



# Kalman Filter

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# Low-pass Filter in Time

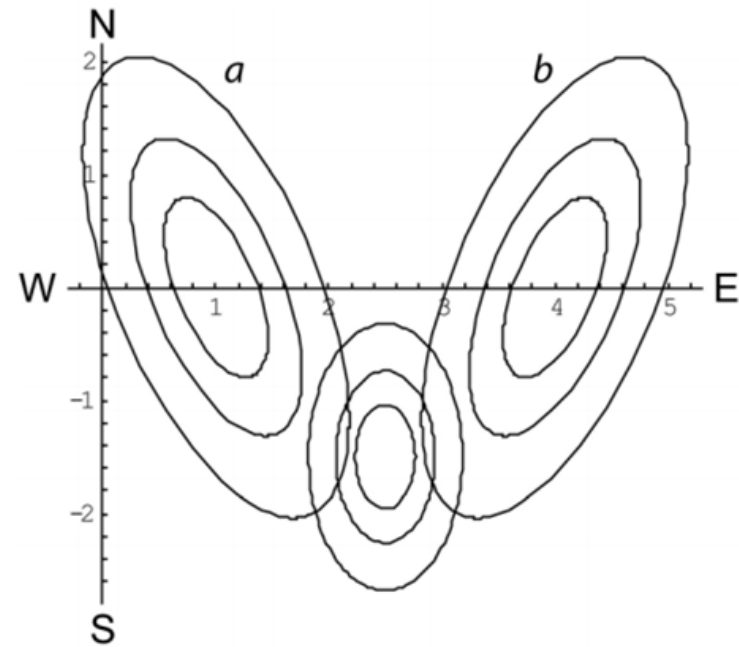
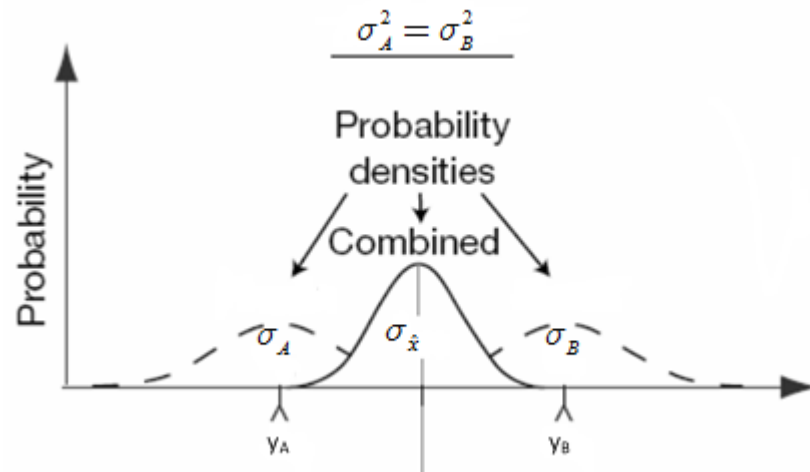
New data  $x_k$  comes in

$$\bar{x}_k = \frac{x_1 + x_2 + \cdots + x_{k-1} + x_k}{k}$$

Recursive

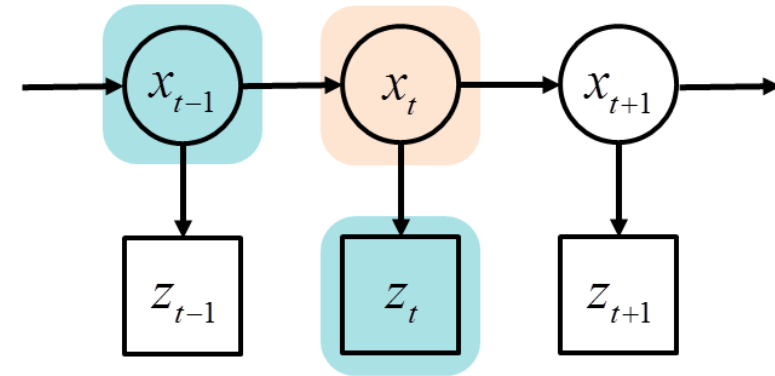
$$\begin{aligned}\bar{x}_k &= \frac{k-1}{k} \bar{x}_{k-1} + \frac{1}{k} x_k \\ &= \alpha \bar{x}_{k-1} + (1 - \alpha) x_k, \quad \alpha = \frac{k-1}{k}\end{aligned}$$

# Sensor Fusion (Two Measured Observations)



# Kalman Filter

- Linear dynamical system of motion
- $A, B, C$  ?
- Continuous State space model
  - For filtering and control applications
  - Linear-Gaussian state space model
  - Widely used in many applications:
    - GPS, weather systems, etc.
- Weakness
  - Linear state space model assumed
  - Difficult to apply to highly non-linear domains



$$\begin{aligned}x_{t+1} &= Ax_t + Bu_t \\ z_t &= Cx_t\end{aligned}$$

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