# Introduction to Python Financial Time Series

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# 4 Financial Time Series

- Time series are ubiquitous in finance.
- pandas is the main library in Python to deal with time series.

#### 4.1 Financial Data

#### Financial data

- For the time being we work with locally stored data files.
- These are in .csv-files (comma-separated values), where the data entries in each row are separated by commas.
- Some initialisation:

```
[1]: import numpy as np
  import pandas as pd
  import matplotlib.pyplot as plt
  plt.style.use('seaborn')
  plt.rcParams['font.family'] = 'serif'
```

# Data import

- pandas provides a numer of different functions and DataFrame methods for importing and exporting data.
- Here we use pd.read\_csv().
- The file that we load contains end-of-day data for different financial instruments retrieved from Thomson Reuters.

```
[2]: # If using colab, then uncomment the line below and comment the line after that

#filename = 'https://raw.githubusercontent.com/packham/Python_CFDS/main/data/

→tr_eikon_eod_data.csv'

filename = './data/tr_eikon_eod_data.csv' # path and filename

f = open(filename, 'r') # this will give an error when using colab; just ignore it

f.readlines()[:5] # show first five lines
```

#### Data import

```
[3]: data = pd.read_csv(filename, # import csv-data into DataFrame index_col=0, # take first column as index parse_dates=True) # index values are datetime
```

[4]: data.info() # information about the DataFrame object

<class 'pandas.core.frame.DataFrame'>

DatetimeIndex: 2216 entries, 2010-01-01 to 2018-06-29

Data columns (total 12 columns):

#	Column	Non-Null Count	Dtype					
0	AAPL.O	2138 non-null	float64					
1	MSFT.O	2138 non-null	float64					
2	INTC.O	2138 non-null	float64					
3	AMZN.O	2138 non-null	float64					
4	GS.N	2138 non-null	float64					
5	SPY	2138 non-null	float64					
6	.SPX	2138 non-null	float64					
7	.VIX	2138 non-null	float64					
8	EUR=	2216 non-null	float64					
9	XAU=	2211 non-null	float64					
10	GDX	2138 non-null	float64					
11	GLD	2138 non-null	float64					
d+ 1175	d+vrnog, floo+64(12)							

dtypes: float64(12)
memory usage: 225.1 KB

### Data import

[5]: data.head()

[5]:		AAPL.O	MSFT.O	INTC.O	AMZN.O	GS.N	SPY	.SPX	.VIX	\
	Date									
	2010-01-01	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN	
	2010-01-04	30.572827	30.950	20.88	133.90	173.08	113.33	1132.99	20.04	
	2010-01-05	30.625684	30.960	20.87	134.69	176.14	113.63	1136.52	19.35	
	2010-01-06	30.138541	30.770	20.80	132.25	174.26	113.71	1137.14	19.16	
	2010-01-07	30.082827	30.452	20.60	130.00	177.67	114.19	1141.69	19.06	
		EUR=	XAU=	GDX	GLD					

	FOV-	AAU-	GDV	GLD
Date				
2010-01-01	1.4323	1096.35	NaN	NaN
2010-01-04	1.4411	1120.00	47.71	109.80
2010-01-05	1.4368	1118.65	48.17	109.70
2010-01-06	1.4412	1138.50	49.34	111.51
2010-01-07	1.4318	1131.90	49.10	110.82

### Data import

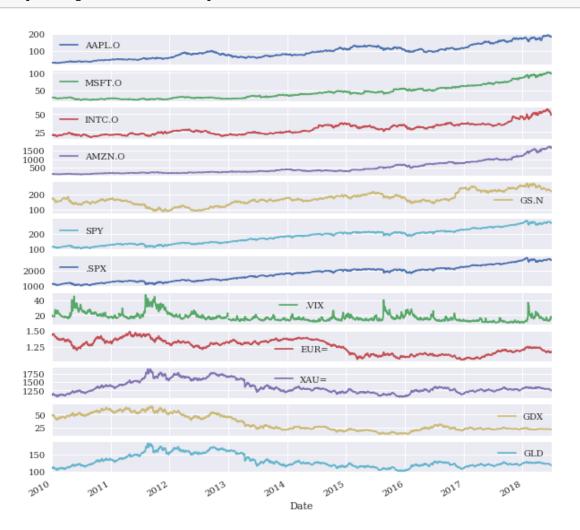
[6]: data.tail()

[6]: AAPL.O MSFT.O INTC.O AMZN.O GS.N SPY .SPX .VIX \

```
2717.07
2018-06-25
            182.17
                     98.39
                              50.71
                                     1663.15
                                              221.54
                                                       271.00
                                                                         17.33
                     99.08
2018-06-26
            184.43
                              49.67
                                     1691.09
                                               221.58
                                                       271.60
                                                               2723.06
2018-06-27
            184.16
                     97.54
                              48.76
                                     1660.51
                                               220.18
                                                       269.35
                                                               2699.63
                                                                         17.91
2018-06-28
            185.50
                     98.63
                              49.25
                                     1701.45
                                               223.42
                                                       270.89
                                                               2716.31
                                                                         16.85
2018-06-29
            185.11
                     98.61
                              49.71
                                     1699.80
                                               220.57
                                                       271.28
                                                               2718.37
                                                                         16.09
              EUR=
                       XAU=
                                GDX
                                        GLD
Date
2018-06-25
            1.1702
                    1265.00
                              22.01
                                     119.89
2018-06-26
            1.1645
                    1258.64
                              21.95
2018-06-27
                    1251.62
                              21.81
            1.1552
                                     118.58
2018-06-28
            1.1567
                    1247.88
                              21.93
                                     118.22
2018-06-29
            1.1683
                    1252.25
                              22.31
                                     118.65
```

#### Data import

#### [7]: data.plot(figsize=(10, 10), subplots=True);



### Data import

- The identifiers used by Thomson Reuters are so-called RIC's.
- The financial instruments in the data set are:

#### Data import

```
[9]: for ric, name in zip(data.columns, instruments):
    print('{:8s} | {}'.format(ric, name))
```

```
AAPL.O
         | Apple Stock
MSFT.0
         | Microsoft Stock
         | Intel Stock
INTC.O
         | Amazon Stock
AMZN.O
         | Goldman Sachs Stock
GS.N
         | SPDR S&P 500 ETF Trust
SPY
.SPX
         | S&P 500 Index
         | VIX Volatility Index
.VIX
         | EUR/USD Exchange Rate
EUR=
XAU =
         | Gold Price
GDX
         | VanEck Vectors Gold Miners ETF
GLD
         | SPDR Gold Trust
```

### **Summary statistics**

# [10]: data.describe().round(2)

[10]:		AAPL.O	MSFT.O	INTC.O	AMZN.O	GS.N	SPY	.SPX	.VIX	\
	count	2138.00	2138.00	2138.00	2138.00	2138.00	2138.00	2138.00	2138.00	
	mean	93.46	44.56	29.36	480.46	170.22	180.32	1802.71	17.03	
	std	40.55	19.53	8.17	372.31	42.48	48.19	483.34	5.88	
	min	27.44	23.01	17.66	108.61	87.70	102.20	1022.58	9.14	
	25%	60.29	28.57	22.51	213.60	146.61	133.99	1338.57	13.07	
	50%	90.55	39.66	27.33	322.06	164.43	186.32	1863.08	15.58	
	75%	117.24	54.37	34.71	698.85	192.13	210.99	2108.94	19.07	
	max	193.98	102.49	57.08	1750.08	273.38	286.58	2872.87	48.00	
		EUR=	XAU=	GDX	GLD					
	count	2216.00	2211.00	2138.00	2138.00					
	mean	1.25	1349.01	33.57	130.09					
	std	0.11	188.75	15.17	18.78					
	min	1.04	1051.36	12.47	100.50					
	25%	1.13	1221.53	22.14	117.40					
	50%	1.27	1292.61	25.62	124.00					
	75%	1.35	1428.24	48.34	139.00					
	max	1.48	1898.99	66.63	184.59					

#### Summary statistics

• The aggregate()-function allows to customise the statistics viewed:

```
max]
      ).round(2)
[11]:
               AAPL.O
                        MSFT.0
                                 INTC.O
                                            AMZN.O
                                                       GS.N
                                                                 SPY
                                                                          .SPX
                                                                                  .VIX
                                                                                        EUR=
                27.44
                         23.01
                                  17.66
                                            108.61
                                                     87.70
                                                             102.20
                                                                      1022.58
                                                                                  9.14
                                                                                        1.04
      min
                                                             180.32
                                                                      1802.71
      mean
                93.46
                         44.56
                                  29.36
                                           480.46
                                                    170.22
                                                                                 17.03
                                                                                        1.25
      std
                40.55
                         19.53
                                   8.17
                                            372.31
                                                      42.48
                                                              48.19
                                                                        483.34
                                                                                  5.88
                                                                                        0.11
                90.55
                         39.66
                                                                      1863.08
      median
                                  27.33
                                           322.06
                                                    164.43
                                                             186.32
                                                                                 15.58
                                                                                        1.27
                                                    273.38
                                                             286.58
               193.98
                        102.49
                                  57.08
                                          1750.08
                                                                      2872.87
      max
                                                                                 48.00
                                                                                        1.48
                   XAU=
                            GDX
                                     GLD
      min
               1051.36
                         12.47
                                 100.50
               1349.01
                         33.57
                                 130.09
      mean
                188.75
                         15.17
                                  18.78
      std
               1292.61
                         25.62
                                 124.00
      median
      max
               1898.99
                         66.63
                                 184.59
```

#### Returns

- When working with financial data we typically (=always you must have good reasons to deviate from this) work with performance data, i.e., **returns**.
- Reasoning:
  - Historical data are mainly used to make forecasts one or several time periods forward.
  - The daily average stock price over the last eight years is meaningless to make a forecast for tomorrow's stock price.
  - However, the daily returns are possible scenarios for the next time period(s).
- $\bullet$  The function pct\_change() calculates discrete returns:

$$r_t^{\rm d} = \frac{S_t - S_{t-1}}{S_{t-1}},$$

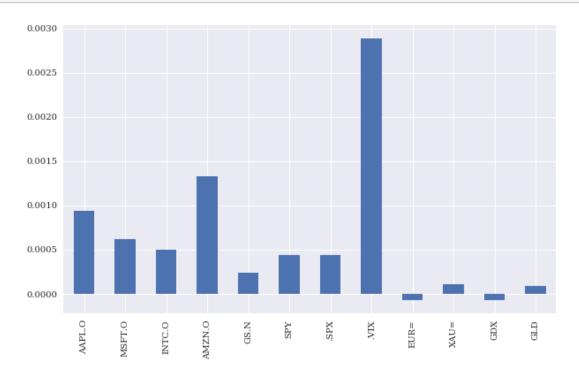
where  $S_t$  denotes the stock price at time t.

np.median,

#### Returns

#### data.pct\_change().round(3).head() [12]: AAPL.O MSFT.0 INTC.O AMZN.O GS.N SPY .SPX .VIX EUR= Date 2010-01-01 NaN NaN NaN NaN NaN NaN NaN NaN NaN 2010-01-04 0.006 NaN NaN NaN NaN NaN NaN NaN ${\tt NaN}$ 2010-01-05 0.002 0.000 -0.000 0.006 0.018 0.003 0.003 -0.034 -0.003 2010-01-06 -0.016 -0.006 -0.003 -0.018 -0.011 0.001 0.001 -0.010 2010-01-07 -0.002 -0.010 -0.010 -0.017 0.020 0.004 0.004 -0.005 -0.007 XAU= GDX GLD Date 2010-01-01 NaN NaN NaN2010-01-04 0.022 NaN NaN2010-01-05 -0.001 0.010 -0.001 0.018 2010-01-06 0.024 2010-01-07 -0.006 -0.005 -0.006

#### Returns



#### Returns

- In finance, log-returns, also called continuous returns, are often preferred over discrete returns:  $r_t^c = \ln\left(\frac{S_t}{S_{t-1}}\right)$ .
- The main reason is that log-return are additive over time.
- ullet For example, the log-return from t-1 to t+1 is the sum of the single-period log-returns:

$$r_{t-1,t+1}^{\text{c}} = \ln\left(\frac{S_{t+1}}{S_t}\right) + \ln\left(\frac{S_t}{S_{t-1}}\right) = \ln\left(\frac{S_{t+1}}{S_t} \cdot \frac{S_t}{S_{t-1}}\right) = \ln\left(\frac{S_{t+1}}{S_{t-1}}\right).$$

• Note: If the sampling (time) interval is small (e.g. one day or one week), then the difference between discrete returns and log-returns is negligible.

#### Returns

Date

```
2010-01-01 NaN NaN NaN NaN 2010-01-04 0.021 NaN NaN 2010-01-05 -0.001 0.010 -0.001 2010-01-06 0.018 0.024 0.016 2010-01-07 -0.006 -0.005 -0.006
```

#### Returns



# 4.2 Correlation analysis and linear regression

- To further illustrate how to work with financial time series we consider the S&P 500 stock index and the VIX volatility index.
- Empirical stylised fact: As the S&P 500 rises, the VIX falls, and vice versa.
- Note: This is about **correlation** not **causation**.

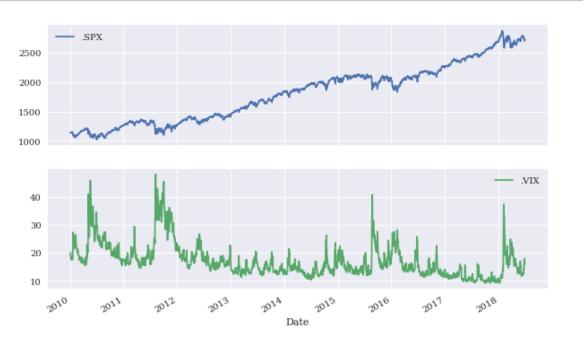
# Correlation analysis

[17]: .SPX .VIX
Date
2018-06-25 2717.07 17.33

```
2018-06-26 2723.06 15.92
2018-06-27 2699.63 17.91
2018-06-28 2716.31 16.85
2018-06-29 2718.37 16.09
```

### Correlation analysis

```
[18]: data.plot(subplots=True, figsize=(10, 6));
```



# Correlation analysis

• Transform both data series into log-returns:

```
[19]: rets = np.log(data / data.shift(1))
    rets.head()
```

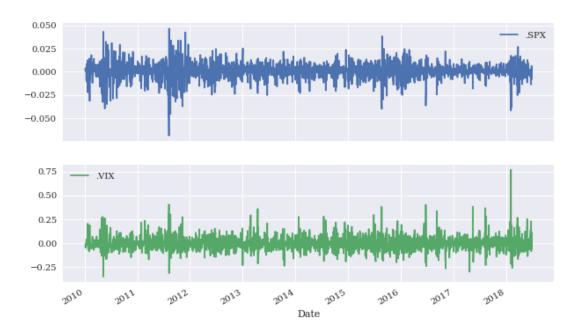
```
[19]: .SPX .VIX

Date
2010-01-04 NaN NaN
2010-01-05 0.003111 -0.035038
2010-01-06 0.000545 -0.009868
2010-01-07 0.003993 -0.005233
2010-01-08 0.002878 -0.050024
```

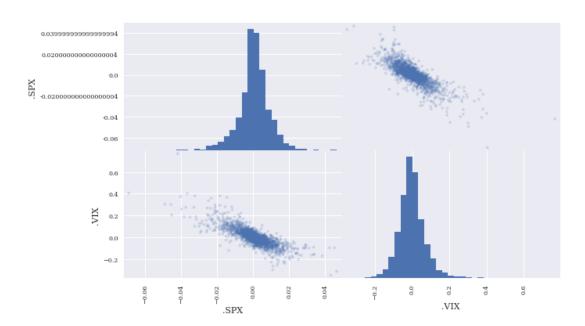
```
[20]: rets.dropna(inplace=True) # drop NaN (not-a-number) entries
```

#### Correlation analysis

```
[21]: rets.plot(subplots=True, figsize=(10, 6));
```



# Correlation analysis



#### Correlation analysis

[23]: rets.corr()

[23]: .SPX .VIX .SPX 1.000000 -0.804382 .VIX -0.804382 1.000000

#### **OLS** regression

- Linear regression captures the linear relationship between two variables.
- For two variables x, y, we postulate a linear relationship:

$$y = \alpha + \beta x + \varepsilon, \quad \alpha, \beta \in \mathbb{R}.$$

- Here,  $\alpha$  is the intercept,  $\beta$  is the slope (coefficient) and  $\varepsilon$  is the error term.
- Given data sample of joint observations  $(x_1, y_1), \ldots, (x_n, y_n)$ , we set

$$y_i = \hat{\alpha} + \hat{\beta}x_i + \hat{\varepsilon}_i,$$

where  $\hat{\alpha}$  and  $\hat{\beta}$  are estimates of  $\alpha, \beta$  and  $\hat{\varepsilon}_1, \dots, \hat{\varepsilon}_n$  are the so-called **residuals**.

• The **ordinary least squares (OLS)** estimator  $\hat{\alpha}, \hat{\beta}$  corresponds to those values of  $\alpha, \beta$  that minimise the sum of squared residuals:

$$\min_{\alpha,\beta} \sum_{i=1}^{n} \varepsilon_i^2 = \sum_{i=1}^{n} (y_i - \alpha - \beta x_i)^2.$$

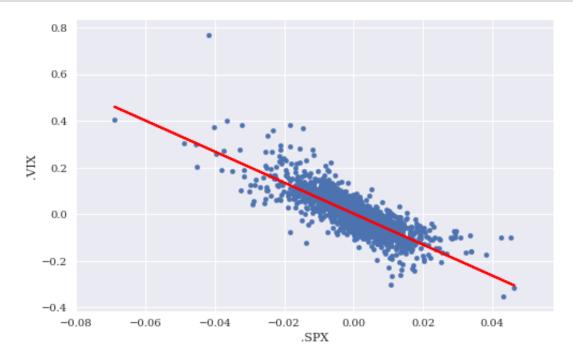
#### **OLS** regressions

• Simplest form of OLS regression:

```
[24]: reg = np.polyfit(rets['.SPX'], rets['.VIX'], deg=1) # fit a linear equation (a<sub>□</sub> → polynomial of degree 1) reg.view() # the fitted paramters
```

[24]: array([-6.65160028e+00, 2.62132142e-03])

```
[25]: ax = rets.plot(kind='scatter', x='.SPX', y='.VIX', figsize=(8, 5))
ax.plot(rets['.SPX'], np.polyval(reg, rets['.SPX']), 'r', lw=2);
```



### **OLS** regression

• To do a more refined OLS regression with a proper analysis, use the package statsmodels.

### **OLS** regression

[30]: print(results.summary())

#### OLS Regression Results

Dep. Variable: Model:	.VIX OLS	R-squared: Adj. R-squared:	0.647 0.647
Method:	Least Squares F-statistic:		3914.
Date:	Tue, 06 Dec 2022	Prob (F-statistic):	0.00
Time:	14:44:29	Log-Likelihood:	3550.1
No. Observations:	2137	AIC:	-7096.
Df Residuals:	2135	BIC:	-7085.
Df Model:	1		
Covariance Type:	nonrobust		

	coef	std err	t	P> t	[0.025	0.975]
const	0.0026	0.001	2.633	0.009	0.001	0.005
.SPX	-6.6516	0.106	-62.559	0.000	-6.860	-6.443
	========		=========		========	
Omnibus:		518.	582 Durbi	n-Watson:		2.094
Prob(Omnib	us):	0.	000 Jarqu	e-Bera (JB):		6789.425
Skew:		0.	766 Prob(	JB):		0.00
Kurtosis:		11.	597 Cond.	No.		107.

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

#### OLS regression: Interpretation of output and forecasting

- The column coef lists the coefficients of the regression: the coefficient in the row labelled const corresponds to  $\hat{\alpha}$  (= 0.0026) and the coefficient in the row .SPX denotes  $\hat{\beta}$  (= -6.6515).
- The estimated model in the example is thus:

$$.VIX = 0.0026 - 6.6516.SPX.$$

• The best forecast of the VIX return when observing an S&P return of 2% is therefore  $0.0026 - 6.6516 \cdot 0.02 = -0.130432 = -13.0432\%$ .

# OLS regression: Validation $(R^2)$

- To validate the model, i.e., to determine, if the model in itself and the explanatory variable(s) make sense, we look  $R^2$  and various p-values (or confidence intervals or t-statistics).
- $R^2$  measures the fraction of variance in the dependent variable Y that is captured by the regression line;  $1 R^2$  is the fraction of Y-variance that remains in the residuals  $\varepsilon_i^2$ , i = 1, ..., n.
- In the output above  $R^2$  is given as 0.647. In other words, 64.7% of the variance in VIX returns are "explained" by SPX returns.
- A high  $R^2$  (and this one is high) is necessary for making forecasts.

#### OLS regression: Validation (confidence interval)

- An important hypothesis to test in any regression model is whether the explanatory variable(s) have an effect on the independent variable.
- This can be translated into testing whether  $\beta \neq 0$ . ( $\beta = 0$  is the same as saying that the X variable can be removed from the model.)
- Formally, we test the null hypothesis  $H_0: \beta = 0$  against the alternative hypothesis  $H_1: \beta \neq 0$ .
- There are several statistics to come to the same conclusion: confidence intervals, t-statistics and p-values.
- The **confidence interval** is an interval around the estimate  $\hat{\beta}$  that we are confident contains the true parameter  $\beta$ . A typial **confidence level** is 95%.
- If the 95% confidence interval does **not** contain 0, then we say  $\beta$  is **statistically significant** at the 5% (=1-95%) level, and we conclude that  $\beta \neq 0$ .

#### OLS regression: Validation (t-statistic)

- The t-statistic corresponds to the **number of standard deviations** that the estimated coefficient  $\hat{\beta}$  is away from 0 (the mean under  $H_0$ ).
- For a normal distribution, we have the following rules of thumb:
  - 66% of observations lie within one standard deviation of the mean
  - -95% of observations lie within two standard deviations of the mean
  - 99.7% of observations lie within three standard deviations of the mean
- If the sample size is large enough, then the t-statistic is approximately normally distributed, and if it is large (in absolute terms), then this is an indication against  $\beta = 0$ .
- In the example above, the t-statistics is -62.559, i.e.,  $\hat{\beta}$  is approx. 63 standard deviations away from zero, which is practically impossible.

#### OLS regression: Validation (p-value)

- The p-value expresses the probability of observing a coefficient estimate as extreme (away from zero) as  $\hat{\beta}$  under  $H_0$ , i.e., when  $\beta = 0$ .
- In other words, it measures the probability of observing a t-statistic as extreme as the one observed if  $\beta = 0$ .
- If the p-value (column P>|t|) is smaller than the desired level of significance (typically 5%), then the  $H_0$  can be rejected and we conclude that  $\beta \neq 0$ .

- In the example above, the *p*-value is given as 0.000, i.e., it is so small, that we can conclude the estimated coefficient  $\hat{\beta}$  is so extreme (= away from zero) that is virtually impossible to obtain such an estimated if  $\beta = 0$ .
- Finally, the F-test tests the hypotheses  $H_0: R^2 = 0$  versus  $H_1: R^2 \neq 0$ . In a multiple regression with k independent variables, this is equivalent to  $H_0: \beta_1 = \cdots = \beta_k = 0$ .
- $\bullet$  In the example above, the *p*-value of the *F*-test is 0, so we conclude that the model overall has explanatory power.