

# Decimal to binary

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- 00215547  
- 03/01/2023

$(10)_{10} \rightarrow \text{binary}$

$$\begin{array}{r} 10 \quad \underline{2} \\ 0 \quad 5 \quad \underline{2} \\ \quad 1 \quad 2 \quad \underline{2} \\ \quad \quad 0 \quad 1 \end{array} \rightarrow (1010)_2$$

$(1369)_{10} \rightarrow \text{binary}$

$$\begin{array}{r} 1369 \quad \underline{2} \\ 16 \quad 684 \quad \underline{2} \\ 09 \quad 0 \quad 342 \quad \underline{2} \\ 1 \quad \quad 0 \quad 171 \quad \underline{2} \\ \quad \quad 11 \quad 85 \quad \underline{2} \\ \quad \quad 1 \quad 1 \quad 42 \quad \underline{2} \\ \quad \quad \quad 0 \quad 21 \quad \underline{2} \\ \quad \quad \quad 1 \quad 10 \quad \underline{2} \\ \quad \quad \quad \quad 0 \quad 5 \quad \underline{2} \\ \quad \quad \quad \quad 1 \quad 2 \quad \underline{2} \\ \quad \quad \quad \quad \quad 0 \quad 1 \end{array} \rightarrow (10101011001)_2$$

$(9234876)_{10} \rightarrow \text{binary}$

$$\begin{array}{r} 9234876 \quad \underline{2} \\ 0 \quad 4617438 \quad \underline{2} \\ \quad 0 \quad 2308719 \quad \underline{2} \\ \quad \quad 1 \quad 1154359 \quad \underline{2} \\ \quad \quad \quad 1 \quad 577179 \quad \underline{2} \\ \quad \quad \quad 1 \quad 288589 \quad \underline{2} \\ \quad \quad \quad \quad 1 \quad 144294 \quad \underline{2} \\ \quad \quad \quad \quad 0 \quad 72147 \quad \underline{2} \\ \quad \quad \quad \quad \quad 1 \quad 36073 \quad \underline{2} \\ \quad \quad \quad \quad \quad \quad 1 \quad 18036 \quad \underline{2} \\ \quad \quad \quad \quad \quad \quad \quad 0 \quad 9018 \\ \quad \quad \quad \quad \quad \quad \quad \quad 0 \quad 70 \quad \underline{2} \\ \quad \quad \quad \quad \quad \quad \quad \quad 0 \quad 35 \quad \underline{2} \\ \quad \quad \quad \quad \quad \quad \quad \quad 1 \quad 17 \quad \underline{2} \\ \quad \quad \quad \quad \quad \quad \quad \quad 1 \quad 8 \quad \underline{2} \\ \quad \quad \quad \quad \quad \quad \quad \quad 0 \quad 4 \quad \underline{2} \\ \quad \quad \quad \quad \quad \quad \quad \quad 0 \quad 2 \quad \underline{2} \\ \quad \quad \quad \quad \quad \quad \quad \quad 0 \quad 1 \end{array} \rightarrow (100011001110100110111100)_2$$

$(49\ 263\ 749)_{10} \rightarrow \text{binary}$

$49\ 263\ 749 \underline{2}$   
 $\quad 1\ 24631874 \underline{2}$   
 $\quad\quad 0\ 12315937 \underline{2}$   
 $\quad\quad\quad 1\ 6157968 \underline{2}$   
 $96120 \underline{2}$   
 $\quad 0\ 48109 \underline{2}$   
 $\quad\quad 1\ 24054 \underline{2}$   
 $\quad\quad\quad 0\ 12027 \underline{2}$   
 $\quad\quad\quad\quad 1\ 6013 \underline{2}$   
 $\quad\quad\quad\quad\quad 1\ 3006 \underline{2}$   
 $\quad\quad\quad\quad\quad\quad 0\ 1503 \underline{2}$   
 $\quad\quad\quad\quad\quad\quad\quad 1\ 751 \underline{2}$   
 $\quad\quad\quad\quad\quad\quad\quad\quad 1\ 375 \underline{2}$   
 $\quad\quad\quad\quad\quad\quad\quad\quad\quad 1\ 187 \underline{2}$   
 $\quad\quad\quad\quad\quad\quad\quad\quad\quad\quad 1\ 93 \underline{2}$   
 $\quad\quad\quad\quad\quad\quad\quad\quad\quad\quad\quad 1\ 46 \underline{2}$   
 $\quad\quad\quad\quad\quad\quad\quad\quad\quad\quad\quad\quad 0\ 23 \underline{2}$   
 $\quad\quad\quad\quad\quad\quad\quad\quad\quad\quad\quad\quad\quad 1\ 11 \underline{2}$   
 $\quad\quad\quad\quad\quad\quad\quad\quad\quad\quad\quad\quad\quad\quad 1\ 5 \underline{2}$   
 $\quad\quad\quad\quad\quad\quad\quad\quad\quad\quad\quad\quad\quad\quad\quad 1\ 2 \underline{2}$   
 $\quad\quad\quad\quad\quad\quad\quad\quad\quad\quad\quad\quad\quad\quad\quad\quad 0\ 1$

$\rightarrow (1011101111011010010000101)_2$

## Decimal to binary (2's complement)

$(-20)_{10} \rightarrow \text{binary (2's complement)}$

Positive value:

$20 \underline{2}$   
 $\quad 0\ 10 \underline{2}$   
 $\quad\quad 0\ 5 \underline{2}$   
 $\quad\quad\quad 1\ 2 \underline{2}$   
 $\quad\quad\quad\quad 0\ 1$

$\rightarrow (20)_{10} \rightarrow (10100)_2$

1's complement

$10100$   
 $\quad \neg$   
 $01011$

2's complement

$01011$   
 $\quad + 1$   
 $01100$

$\rightarrow (101100)_2$   
 $\quad \underbrace{\hspace{1.5cm}}_{6 \text{ digits}}$

$(-1025)_{10} \rightarrow \text{binary (2's complement)}$

Positive value:  $1025 \xrightarrow{2} 512 \xrightarrow{2} 256 \xrightarrow{2} 128 \xrightarrow{2} 64 \xrightarrow{2} 32 \xrightarrow{2} 16 \xrightarrow{2} 8 \xrightarrow{2} 4 \xrightarrow{2} 2 \xrightarrow{2} 1$   $\rightarrow (1000000001)_2$

1's complement  $\begin{array}{r} 1000000001 \\ \neg \end{array}$  2's complement  $\begin{array}{r} 0111111110 \\ + 1 \\ \hline 0111111111 \end{array} \rightarrow \overline{(1011111111)}_2$   
12 digits

$(-3925)_{10} \rightarrow \text{binary (2's complement)}$

Positive value:

$3925 \xrightarrow{2} 1962 \xrightarrow{2} 981 \xrightarrow{2} 490 \xrightarrow{2} 245 \xrightarrow{2} 122 \xrightarrow{2} 61 \xrightarrow{2} 30 \xrightarrow{2} 15 \xrightarrow{2} 7 \xrightarrow{2} 3 \xrightarrow{2} 1$   $\rightarrow (111101010101)_2$

1's complement

$\begin{array}{r} 111101010101 \\ \neg \end{array}$  2's complement  $\begin{array}{r} 000010101010 \\ + 1 \\ \hline 000010101011 \end{array} \rightarrow \overline{(1000010101011)}_2$   
13 digits

$(-104596)_{10} \rightarrow \text{binary (2's complement)}$

Positive value:

$$\begin{array}{rcl}
 104596 & \underline{2} & \\
 \bigcirc & 52298 & \underline{2} \\
 \bigcirc & 26149 & \underline{2} \\
 1 & 13074 & \underline{2} \\
 \bigcirc & 6537 & \underline{2} \\
 1 & 3268 & \underline{2} \\
 \bigcirc & 1634 & \underline{2} \\
 \bigcirc & 817 & \underline{2} \\
 1 & 408 & \underline{2} \\
 \bigcirc & 204 & \underline{2} \\
 \bigcirc & 102 & \underline{2} \\
 \bigcirc & 51 & \underline{2} \\
 1 & 25 & \underline{2} \\
 1 & 12 & \underline{2} \\
 \bigcirc & 6 & \underline{2} \\
 \bigcirc & 3 & \underline{2} \\
 1 & 1 & 
 \end{array}
 \longrightarrow (11001100010010100)_2$$

1's complement

$$\begin{array}{r}
 11001100010010100 \\
 \hline
 00110011101101011
 \end{array}$$

2's complement

$$\begin{array}{r}
 00110011101101011 \\
 + 1 \\
 \hline
 00110011101101100
 \end{array}$$

$$\begin{array}{c}
 \overline{\phantom{00110011101101100}} \\
 (1\ 00110011101101100)_2 \\
 \hline
 18 \text{ digits}
 \end{array}$$

# Unsigned binary to Hex

- $(110011110101011001101110110110000101001)_2$

## Long method

1. Binary to decimal:  $\rightarrow 890508335145$

2. Decimal to Hex:

890508335145 16  
 9 55656770946 16  $\rightarrow$  CF566E0829  
 2 3478548184 16  
 8 217409261 16  
 53078 16 13 13588078 16  
 6 3317 16 14 849254 16  
 5 207 16 6 53078  
 15 12

## Short Method

1100	1111	0101	0110	0110	1110	1101	1000	0010	1001
└─┘	└─┘	└─┘	└─┘	└─┘	└─┘	└─┘	└─┘	└─┘	└─┘
12	15	5	6	6	14	13	8	2	9

 $\rightarrow$  CF566E0829

- $(1000011110001110011110001110001111110011)_2$

## Long method

1. Binary to decimal:  $\rightarrow 582206678003$

2. Decimal to Hex:

582206678003 16  
 3 36387997375 16  $\rightarrow$  878E38E3F3  
 15 2274244835 16  
 3 142140302 16  
 34702 16 14 8883768 16  
 14 2168 16 8 555235 16  
 8 135 16 3 34702  
 7 8

## Short Method

1000	0111	1000	1110	0111	1000	1110	0011	1111	0011
└─┘	└─┘	└─┘	└─┘	└─┘	└─┘	└─┘	└─┘	└─┘	└─┘
8	7	8	14	3	8	14	3	15	3

 $\rightarrow$  878E38E3F3

•  $(1010\ 1101\ 0101\ 1100\ 0110\ 0101\ 0100\ 1010\ 1010\ 1010)_2$

Long method

1. Binary to decimal:  $\rightarrow 744579484330$

2. Decimal to Hex:

744579484330 16  
 10 46536217770 16  $\rightarrow$  A05C654AAA  
 10 29085136100 16  
 44380 16 10 181782100 16  
 12 2773 16 4 11361381 16  
 5 173 16 5 710086 16  
 13 10 6 44380

Short Method

1010 1101 0101 1100 0110 0101 0100 1010 1010 1010  
 ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓  
 10 13 5 12 6 5 4 10 10 10  $\rightarrow$  A05C654AAA

•  $(1010\ 0010\ 1010\ 1010\ 1010\ 1010\ 1011\ 1111\ 1100\ 0000)_2$

Long method

1. Binary to decimal:  $\rightarrow 698648018880$

2. Decimal to Hex:

698648018880 16  
 10 436790501280 16  $\rightarrow$  A2AAAA BFC0  
 12 2724003323 16  
 15 1705563363 16  
 11 10660522 16  
 10 666282 16  
 2 10 10 41642

Short Method

1010 0010 1010 1010 1010 1010 1011 1111 1100 0000  
 ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓  
 10 2 10 10 10 10 11 15 12 0  $\rightarrow$  A2AAAA BFC0

# Signed Binary to octal

- $(111\ 111\ 000\ 001\ 111\ 100\ 000\ 001\ 110\ 101\ 011)_2$

Long method (Negative number)

1. Binary to decimal:  $\rightarrow 130153557$

2. Decimal to Octal:

130153557 8  
 5 16269194 8  $\rightarrow -760376125$   
 2 2033649 8  
 1 254206 8  
 6 31775 8  
 7 3971 8  
 3 496 8  
 0 62 8  
 6 7

Short Method (Negative number)

2's complement: 000 000 111 110 000 011 111 110 001 010 101

000 000 111 110 000 011 111 110 001 010 101  
 ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓  
 / / - 7 6 0 3 7 6 1 2 5  $\rightarrow -760376125$

- $(010\ 101\ 010\ 101\ 111\ 111\ 111\ 111\ 110\ 000\ 000)_2$

Long method (Positive number)

1. Binary to decimal:  $\rightarrow 286\ 470\ 9504$

2. Decimal to Octal:

2864709504 8  
 0 358088688 8  $\rightarrow 25257777600$   
 0 44761086 8  
 6 6595135 8  
 7 699391 8  
 7 87423 8  
 7 10927 8  
 7 1365 8  
 5 170 8  
 2 21 8  
 5 2

Short Method (Negative number)

010 101 010 101 111 111 111 111 110 000 000  
 ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓  
 2 5 2 5 7 7 7 7 6 0 0  $\rightarrow 25257777600$

- $(11100011100000011111110000101010)_2$ ,

Long method (Negative number)

1. Binary to decimal:  $\rightarrow 1912080372$

2. Decimal to Octal:

1912080372 8  
 6 239010042 8  
 2 29876255 8  
 7 3734531 8  
 3 466816 8  
 0 58352 8  
 0 7294 8  
 6 911 8  
 7 113 8  
 1 14 8  
 6 1 8

$\rightarrow -16176003726$

Short Method (Negative number)

2's complement: 001110001111100000011111010110

001	110	001	111	110	000	000	011	111	010	110
↓	↓	↓	↓	↓	↓	↓	↓	↓	↓	↓
1	6	1	7	6	0	0	3	7	2	6

$\rightarrow -16176003726$

- $(10101010101000010101010101111000)_2$

Long method (Negative number)

1. Binary to decimal:  $\rightarrow 572944424$

2. Decimal to Octal:

572944424 8  
 0 71615553 8  
 1 89519944 8  
 4 11189930 8  
 2 1398741 8  
 5 174042 8  
 2 21855 8  
 7 2731 8  
 3 341 8  
 5 42 8  
 2 5 8

$\rightarrow -52537252410$

Short Method (Negative number)

2's complement: 101010101011110101010100001000

101	010	101	011	111	010	101	010	100	001	000
↓	↓	↓	↓	↓	↓	↓	↓	↓	↓	↓
5	2	5	3	7	2	5	2	4	1	0

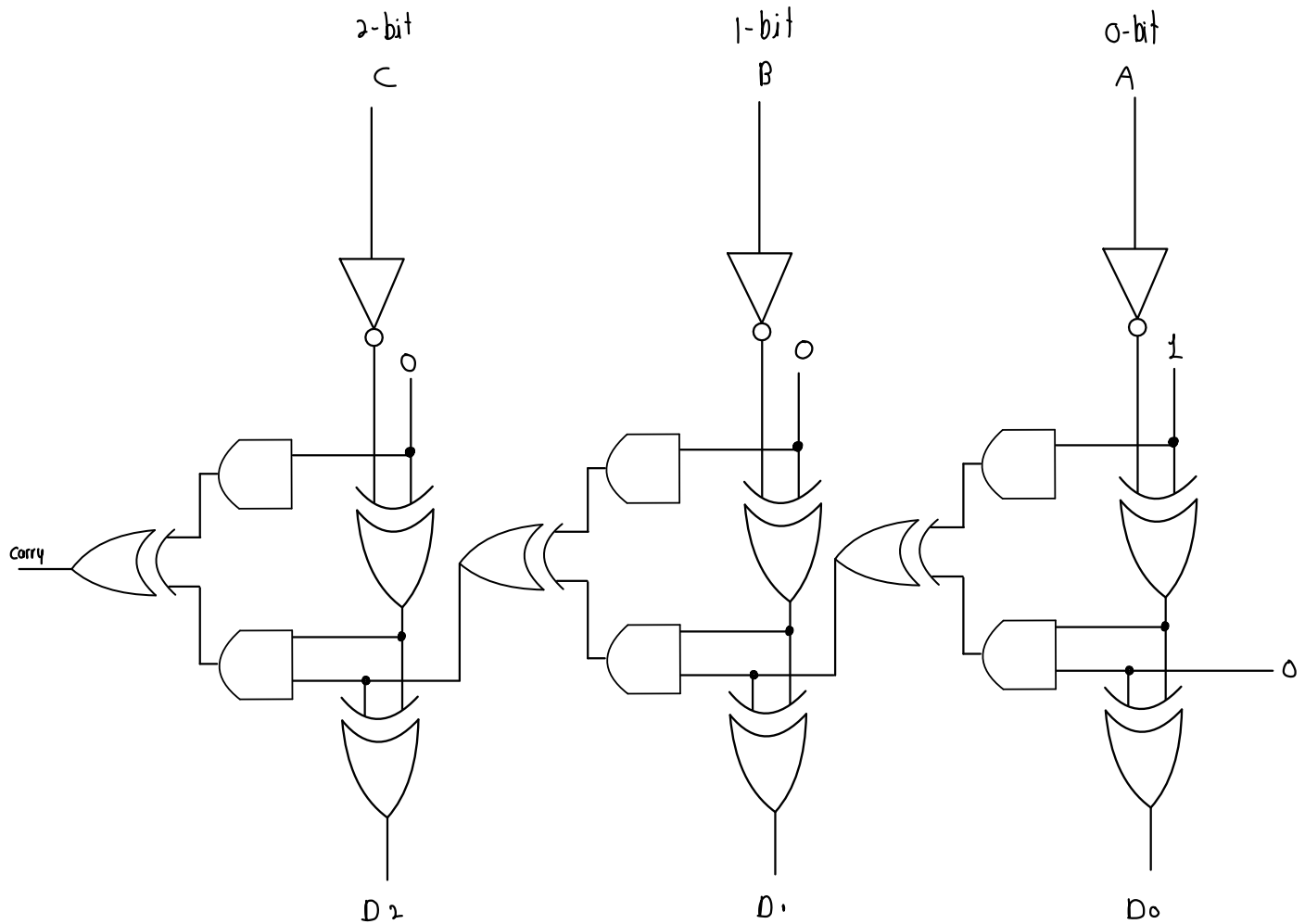
$\rightarrow -52537252410$



## 2. Boolean Circuits

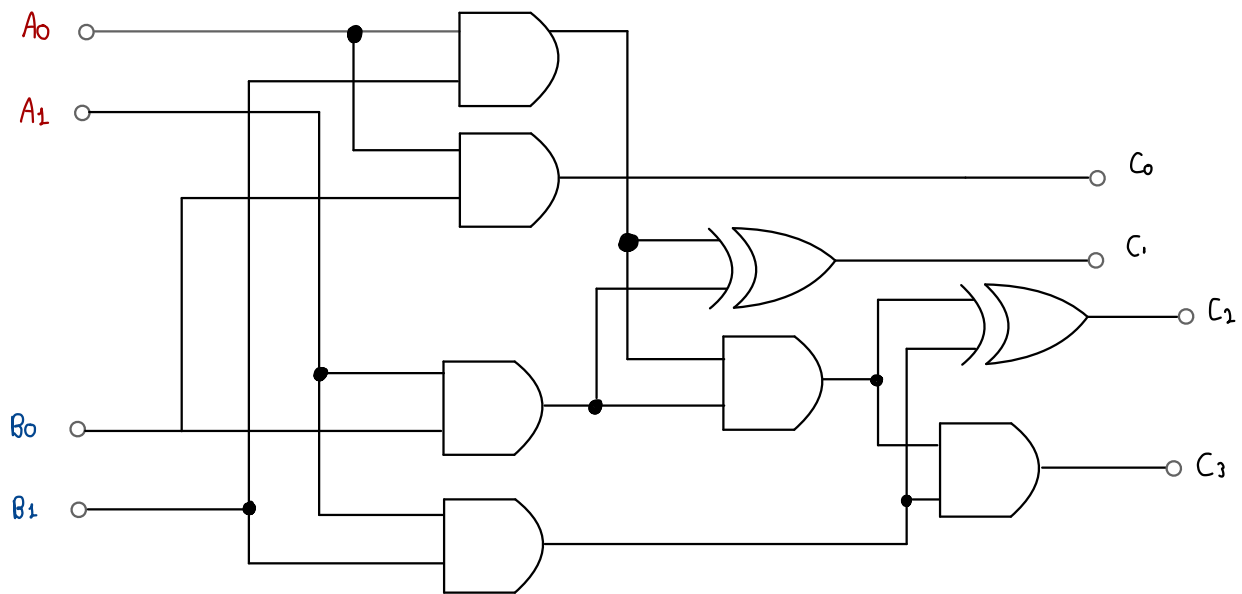
Circuit and truth table for:

- Multiplication of two binary numbers of length 2 bits



A	B	C	D <sub>0</sub>	D <sub>1</sub>	D <sub>2</sub>
0	0	0	0	0	0
0	0	1	1	1	1
0	1	0	1	1	0
0	1	1	1	0	1
1	0	0	1	0	0
1	0	1	0	1	1
1	1	0	0	1	0
1	1	1	0	0	1

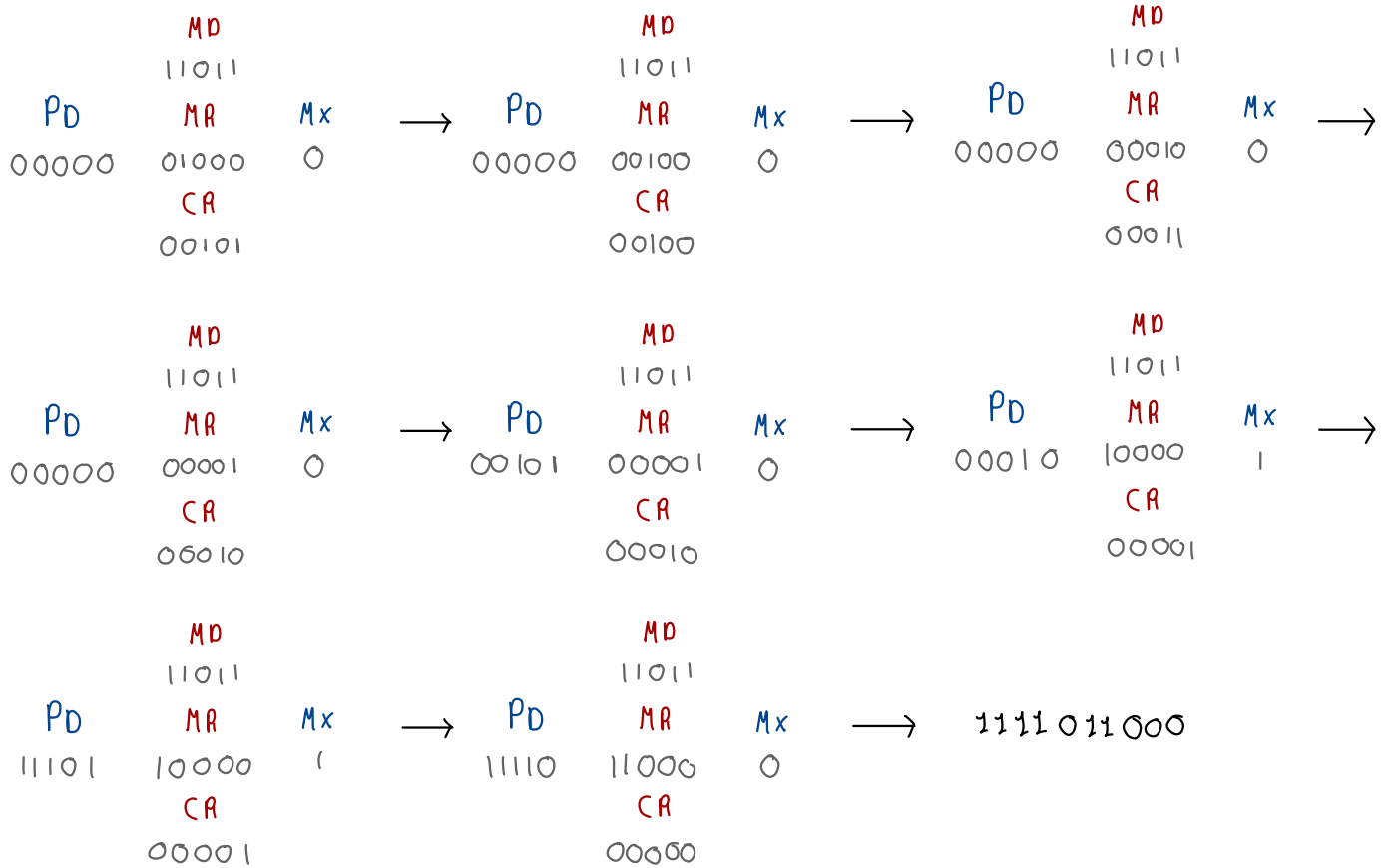
- Two's complement for a binary number of length 3 bits



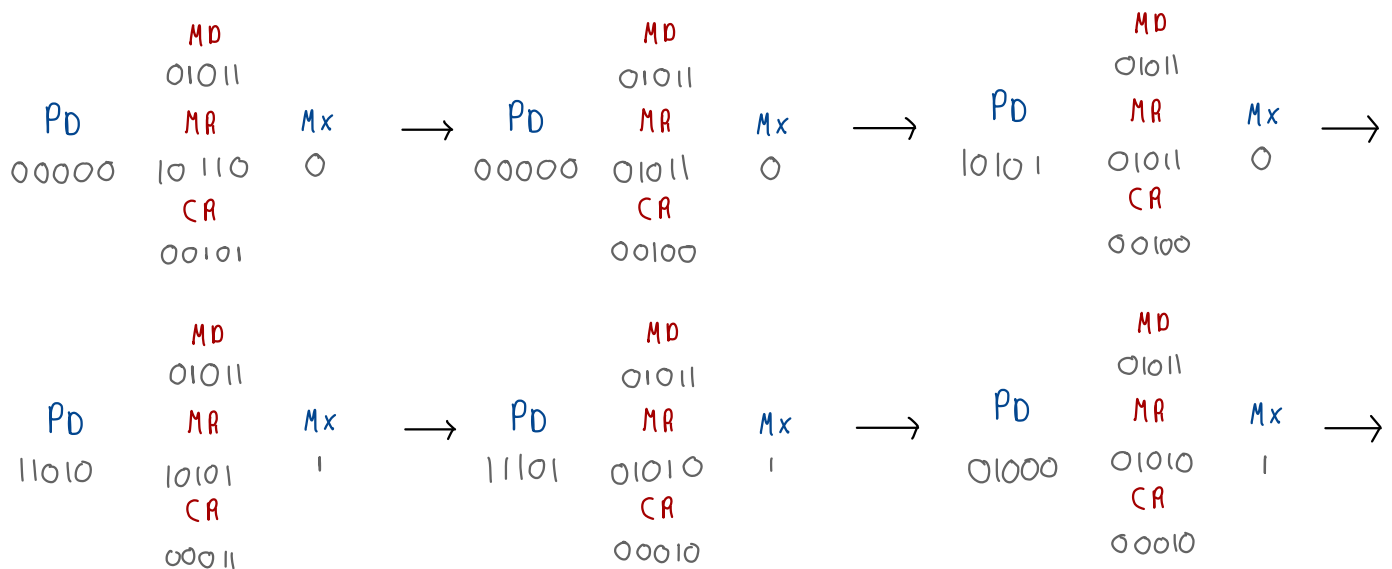
$A_0$	$A_1$	$B_0$	$B_1$	$C_0$	$C_1$	$C_2$	$C_3$
0	0	0	0	0	0	0	0
0	0	0	1	0	0	0	0
0	0	1	0	0	0	0	0
0	0	1	1	0	0	0	0
0	1	0	0	0	0	0	0
0	1	0	1	0	0	0	1
0	1	1	0	0	0	1	0
0	1	1	1	0	0	1	1
1	0	0	0	0	0	0	0
1	0	0	1	0	0	1	0
1	0	1	0	0	1	0	0
1	0	1	1	0	1	1	0
1	1	0	0	0	0	0	0
1	1	0	1	0	0	1	1
1	1	1	0	0	1	1	0
1	1	1	1	1	0	0	1

### 3. Binary Multiplication

•  $-5 \times 8$  :  $5 \rightarrow 00101 \xrightarrow{2's} 11011$  MO  
 $8 \rightarrow 01000$  MR



•  $11 \times (-10)$  :  $11 \rightarrow 01011$  MO  
 $10 \rightarrow 01010 \xrightarrow{2's} 10110$  MR



$$\begin{array}{c}
 \text{PD} \\
 00100
 \end{array}
 \begin{array}{c}
 \text{MD} \\
 01011 \\
 \text{MR} \\
 00101 \\
 \text{CR} \\
 00001
 \end{array}
 \begin{array}{c}
 \text{Mx} \\
 0
 \end{array}
 \longrightarrow
 \begin{array}{c}
 \text{PD} \\
 11001
 \end{array}
 \begin{array}{c}
 \text{MD} \\
 01011 \\
 \text{MR} \\
 00101 \\
 \text{CR} \\
 00001
 \end{array}
 \begin{array}{c}
 \text{Mx} \\
 0
 \end{array}
 \longrightarrow
 \begin{array}{c}
 \text{PD} \\
 11100
 \end{array}
 \begin{array}{c}
 \text{MD} \\
 01011 \\
 \text{MR} \\
 10010 \\
 \text{CR} \\
 00000
 \end{array}
 \begin{array}{c}
 \text{Mx} \\
 1
 \end{array}
 \longrightarrow$$

$$\longrightarrow 1110010010$$

•  $2 \times 3$ :  $2 \rightarrow 010$  MD  
 $3 \rightarrow 011$  MR

$$\begin{array}{c}
 \text{PD} \\
 000
 \end{array}
 \begin{array}{c}
 \text{MD} \\
 010 \\
 \text{MR} \\
 011 \\
 \text{CR} \\
 011
 \end{array}
 \begin{array}{c}
 \text{Mx} \\
 0
 \end{array}
 \longrightarrow
 \begin{array}{c}
 \text{PD} \\
 110
 \end{array}
 \begin{array}{c}
 \text{MD} \\
 010 \\
 \text{MR} \\
 011 \\
 \text{CR} \\
 011
 \end{array}
 \begin{array}{c}
 \text{Mx} \\
 0
 \end{array}
 \longrightarrow
 \begin{array}{c}
 \text{PD} \\
 111
 \end{array}
 \begin{array}{c}
 \text{MD} \\
 010 \\
 \text{MR} \\
 001 \\
 \text{CR} \\
 010
 \end{array}
 \begin{array}{c}
 \text{Mx} \\
 1
 \end{array}
 \longrightarrow$$

$$\begin{array}{c}
 \text{PD} \\
 111
 \end{array}
 \begin{array}{c}
 \text{MD} \\
 010 \\
 \text{MR} \\
 100 \\
 \text{CR} \\
 001
 \end{array}
 \begin{array}{c}
 \text{Mx} \\
 1
 \end{array}
 \longrightarrow
 \begin{array}{c}
 \text{PD} \\
 001
 \end{array}
 \begin{array}{c}
 \text{MD} \\
 010 \\
 \text{MR} \\
 100 \\
 \text{CR} \\
 001
 \end{array}
 \begin{array}{c}
 \text{Mx} \\
 1
 \end{array}
 \longrightarrow
 \begin{array}{c}
 \text{PD} \\
 000
 \end{array}
 \begin{array}{c}
 \text{MD} \\
 010 \\
 \text{MR} \\
 110 \\
 \text{CR} \\
 000
 \end{array}
 \begin{array}{c}
 \text{Mx} \\
 0
 \end{array}
 \longrightarrow$$

$$\longrightarrow 000110$$

•  $(-4) \times (-8)$ :  $4 \rightarrow 00100 \xrightarrow{2's} 11100$  MD  
 $8 \rightarrow 01000 \xrightarrow{2's} 11000$  MR

$$\begin{array}{c}
 \text{PD} \\
 00000
 \end{array}
 \begin{array}{c}
 \text{MD} \\
 11100 \\
 \text{MR} \\
 11000 \\
 \text{CR} \\
 00101
 \end{array}
 \begin{array}{c}
 \text{Mx} \\
 0
 \end{array}
 \longrightarrow
 \begin{array}{c}
 \text{PD} \\
 00000
 \end{array}
 \begin{array}{c}
 \text{MD} \\
 11100 \\
 \text{MR} \\
 01100 \\
 \text{CR} \\
 00100
 \end{array}
 \begin{array}{c}
 \text{Mx} \\
 0
 \end{array}
 \longrightarrow
 \begin{array}{c}
 \text{PD} \\
 00000
 \end{array}
 \begin{array}{c}
 \text{MD} \\
 11100 \\
 \text{MR} \\
 00110 \\
 \text{CR} \\
 00011
 \end{array}
 \begin{array}{c}
 \text{Mx} \\
 0
 \end{array}
 \longrightarrow$$

$$\begin{array}{c}
 \text{PD} \\
 00000
 \end{array}
 \begin{array}{c}
 \text{MD} \\
 11100 \\
 \text{MR} \\
 00011 \\
 \text{CR} \\
 00010
 \end{array}
 \begin{array}{c}
 \text{Mx} \\
 0
 \end{array}
 \longrightarrow
 \begin{array}{c}
 \text{PD} \\
 00100
 \end{array}
 \begin{array}{c}
 \text{MD} \\
 11100 \\
 \text{MR} \\
 00011 \\
 \text{CR} \\
 00010
 \end{array}
 \begin{array}{c}
 \text{Mx} \\
 0
 \end{array}
 \longrightarrow
 \begin{array}{c}
 \text{PD} \\
 00010
 \end{array}
 \begin{array}{c}
 \text{MD} \\
 11100 \\
 \text{MR} \\
 00001 \\
 \text{CR} \\
 00001
 \end{array}
 \begin{array}{c}
 \text{Mx} \\
 1
 \end{array}
 \longrightarrow$$

$$\begin{array}{ccccc}
 & & \text{MD} & & \\
 & & 11100 & & \\
 \text{Pd} & & \text{MR} & \text{Mx} & \rightarrow \\
 00001 & & 00000 & 1 & 0000100000 \\
 & & \text{CR} & & \\
 & & 00000 & & 
 \end{array}$$