# University of Toronto Department of Political Science

# UofT GASPS Workshop on Analysing Trade with the Structural Gravity Model

Pacha v. 2022-12-15 12:01

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# Contents

1	Disclaimer	1
2	Getting the most out of this material	1
3	Packages	1
4	Data	1
5	OLS estimates	3
6	Poisson Pseudo Maximum Likelihood	7
R	eferences	10

#### 1 Disclaimer

The views and opinions expressed in this course are solely those of the author and do not necessarily reflect the official position of any unit of the OECD, the University of Toronto or the Pontifical Catholic University of Chile.

This workshop is based on Borchert et al. (2021), Gurevich and Herman (2020) and Yotov et al. (2016) and assumes basic R knowledge.

# 2 Getting the most out of this material

You can clone the GitHub repository to obtain the editable R files:

```
git clone https://github.com/pachadotdev/uoft-gasps-gravity-2022.git
```

Please read https://happygitwithr.com/ if you have questions about git or GitHub.

# 3 Packages

Required packages for this workshop:

```
library(usitcgravity) # data
library(dplyr) # data cleaning/transformation/aggregation
library(tidyr) # nest/unnest data
library(purrr) # iteration
library(fixest) # regression
library(broom) # tidy regression results
library(duckdb) # additional SQL operations
```

usitcgravity has to be installed from GitHub. One option to install it is by running:

```
install.packages("remotes")
install_github("pachadotdev/usitcgravity")
```

## 4 Data

We are going to read directly from SQL. We can open a connection by using a function in usitcgravity.

```
con <- usitcgravity_connect()</pre>
```

Let's create a panel for the period 1986-2006 in intervals of 4 years. The required steps are:

- 1. Aggregate trade at sector level (4 sectors)
- 2. Add sector names
- 3. Add structural gravity variables

- 4. Move the data into R
- 5. Log trade and distance + create pair variable

Let's have a look at the tables:

```
dbListTables(con)
```

```
## [1] "country_names" "gravity" "industry_names" "metadata"
## [5] "region_names" "sector_names" "trade"
```

Then check the sector\_names table:

```
tbl(con, "sector_names") %>% collect()
```

In order to create four panels (one per sector), we can create vectors to filter the years and sectors, iterate over broad\_sector\_id, and proceed with the rest of the steps.

In this particular case I transform the variables at the end, because it is more flexible to transform data in R than in SQL.

By using purrr we can create a list of tibbles which shall be used to estimate four models (i.e., specific sector effects) for the price of one.

This can be done in one chunk:

```
yrs <- seq(1986L, 2006L, 4)

sctrs <- tbl(con, "sector_names") %>%
  pull(broad_sector_id)

gravity <- map(
    sctrs,
  function(s) {
    tbl(con, "trade") %>%
      filter(year %in% yrs, broad_sector_id == s) %>%
        select(year, exporter_iso3, importer_iso3, broad_sector_id, trade) %>%
        group_by(year, exporter_iso3, importer_iso3, broad_sector_id) %>%
        summarise(trade = sum(trade, na.rm = T)) %>%

    left_join(
        tbl(con, "sector_names")
    ) %>%
```

```
select(year, exporter_iso3, importer_iso3, broad_sector, trade) %>%

left_join(
   tbl(con, "gravity") %>%
    select(year,
        exporter_iso3 = iso3_o, importer_iso3 = iso3_d, distance,
        contiguity, common_language, colony_ever
   )
) %>%

collect() %>%

mutate(
   log_trade = log(trade),
   log_distance = log(distance),
   pair = paste(exporter_iso3, importer_iso3, sep = "_"),
)
}
)
dbDisconnect(con, shutdown = T)
```

#### 5 OLS estimates

Consider a simple especification of the structural gravity model of trade:

$$\log X_{ij,k,t} = \beta_0 + \beta_1 DIST_{i,j} + \beta_2 CNTG_{i,j} + \beta_3 LANG_{i,j} + \beta_4 CLNY_{i,j} + \varepsilon_{ij,t}$$
(1)

We need to remove 0 flows. If we don't do this, lm fails because log(0) = -Inf.

```
map(
    seq_along(gravity),
    function(s) {
        d <- gravity[[s]] %>%
            filter(exporter_iso3 != importer_iso3, trade > 0)

        fit <- feols(log_trade ~ log_distance + contiguity + common_language +
            colony_ever,
        data = d
        )

        return(tidy(fit))
    }
}</pre>
```

```
## [[1]]
## # A tibble: 5 x 5
```

```
##
                    estimate std.error statistic
                                                 p.value
    term
##
    <chr>
                      <dbl>
                                <dbl>
                                         <dbl>
                                                   <dbl>
## 1 (Intercept)
                                          13.5 1.97e- 41
                      1.78
                               0.132
## 2 log_distance
                     -0.328
                               0.0151
                                         -21.7 8.83e-104
## 3 contiguity
                      1.74
                               0.0715
                                         24.4 6.07e-131
                     -0.141
1.97
## 4 common_language
                                         -5.52 3.47e- 8
                               0.0256
## 5 colony_ever
                               0.0684
                                         28.9 3.38e-182
##
## [[2]]
## # A tibble: 5 x 5
           estimate std.error statistic p.value
##
##
    <chr>
                      <dbl>
                               <dbl>
                                         <dbl>
                                                   <dbl>
                     8.11
## 1 (Intercept)
                               0.137
                                         59.3 0
## 2 log_distance
                     -0.964 0.0155 -62.0 0
## 3 contiguity
                     2.13
                               0.0898
                                         23.7 6.89e-124
## 4 common_language -0.112
                               0.0251
                                         -4.46 8.02e- 6
                                         38.0 4.00e-314
## 5 colony_ever
                      3.33
                               0.0876
##
## [[3]]
## # A tibble: 5 x 5
##
    term
                    estimate std.error statistic p.value
##
    <chr>
                     <dbl> <dbl> <dbl>
                                                <dbl>
                               0.221
## 1 (Intercept)
                      0.982
                                          4.43 9.31e- 6
## 2 log_distance
                                        -11.9 1.88e-32
                     -0.306
                               0.0258
## 3 contiguity
                     2.18
                               0.109
                                         20.1 5.21e-89
## 4 common_language
                     -0.174
                               0.0470
                                          -3.71 2.11e- 4
## 5 colony_ever
                    1.13
                               0.108
                                         10.4 1.80e-25
##
## [[4]]
## # A tibble: 5 x 5
##
    term
                    estimate std.error statistic p.value
##
    <chr>
                      <dbl>
                                <dbl>
                                         <dbl>
                                                  <dbl>
## 1 (Intercept)
                      6.95
                               0.378
                                          18.4 1.81e-73
## 2 log_distance
                     -0.527
                               0.0451
                                         -11.7 3.37e-31
## 3 contiguity
                      0.827
                               0.222
                                          3.72 1.98e- 4
                                         12.8 7.16e-37
## 4 common_language
                      1.30
                               0.102
## 5 colony_ever
                      2.19
                               0.250
                                          8.79 1.96e-18
```

It is good practice to compute clustered standard errors, so we use the "pair" variable previously created.

```
map(
  seq_along(gravity),
  function(s) {
    d <- gravity[[s]] %>%
       filter(exporter_iso3 != importer_iso3, trade > 0)

    fit <- feols(log_trade ~ log_distance + contiguity + common_language +</pre>
```

```
colony_ever,
   data = d,
   cluster = "pair
   )
   return(tidy(fit))
  }
)
## [[1]]
## # A tibble: 5 x 5
##
     term
                  estimate std.error statistic p.value
##
     <chr>
                        <dbl>
                                  <dbl>
                                            <dbl>
                                                     <dbl>
## 1 (Intercept)
                       1.78
                                 0.250
                                             7.13 1.07e-12
## 2 log_distance
                      -0.328
                                 0.0285
                                           -11.5 1.85e-30
## 3 contiguity
                       1.74
                                           13.4 7.31e-41
                                 0.130
## 4 common_language
                      -0.141
                                 0.0477
                                            -2.96 3.10e- 3
## 5 colony_ever
                        1.97
                                 0.128
                                            15.5 1.45e-53
##
## [[2]]
## # A tibble: 5 x 5
##
    term
                     estimate std.error statistic
                                                    p.value
##
     <chr>
                       <dbl>
                                  <dbl>
                                            <dbl>
                                                      <dbl>
## 1 (Intercept)
                                 0.246
                                            33.0 8.48e-236
                        8.11
## 2 log_distance
                       -0.964
                                 0.0278
                                           -34.7 5.04e-259
## 3 contiguity
                        2.13
                                 0.154
                                            13.8 1.80e- 43
## 4 common_language
                      -0.112
                                 0.0440
                                            -2.55 1.07e- 2
## 5 colony_ever
                        3.33
                                 0.144
                                            23.2 8.39e-118
##
## [[3]]
## # A tibble: 5 x 5
##
     term
                     estimate std.error statistic p.value
     <chr>
                                                     <dbl>
##
                       <dbl>
                                 <dbl>
                                            <dbl>
                                             2.72 6.46e- 3
## 1 (Intercept)
                        0.982
                                 0.360
## 2 log_distance
                                            -7.29 3.36e-13
                       -0.306
                                 0.0420
## 3 contiguity
                        2.18
                                 0.178
                                            12.2 3.20e-34
## 4 common_language
                                 0.0780
                                            -2.23 2.56e- 2
                      -0.174
## 5 colony_ever
                        1.13
                                 0.184
                                             6.16 7.66e-10
##
## [[4]]
## # A tibble: 5 x 5
##
    term
                     estimate std.error statistic p.value
     <chr>
                                                     <dbl>
##
                        <dbl>
                                 <dbl>
                                            <dbl>
## 1 (Intercept)
                        6.95
                                 0.409
                                            17.0 1.25e-62
## 2 log_distance
                       -0.527
                                 0.0499
                                           -10.6 9.88e-26
## 3 contiguity
                        0.827
                                 0.238
                                             3.47 5.22e- 4
## 4 common_language
                        1.30
                                 0.110
                                            11.9 6.70e-32
```

```
## 5 colony_ever 2.19 0.246 8.90 7.98e-19
```

It is (extremely) important to conduct a misspecification test. Some of the models pass the misspecification test.

```
map(
  seq_along(gravity),
 function(s) {
   d <- gravity[[s]] %>%
      filter(exporter_iso3 != importer_iso3, trade > 0)
   fit <- feols(log_trade ~ log_distance + contiguity + common_language +</pre>
      colony_ever,
   data = d,
   cluster = "pair
   d <- augment(fit, newdata = d) %>%
     mutate(.fitted2 = .fitted^2)
   fit_reset <- feols(log_trade ~ log_distance + contiguity + common_language +
      colony_ever + .fitted2,
   data = d,
   cluster = ~pair
   )
   return(
     tidy(fit_reset) %>%
       filter(term == ".fitted2")
   )
  }
## [[1]]
## # A tibble: 1 x 5
          estimate std.error statistic p.value
                <dbl> <dbl> <dbl> <dbl>
##
     <chr>
```

```
## 1 .fitted2 -0.0526 0.0353
                               -1.49 0.137
##
## [[2]]
## # A tibble: 1 x 5
             estimate std.error statistic p.value
##
    term
                       <dbl>
                                  <dbl>
    <chr>
             <dbl>
                                           <dbl>
## 1 .fitted2 -0.0767 0.0115
                                  -6.65 3.07e-11
##
## [[3]]
## # A tibble: 1 x 5
             estimate std.error statistic p.value
```

```
##
                 <dbl>
                           <dbl>
                                      <dbl>
                                              <dbl>
     <chr>>
## 1 .fitted2 -0.0861
                          0.0709
                                      -1.21
                                              0.225
##
## [[4]]
## # A tibble: 1 x 5
##
     term
              estimate std.error statistic p.value
                 <dbl>
##
     <chr>
                           <dbl>
                                      <dbl>
                                               <dbl>
                          0.0415
                                      -7.52 6.50e-14
## 1 .fitted2
              -0.312
```

#### 6 Poisson Pseudo Maximum Likelihood

The PPML model is written in multiplicative form and allows zero flows.

$$X_{ij,k,t} = \exp[\beta_0 + \beta_1 DIST_{i,j} + \beta_2 CNTG_{i,j} + \beta_3 LANG_{i,j} + \beta_4 CLNY_{i,j}] \times \varepsilon_{ij,t}$$
 (2)

We evaluate the model as we did before, the code changes are minimal.

```
map(
    seq_along(gravity),
    function(s) {
        d <- gravity[[s]] %>%
            filter(exporter_iso3 != importer_iso3)

        fit <- fepois(trade ~ log_distance + contiguity + common_language +
            colony_ever,
        data = d,
        cluster = ~pair
        )

        return(tidy(fit))
    }
)</pre>
```

```
## [[1]]
## # A tibble: 5 x 5
##
    term
                    estimate std.error statistic p.value
##
     <chr>
                       <dbl>
                                 <dbl>
                                           <dbl>
                                                    <dbl>
## 1 (Intercept)
                       3.60
                                0.806
                                           4.47 7.65e- 6
## 2 log_distance
                                0.0928
                                          -2.14 3.23e- 2
                      -0.199
## 3 contiguity
                      1.98
                                0.317
                                           6.25 4.03e-10
## 4 common_language -0.126
                                0.138
                                          -0.915 3.60e- 1
## 5 colony_ever
                     1.08
                                0.210
                                           5.13 2.93e- 7
##
## [[2]]
## # A tibble: 5 x 5
##
    term
                    estimate std.error statistic p.value
##
    <chr>
                       <dbl>
                                 <dbl>
                                           <dbl>
                                                    <dbl>
```

```
8.98
                             0.834
                                       10.8 5.14e-27
## 1 (Intercept)
## 2 log_distance
                    -0.493
                             0.0962
                                       -5.12 2.98e- 7
## 3 contiguity
                    2.08
                                       5.69 1.26e- 8
                             0.365
                                       -2.88 4.00e- 3
## 4 common_language -0.417
                             0.145
                                       4.68 2.88e- 6
## 5 colony_ever
                    1.29
                             0.277
##
## [[3]]
## # A tibble: 5 x 5
##
                estimate std.error statistic
   term
                                             p.value
                   <dbl>
##
    <chr>
                            <dbl>
                                      <dbl>
                                               <dbl>
## 1 (Intercept)
                   3.78
                            0.980
                                      3.86 0.000115
## 2 log_distance
                   -0.0574 0.112
                                     -0.511 0.610
## 3 contiguity
                   1.83
                            0.466 3.92 0.0000889
                           0.172
## 4 common_language -0.288
                                     -1.67 0.0940
## 5 colony_ever 1.05
                            0.294
                                     3.59 0.000337
##
## [[4]]
## # A tibble: 5 x 5
##
            estimate std.error statistic p.value
    term
##
    <chr>
                   <dbl> <dbl> <dbl>
                                               <dbl>
                   7.92
## 1 (Intercept)
                             0.599
                                     13.2
                                            6.37e-40
## 2 log_distance
                  -0.226
                            0.0749 -3.02 2.50e- 3
                                      3.64 2.73e- 4
## 3 contiguity
                  1.03
                             0.284
## 4 common_language 0.0906
                                      0.538 5.91e- 1
                             0.169
## 5 colony_ever
                  1.26
                             0.332
                                       3.80 1.45e- 4
```

Now we explore the RESET test as before. The RESET test fails for some models.

```
map(
  seq_along(gravity),
 function(s) {
    d <- gravity[[s]] %>%
      filter(exporter_iso3 != importer_iso3)
    fit <- feols(trade ~ log_distance + contiguity + common_language +</pre>
      colony_ever,
    data = d,
    cluster = ~pair
    )
    d <- augment(fit, newdata = d, type.predict = "link") %>%
      mutate(.fitted2 = .fitted^2)
    fit_reset <- feols(trade ~ log_distance + contiguity + common_language +
      colony_ever + .fitted2,
    data = d,
    cluster = "pair
    )
```

```
return(
     tidy(fit_reset) %>%
       filter(term == ".fitted2")
   )
  }
)
## [[1]]
## # A tibble: 1 x 5
  term estimate std.error statistic p.value
    <chr>
              <dbl> <dbl> <dbl> <dbl>
## 1 .fitted2 -0.00701 0.00967
                              -0.725 0.469
##
## [[2]]
## # A tibble: 1 x 5
##
    term estimate std.error statistic p.value
##
  <chr>
             <dbl> <dbl> <dbl> <dbl> <
## 1 .fitted2 -0.000144 0.000516
                                 -0.280
                                         0.779
##
## [[3]]
## # A tibble: 1 x 5
##
  term estimate std.error statistic p.value
##
    <chr>
               <dbl>
                        <dbl>
                                 <dbl>
                                        <dbl>
## 1 .fitted2 0.00777 0.00726
                                 1.07
                                        0.284
##
## [[4]]
## # A tibble: 1 x 5
##
    term estimate std.error statistic p.value
##
              <dbl> <dbl> <dbl> <dbl>
    <chr>
## 1 .fitted2 -0.000453 0.000203
                                  -2.23 0.0257
```

## References

Borchert, Ingo, Mario Larch, Serge Shikher, and Yoto V. Yotov. 2021. "The International Trade and Production Database for Estimation (ITPD-E)." *International Economics* 166 (August): 140–66. https://doi.org/10.1016/j.inteco.2020.08.001.

Gurevich, Tamara, and Peter Herman. 2020. "The Dynamic Gravity Dataset: 1948-2016." 2018-2. U.S. International Trade Comission. https://www.usitc.gov/data/gravity/dgd.htm.

Yotov, Yoto V., Roberta Piermartini, José-Antonio Monteiro, and Mario Larch. 2016. An Advanced Guide to Trade Policy Analysis: The Structural Gravity Model. WTO iLibrary. https://doi.org/10.30875/abc0167e-en.