2024 Olympics - Integration

1.
$$\int x(2x+6)^{10} dx$$

$$2. \int 4x(3x^2+1)^5 \, dx$$

$$3. \int x \ln|x^2| \, dx$$

$$4. \int \tan^3 x \, dx$$

$$5. \int \sin^3 x \cos^2 x \, dx$$

$$6. \int 2x \cos(3x+1) \, dx$$

$$7. \int \sqrt{1-x^2} \, dx$$

8.
$$\int \frac{\sin 2\theta}{\sin \theta - \sin^3 \theta} d\theta$$