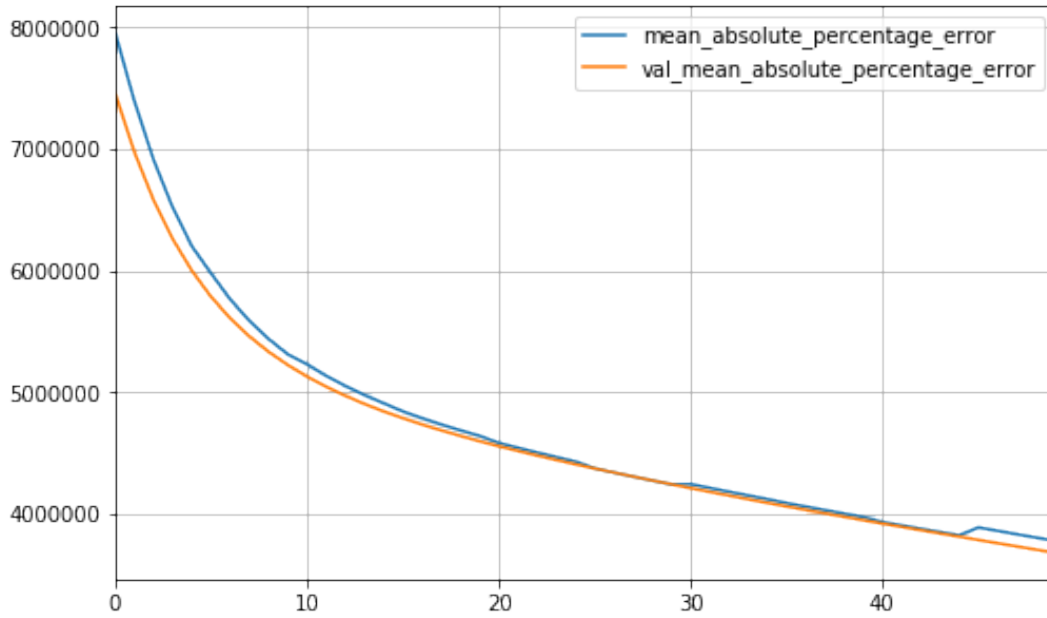
-depth=1-height=6-whole\_epochs=1-epoch\_per\_batch=5-loss=mean\_absolute\_percentage\_error-rate=1e-12



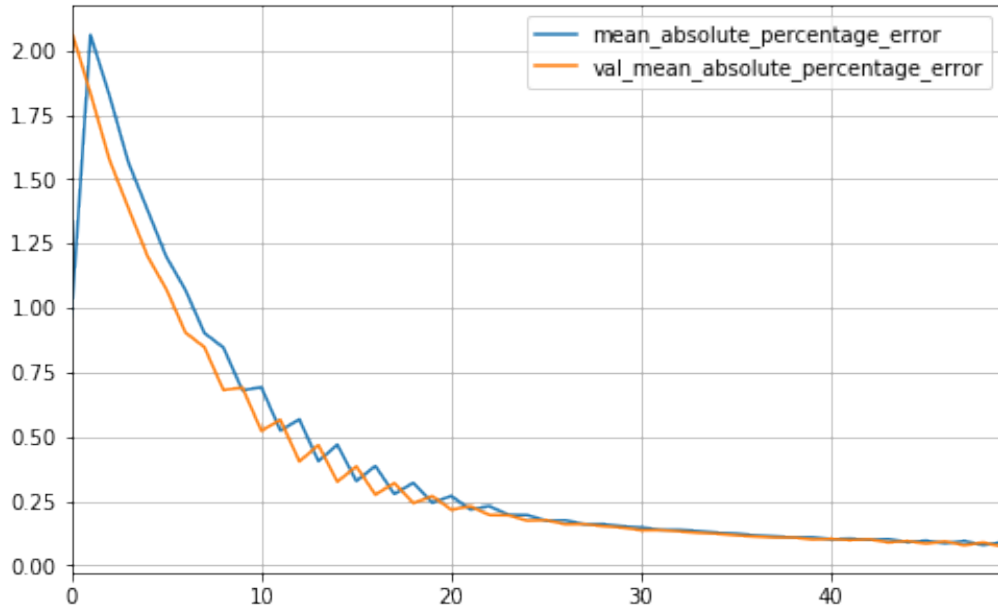
-depth=2-height=6-whole\_epochs=1-epoch\_per\_batch=5-loss=mean\_absolute\_percentage\_error-rate=1e-12



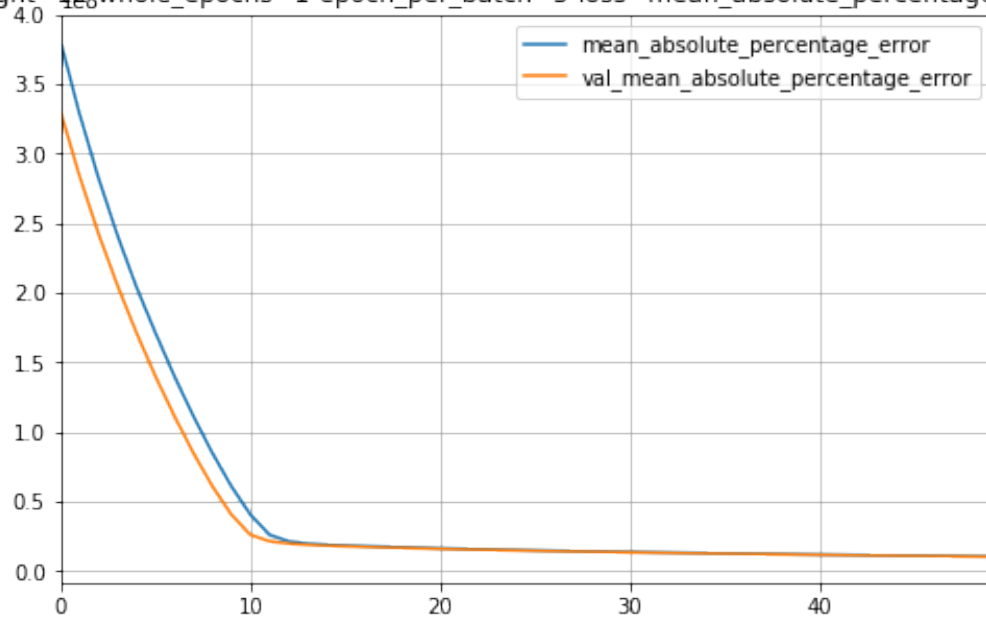
-depth=3-height=6-whole\_epochs=1-epoch\_per\_batch=5-loss=mean\_absolute\_percentage\_error-rate=1e-12



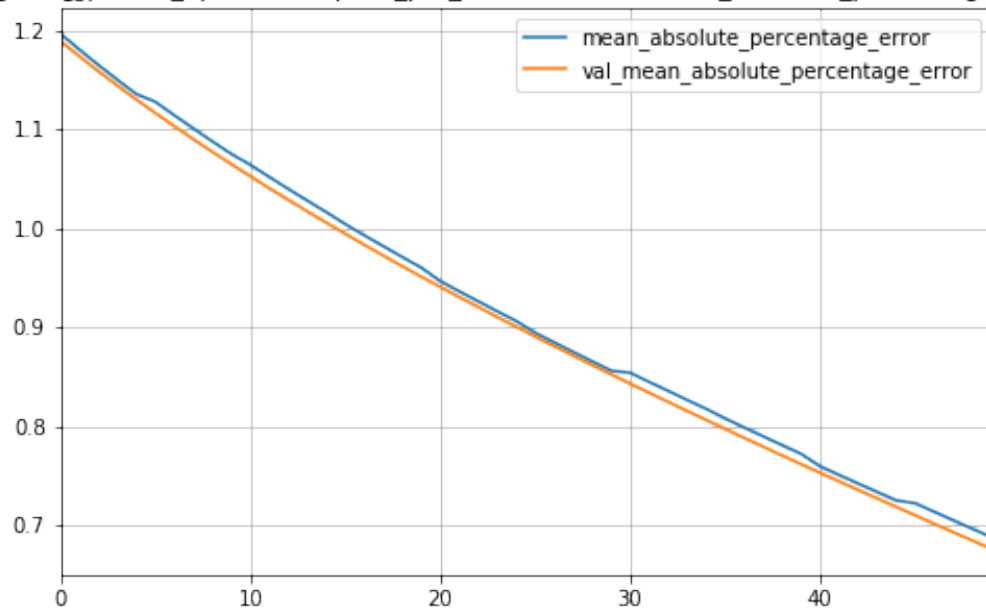
-depth=1-height=12-whole\_epochs=1-epoch\_per\_batch=5-loss=mean\_absolute\_percentage\_error-rate=1e-12



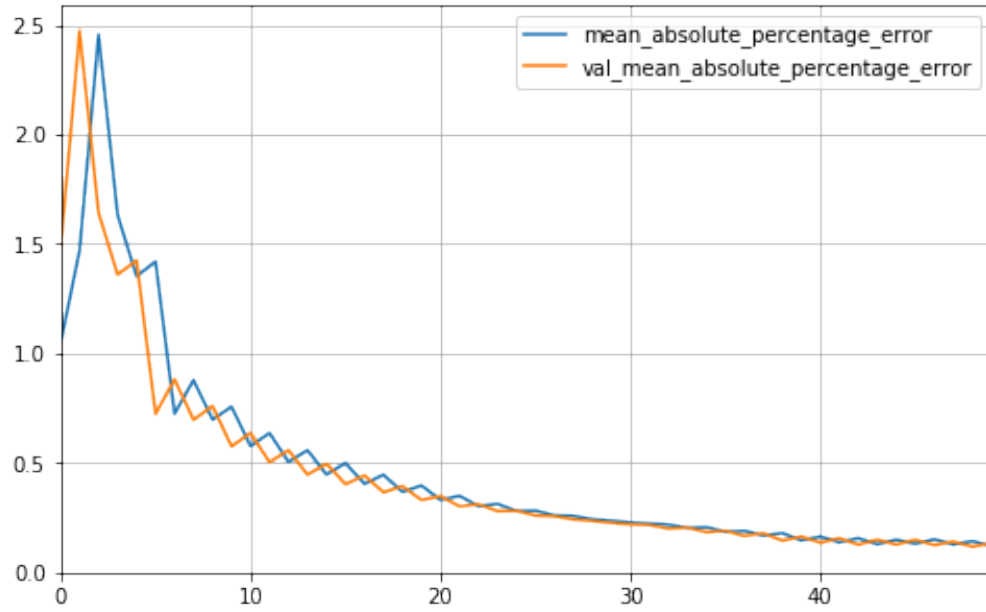
-depth=2-height=12-whole\_epochs=1-epoch\_per\_batch=5-loss=mean\_absolute\_percentage\_error-rate=1e-12



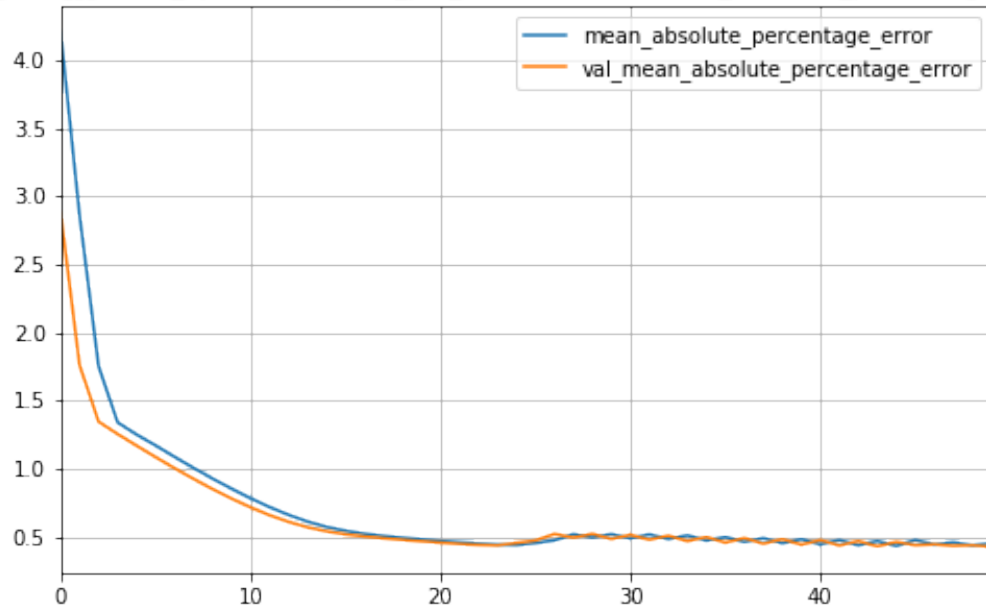
-depth=3-height=12-whole\_epochs=1-epoch\_per\_batch=5-loss=mean\_absolute\_percentage\_error-rate=1e-12



-depth=1-height=18-whole\_epochs=1-epoch\_per\_batch=5-loss=mean\_absolute\_percentage\_error-rate=1e-12



-depth=2-height=18-whole\_epochs=1-epoch\_per\_batch=5-loss=mean\_absolute\_percentage\_error-rate=1e-12



-depth=3-height=18-whole\_epochs=1-epoch\_per\_batch=5-loss=mean\_absolute\_percentage\_error-rate=1e-12

