11.7. Taylor settes (construmed) It is oreful to know the Toylor series of women functions seeme we can generate new Taylor series from all over. This is become of the migneres of a Taylor series. $e^{x} = \sum_{n=0}^{\infty} \frac{x^{n}}{n!}$, $f_{n}(x) = \sum_{n=0}^{\infty} \frac{(-1)^{n}}{(2n+1)!} \frac{x^{2n+1}}{(2n+1)!}$. $w_{1}(x) = \sum_{n=0}^{\infty} \frac{(-1)^{n}}{(2n)!}$ Example: Find the Moderation series for x 4 e x ×4. ex = x4. \(\frac{1}{20} \) \(\frac{(-x)^n}{n!} = \frac{1}{20} \) \(\frac{(-1)^n}{n!} \) Example: Find the Toplar selies for luck around c= 2. (x) = wext, f'(x) = \frac{1}{x}, f''(x) = \frac{1}{x^2}, f''(x) = \frac{2}{x^3}, f(x) = \frac{2}{x^4} so fat (x) = (-1) x (n-1)! - times: f(2) = (-1) x (n-1)! $T(x) = \ln(2) + \sum_{n=1}^{\infty} (-1)^{n+1} (nq-1)! \cdot \frac{1}{n!} \cdot (x-2)^n = \ln(2) + \sum_{n=1}^{\infty} (-1)^{n+1} (x-2)^n \cdot \frac{1}{n!} \cdot$ Example: First the Taylor series for (x-lu(x) aron The Taylor series of luck) is above, the Taylor series for x is 2+(x-2), so combining the $T(x) = (2+(x-2)) \cdot (\ln(2) + \sum_{n=1}^{\infty} \frac{(-1)^{n+1}(x-2)^n}{n! 2^n}) =$ = ln(4) || + ln(2) (x-2) + 2. = (-1) 1/1 (x-2) + = (-1) (x-2) = |u(u)| + |u(2)+1| |(x-2)| + $\sum_{n=1}^{\infty} \left(\frac{(-1)^n \cdot (x-2)^{n+1}}{(n+1)\cdot 2^n} + \frac{(-1)^{n+1} \cdot (x-2)}{n\cdot 2^n}\right)$ = In(4) + (1+In(21)(x-2)+ = (-1) +1 (x-2) ++ Example: Find the TS(X) of arctan(X) -- = = = x , arton(x) = = = (-1) x 2n+1 $(1+x+x^2+x^3+x^4)(x-\frac{x^3}{3}+\frac{x^5}{5}) \rightarrow x-\frac{x^3}{3}+\frac{x^5}{5}+x^2-\frac{x^4}{3}+x^3$ $-\frac{x^{3}}{3} + x^{4} + x^{5} = x + x^{2} + \frac{2x^{3}}{3} + \frac{2}{3} \times \frac{4}{15} + \frac{13}{15} \cdot x^{5}.$