



# ember entropy metrics for biological exploration

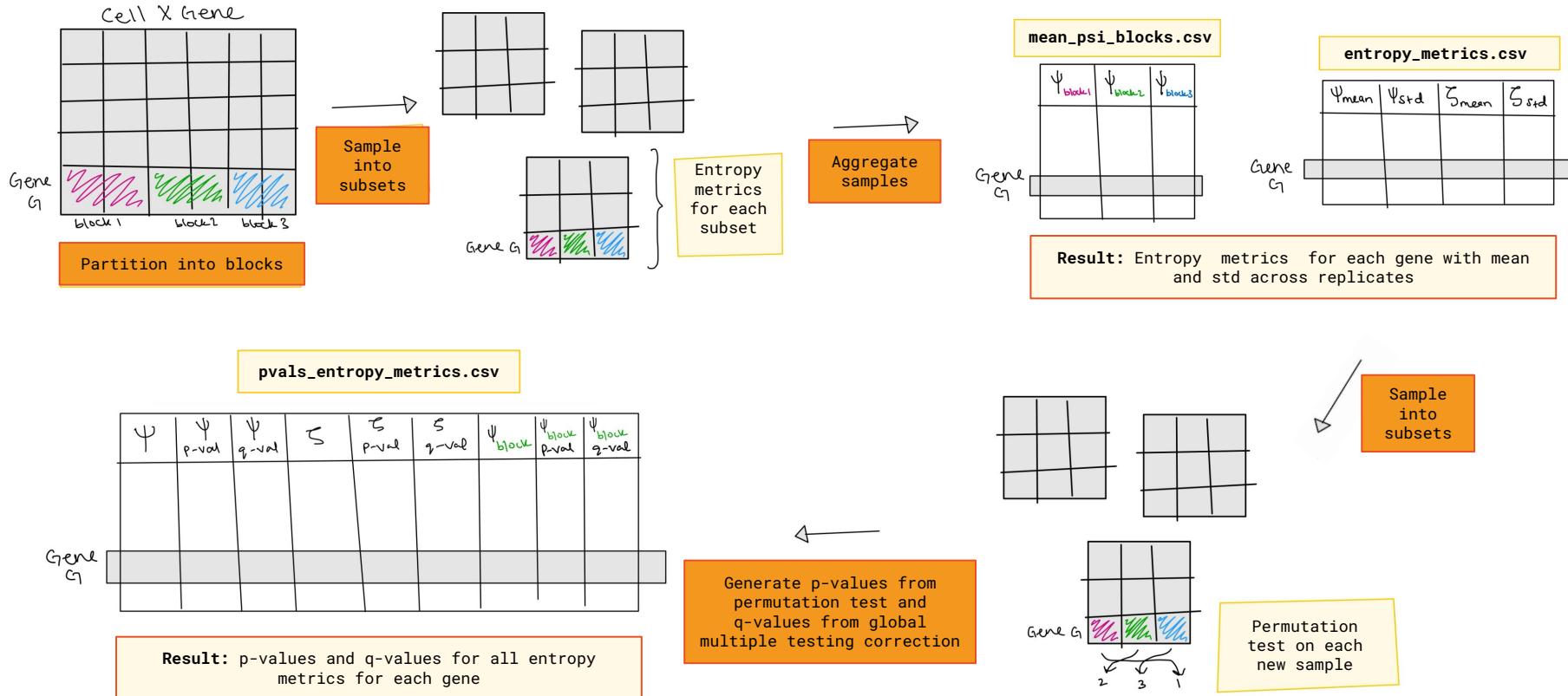
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[Download link](#)  
<https://github.com/pachterlab/ember>

# light\_ember workflow



# ember entropy metrics for biological exploration

## light\_ember

- one stop shop for generating entropy metrics and p-values

### INPUT

- **h5ad\_dir** (path to adata)
- **partition\_label** (col in adata.obs)
- **save\_dir** (path to save results)
- sampling= True
  - sample\_id\_col=None
  - category\_col=None
  - condition\_col=None
  - num\_draws=100
  - save\_draws = False
  - seed = 42
- partition\_pvals=True
- block\_pvals=False
  - block\_label=None
  - n\_pval\_iterations=1000
- n\_cpus=1 (for parallel processing of sampling)



### OUTPUT

- csv file in save\_dir with all entropy metrics
- csv file in Psi\_block\_df folder with psi block
  - Separate file for pvals
  - Separate files for each partition
  - Alternate file names depending on sampling on or off.

# ember 🌈 entropy metrics for biological exploration

## generate\_pvals

- manual access to generate pvals after initial investigation using `light_ember`

### INPUT

- `h5ad_dir` (path to adata)
- `partition_label` (col in adata.obs)
- `entropy_metrics_dir` (path to light\_ember output files)
- `save_dir` (path to save results)
- `sample_id_col`
- `category_col`
- `condition_col`
- `block_label=None`
- `seed = 42`
- `n_iterations=1000`
- `n_cpus=1`



### OUTPUT

- csv file in `save_dir` with entropy metrics and corresponding p-values and FDR q-values
  - Separate files for each partition

# ember entropy metrics for biological exploration

## highly\_specific\_to\_partition

### INPUT

- **partition\_label**
- **pvals\_dir**
- **save\_dir**
- **psi\_thresh**
- **zeta\_thresh**
- **q\_thresh**

### OUTPUT

CSV file with genes highly specific to a partition

- Ordered from most to least specific

## top\_genes

## non\_specific\_to\_partition

### INPUT

- **partition\_label**
- **pvals\_dir**
- **save\_dir**
- **psi\_thresh**
- **zeta\_thresh**
- **q\_thresh**

### OUTPUT

CSV file with non-specific **housekeeping genes** to a partition

- Ordered from most to least specific

## highly\_specific\_to\_block

### INPUT

- **partition\_label**
- **block\_label**
- **pvals\_dir**
- **save\_dir**
- **psi\_thresh**
- **zeta\_thresh**
- **q\_thresh**

### OUTPUT

CSV file with **marker genes** for a block

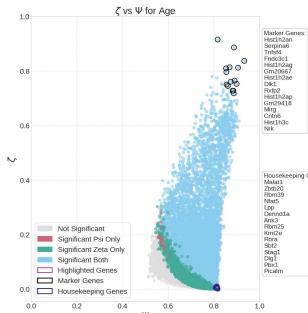
- Ordered from most to least specific

# ember entropy metrics for biological exploration

## plot\_partition\_specificity

## **INPUT**

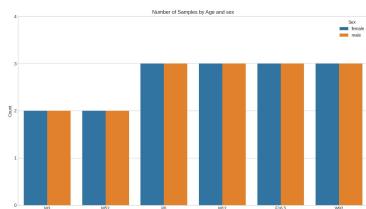
- `partition_label`
  - `pvals_dir`
  - `save_dir`
  - `highlight_genes`
  - `fontsize`
  - `color_palette`



## plot\_sample\_counts

## **INPUT**

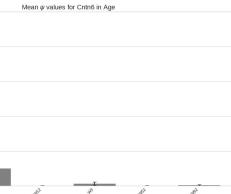
- `h5ad_dir`
  - `save_dir`
  - `sample_id_col`
  - `category_col`
  - `condition_col`
  - `fontsize`



## plot\_psi\_blocks

## **INPUT**

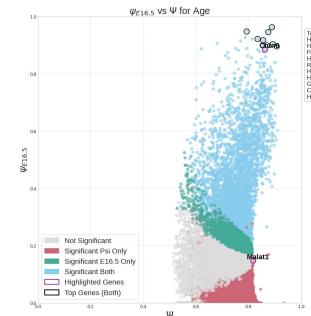
- gene\_name
  - partition\_label
  - psi\_block\_df\_dir
  - save\_dir
  - fontsize



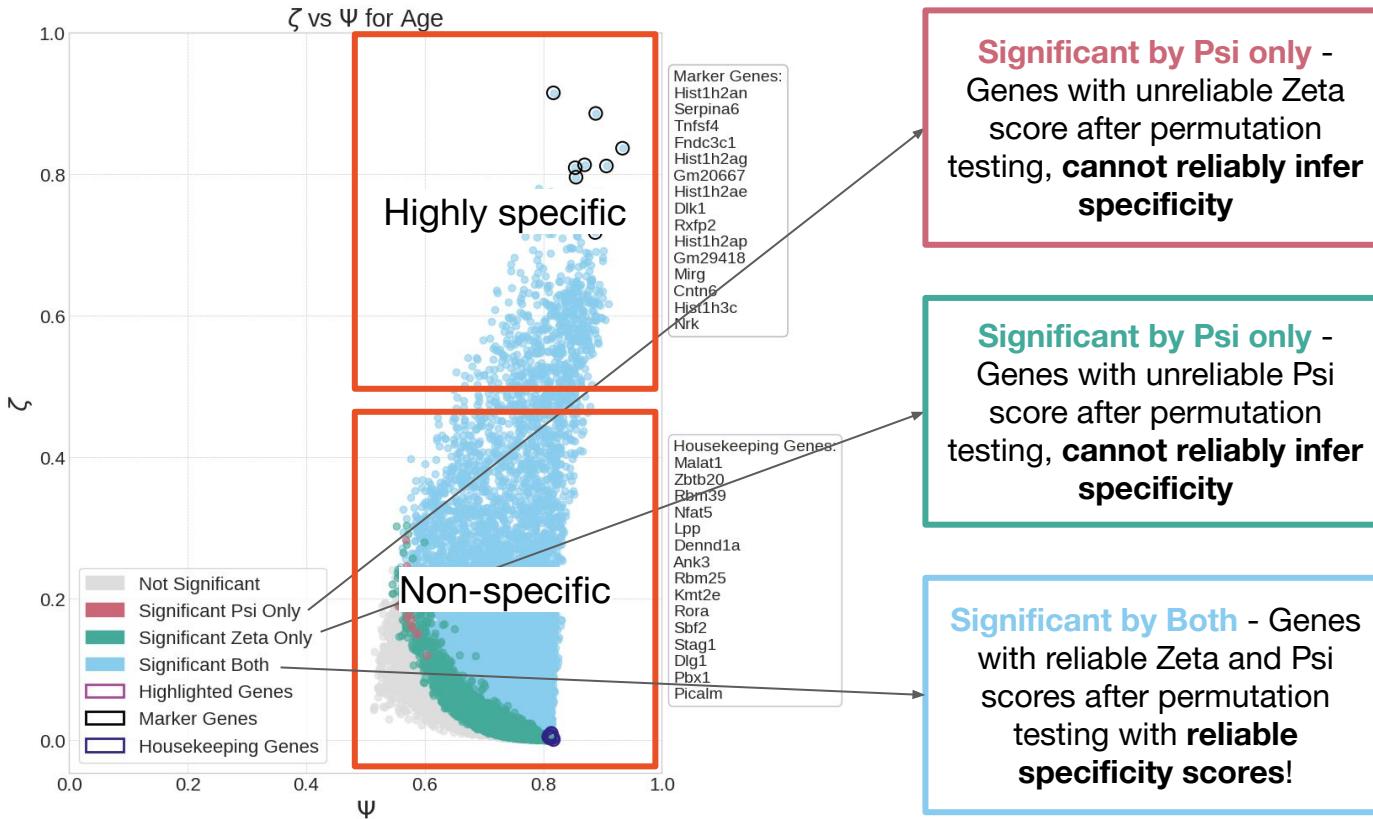
## plot\_block\_specificity

## **INPUT**

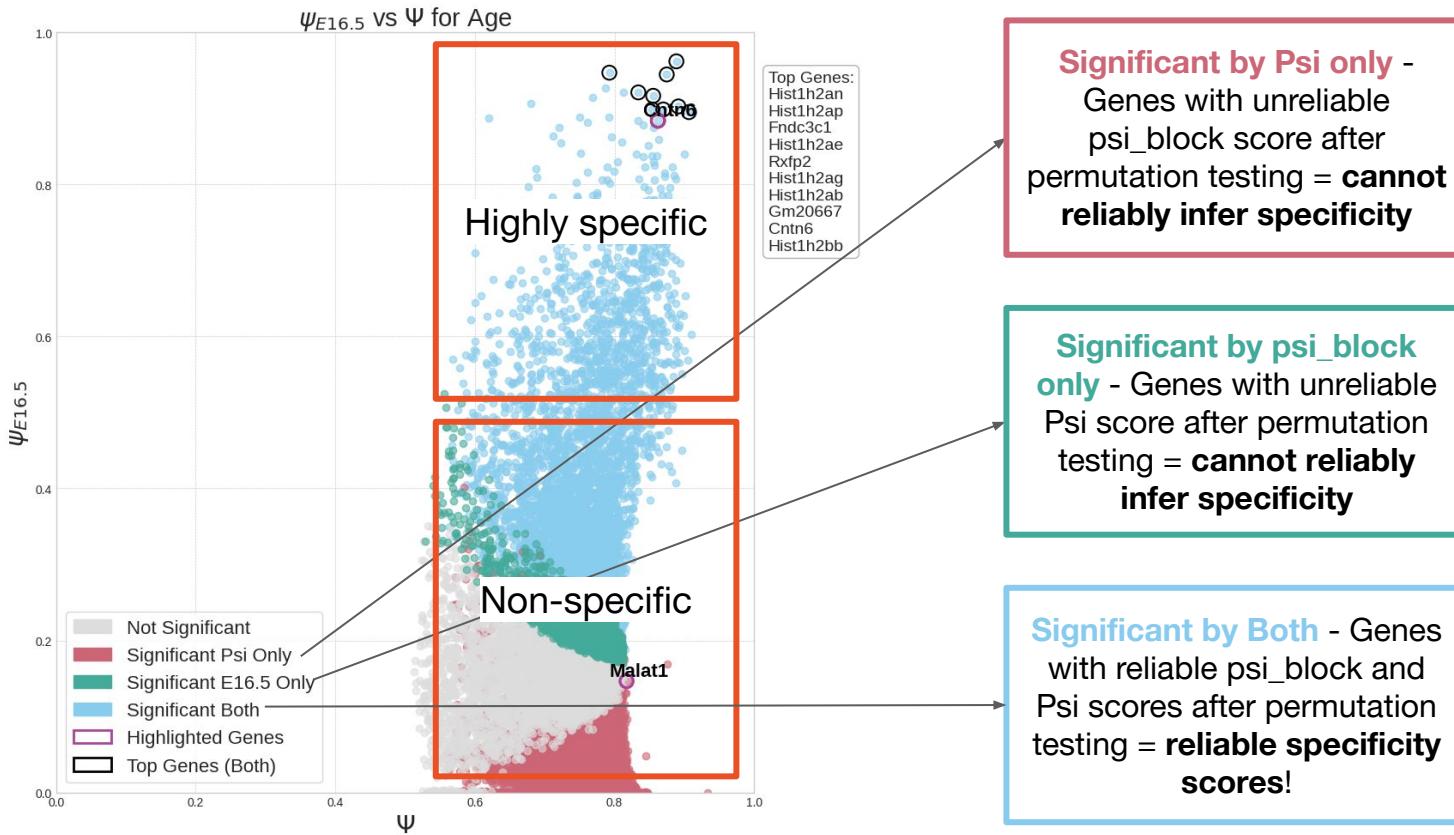
- `partition_label`
  - `block_label`
  - `pvals_dir`
  - `save_dir`
  - `highlight_genes`
  - `fontsize`
  - color palette



# How to interpret `plot_partition_specificity`



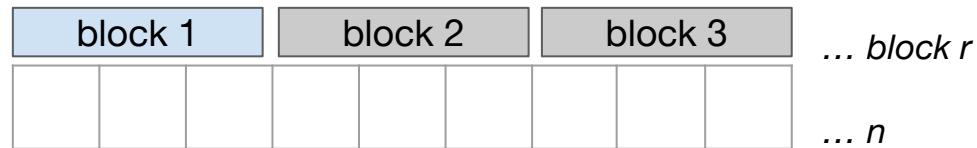
# How to interpret `plot_block_specificity`



# Defining entropy metrics for biological exploration

For a given gene in a count matrix that can be partitioned into  $r$  blocks (based on sex, strain, cell type, tissue, etc), we introduce **3 measures of specificity**:

- $\Psi$  ( $\Psi$ )
- $\Psi_{block}$  ( $\Psi_{block}$ )
- Zeta ( $\zeta$ )



$\Psi$	$\Psi_{block}$	$\zeta$
Fraction of information explained by partitioning	Specificity to a block	Specificity to a partition

# $\Psi$ - Information Fraction by Partition

The fraction of information explained by using a particular partition on gene  $g$ 's counts is given by:

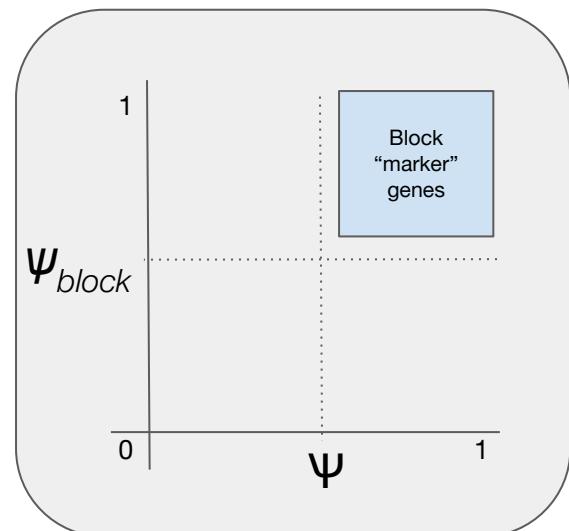
$$\Psi = \frac{E_W}{E_T} = 1 - \frac{E_B}{E_T}$$

The Specificity of Information to Block, denoted by  $\psi_{block}$ , is the contribution of each block to  $\Psi$ :

$$1 = \boxed{\Psi_1} + \boxed{\Psi_2} + \dots + \boxed{\Psi_r}$$

$\frac{p_1 E_1}{E_W}$        $\frac{p_2 E_2}{E_W}$        $\frac{p_r E_r}{E_W}$

block 1	block 2	block 3	... block $r$

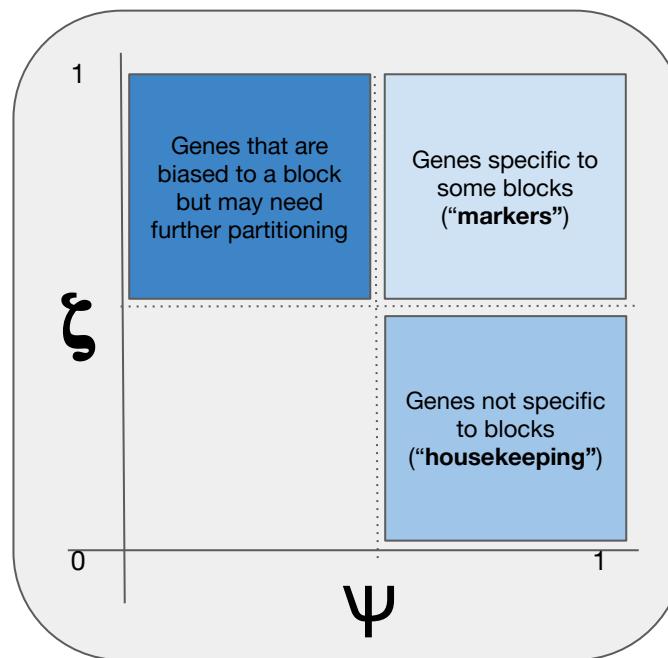


# $\zeta$ - Specificity of Information to Partition

The specificity of information to a partition ( $\zeta$ ) is given by:

$$\zeta = 1 - \frac{H(\psi_{\text{blocks}})}{\log r}$$

Comparison of the SIB distribution to the uniform distribution



# How to select category and condition

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Category - Mouse strain  
Condition - Sex

Sample	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
Mouse strain	Strain A				Strain B				Strain C				Strain D			
Sex	Male	Female		Male		Female		Male		Female		Male		Female		

## Number of unique draws

$$\begin{aligned} &= (\text{Number of replicates per category-condition group})^{\text{(Number of category-condition groups)}} \\ &= 2^8 = \mathbf{256} \end{aligned}$$

One example draw:

Sample	1	3	5	7	9	11	13	15
Mouse strain	Strain A		Strain B		Strain C		Strain D	
Sex	Male	Female	Male	Female	Male	Female	Male	Female

# How to select category and condition

Category - Cell line  
Condition - Gene perturbation

Sample	1	2	3	4	5	6	7	8	9	10	11	12
Cell line	Cell line A						Cell line B					
Gene perturbation	Wildtype	Overexpression	Knockout			Wildtype	Overexpression	Knockout				

## Number of unique draws

$$\begin{aligned} &= (\text{Number of replicates per category-condition group})^{\text{(Number of category-condition groups)}} \\ &= 2^6 = \mathbf{64} \end{aligned}$$

One example draw:

Sample	1	3	5	7	9	11
Cell line	Cell line A			Cell line B		
Gene perturbation	WT	OE	KO	WT	OE	KO

# How to select category and condition

Category - Mouse strain  
Condition - Sex

Sample	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
Mouse strain	Strain A				Strain B				Strain C				Strain D			
Sex	Male	Female			Male		Female		Male		Female		Male		Female	

**Number of unique draws**  
=  $\prod$  (Number of replicates per category-condition group)  
=  $1 \times 3 \times 2 \times 2 \times 3 \times 2 \times 2 \times 1 = 144$

One example draw:

Sample	1	2	5	7	9	12	14	16		
Mouse strain	Strain A			Strain B			Strain C		Strain D	
Sex	Male	Female	Male	Female	Male	Female	Male	Female		

Note: #1 and #16 will appear in every draw since there are no replicates for these groups