CFDS® – Chartered Financial Data Scientist

Introduction to Python

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29 November and 13 December 2023

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Financial Time Series

- Time series are ubiquitous in finance.
- `pandas` is the main library in Python to deal with time series.

Financial Data

Financial data

- For the time being we work with locally stored data files.
- These are in `.csv`-files (comma-separated values), where the data entries in each row are separated by commas.
- Some initialisation:

In [31]:

```
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
plt.style.use('seaborn')
plt.rcParams['font.family'] = 'serif'
```

```
/var/folders/46/b127yp714m71zfmt9j7_lhwh0000gq/T/ipykernel_5169
8/2492143664.py:4: MatplotlibDeprecationWarning: The seaborn st
yles shipped by Matplotlib are deprecated since 3.6, as they no
longer correspond to the styles shipped by seaborn. However, th
ey will remain available as 'seaborn-v0_8-<style>'. Alternative
ly, directly use the seaborn API instead.
  plt.style.use('seaborn')
```

Data import

- `pandas` provides a numer of different functions and `DataFrame` methods for importing and exporting data.
- Here we use `pd.read_csv()`.
- The file that we load contains end-of-day data for different financial instruments retrieved from Thomson Reuters.

In [32]:

```
# If using colab, then uncomment the line below and comment the line af
#filename = 'https://raw.githubusercontent.com/packham/Python_CFDS/mair
filename = './data/tr_eikon_eod_data.csv' # path and filename
f = open(filename, 'r') # this will give an error when using colab; jus
f.readlines()[:5]  # show first five lines
```

Out[32]:

```
['Date,AAPL.O,MSFT.O,INTC.O,AMZN.O,GS.N,SPY,.SPX,.VIX,EUR=,XAU
=,GDX,GLD\n',
 '2010-01-01,,,,,,,,,1.4323,1096.35,,\n',
 '2010-01-04,30.57282657,30.95,20.88,133.9,173.08,113.33,1132.9
9,20.04,1.4411,1120.0,47.71,109.8\n',
 '2010-01-05,30.625683660000004,30.96,20.87,134.69,176.14,113.6
3,1136.52,19.35,1.4368,1118.65,48.17,109.7\n',
 '2010-01-06,30.138541290000003,30.77,20.8,132.25,174.26,113.7
1,1137.14,19.16,1.4412,1138.5,49.34,111.51\n']
```

Data import

In [33]:
```
data = pd.read_csv(filename,  # import csv-data into DataFrame
                   index_col=0, # take first column as index
                   parse_dates=True)  # index values are datetime
```

In [34]:
```
data.info()  # information about the DataFrame object
```

```
<class 'pandas.core.frame.DataFrame'>
DatetimeIndex: 2216 entries, 2010-01-01 to 2018-06-29
Data columns (total 12 columns):
 #   Column  Non-Null Count  Dtype  
---  ------  --------------  -----  
 0   AAPL.O  2138 non-null   float64
 1   MSFT.O  2138 non-null   float64
 2   INTC.O  2138 non-null   float64
 3   AMZN.O  2138 non-null   float64
 4   GS.N    2138 non-null   float64
 5   SPY     2138 non-null   float64
 6   .SPX    2138 non-null   float64
 7   .VIX    2138 non-null   float64
 8   EUR=    2216 non-null   float64
 9   XAU=    2211 non-null   float64
 10  GDX     2138 non-null   float64
 11  GLD     2138 non-null   float64
dtypes: float64(12)
memory usage: 225.1 KB
```

Data import

In [35]:
```
data.head()
```

Out[35]:

Date	AAPL.O	MSFT.O	INTC.O	AMZN.O	GS.N	SPY	.SPX	.VIX	EU
2010-01-01	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN	1.43
2010-01-04	30.572827	30.950	20.88	133.90	173.08	113.33	1132.99	20.04	1.44
2010-01-05	30.625684	30.960	20.87	134.69	176.14	113.63	1136.52	19.35	1.43
2010-01-06	30.138541	30.770	20.80	132.25	174.26	113.71	1137.14	19.16	1.44
2010-01-07	30.082827	30.452	20.60	130.00	177.67	114.19	1141.69	19.06	1.43

Data import

In [36]:

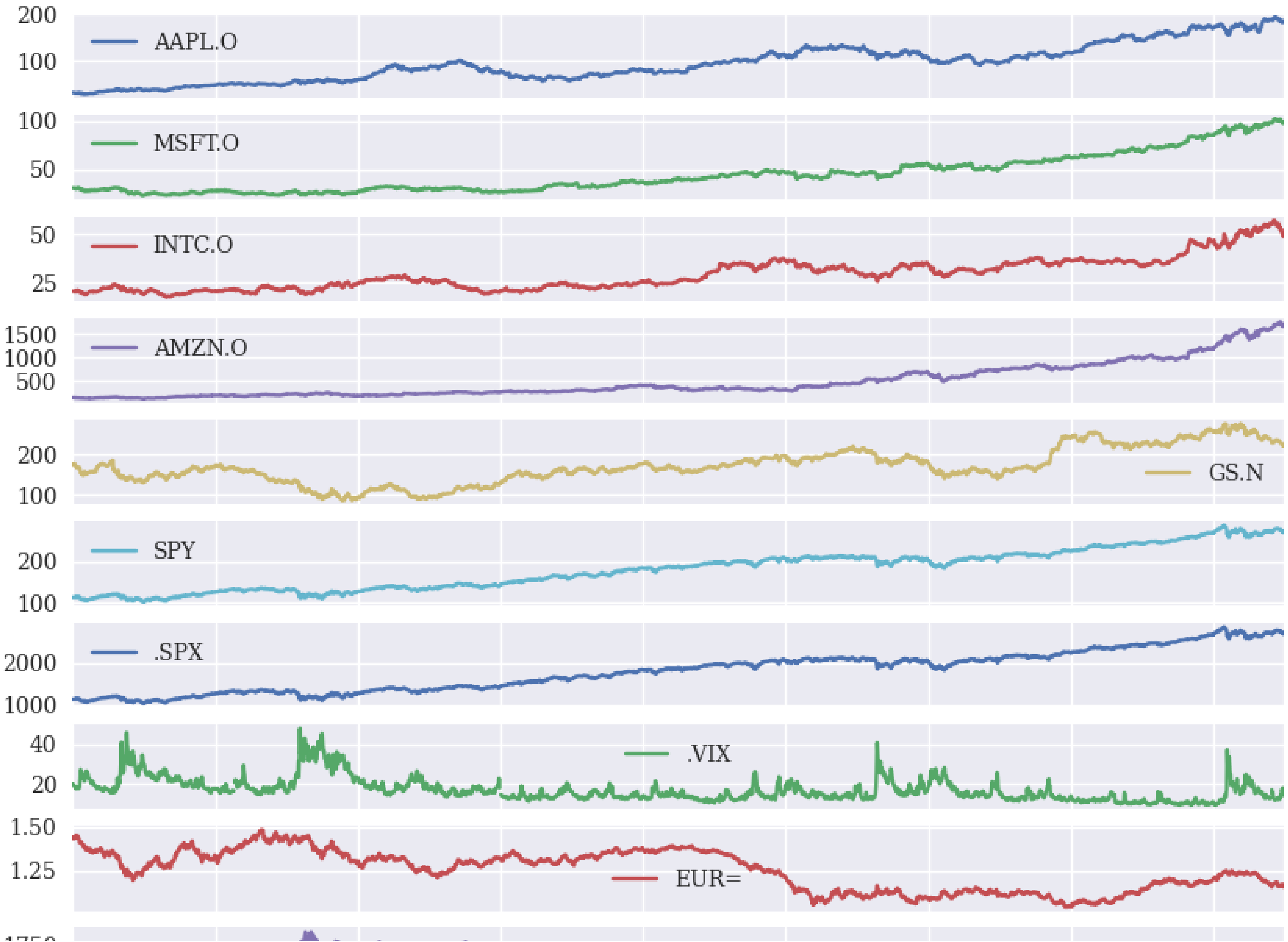
```
data.tail()
```

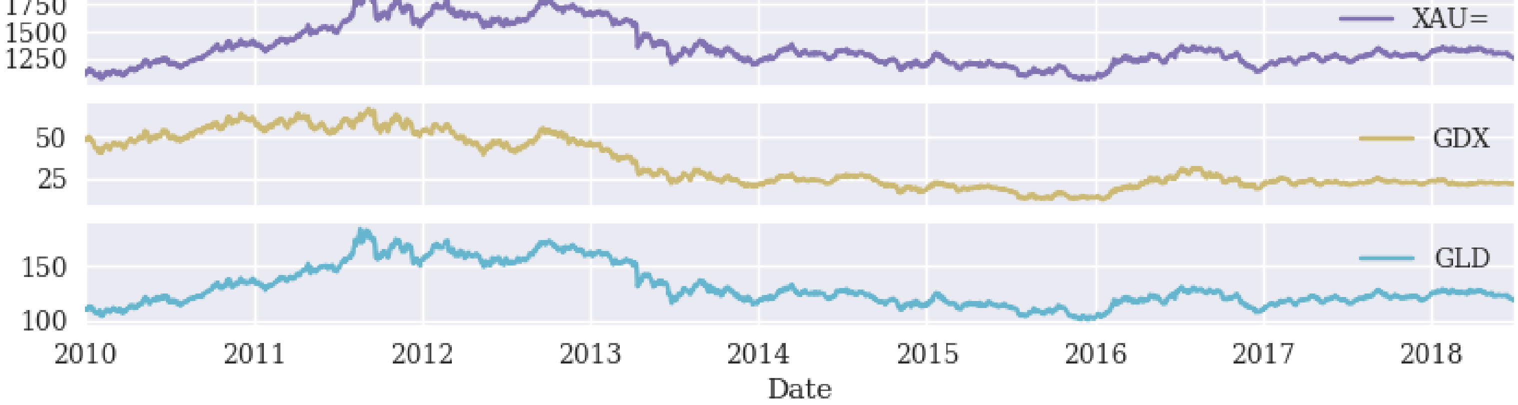
Out[36]:

Date	AAPL.O	MSFT.O	INTC.O	AMZN.O	GS.N	SPY	.SPX	.VIX	EUR=
2018-06-25	182.17	98.39	50.71	1663.15	221.54	271.00	2717.07	17.33	1.170
2018-06-26	184.43	99.08	49.67	1691.09	221.58	271.60	2723.06	15.92	1.164
2018-06-27	184.16	97.54	48.76	1660.51	220.18	269.35	2699.63	17.91	1.155
2018-06-28	185.50	98.63	49.25	1701.45	223.42	270.89	2716.31	16.85	1.156
2018-06-29	185.11	98.61	49.71	1699.80	220.57	271.28	2718.37	16.09	1.168

Data import

In [37]:
```
data.plot(figsize=(10, 10), subplots=True);
```





1750
1500
1250
XAU=
50
25
GDX
150
100
GLD
2010
2011
2012
2013
2014
2015
2016
2017
2018
Date

Data import

- The identifiers used by Thomson Reuters are so-called RIC's.
- The financial instruments in the data set are:

In [38]:

```
instruments = ['Apple Stock', 'Microsoft Stock',
               'Intel Stock', 'Amazon Stock', 'Goldman Sachs Stock',
               'SPDR S&P 500 ETF Trust', 'S&P 500 Index',
               'VIX Volatility Index', 'EUR/USD Exchange Rate',
               'Gold Price', 'VanEck Vectors Gold Miners ETF',
               'SPDR Gold Trust']
```

Data import

In [39]:
```
for ric, name in zip(data.columns, instruments):
    print('{:8s} | {}'.format(ric, name))
```

```
AAPL.O    | Apple Stock
MSFT.O    | Microsoft Stock
INTC.O    | Intel Stock
AMZN.O    | Amazon Stock
GS.N      | Goldman Sachs Stock
SPY       | SPDR S&P 500 ETF Trust
.SPX      | S&P 500 Index
.VIX      | VIX Volatility Index
EUR=      | EUR/USD Exchange Rate
XAU=      | Gold Price
GDX       | VanEck Vectors Gold Miners ETF
GLD       | SPDR Gold Trust
```

Summary statistics

In [40]:

```python
data.describe().round(2)
```

Out[40]:

	AAPL.O	MSFT.O	INTC.O	AMZN.O	GS.N	SPY	.SPX	.VIX
count	2138.00	2138.00	2138.00	2138.00	2138.00	2138.00	2138.00	2138.00
mean	93.46	44.56	29.36	480.46	170.22	180.32	1802.71	17.03
std	40.55	19.53	8.17	372.31	42.48	48.19	483.34	5.88
min	27.44	23.01	17.66	108.61	87.70	102.20	1022.58	9.14
25%	60.29	28.57	22.51	213.60	146.61	133.99	1338.57	13.07
50%	90.55	39.66	27.33	322.06	164.43	186.32	1863.08	15.58
75%	117.24	54.37	34.71	698.85	192.13	210.99	2108.94	19.07
max	193.98	102.49	57.08	1750.08	273.38	286.58	2872.87	48.00

Summary statistics

- The `aggregate()` -function allows to customise the statistics viewed:

In [41]:

```
data.aggregate([min,
                np.mean,
                np.std,
                np.median,
                max]
).round(2)
```

Out[41]:

	AAPL.O	MSFT.O	INTC.O	AMZN.O	GS.N	SPY	.SPX	.VIX	EUR
min	27.44	23.01	17.66	108.61	87.70	102.20	1022.58	9.14	1.0
mean	93.46	44.56	29.36	480.46	170.22	180.32	1802.71	17.03	1.2
std	40.55	19.53	8.17	372.31	42.48	48.19	483.34	5.88	0.
median	90.55	39.66	27.33	322.06	164.43	186.32	1863.08	15.58	1.2
max	193.98	102.49	57.08	1750.08	273.38	286.58	2872.87	48.00	1.4

Returns

- When working with financial data we typically (=always - you must have good reasons to deviate from this) work with performance data, i.e., **returns**.
- Reasoning:
    - Historical data are mainly used to make forecasts one or several time periods forward.
    - The daily average stock price over the last eight years is meaningless to make a forecast for tomorrow's stock price.
    - However, the daily returns are possible scenarios for the next time period(s).
- The function `pct_change()` calculates discrete returns:

$$r_t^{\mathrm{d}} = \frac{S_t - S_{t-1}}{S_{t-1}},$$

  where S_t denotes the stock price at time t.

Returns

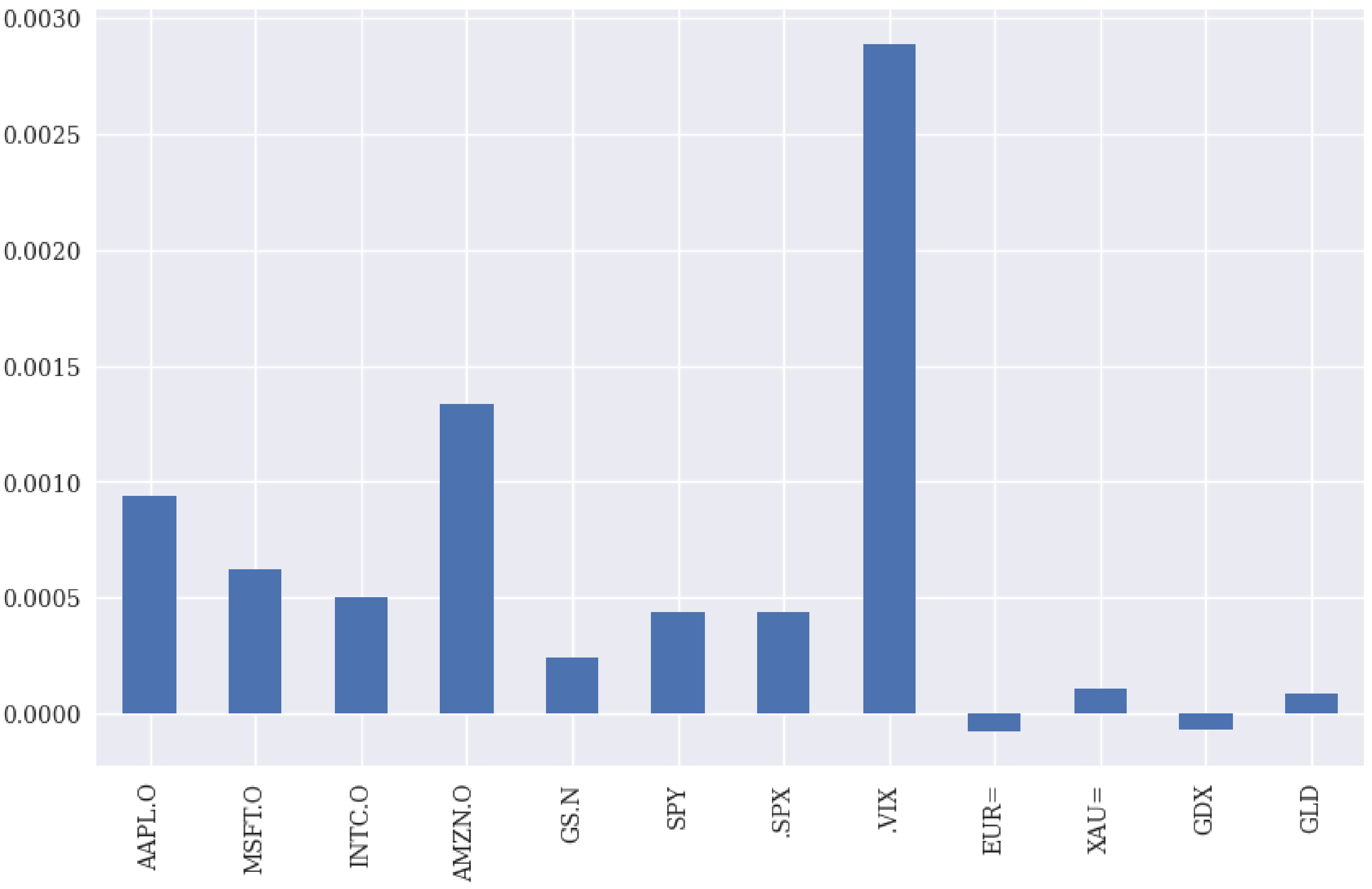
In [42]:
```
data.pct_change().round(3).head()
```

Out[42]:

Date	AAPL.O	MSFT.O	INTC.O	AMZN.O	GS.N	SPY	.SPX	.VIX	EUR=
2010-01-01	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN
2010-01-04	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN	0.006
2010-01-05	0.002	0.000	-0.000	0.006	0.018	0.003	0.003	-0.034	-0.003
2010-01-06	-0.016	-0.006	-0.003	-0.018	-0.011	0.001	0.001	-0.010	0.003
2010-01-07	-0.002	-0.010	-0.010	-0.017	0.020	0.004	0.004	-0.005	-0.007

Returns

In [43]:
```
data.pct_change().mean().plot(kind='bar', figsize=(10, 6));
```



Returns

- In finance, **log-returns**, also called **continuous returns**, are often preferred over discrete returns: $r_t^{\mathrm{c}} = \ln\left(\frac{S_t}{S_{t-1}}\right)$.
- The main reason is that log-return are additive over time.
- For example, the log-return from $t-1$ to $t+1$ is the sum of the single-period log-returns:

$$r_{t-1,t+1}^{\mathrm{c}} = \ln\left(\frac{S_{t+1}}{S_t}\right) + \ln\left(\frac{S_t}{S_{t-1}}\right) = \ln\left(\frac{S_{t+1}}{S_t} \cdot \frac{S_t}{S_{t-1}}\right) = \ln\left(\frac{S_{t+1}}{S_{t-1}}\right).$$

- Note: If the sampling (time) interval is small (e.g. one day or one week), then the difference between discrete returns and log-returns is negligible.

Returns

In [44]:
```
rets = np.log(data / data.shift(1))  # calculates log-returns in a vect
```

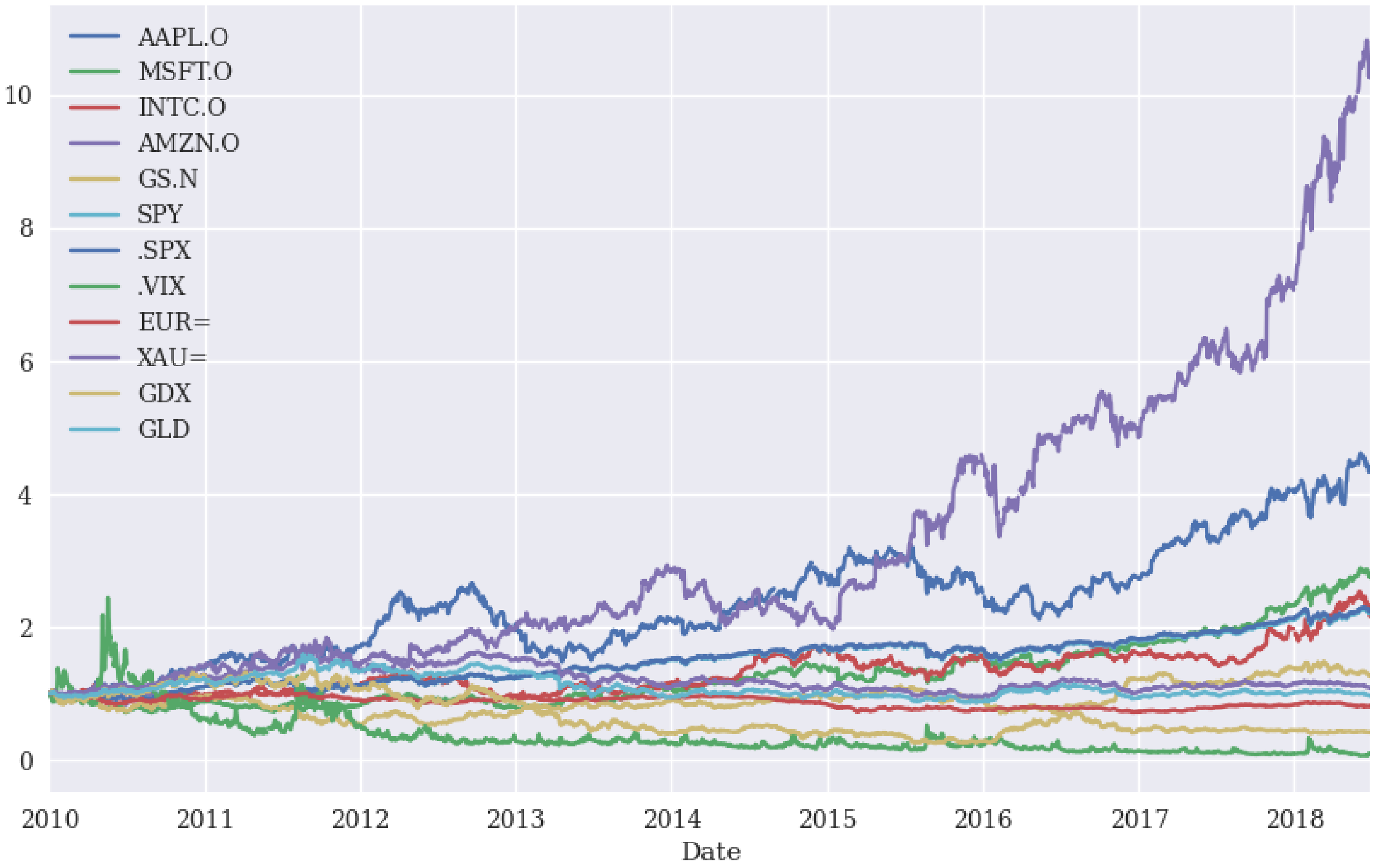
In [45]:
```
rets.head().round(3)
```

Out[45]:

	AAPL.O	MSFT.O	INTC.O	AMZN.O	GS.N	SPY	.SPX	.VIX	EUR=
Date									
2010-01-01	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN
2010-01-04	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN	0.006
2010-01-05	0.002	0.000	-0.000	0.006	0.018	0.003	0.003	-0.035	-0.003
2010-01-06	-0.016	-0.006	-0.003	-0.018	-0.011	0.001	0.001	-0.010	0.003
2010-01-07	-0.002	-0.010	-0.010	-0.017	0.019	0.004	0.004	-0.005	-0.007

Returns

In [46]:
```
rets.cumsum().apply(np.exp).plot(figsize=(10, 6));   # recover price pat
```



Correlation analysis and linear regression

- To further illustrate how to work with financial time series we consider the S&P 500 stock index and the VIX volatility index.
- Empirical stylised fact: As the S&P 500 rises, the VIX falls, and vice versa.
- Note: This is about **correlation** not **causation**.

Correlation analysis

In [47]:

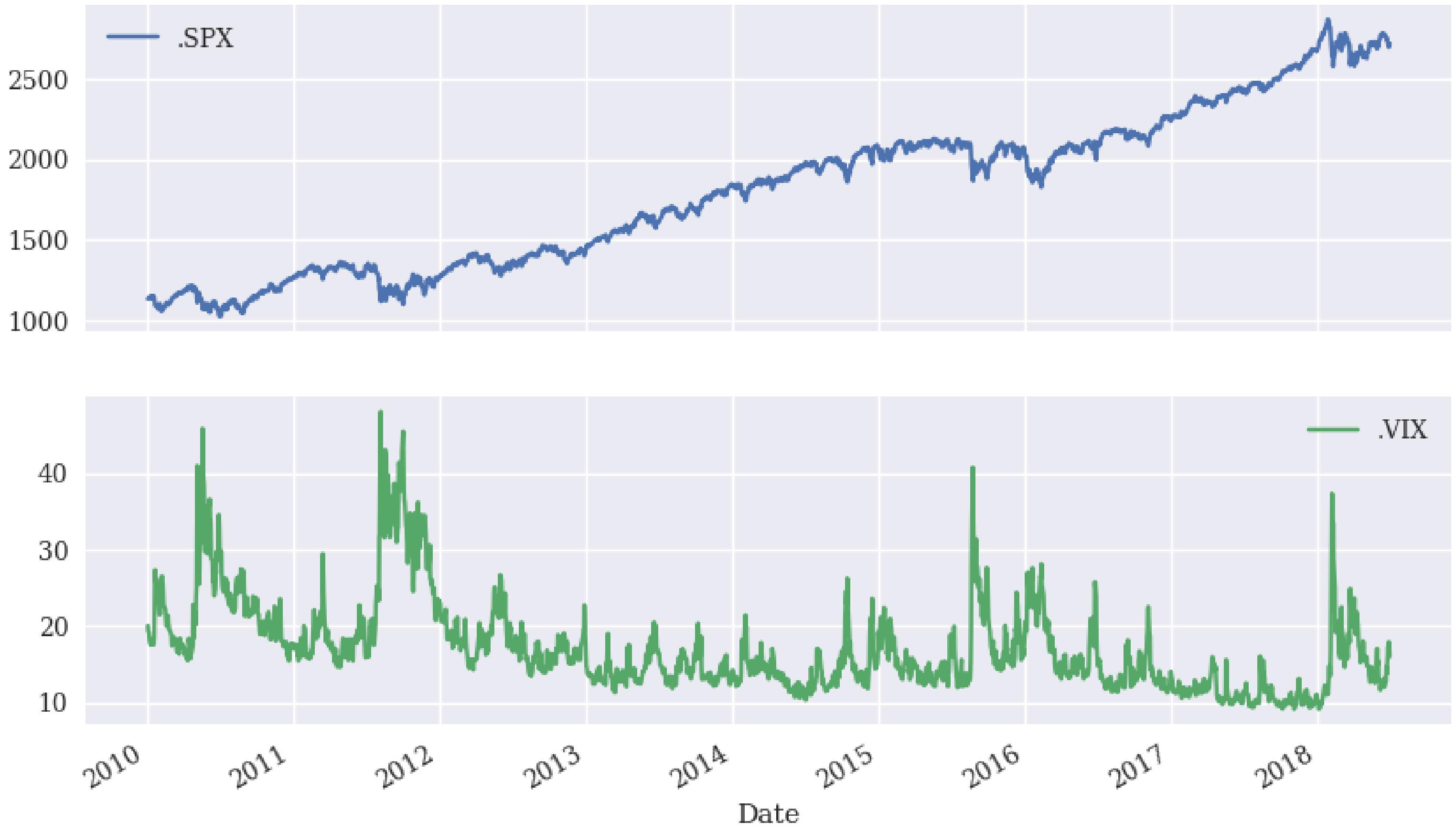
```
# EOD data from Thomson Reuters Eikon Data API

# If using colab, then uncomment the line below and comment the line af
#raw = pd.read_csv('https://raw.githubusercontent.com/packham/Python_CF
raw = pd.read_csv('./data/tr_eikon_eod_data.csv', index_col=0, parse_da
data = raw[['.SPX', '.VIX']].dropna()
data.tail()
```

Out[47]:

	.SPX	.VIX
Date		
2018-06-25	2717.07	17.33
2018-06-26	2723.06	15.92
2018-06-27	2699.63	17.91
2018-06-28	2716.31	16.85
2018-06-29	2718.37	16.09

Correlation analysis

In [48]:
```
data.plot(subplots=True, figsize=(10, 6));
```



Correlation analysis

- Transform both data series into log-returns:

In [49]:
```
rets = np.log(data / data.shift(1))
rets.head()
```

Out[49]:

	.SPX	.VIX
Date		
2010-01-04	NaN	NaN
2010-01-05	0.003111	-0.035038
2010-01-06	0.000545	-0.009868
2010-01-07	0.003993	-0.005233
2010-01-08	0.002878	-0.050024

In [50]:
```
rets.dropna(inplace=True) # drop NaN (not-a-number) entries
```

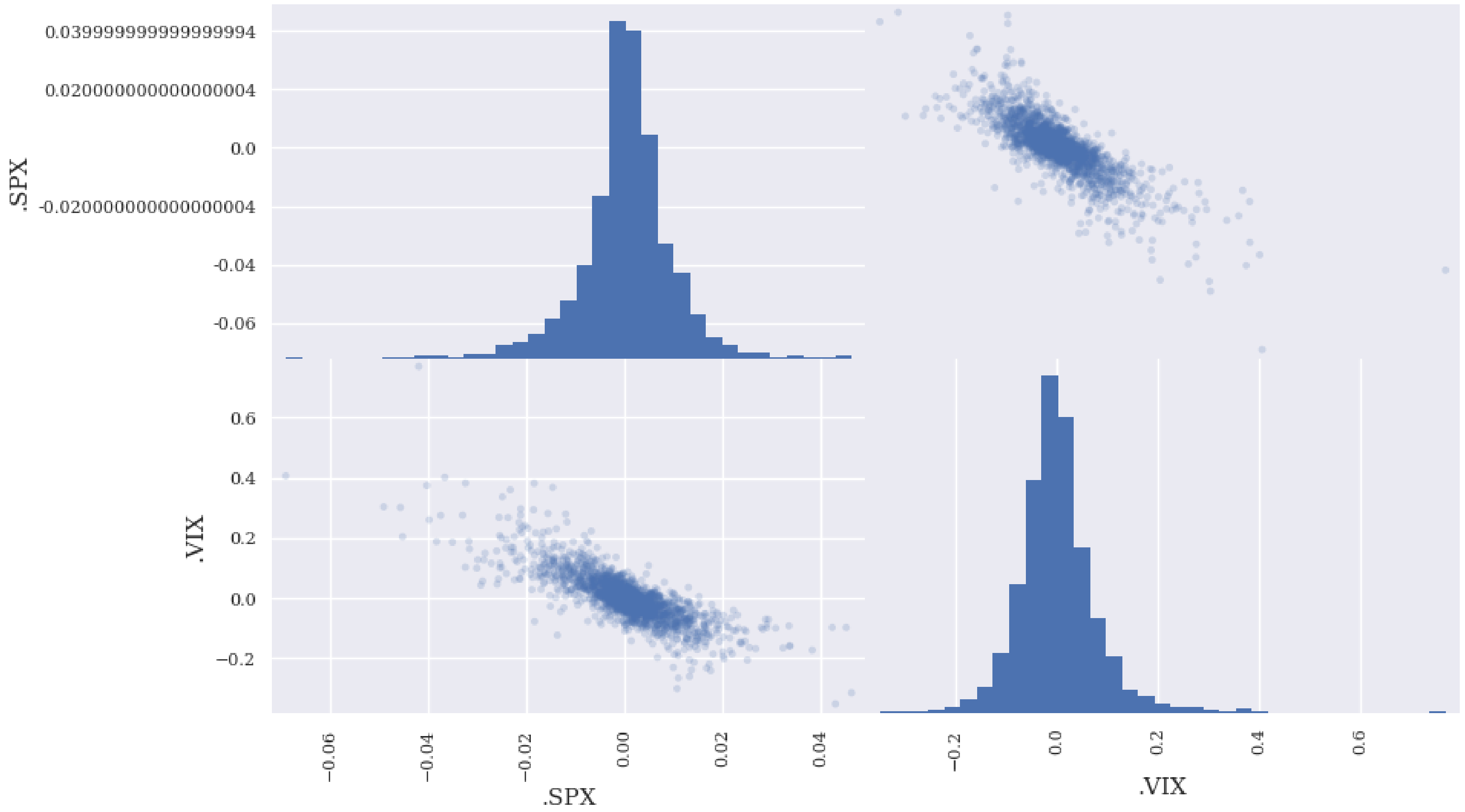
Correlation analysis

In [51]:
```
rets.plot(subplots=True, figsize=(10, 6));
```

Correlation analysis

In [52]:

```
pd.plotting.scatter_matrix(rets,
                           alpha=0.2,
                           diagonal='hist',
                           hist_kwds={'bins': 35},
                           figsize=(10, 6));
```



Correlation analysis

In [53]:
```
rets.corr()
```

Out[53]:

	.SPX	.VIX
.SPX	1.000000	-0.804382
.VIX	-0.804382	1.000000

OLS regression

- **Linear regression** captures the linear relationship between two variables.
- For two variables x, y, we postulate a linear relationship:

$$y = \alpha + \beta x + \varepsilon, \quad \alpha, \beta \in \mathbb{R}.$$

- Here, α is the **intercept**, β is the **slope (coefficient)** and ε is the **error term**.
- Given data sample of joint observations $(x_1, y_1), \ldots, (x_n, y_n)$, we set

$$y_i = \hat{\alpha} + \hat{\beta} x_i + \hat{\varepsilon}_i,$$

  where $\hat{\alpha}$ and $\hat{\beta}$ are estimates of α, β and $\hat{\varepsilon}_1, \ldots, \hat{\varepsilon}_n$ are the so-called **residuals**.
- The **ordinary least squares (OLS)** estimator $\hat{\alpha}, \hat{\beta}$ corresponds to those values of α, β that minimise the sum of squared residuals:

$$\min_{\alpha,\beta} \sum_{i=1}^{n} \varepsilon_i^2 = \sum_{i=1}^{n} (y_i - \alpha - \beta x_i)^2.$$

OLS regressions

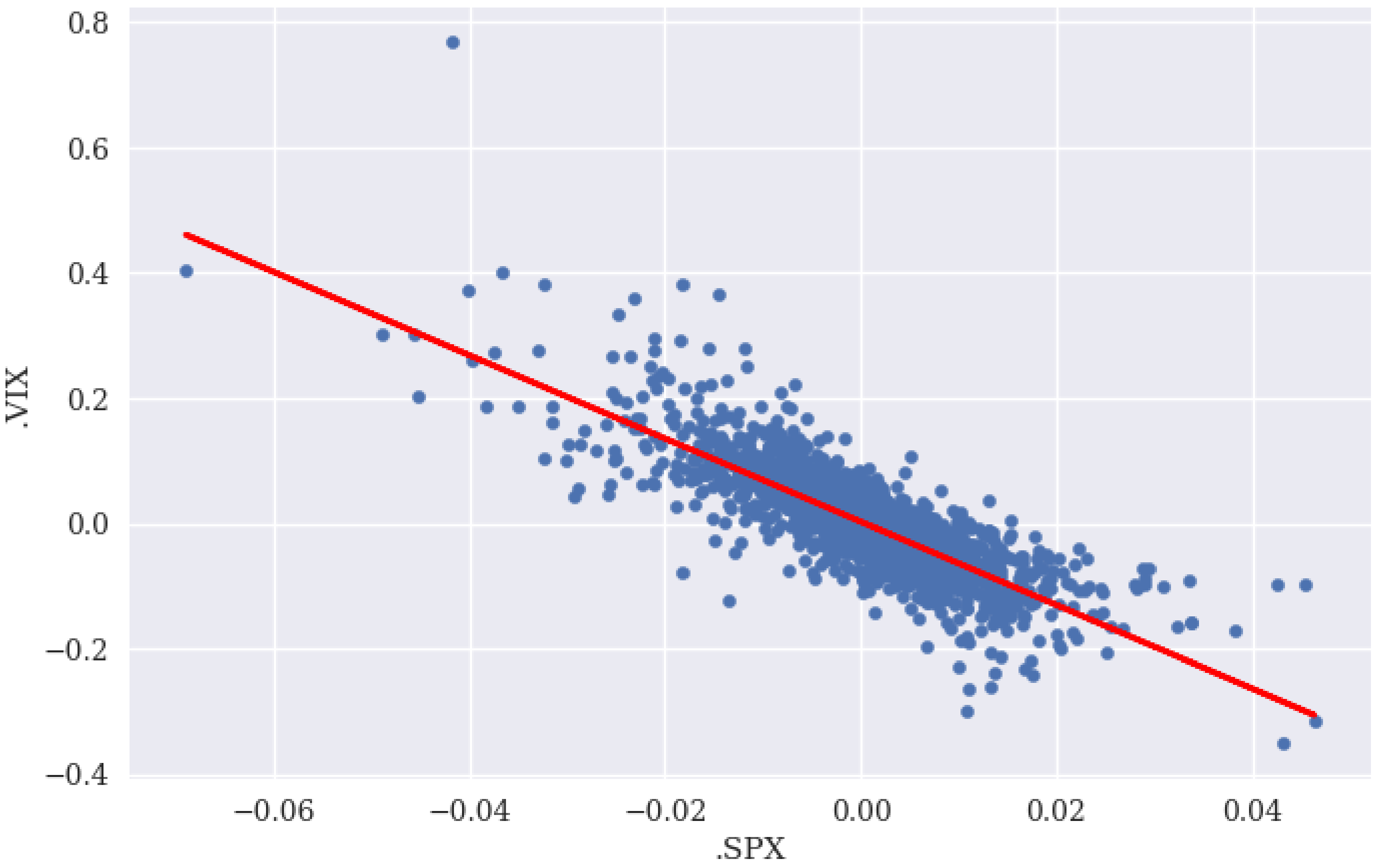
- Simplest form of OLS regression:

In [54]:
```
reg = np.polyfit(rets['.SPX'], rets['.VIX'], deg=1)  # fit a linear equ
reg.view() # the fitted paramters
```

Out[54]:
```
array([-6.65160028e+00,  2.62132142e-03])
```

2.62e-03 is scientific notation: $2.62e-03 = 2.62 \cdot 10^{-3}$.

In [55]:
```
ax = rets.plot(kind='scatter', x='.SPX', y='.VIX', figsize=(8, 5))
ax.plot(rets['.SPX'], np.polyval(reg, rets['.SPX']), 'r', lw=2);
```



0.8
0.6
0.4
0.2
0.0
−0.2
−0.4
.VIX
−0.06
−0.04
−0.02
0.00
0.02
0.04
.SPX

OLS regression

- To do a more refined OLS regression with a proper analysis, use the package `statsmodels`.

In [56]:
```
import statsmodels.api as sm

Y=rets['.VIX']
X=rets['.SPX']
X = sm.add_constant(X)
```

In [57]:
```
model = sm.OLS(Y,X)
results = model.fit()
```

In [58]:
```
results.params
```

Out[58]:
```
const     0.002621
.SPX     -6.651600
dtype: float64
```

In [59]:
```
results.predict()[0:10]
```

Out[59]:
```
array([-0.01807052, -0.0010063 , -0.0239404 , -0.01651898, -0.0
0898726,
        0.06531557, -0.05252965, -0.01349928,  0.07500527, -0.0
8000615])
```

OLS regression

In [60]:
```
print(results.summary())
```

```
                            OLS Regression Results
==============================================================================
Dep. Variable:                   .VIX   R-squared:
0.647
Model:                            OLS   Adj. R-squared:
0.647
Method:                 Least Squares   F-statistic:
3914.
Date:                Sun, 26 Nov 2023   Prob (F-statistic):
0.00
Time:                        15:04:17   Log-Likelihood:
3550.1
No. Observations:                2137   AIC:
-7096.
Df Residuals:                    2135   BIC:
-7085.
Df Model:                           1
Covariance Type:            nonrobust
==============================================================================
                 coef    std err          t      P>|t|      [0.
025      0.975]
------------------------------------------------------------------------------
const          0.0026      0.001      2.633      0.009      0.
```

```
001         0.005
.SPX            -6.6516       0.106    -62.559       0.000       -6.
860        -6.443
==============================================================================
===============
Omnibus:                       518.582   Durbin-Watson:
2.094
Prob(Omnibus):                   0.000   Jarque-Bera (JB):
6789.425
Skew:                            0.766   Prob(JB):
0.00
Kurtosis:                       11.597   Cond. No.
107.
==============================================================================
===============

Notes:
[1] Standard Errors assume that the covariance matrix of the er
rors is correctly specified.
```

OLS regression: Interpretation of output and forecasting

- The column `coef` lists the coefficients of the regression: the coefficient in the row labelled `const` corresponds to $\hat{\alpha}$ ($= 0.0026$) and the coefficient in the row `.SPX` denotes $\hat{\beta}$ ($= -6.6515$).
- The estimated model in the example is thus:

$$.\mathrm{VIX} = 0.0026 - 6.6516 .\mathrm{SPX}.$$

- The best forecast of the VIX return when observing an S&P return of 2% is therefore $0.0026 - 6.6516 \cdot 0.02 = -0.130432 = -13.0432\%$.

OLS regression: Validation (R^2)

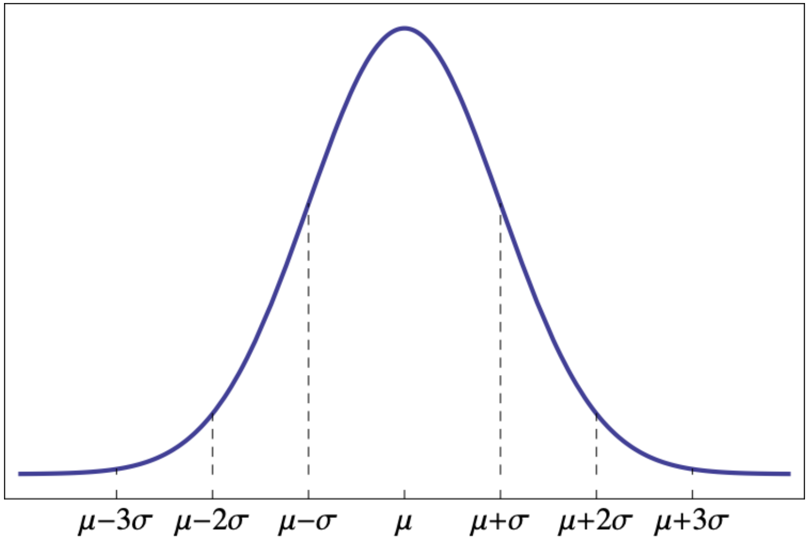
- To **validate** the model, i.e., to determine, if the model in itself and the explanatory variable(s) make sense, we look R^2 and various p-values (or confidence intervals or t-statistics).
- R^2 measures the fraction of variance in the dependent variable Y that is captured by the regression line; $1 - R^2$ is the fraction of Y-variance that remaines in the residuals ε_i^2, $i = 1, \ldots, n$.
- In the output above R^2 is given as 0.647. In other words, 64.7% of the variance in VIX returns are "explained" by SPX returns.
- A high R^2 (and this one is high) is necessary for making forecasts.

OLS regression: Validation (confidence interval)

- An important hypothesis to test in any regression model is whether the explanatory variable(s) have an effect on the independent variable.
- This can be translated into testing whether $\beta \neq 0$. ($\beta = 0$ is the same as saying that the X variable can be removed from the model.)
- Formally, we test the null hypothesis $H_0 : \beta = 0$ against the alternative hypothesis $H_1 : \beta \neq 0$.
- There are several statistics to come to the same conclusion: confidence intervals, t-statistics and p-values.
- The **confidence interval** is an interval around the estimate $\hat{\beta}$ that we are confident contains the true parameter β. A typial **confidence level** is 95%.
- If the 95% confidence interval does **not** contain 0, then we say β is **statistically significant** at the 5% (=1-95%) level, and we conclude that $\beta \neq 0$.

OLS regression: Validation (t-statistic)

- The t-statistic corresponds to the **number of standard deviations** that the estimated coefficient $\hat{\beta}$ is away from 0 (the mean under H_0).
- For a normal distribution, we have the following rules of thumb:
  - 66% of observations lie within one standard deviation of the mean
  - 95% of observations lie within two standard deviations of the mean
  - 99.7% of observations lie within three standard deviations of the mean



- If the sample size is large enough, then the t-statistic is approximately normally distributed, and if it is large (in absolute terms), then this is an indication against $\beta = 0$.
- In the example above, the t-statistics is -62.559, i.e., $\hat{\beta}$ is approx. 63 standard deviations away from zero, which is practically impossible.

OLS regression: Validation (p-value)

- The p-value expresses the probability of observing a coefficient estimate as extreme (away from zero) as $\hat{\beta}$ under H_0, i.e., when $\beta = 0$.
- In other words, it measures the probability of observing a t-statistic as extreme as the one observed if $\beta = 0$.
- If the p-value (column `P>|t|`) is smaller than the desired level of significance (typically 5%), then the H_0 can be rejected and we conclude that $\beta \neq 0$.

- In the example above, the p-value is given as 0.000, i.e., it is so small, that we can conclude the estimated coefficient $\hat{\beta}$ is so extreme (= away from zero) that is virtually impossible to obtain such an estimated if $\beta = 0$.

- Finally, the F-test tests the hypotheses $H_0 : R^2 = 0$ versus $H_1 : R^2 \neq 0$. In a multiple regression with k independent variables, this is equivalent to $H_0 : \beta_1 = \cdots = \beta_k = 0$.

- In the example above, the p-value of the F-test is 0, so we conclude that the model overall has explanatory power.