

Coalescence of cohesive microbial communities

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Abstract

Community assembly, the process whereby species come together and interact to form functioning and coherent aggregations, is an old-age unsolved problem in ecology. In the microbial world, it is common that whole communities come into contact with each other and reassemble into a new community. This process has been termed community coalescence. The mechanisms that govern these events are poorly understood, partly because theoretical work in community coalescence rarely considers communities with mutualistic interactions, which are pervasive in microbial consortia. In this work, I use a new consumer-resource model to simulate communities harbouring competitive and mutualistic interactions, and propose a measure of community cohesion that predicts the outcome of microbial community coalescence. The proposed metric explicitly quantifies the so-called *cohesiveness* exhibited by microbial communities. It reproduces an important previous result, i.e., that more cohesive communities are more successful in community coalescence events while pinning it down to more realistic assumptions about the interactions in the community. These results suggest that the collective coherence exhibited by coalescing communities is a general consequence of ecological interactions, resource partitioning, and the community shaping its environment. The proposed cohesion measure can be used to guide coalescence experiments in which different communities are successively combined until a desired beneficial functioning is reached.

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1 Introduction

Microbial communities are widespread throughout our planet, from the deep ocean to the human gut, and they play a critical role in natural processes ranging from animal development and host health (Huttenhower et al. 2012) to biogeochemical cycles (Falkowski et al. 2008). These communities are very complex, often harbouring hundreds of species (Gilbert et al. 2014), making them hard to characterize. Recently, DNA sequencing has facilitated a high-resolution mapping of these consortia, opening a niche for ambitious theorists and experimentalists to collaboratively disentangle the complexity of these systems (Marsland et al. 2019, Goldford et al. 2018, Goyal & Maslov 2018, Friedman et al. 2017, Costello et al. 2012, Vila et al. 2019). One of the problems yet to be solved is community assembly – the process by which species come together and interact to establish a community. Contrary to what is found in the macroscopic world, in microbial ecology, it is common that whole communities move to a region where they encounter another community. The process by which two or more communities that were previously separated join and reassemble into a new community has been termed *community coalescence* (Rillig et al. 2015). This type of event repeatedly happens in nature due to abiotic (wind, tides or river flow), biotic (animal courtship, parent-offspring interactions or leaves falling), and anthropogenic (industrial anaerobic digestion, agriculture, between-human contact) factors (Castledine et al. 2020). Despite the frequency and importance of microbial community coalescence, the mechanisms responsible for the community structure and function resulting from coalescence events remain poorly understood (Rillig, Lehmann & Aguilar-Trigueros 2016).

Early mathematical models of community-community invasion revealed that when two communities previously separated by a barrier merge due to its removal, asymmetrical dominance of one community over the other one is likely to occur (Gilpin 1994, Toquenaga 1997). As an explanation for this observation, it was argued that, because communities have been assembled through a history of competitive exclusion, they are likely to compete with each other as coordinated entities, rather than as a random collection of species. This result is also shown in new theoretical work, where consumer-resource models are used to show that coalescing microbial communities exhibit an emergent cohesiveness (Tikhonov 2016, Tikhonov & Monasson 2017). These findings suggest that communities arising from the struggle for existence of its members display a certain level of coherence. These communities have been termed Metabolically Cohesive [microbial] Consortium (MeCoCos) by Pascual-García et al. (2020) and suggested to be pervasive in microbial guilds.

Recent results from coalescence experiments of methanogenic communities suggest that during a coalescence event between two communities, multiple taxa from the same community act as cohesive units and are selected together (ecological co-selection) (Sierocinski et al. 2017). Further experimental evidence of co-selection in community coalescence has been reported in Lu et al. (2018), where it was shown that the invasion success of a given taxon is determined by its community members. The microbial communities used in these experiments are characterized by complex cross-feeding interactions (Hansen et al. 2007, Lawrence et al. 2012, Embree et al. 2015), where the metabolic by-products of one species are substrates for others. Furthermore, the type of interactions present in a community has been suggested as a factor that might affect the outcome of community coalescence (Castledine et al. 2020). Yet, theoretical models used in community coalescence studies so far have considered competition between species as the only force driving community assembly.

In this work, I explore the combined role of other types of interactions, namely, compe-

49 titition and mutualism, which appear to be ubiquitous in microbial communities. First,
 50 I use a new consumer-resource model that includes both facilitation of metabolites via
 51 by-product secretion, and competition for substrates, to simulate many instances of com-
 52 munity assembly. Second, I propose a metric of community cohesion that accounts for
 53 both competitive and mutualistic interactions, and I measure the cohesion level in the
 54 simulated communities. Third, I apply the proposed metric to predict the outcome of
 55 microbial community coalescence events.

56 2 Methods

57 Here, I first lay out the model used to simulate communities. Second, I detail the proce-
 58 dure I follow to assembly many synthetic microbial communities. Third, I present the
 59 metric of cohesion and use it on the simulated communities.

60 2.1 Consumer-resource model with cross feeding interactions

61 In order to simulate communities with cross-feeding interactions, I use a consumer-
 62 resource model based on the the work of Marsland et al. (2019).
 63 Consider an environment with m resources present in different concentrations C_β , where $\beta \in$
 64 $\{1 \dots m\}$. Let now N_α denote the abundance of each bacterial strain α , present in the en-
 65 vironment, where $\alpha \in \{1 \dots s\}$. Each species is uniquely characterized by the metabolic
 66 strategy it uses to harvest resources. This strategy is encoded in its reaction network
 67 G_α , a collection of chemical reactions between the metabolites in the environment that
 68 produce energy that is used by bacteria for survival and replication (see Figure 1). If we
 69 now allow the dynamics of this system to unfold, the concentration of each metabolite C_β
 70 determines the dynamics of the abundances N_α of each species, which harvest resources
 71 through their different metabolic strategies. The changes in species abundance therefore
 72 translate into changes in the total supply and demand of resources. In turn, resource
 73 concentrations C_β are depleted until equilibrium is reached. A more rigorous description
 74 of the model, along with its mathematical form will now be presented.

75 Consider the population dynamics of s consumers (eg. bacterial strains) that feed on
 76 m resources. In this model, a species is defined by the metabolic strategy it uses to har-
 77 vest energy from the environment. Let $G_\alpha(\mathcal{M}, \mathcal{N})$ be the metabolic network of species
 78 α (in the network theory sense), where \mathcal{M} is a set of nodes $\mathcal{M} = \{x : x \text{ is an integer}$
 79 $\text{from the interval } [1, m] \text{ labeling the metabolite}\}$ and \mathcal{N} a set of uni-directed edges $\mathcal{N} =$
 80 $\{(x, y) : x \in \mathcal{M}, y \in \mathcal{M} \text{ and } x < y \text{ (} x \text{ and } y \text{ are the product and the substrate of a}$
 81 $\text{chemical reaction, respectively})\}$. The growth power of species α , J_α^{grow} will be given by
 82 the product of the amount of generated energy per reaction event η_i and rate q_i of each
 83 reaction, summed across all reactions in \mathcal{N} .

$$84 \quad J_\alpha^{grow} = \sum_{i=1}^{|\mathcal{N}|} q_i \eta_i \quad (1)$$

85 where $|\cdot|$ denotes cardinality of a set. Refer to subsection 7.1 for specifications on q and
 86 η .

87 Every species has a maintenance cost χ_α that represents the required energy to sustain

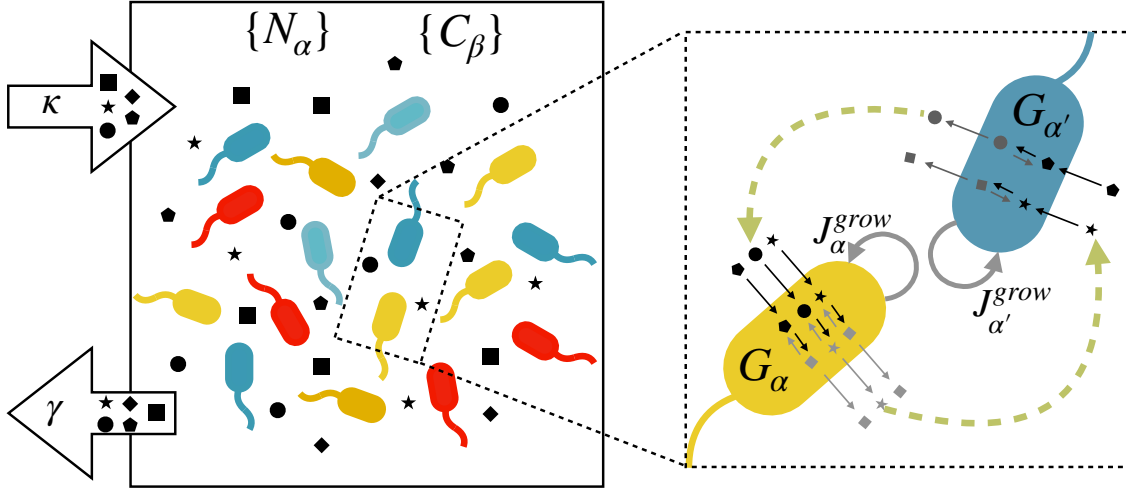


Figure 1: **Schematic of the model.** (left) Consider a chemostat where m metabolites are steadily supplied at rate κ and diluted at rate γ . Different bacterial strains coexist in the chemostat, and they consume the metabolites in the environment, C_β through their reaction networks G_α (right), to obtain the necessary power J_α^{grow} to increase their abundance N_α . The green arrows in the magnified portion emphasize that species α (yellow) facilitates metabolites to species α' (blue) and viceversa. The double arrows shown within the cells denote the fact that the I am considering reversible reactions, so the reaction rate depends on both substrate and product concentrations.

life, which is assumed to take the form

$$\chi_\alpha = \chi_0 \sum_{\mathcal{N}} (y - x) \quad (2)$$

where χ_0 is the average cost per reaction, x and y are the substrate and the product of the reaction, respectively, and the summatory term adds up the metabolite gap of all reactions. Therefore, the maintenance cost of one species increases if one or both of the following quantities increases: (1) the amount of enzymes a species is able to produce, and (2) the energy yielded by the reactions in which these enzymes are involved. Intuitively, the more enzymes a species is capable to express, the higher is the probability that at least two of them require starkly different conditions for optimal function. Therefore, expressing those enzymes simultaneously would imply maintaining two separate compartments, and incur in extra cost (see Supplementary material in Tikhonov & Monasson (2017)). The effect of the cost function (Eq. 2) is to ensure that neither generalists, nor specialists, are systematically favored during the community assembly.

Under this parametrization, the time evolution of the population of species α can be written as

$$\frac{dN_\alpha}{dt} = g_\alpha N_\alpha [J_\alpha^{grow} - \chi_\alpha] \quad (3)$$

where g_α is a proportionality constant relating energy to abundance of strain α . The dynamics of the resources depend on the incoming and outgoing resource fluxes due to the biochemical reactions taking place inside bacteria, as well as the resource external dynamics. The incoming resource flux of metabolite β generated by strain α is its rate of consumption due to all the biochemical reactions possessed by α in which β is a substrate.

109 The outgoing flux is that due to reactions in which β is a product.

$$\begin{aligned}
 v_{\alpha\beta}^{in} &= \sum_S q & \text{with } \mathcal{S} &\equiv N \cap \{(x = \beta, y)\} \\
 v_{\alpha\beta}^{out} &= \sum_{\mathcal{P}} q, & \text{with } \mathcal{P} &\equiv N \cap \{(x, y = \beta)\}
 \end{aligned}
 \tag{4}$$

112 The external resource dynamics are modelled as a supply rate minus a dilution rate that
 113 depends on the resource concentration to ensure convergent dynamics.

$$h_\beta = \kappa - \gamma C_\beta \tag{5}$$

115 Therefore, the variation with time of the concentration of metabolite β has the form

$$\frac{dC_\beta}{dt} = h_\beta + \sum_{\alpha=1}^s (v_{\alpha\beta}^{in} - v_{\alpha\beta}^{out}) N_\alpha \tag{6}$$

117 Thus, the model is a system of $s + m$ coupled differential equations completely specified
 118 by Eqs. 3 & 6.

120 2.2 Community Assembly

121 I use the above model to assemble $n_s = 2000$ communities by numerically integrating the
 122 set of equations in 3 and 6. Each simulation starts with 10 bacterial strains ($s = 10$)
 123 in an environment with 15 different resources ($m = 15$) and a random realization of the
 124 metabolic strategy, G_α , for each species.

125 The values of the parameters of the model remain constant throughout all simulations,
 126 and have been chosen motivated by biological processes (total free energy of photosynthesis or
 127 glucose respiration) and to avoid pathological situations (species always being saturated
 128 or maintenance being higher than the maximum amount of energy that can be harvested)
 129 (subsection 7.2, table 1). The reason for this is that, my aim is not to parametrize
 130 the model to reveal large-scale patterns found in experiments (although that would be a
 131 fruitful endeavour because of the rich parameter space of this model). Rather, I use it to
 132 simulate a set of microbial communities with cross-feeding interactions that will be later
 133 used in the community coalescence experiments.

134 In order to do so, I first create $s \cdot n_s$ random reaction networks, $G_\alpha(\mathcal{M}, \mathcal{N})$ (one for each
 135 strain) using the following procedure. Consider, the $m \times m$ adjacency matrix A_{ij}^α , whose
 136 elements, the edges (i, j) of G_α , represent chemical reactions. Since the reaction network
 137 is hierarchical ($i < j$, subsection 7.1), the adjacency matrix is an upper triangular matrix
 138 with zeros in the main diagonal (see figure **2B**), and the reactions possessed by strain α
 139 can be expressed as $(i, i + k)$, where k represents the k^{th} diagonal of A ($k \in \{1, \dots, m - 1\}$
 140 with $k = 0$ being the main diagonal), and i is the row number of one of its elements
 141 ($i = 1 \dots m$). The reaction network G_α is constructed by sampling n_r reactions from
 142 different diagonals, with decreasing probability as the order of the diagonal increases.
 143 Thus, I choose n_r pairs of integers (i, k) according to the algorithm summarized below.

- 144 1. Choose n_r by sampling it from a uniform distribution $U(1, m)$
- 145 2. Choose k by sampling one value from a truncated normal distribution $N(1, \sqrt{m - 1})$
 146 with limits $[1, m - 1]$, and rounding it to the closest integer.

- 147 3. Sample i from a uniform distribution of integers $U(0, m - k)$.
- 148 4. The reaction $(i, i + k)$ is stored, and the process is repeated until n_r reactions have
- 149 been sampled.

150 Several things are important to note about this algorithm. Firstly, sampling k from a
 151 truncated normal distribution ensures that high metabolite gaps (very energetic reac-
 152 tions) are not likely to happen. This introduces a bias against the precence of organisms
 153 with few and very energetic reactions, which are rare in microbial communities. Second,
 154 the truncation limits in step 2 have been chosen to respect the imposed constraint that
 155 reactions can only be of the form $i < j$. Third, the upper limit of the uniform distribution
 156 from which i is sampled is bounded by k , the diagonal we are sampling from.

157 When the sampling of reaction networks is completed, Eqs. 6 and 3 are integrated using
 158 a Runge Kutta method (Dormand & Prince 1980) with initial conditions $N_\alpha(t = 0) = 2$
 159 and $C_\beta(t = 0) = 0$.

160

161 2.3 A metric of community cohesion

162 The cohesion of a community is ultimately determined by the nature of the interactions
 163 between its members. Since I am considering two types of interactions, namely, competi-
 164 tion, and mutualism, the simplest way to render them into a mathematical expression is
 165 to subtract them.

$$166 \quad \text{Cohesion} = \text{Facilitation} - \text{Competition} \quad (7)$$

167 Measuring levels of facilitation and competition within a microbial community is exper-
 168 imentally challenging. However, the metabolic strategies of each species are well de-
 169 termined in this theoretical framework. Therefore, I use the reaction network of each
 170 bacterial strain to compute their competition and facilitation indices with the rest of the
 171 species in the community.

172 Let s_1 and s_2 be two sequences of integers labeling metabolites. I am interested in
 173 measuring their *overlapping degree* $\xi(s_1, s_2)$, ie, the proportion of metabolites of s_1 that
 174 intersect with s_2 summed with the proportion of metabolites of s_2 that intersect with s_1 ,
 175 normalized to 1.

$$176 \quad \xi(s_1, s_2) = \frac{1}{2} \sum_{k \in s_1 \cap s_2} \left(\frac{D_{s_1}(k)}{|s_1|} + \frac{D_{s_2}(k)}{|s_2|} \right) \quad (8)$$

177 Here, k takes the values in the set that result from intersecting s_1 and s_2 . $D_s(k)$ is the
 178 number of elements from the sequence s that are equal to k . Vertical bars $| \cdot |$ express
 179 cardinality of a sequence. The purpose of all denominators in equation 8 is to normalize
 180 ξ to 1.

181 One way to capture the facilitation of a community is by calculating its facilitation matrix
 182 F , which is composed of the facilitation indices of all possible ordered pairs i, j of species
 183 in the community. Precisely, the facilitation index f_{ij} of species i towards species j , is
 184 given by the overlapping degree of the sequence of products y_i of species i , with the
 185 sequence of substrates x_j of species j . Equivalently, the competition matrix C gathers
 186 the competition level of the community. The competition index between species i and j ,
 187 c_{ij} is given by the overlapping degree of the sequence of substrates x_i of species i , and
 188 the sequence of substrates x_j of species j . Thus,

$$189 \quad F_{ij} = \begin{cases} \xi(y_i, x_j) & \text{if } i \neq j \\ 0 & \text{if } i = j \end{cases} \quad C_{ij} = \begin{cases} \xi(x_i, x_j) & \text{if } i \neq j \\ 0 & \text{if } i = j \end{cases} \quad (9)$$

190 Note that facilitation is directional but competition is not. This implies that $F_{ij} \neq F_{ji}$
 191 and F is not symmetric, but $C_{ij} = C_{ji}$ and C is symmetric.
 192 Following the idea sketched in equation 7, a cohesion matrix Ψ can be defined using
 193 equations in 9, as an upper triangular $s \times s$ matrix whose elements are given by

$$194 \quad \Psi_{ij} = \begin{cases} \frac{1}{2} (F_{ij} + F_{ji}) - C_{ij} & \text{if } i < j \\ 0 & \text{if } i \geq j \end{cases} \quad (10)$$

195 I choose to define Ψ as an upper triangular matrix because cohesion is not a directional
 196 measure; two species are not more cohesive if measured from i to j , than from j to i .
 197 Instead, cohesion is a pairwise estimate independent of the direction of measure, so its
 198 matrix representation should be either symmetric or triangular. The triangular definition
 199 of Ψ allows me to interpret it as the adjacency matrix of a directed weighted network
 200 of cohesion between species. Under this interpretation it is natural to define the total
 201 cohesion level of species α with the rest of species in the network, as the sum of all the
 202 edge weights connected to node α

$$203 \quad s_\alpha = \sum_{j \neq \alpha} \Psi_{\alpha j} \quad (11)$$

204 Another relevant measure stemming from the definition of Ψ is the community-level cohesion
 205 Θ , calculated as the average of all its weights.

$$206 \quad \Theta = \frac{1}{T_s} \sum_{i < j} \Psi_{ij} \quad (12)$$

207 Where $T_s = \binom{s+1}{2}$ is the number of elements being summed: those in the upper diagonal
 208 of Ψ (the triangular number of order s).

209 An example of the cohesion network, corresponding to the instance of community assembly
 210 shown in figures **2A** and **2B**, is illustrated before and after assembly in figures **3A** and
 211 **3B**, respectively.

212 3 Results

213 Relevant results stemming from the simulations of community assembly events are plot-
 214 ted in figure **2**. The first two figures convey information about the dynamics and the
 215 resource consumption map of one particular community. In figure (**2A**), all abundances
 216 start increasing because all resources are present and steadily supplied. As the dynamics
 217 evolve, the community engineers its own environment by consumption of metabolites and
 218 secretion of by-products, causing the creation of ecological niches. During this process,
 219 species sorting results in competitive exclusion of species whose niches overlap. Alterna-
 220 tively, species whose niches are separate may engage in mutualistic relationships through
 221 metabolic complementarity (see figure **1**), resulting in a net benefit to the interacting
 222 partners (Pascual-García et al. 2020). Figure (**2B**), shows that all metabolites are being
 223 consumed (all rows have at least one non-zero element), which is to say, that all vacant
 224 niches are being occupied.

225 The community assembly simulations generated communities with richness spanning from
 226 1 to 9 species (figure **2C**), where specialists are, on average, more abundant than gener-
 227 alists (figure **2D**, blue points). This can be attributed to several specialists being able to

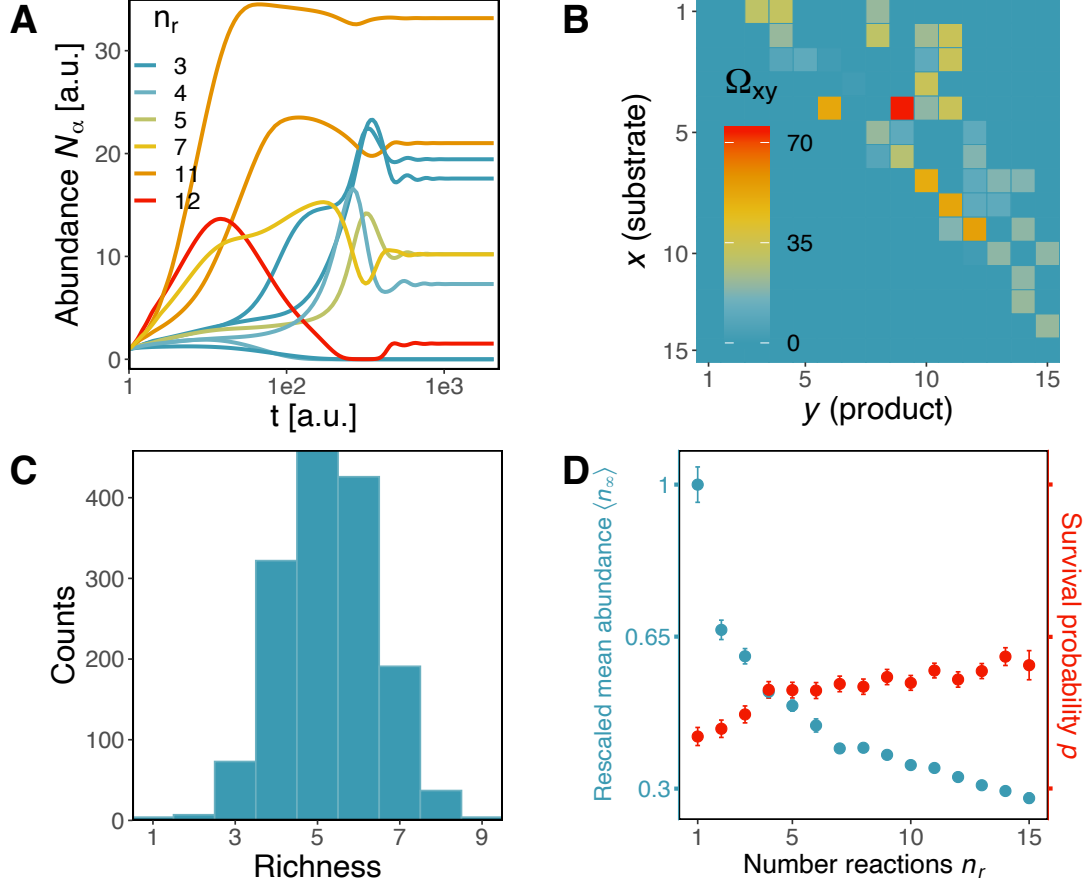


Figure 2: **Results from community assembly simulations.** Plots (A) and (B) exemplify one community assembly event and (C) and (D) convey results accross simulations. (A) Time variation of species' abundance for one instance of community assembly with $m = 15$, $s = 10$, and a set of s randomly generated reaction networks. Time (x-axis) and population (y-axis) are measured in arbitrary units. Each time series is coloured according to n_r , the number of reactions possessed by the reaction network of each strain. (B) Community reaction network, obtained by summing the reaction network adjacency matrices of all species weighted by their respective carrying capacity: $\Omega = \sum_{k=1}^s N_\infty^k A_k$. The community reaction network is unique for each community, and it constitutes a blueprint of how that community depletes resources in the environment. Note that, according to the imposed constraints, reactions where $x > y$ are absent, and those where $y \gg x$, are rare. (C) Histogram of richness of the n_s simulations. (D). In blue, mean value of carrying capacity rescaled to 1 against the number of reactions n_r . In red, survival probability against number of reactions n_r . Species with less reactions (specialists) tend to be present at higher abundances than those with higher n_r (generalists), but they have a lower surviving probability.

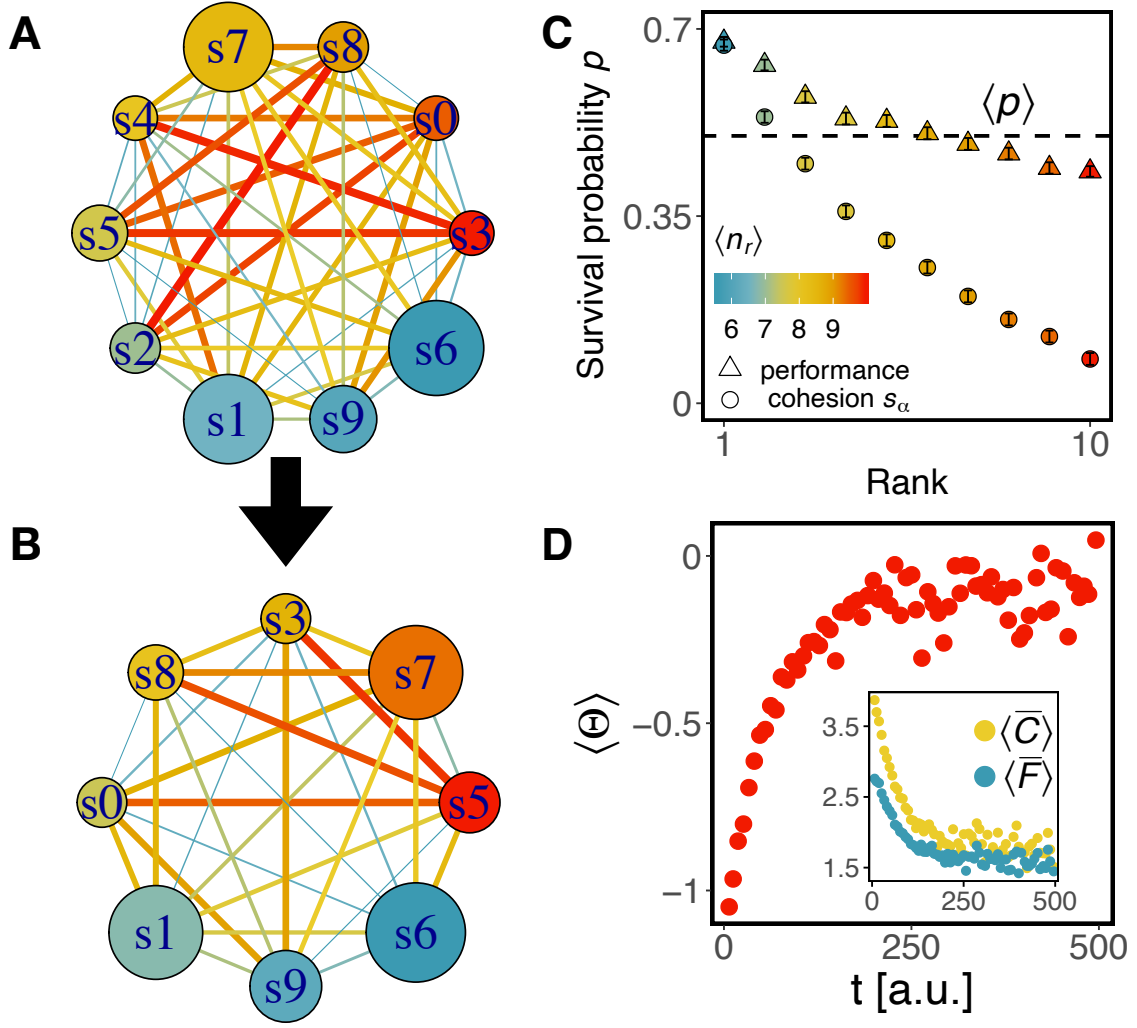


Figure 3: **Cohesion metric across community assembly events.** Cohesion network before (A) and after (B) community assembly. Thicker and red edges represent higher cohesion coefficient Ψ_{ij} between its nodes, species i and j . The color of the nodes changes from red to blue in anti-clockwise direction indicating decreasing total cohesion level s_α . The size of the node represents the number of reactions possessed by that species. (C) Median survival probability after community assembly as a function of cohesion rank (circles) and individual performance rank (triangles) of species in the random community (before assembly) across all simulations. Circles are weighted by the cohesion rank measured in the assembled community, e.g., weight is maximum when the first ranked species in the random community remains first ranked after assembly. The dashed line is the average number of extinctions across simulations. Species with higher cohesion and individual performance are less likely to go extinct during community assembly. However, cohesion predicts survival probability better than individual performance. The color of the points reflects the mean number of reactions of species in each rank. There is a weak correlation between the number of reactions and the survival probability. (D) Community-level cohesion averaged across all community assembly events, $\langle \Theta \rangle$, as a function of time. Every time a species goes extinct during community assembly, the community cohesion is recalculated with the remaining species. On average, community assembly follows trajectories where community cohesion increases. (D, inset) Community competition and facilitation levels averaged across all simulations. Both decrease during community assembly, but competition decreases faster. Decrease of facilitation is explained by the positive correlation between $\langle C \rangle$ and $\langle F \rangle$ (see Figure 4, A).

deplete all resources through their combined action more efficiently than one generalist (Pascual-García et al. 2020), thus, dominating the community at equilibrium. Note that in the simulated communities, while specialists tend to be present at higher abundances than generalists, their survival probability is lower (figure **2D**, red points). Generalists have more alternatives to obtain energy than specialists. Consequently, they are more resistant to extinctions.

During community assembly, I track the cohesion network adjacency matrix, Ψ . An example of this network is shown in figure **3A** (before community assembly) and **3B** (after community assembly). In these figures, the nodes represent species and edges are weighted by their corresponding element in the cohesion matrix (represented in the figures by line thickness and color). Each species has a different node size and color. The size of the species encodes the number of reactions in its reaction network. The color encodes the node strength s_α . The two networks illustrated in figures **3A** and **3B** show that the top 4 species (s3, s0, s8 and s7) with higher total cohesion levels s_α remain extant after the community assembles. Additionally, the bottom 3 species (s1, s9 and s6) with lower s_α have more reactions in their reaction networks than the average. To test the generality of these observations I calculate the median survival probability after community assembly for each s_α rank position in the random community, across all instances of community assembly. Figure **3C** shows a clear correlation between these two measures, indicating that species with lower s_α go extinct more easily than more cohesive species. The survival probability is also plotted as a function of individual performance rank in figure **3C** (see subsection 7.4 for details on the calculation of the proxy of individual performance). The individual performance of a species is calculated here by measuring its equilibrium abundance in isolation. Interestingly, individual performance does not predict survival probability as well as total cohesion level, suggesting that in these experiments, the individual fitness of a species becomes decoupled from its probability of success. This observation reflects the well-known fact that the success of a species is context-dependent, and observing a species in isolation does not measure its performance in the relevant environment (Tikhonov 2016, McGill et al. 2006, McIntire & Fajardo 2014).

The stabilization of the communities during the assembly is normally accompanied by a cascade of extinctions. To investigate how the community-level cohesion changes over the course of community assembly, I measure Θ after the occurrence of every extinction across all simulations. This variation can be seen in figure **3D**, where the binned averaged value of all measures of Θ is represented during the first 500 units of time for all simulations. A systematic increase of community-level cohesion during the first half of measured time, and following stabilization near $\Theta = 0$ is observed. This increase is due to a faster decrease in community competition and facilitation levels, $\langle \bar{C} \rangle$, and $\langle \bar{F} \rangle$, averaged across simulations. (**3D, inset**).

Having assembled many communities, and measured their cohesion levels, I am in good shape to perform community coalescence experiments of pairs of communities.

Consider a coalescence event, whereby two communities previously separated come into sudden contact. In general, monodominance of one community after the mix reaches stable state is not guaranteed. Instead, both communities will contribute species to the final equilibrium. Can we predict which community will do so more successfully?

To answer this question I firstly, use all the simulated communities to populate a facilitation-competition (F-C) diagram where the axes are $\langle F \rangle$ and $\langle C \rangle$; community-level facilitation and competition respectively. They are calculated by averaging the non-diagonal elements of facilitation and competition matrices. Communities are scattered across the plot, bringing out two regimes: a mutualistic regime where $\langle F \rangle > \langle C \rangle$, and a competitive

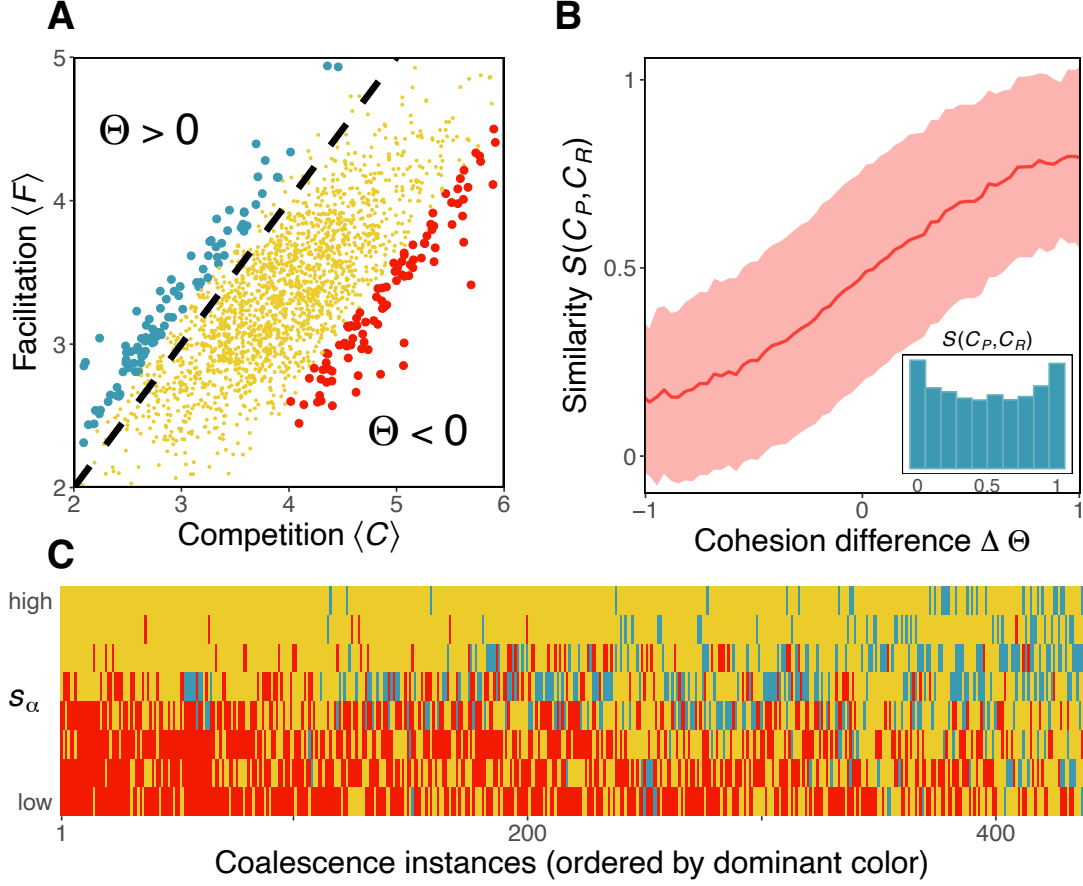


Figure 4: **Results from community coalescence experiments.** (A) Each simulated community is plotted in a competition-facilitation diagram. Communities above the dashed line $\langle C \rangle = \langle F \rangle$ have $\Theta > 0$, and thus they are in the facilitation-dominated regime. Communities below the dashed line have $\Theta < 0$, and therefore they belong to the competition-dominated regime. The extremes of each regime are selected (blue and red dots), and coalescence experiments where one community from the blue group mixes with one community from the red group are performed, only for communities of richness 4. (C) Altruistic communities ($\Theta > 0$) outperform competitive communities ($\Theta < 0$) in the latter experiments. In this elimination assay, each column represents one coalescence instance, and each element in a column is a species. Extinctions are coloured to match the group in plot A to which the extinct species belonged. There is a higher proportion of extinct species from the red group (more red tiles than blue tiles). (B) The outcome of community coalescence is predicted by community-level cohesion. The similarity between the post-coalescence community and the resident community, $S(C_P, C_R)$ is plotted as a function of the community cohesion difference $\Delta \Theta$ between them, for all possible coalescence events between 2 communities of richness 5. Shown is binned mean (100 bins) over communities with similar $\Delta \Theta$ (solid line) $\pm \sigma$ (shaded) (B, inset) Histogram of similarity showing that monodominance of one community after coalescence ($S = 0$, $S = 1$) is more frequent than a perfect mixing ($S = 0.5$)

regime where $\langle F \rangle < \langle C \rangle$. The former case has a community-level cohesion Θ satisfying,
 $\Theta > 0$ whereas the latter has $\Theta < 0$ for the former (see subsection 7.3 for a rigorous
 description of the relationships between these variables). I then select communities with
 4 species from the extremes of the two regimes, $\Theta \gg 0$ and $\Theta \ll 0$. This puts at my
 disposal two groups of communities with higher and lower levels of cohesion (blue and red
 strips in figure 4A). I now perform coalescence experiments where a resident community
 \mathcal{C}_R from one group is mixed with an invading one \mathcal{C}_I from the other group. One would
 expect that communities from the mutualistic regime are more successful on average than
 those from the competitive regime. To confirm this, results from an “elimination assay”
 competing pairs of communities from each group is presented in figure 4C. Near five hun-
 dred pairs of communities are mixed, and correspond to the columns in figure 4C. For
 each pair, species from both communities are equilibrated together. The rows in figure 4C
 correspond to these species, and are ordered increasingly according to their total cohesion
 level s_α . For each species that goes extinct during the coalescent event, its provenance is
 identified (i.e. does it come from the blue or the red community?), and the corresponding
 tile in figure 4C is coloured accordingly. The dominant colour is red, confirming that
 communities in the competitive regime experiment more extinctions, and thus, are worse
 at contributing with their members to the final equilibrium.
 Finally, I select the N communities with 5 species (figure 2B), and perform all $\binom{N}{2}$ pos-
 sible community coalescence events in which a resident community \mathcal{C}_R is mixed with an
 invading one \mathcal{C}_I . At each event, I calculate the similarity of between post-coalescence and
 resident communities as the normalized scalar product of their species abundance vector
 at stable state.

$$S(\mathcal{C}_R, \mathcal{C}_P) = \frac{\vec{N}_\infty^R \cdot \vec{N}_\infty^P}{\sqrt{|\vec{N}_\infty^R|} \sqrt{|\vec{N}_\infty^P|}} \quad (13)$$

Additionally, I calculate the community-level cohesion difference $\Delta\Theta$ between the two co-
 alescing communities. A clear non-linear correlation emerges when I plot similarity versus
 cohesion difference (figure 4B). The larger the difference between community cohesion,
 the more similar is the post-coalescent community to its more cohesive parent. The non-
 linearity of this curve is a manifestation of the asymmetrical dominance reported in the
 first works of community coalescence (Gilpin 1994). This is more evident when looking
 at the histogram of similarities (4B, inset) for the coalescence experiments performed,
 where monodominance of one community ($S = 1, S = 0$) is more frequent than a perfect
 mixing ($S = 0.5$)

4 Discussion

A frequent way in which microbial communities come to be is through the fusion of two
 or more communities, an event that has been termed community coalescence (Rillig et al.
 2015). Numerous theoretical and experimental studies suggest that coalescing communi-
 ties behave as “coherent wholes”, and compete against each other like coordinated armies
 (Gilpin 1994, Toquenaga 1997, Livingston et al. 2013, Tikhonov 2016, Tikhonov & Monas-
 son 2017, Sierocinski et al. 2017, Lu et al. 2018). To date, competition in coalescence is
 the most studied interaction, but more work is needed to understand how other types of
 interactions lead to different coalescence outcomes (Castledine et al. 2020). In this work,
 I investigated the behaviour of pairs of coalescent communities that harboured organism
 interdependence through metabolic complementarity (i.e., cross-feeding). How does in-
 cluding mutualistic interactions affect the outcome of community coalescence?

To answer this question, I quantified the coherence of these consortia through a metric of community cohesion, Ψ , which computes the level of positive feedback between every pair of species in the community. I found that Ψ increased on average during community formation (see Figure **2D**). Tracking cohesion in coalescence events revealed a non-linear relationship between cohesiveness and post-coalescence success, that is, more cohesive communities were coherently favoured during species sorting and therefore dominated at equilibrium. This result constitutes strong evidence supporting that a community undergoing a coalescence event behaves as a 'coherent whole'. It is expected that members of cohesive communities have been ecologically co-selected; those individuals from a key taxon whose presence provides an advantage for individuals from other taxa are positively selected (Sierocinski et al. 2017). This contrasts with the alternative hypothesis suggesting that those communities harbouring species with higher individual performance are the ones that would dominate in the formation of communities. Only weak support was found for this hypothesis (see Figure **2C**). These two hypotheses are two extremes of a continuum. Although it certainly seems an exaggeration to view the community as a "super-organism", it is also a perilous simplification to consider it as a mere collection of individuals, ignoring the fact that coevolutionary processes can play an important role in it (Rillig & Mansour 2017).

A recent idea that smoothly interpolates between these two extremes has been proposed in (Pascual-García et al. 2020). Metabolically Cohesive microbial Consortium (MeCoCos) are groups of microbes that exhibit a positive feedback loop, whereby they engineer their environment by both creating and using resources. They constitute an intermediate level of organization between the community and the individual. These groups have been hypothesized to be resistant against invasions because no other species would be able to harvest resources rapidly enough to compete with the established members. My finding that more metabolically cohesive consortia are more successful in community coalescence experiments confirms their hypothesis. A possible line for future research would be to use the metric of cohesion to identify MeCoCos in the synthetic communities, and track their behaviour to try to answer the following question: can we understand microbial community assembly as a succession of MeCoCos coalescence events?

Another prediction of Pascual-García et al. (2020) is that MeCoCos efficiently deplete resources to the lowest concentration. This result was obtained in the absence of mutualistic interactions by Tikhonov (2016), who showed that when two communities compete, the one that is more efficient at simultaneously depleting all substrates (higher community-level fitness), will dominate. The *cohesive* communities of my work behave in the same way as the *fit* communities in his work when it comes to community coalescence (compare figure **4B** here with figure 4D in Tikhonov (2016)). This confirms the above prediction that more cohesive communities are also more efficient at simultaneously depleting all resources.

The dynamics of the model presented in Tikhonov (2016) conveniently took the form of optimizing a community level function inspired by the work of MacArthur (1969). In this more general model, collective dynamics were not reducible to solving an optimization problem. Yet, the results presented here are consistent with the ones in Tikhonov (2016), reinforcing the relevance of this approach as a method for characterizing community coalescence events in more complex communities. These results, and the ones reported in works of community-community competition up to date, have been consistent across different models, and types of interactions. Therefore, the coherence exhibited by microbial communities seems to be a general consequence of ecological interactions, resource partitioning, and the community shaping its own environment (niche construction).

Several simplifications were made in this study. First, the parameters of the model were kept constant throughout the simulations. The reason behind this is that the aim of this study was to show that the strength and type of interactions present in microbial communities influence the outcome of community coalescence. For this purpose, experimental parametrization of the model was not strictly necessary and was left to be developed in future work. Second, the model used here left out stochastic effects and spacial structure. Although these two considerations are tremendously important in most cases, their removal in this work helped to smoothly build on the work of Tikhonov (2016), and to make the dynamics computationally tractable. Third, the measure of community-level cohesion, Θ , was calculated as the rough average of all pairwise cohesion levels. A more refined measure of community cohesion, for example, counting the number of closed feedback loops, weighted by their strength, might help reduce the noise of the correlation shown in figure 4B.

4.1 Empirical relevance

Measuring cohesion in the synthetic communities used in this work was possible because the theoretical framework of the model provided readily usable reaction networks. The aim of these is to resemble bacterial metabolic pathways, and thus lay out the foundations for the formulation of consumer-resource models that characterize more realistic microbial communities. A promising direction of research would be to focus on parametrizing the model based on available high-resolution metabolic networks in the literature and then attempting to use it, in combination with the proposed cohesion measure, to predict the outcome of real-life community coalescence events either *in-vitro* or *in-vivo*. This could then be applied then to drive the community in question, through successive coalescence events, towards states where certain functions are optimized, as demonstrated in Sierocinski et al. (2017), and suggested in Rillig, Tsang & Roy (2016). Another example of this is the coalescence events whereby microbial communities are introduced in degraded soil ecosystems in order to restore N-cycle functioning (Calderón et al. 2017). Finally, the predictive power of the presented cohesion metric has a relevant application in the area of faecal microbiota transplantation. This is a method to directly change the recipient's gut microbiota to normalize its composition and restore a therapeutic benefit (Wang et al. 2019, Wilson et al. 2019). The application of the technique presented here to this discipline can yield beneficial insights from an anthropocentric perspective.

4.2 Conclusion

- General idea
- Applied to real communities
-

7 Appendix

7.1 Reversible enzyme kinetics

Outside the the bacterial cell, the energy resides in the form of chemical potential μ held by the metabolites, and biochemical reactions inside the cell produce energy due to a difference in the chemical potentials of substrate and product. I assigned chemical potentials to each metabolite according to

$$\mu_\beta = E \left(1 - \sqrt{\frac{\beta - 1}{m - 1}} \right) \quad (14)$$

where $\beta = 1, \dots, m$ and E is the energy of the most energetic metabolite. I have chosen this chemical potential function because I hope to find papers where they explain that there is a hierarchy on the metabolite energetic spectrum. This means that the energy produced by a reaction of the type $(\beta, \beta + 1)$ decreases as you go down the hierarchy. Reactions involving metabolites situated higher in the hierarchy are more energetic than reactions that involve those lower in the hierarchy.

The rate at which a given chemical reaction transforms substrate into product is modelled using reversible Michaelis-Menten enzyme kinetics. Thus, the model considers chemical reactions where a substrate S binds to an enzyme E to form an enzyme-substrate complex ES , which in turn produces a product P and recovers enzyme E .



The choice of fully reversible enzyme kinetics, instead of the traditional assumption of irreversibility in the second reaction, aims to capture more accurately the nature of biochemical reactions taking place in microbial communities. In these reactions the Gibbs energy change ΔG is not always big, which implies that the reaction of product formation can reach equilibrium at a similar time scale as the formation of the complex (Keener & Sneyd 2008). In this case, the traditional irreversible Michaelis-Menten scheme breaks down, and more elaborated frameworks, like the fully reversible one that this model offers, need to be used.

To comply with 2^{nd} law of thermodynamics, the network G_α is completely hierarchical, ie. the edges are unidirectional ($x < y$), going from the more energetic, to the less energetic metabolite. Thus, for the reaction scheme in 15 and the imposed thermodynamic constraint only reactions where $\Delta G^0 = \mu_P - \mu_S < 0$ can take place.

With all the above considerations, the expression for the rate of reaction i possessed by strain α is given below. A formal derivation of equation 16 can be found in Hoh & Cord-Ruwisch (2000)

$$q_{\alpha i} = \frac{q_m^{\alpha i} S_\alpha (1 - \theta_\alpha)}{K_S^{\alpha i} + S_\alpha (1 + k_R^{\alpha i} \theta_\alpha)} \quad (16)$$

Here, θ_α measures how far is the reaction from equilibrium (0 being the furthest, and 1 being equilibrium).

$$\theta = \frac{[P]}{[S]K_{eq}} \quad (17)$$

where $[]$ denote concentration and K_{eq} is the equilibrium constant

$$K_{eq} = \exp \left(\frac{-\Delta G^0 - \eta \Delta G_{ATP}}{RT} \right) \quad (18)$$

523 The energy produced by the reaction is then stored in the form of ATP molecules. In
 524 the model, η represents the moles of ATP molecules produced per mole of reaction. For
 525 a given reaction (x, y) eta I calculate eta as

$$526 \quad \eta = \frac{y - x}{m} \quad (19)$$

527 which represents the normalized metabolite gap between substrate and product of the
 528 reaction. Therefore, the higher the gap, the more energy will be stored.
 529

530 7.2 Table of parameter values and meaning

Parameter	Meaning	Value
m	Number of metabolites	100
s	Number of strains	10
ΔG_{ATP}	ATP Gibbs energy	$7.5 \cdot 10^4$
μ_0	Most energetic metabolite	$3 \cdot 10^4$
nATP	$\max\left(\frac{\Delta G_{S \rightarrow P}^0}{\Delta G_{ATP}}\right)$	4
η	Moles of ATP energy per reaction	0.5
q_m	Maximum reaction rate	1
K_S	Saturation constant	0.1
k_r	Reversibility constant	10
g	Growth factor	1
m	Maintenance factor	$0.2 \cdot J_{grow}$
κ	Externally supplied resource	1
γ	Dilution rate	0.5
N_0	Populations initial conditions	(1, 1, ..., 1)
C_0	Concentrations initial condition	(0, 0, ..., 0)

Table 1: Parameter meanings and their values

531 7.3 Relationship between Θ , F , C , and Ψ

532 7.4 Calculation of individual fitness

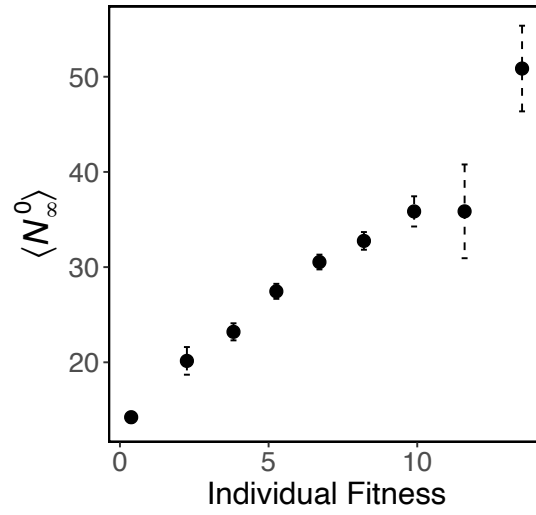


Figure 5: Abundance of 500 random species at isolated equilibrium as a function of proxy of individual fitness. Shown is binned mean (10 bins) over species with similar individual fitness. Errorbars are 1 standard error.

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