ember entropy metrics for biological exploration

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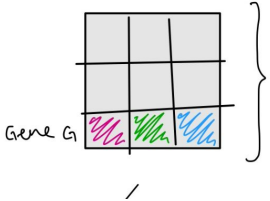
ember **e**ntropy **m**etrics for **b**iological **e**xplo**r**ation

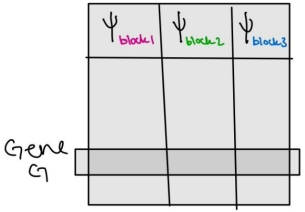
Partition into blocks

Sample into subsets

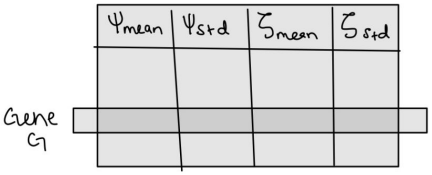


Entropy metrics for each subset

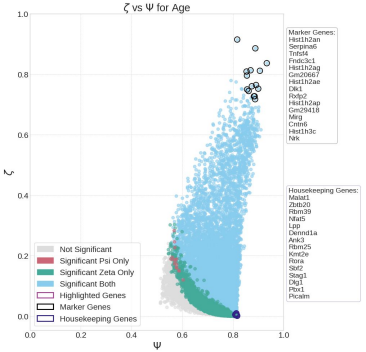
mean_psi_blocks.csv



entropy_metrics.csv



Result: Entropy metrics for each gene with mean and std across replicates + visualize as plots!



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`light_ember` - one stop shop for generating entropy metrics and p-values

INPUT

- **h5ad_dir** (path to adata)
- **partition_label** (col in adata.obs)
- **save_dir** (path to save results)
- sampling= True
  - sample_id_col=None
  - category_col=None
  - condition_col=None
  - num_draws=100
  - save_draws = False
  - seed = 42
- partition_pvals=True
- block_pvals=False
  - block_label=None
  - n_pval_iterations=1000
- n_cpus=1 (for parallel processing of sampling)

→ **`light_ember`** →

OUTPUT

- csv file in save_dir with all entropy metrics
- csv file in Psi_block_df folder with psi block
  - Separate file for pvals
  - Separate files for each partition
  - Alternate file names depending on sampling on or off.

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`generate_pvals` - manual access to generate pvals after initial investigation using **`light_ember`**

INPUT

- **h5ad_dir** (path to adata)
- **partition_label** (col in adata.obs)
- **entropy_metrics_dir** (path to light_ember output files)
- **save_dir** (path to save results)
- **sample_id_col**
- **category_col**
- **condition_col**
- block_label=None
- seed = 42
- n_iterations=1000
- n_cpus=1

→ **`generate_pvals`** →

OUTPUT

- csv file in save_dir with entropy metrics and corresponding p-values and FDR q-values
  - Separate files for each partition

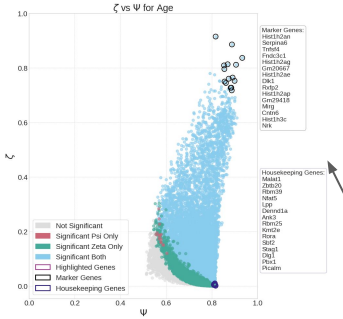
ember entropy metrics for biological exploration

plots

plot_partition_specificity

INPUT

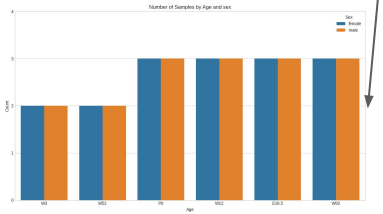
- **partition_label**
- **pvals_dir**
- **save_dir**
- highlight_genes
- fontsize
- color_palette



plot_sample_counts

INPUT

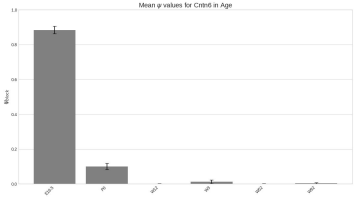
- **h5ad_dir**
- **save_dir**
- **sample_id_col**
- **category_col**
- **condition_col**
- fontsize



plot_psi_blocks

INPUT

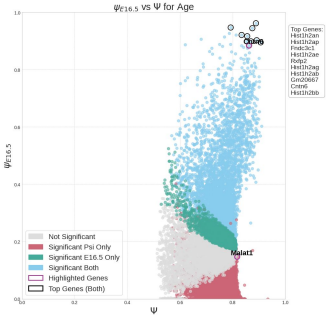
- **gene_name**
- **partition_label**
- **psi_block_df_dir**
- **save_dir**
- fontsize



plot_block_specificity

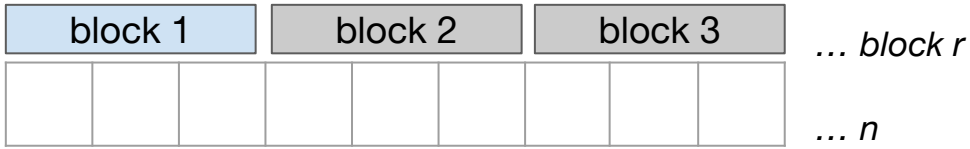
INPUT

- **partition_label**
- **block_label**
- **pvals_dir**
- **save_dir**
- highlight_genes
- fontsize
- color_palette



Defining entropy metrics for biological exploration

For a given gene in a count matrix that can be partitioned into r blocks (based on sex, strain, cell type, tissue, etc), we introduce **3 measures of specificity**:



- Psi (Ψ)
- Psi_{block} ($Ψ_{block}$)
- Zeta (ζ)

ψ	ψ_{block}	ζ
Fraction of information explained by partitioning	Specificity to a block	Specificity to a partition

6

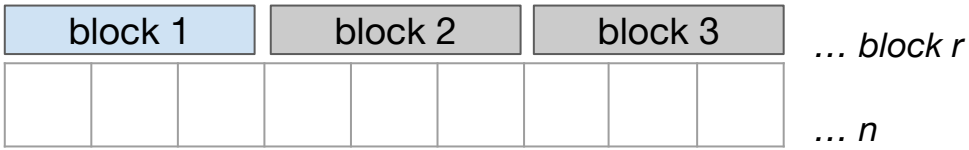
Ψ- Information Fraction by Partition

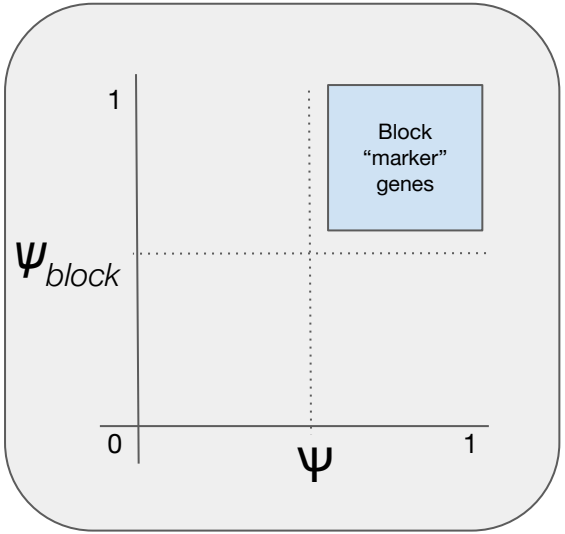
The fraction of information explained by using a particular partition on gene *g*'s counts is given by:

$$\Psi = \frac{E_W}{E_T} = 1 - \frac{E_B}{E_T}$$

The Specificity of Information to Block, denoted by ψ_{block}, is the contribution of each block to Ψ:

$$1 = \boxed{\psi_1 \ \frac{p_1 E_1}{E_W}} + \boxed{\psi_2 \ \frac{p_2 E_2}{E_W}} + \cdots + \boxed{\psi_r \ \frac{p_r E_r}{E_W}}$$



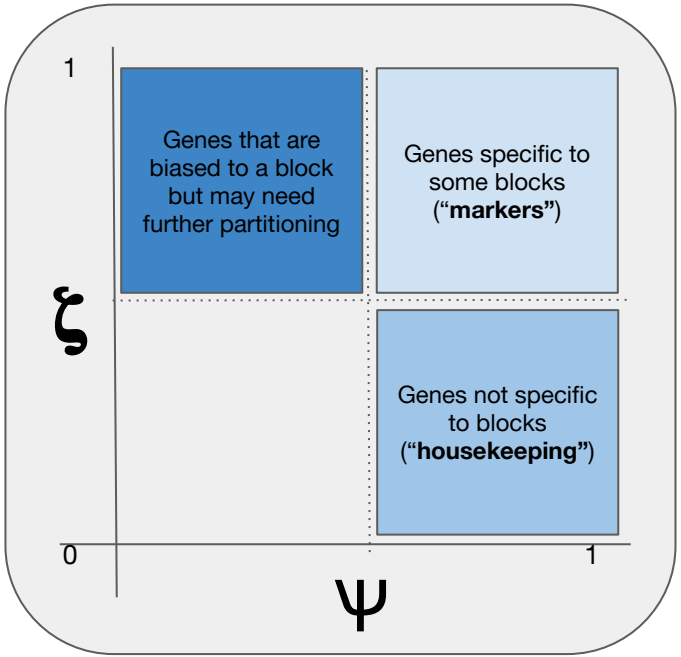


ζ - Specificity of Information to Partition

The specificity of information to a partition (ζ) is given by:

$$\zeta = 1 - \frac{H(\psi_{\text{blocks}})}{\log r}$$

Comparison of the SIB distribution to the uniform distribution



How to select category and condition

Category - Mouse strain
Condition - Sex

Sample	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
Mouse strain	Strain A				Strain B				Strain C				Strain D			
Sex	Male		Female		Male		Female		Male		Female		Male		Female	

Number of unique draws
= (Number of replicates per category-condition group)^(Number of category-condition groups)
= 2^8 = **256**

One example draw:

Sample	1	3	5	7	9	11	13	15
Mouse strain	Strain A		Strain B		Strain C		Strain D	
Sex	Male	Female	Male	Female	Male	Female	Male	Female

How to select category and condition

Category - Cell line
Condition - Gene perturbation

Sample	1	2	3	4	5	6	7	8	9	10	11	12
Cell line	Cell line A						Cell line B					
Gene perturbation	Wildtype		Overexpression		Knockout		Wildtype		Overexpression		Knockout	

Number of unique draws
= (Number of replicates per category-condition group)^(Number of category-condition groups)
= 2^6 = **64**

One example draw:

Sample	1	3	5	7	9	11
Cell line	Cell line A			Cell line B		
Gene perturbation	WT	OE	KO	WT	OE	KO

How to select category and condition

Category - Mouse strain
Condition - Sex

Sample	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
Mouse strain	Strain A				Strain B				Strain C					Strain D		
Sex	Male	Female			Male		Female		Male			Female		Male		Female

Number of unique draws
= ∏ (Number of replicates per category-condition group)
= 1*3*2*2*3*2*2*1 = **144**

One example draw:

Sample	1	2	5	7	9	12	14	16
Mouse strain	Strain A		Strain B		Strain C		Strain D	
Sex	Male	Female	Male	Female	Male	Female	Male	Female

Note: #1 and #16 will appear in every draw since there are no replicates for these groups