AOS Math 10, Spring 2024 Derivatives Test (#14)

/ 57



ACADEMIES OF LOUDOUN HONOR CODE



Honesty and integrity are the foundations of good academic work. Whether you are working on a problem set, lab report, project, presentation, or paper, do not engage in plagiarism, unauthorized collaboration, cheating, or facilitating academic dishonesty. Our expectation is for our students to be successful while being trustworthy. The honor code is not intended to be punitive, but rather a guide for all students and faculty to follow. For these reasons, the Academies of Loudoun will uphold the following Honor Code:

Student Signature	Class	May 10, 2024 Date	
			_
the Hollor Code Fledge below a	and sign tins document.		
the Honor Code Pledge below a		e Academies Honor Code. Please write	
As an Academies of Loudoun s	tudent, wen agreed to unheld th	a Academies Hoper Code Please write	
On my honor, I have not accep	oted or provided any unauthoriz	zed aid on this test, quiz, or assignment.	

Print Name:

Instructions: Questions 1-14 are multiple choice. For each problem, circle the letter of the best answer. You **must show** all **work** for credit. Partial credit may be awarded as appropriate. Each question is valued at 3 points.

- 1. If $h(x) = f(x^2 + 1)$ then which of the following is true?
 - (a) $h'(x) = 2xf'(x^2 + 1)$
 - (b) h'(x) = 2xf'(2x)
 - (c) h'(x) = f'(2x)
 - (d) $h'(x) = f'(x^2 + 1)$
- 2. What is the value of

$$\lim_{\Delta x \to 0} \frac{2(x + \Delta x)^2 - 2x^2}{\Delta x}$$

- (a) 4x
- (b) 2
- (c) 4
- (d) 2x
- 3. The line tangent to the curve $y = \sqrt{16-x}$ at the point (0,4) has slope
 - (a) $\frac{1}{8}$
 - (b) $\frac{-1}{8}$
 - (c) -4
 - (d) 4
- 4. What is the derivative of $s(t) = \cos(t^2 + 1)$?
 - (a) $\cos(2t)$
 - (b) $-\sin(2t)$
 - (c) $-(t^2+1)\sin(t^2+1)$
 - (d) $-2t\sin(t^2+1)$

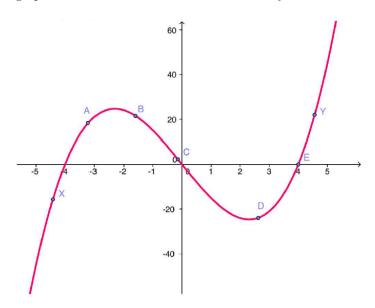
- 5. If $y(x) = \frac{\sin(2x)}{x^2}$ find y'(x)
 - (a) $\frac{x^2 \sin(2x) + 2\cos(2x)}{x^4}$
 - (b) $\frac{x^2\cos(2x) \sin(2x)}{x^3}$
 - (c) $\frac{2x\cos(2x) 2\sin(2x)}{x^3}$
 - (d) $\frac{2\cos(2x)}{x}$
- 6. Calculate $\frac{d}{dt} \left(\ln(e^{2t}) 2t \right)$
 - (a) $\frac{2}{e^{2t}} 2$
 - (b) $\frac{1}{2t} 2$
 - (c) $\frac{1}{2e^{2t}} 2$
 - (d) 0
- 7. If f and h are nonzero differentiable functions, then the derivative of $\frac{f}{h}$ is
 - (a) $\frac{f'h fh'}{h^2}$
 - (b) $\frac{fh' f'h}{h^2}$
 - (c) $\frac{f'h + fh'}{h^2}$
 - (d) $\frac{f'}{h'}$
- 8. At which x value does the graph of $y = 3x^2 10x + 15$ have a horizontal tangent line?
 - (a) $\frac{-3}{5}$
 - (b) $\frac{3}{5}$
 - (c) $\frac{-5}{3}$
 - (d) $\frac{5}{3}$

- 9. If $w(t) = \sqrt{t^2 1}$ what is the value of w'(4)?
 - (a) $\frac{2}{\sqrt{15}}$
 - (b) $\frac{4}{\sqrt{15}}$
 - (c) $\frac{1}{\sqrt{15}}$
 - (d) $\frac{1}{2\sqrt{15}}$
- 10. If $f(x) = \sin(2x + 1)$ and g(x) = f'(x), find g'(x)
 - (a) $g'(x) = 2\sin(2x+1)$
 - (b) $g'(x) = 4\sin(2x+1)\cos(2x+1)$
 - (c) $g'(x) = -4\sin(2x+1)$
 - (d) $g'(x) = -4x\cos(2x+1)$
- 11. Let $f(x) = x^3 6x^2 + 10$. At which point(s) on the graph of f is the tangent line parallel to the line 15x y = 11?
 - (a) (2, -6) and (-2, 22)
 - (b) (5, -15) and (-1, 3)
 - (c) (5, -15) and (2, -6)
 - (d) (2, -6) and (-2, -22)
- 12. Let $f(x) = \sqrt{x}$. What is the equation of the tangent line to f at the point (4,2)?
 - (a) $y = \frac{1}{2}x$
 - (b) y = 2x 6
 - (c) $y = -\frac{1}{2}x + 3$
 - (d) $y = \frac{1}{4}x + 1$

13. If $y = 6\ln(3x)$ then what is y'?

- (a) $\frac{6}{x}$
- (b) $\frac{18}{x}$
- (c) $\frac{1}{3x}$
- (d) $\frac{2}{x}$

14. The graph of a continuous differentiable function f is shown below.



Using the above graph, select the one true statement below.

- (a) f'(X) < f'(Y) < f'(C)
- (b) f'(C) < f'(D) < f'(Y)
- (c) f'(X) < f'(B) < f'(E)
- (d) f'(A) < f'(B) < f'(C)

Free Response Section: Selected values of $f,g,f^{\prime},g^{\prime}$ are given in the table below.

x	0	1	2	3	4
f(x)	$\frac{1}{2}$	$\frac{1}{3}$	1	-1	3
g(x)	-2	1	$-\frac{1}{2}$	2	$-\frac{1}{3}$
f'(x)	$\frac{3}{2}$	$\frac{5}{3}$	$\frac{1}{4}$	0	$-\frac{4}{5}$
g'(x)	-1	$\frac{2}{3}$	-4	-3	$-\frac{1}{3}$

Using the values in the table, evaluate the following derivatives. You must show the symbolic derivative as the first part of your answer for credit!

15.
$$\frac{d}{dx}(f(x) + g(x)) \text{ at } x = 4$$

16.
$$\frac{d}{dx}(f(x)g(x)) \text{ at } x = 1$$

17.
$$\frac{d}{dx} \left(\frac{f(x)}{g(x)} \right)$$
 at $x = 0$

18.
$$\frac{d}{dx}(f(g(x))) \text{ at } x = 3$$

19.
$$\frac{d}{dx} (g(x + f(x))) \text{ at } x = 3$$

KEY

- 1. A
- 2. A
- 3. B
- 4. D
- 5. C
- 6. D
- 7. A
- 8. D
- 9. B
- 10. C
- 11. B
- 12. D
- 13. A
- 14. B

Test ID: 5002 Page: 6