AOS Math 10, Spring 2024 Cumulative, Quarter 3 (Parametric, Polar, Vectors, Complex)

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On my honor, I have not accepte	ed or provided any unautho	orized aid on this test, quiz,	or assignment.

Print Name:

1. Eliminate the parameter t: $x = t^3 - 2$ and $2y = 1 - t^2$

(a)
$$y = 1 - \sqrt[3]{(x+2)^2}$$

(b)
$$y = 1 + \sqrt{(x+2)^3}$$

(c)
$$y = 1 + \sqrt[3]{(x+2)^2}$$

(d)
$$y = 1 - \sqrt[3]{(x+2)^2}$$

2. Eliminate the parameter t: $x = 4\sin(t) + 1$ and $y = 3\cos(t) - 2$

(a)
$$\frac{(x-1)^2}{16} + \frac{(y+1)^2}{9} = 1$$

(b)
$$\frac{(x-1)^2}{4} + \frac{(y+1)^2}{3} = 1$$

(c)
$$\frac{x^2}{16} + \frac{y^2}{9} = 1$$

(d)
$$\frac{(x-1)^2}{3} + \frac{(y+1)^2}{4} = 1$$

3. Convert the polar coordinate $(6,-2\pi/3)$ to rectangular coordinates

(a)
$$(3, 3\sqrt{3})$$

(b)
$$(3\sqrt{3}, -3\sqrt{3})$$

(c)
$$(-3, -3\sqrt{3})$$

(d)
$$(-3, -3)$$

(e)
$$(3, 3\sqrt{3})$$

4. Convert this equation to polar coordinates: $x^2 - y^2 = 16$

(a)
$$r^2 = \frac{4}{\cos \theta - \sin \theta}$$

(b)
$$r^2 = \frac{4}{\cos^2 \theta + \sin^2 \theta}$$

(c)
$$r^2 = \frac{16}{\cos^2 \theta + \sin^2 \theta}$$

(d)
$$r^2 = \frac{16}{\cos^2 \theta - \sin^2 \theta}$$

- 5. Convert this equation to rectangular coordinates: $r=3\sec\theta$
 - (a) y = 1
 - (b) x = 1
 - (c) x = 3
 - (d) y = 3
- 6. Which of the following is the graph of $r = \cos(3\theta)$.
 - (a) A 6 leaf rose with x-intercepts $(0,0), (\pm 1,0)$
 - (b) A 3 leaf rose with no x intercept
 - (c) A 3 leaf rose with x-intercepts (0,0),(1,0)
 - (d) A 6 leaf rose with no x intercept
- 7. A baseball pitcher throws a baseball with an initial speed of 138 feet per second at an angle of 20° to the horizontal. The ball leaves the pitcher's hand at a height of 4 feet above the ground. Write the equations of motion, v_x and v_y for velocity and s_x , s_y for position.
 - (a) $v_x(t) = 129.7$, $v_y(t) = 47.2 + 32t$, $s_x(t) = 129.7t$, $s_y(t) = 47.2t 16t^2$
 - (b) $v_x(t) = 129.7$, $v_y(t) = 47.2 32t$, $s_x(t) = 129.7t$, $s_y(t) = 47.2t 16t^2$

 - (d) $v_x(t) = 129.7$, $v_y(t) = 47.2 32t$, $s_x(t) = 129.7t$, $s_y(t) = 47.2t 16t^2 + 4t$
- 8. Let $u=\langle -3,5\rangle$ and $\vec{v}=\langle 1,4\rangle$ and $\vec{w}=\langle 6,-3\rangle$ find $\vec{u}+2\vec{v}-\vec{w}$
 - (a) $\langle -7, 16 \rangle$
 - (b) $\langle -7, 14 \rangle$
 - (c) $\langle -8, 16 \rangle$
 - (d) $\langle -6, 14 \rangle$
- 9. Given $\vec{u} = \langle 3\sqrt{3}, -5 \rangle$, find $||\vec{u}||$
 - (a) $3\sqrt{17}$
 - (b) $3\sqrt{13}$
 - (c) $2\sqrt{13}$
 - (d) $2\sqrt{17}$

10. Given $\vec{u} = \langle -10, 9 \rangle$, find a unit vector in the direction of \vec{u}

- (a) $\langle -\frac{10}{\sqrt{181}}, \frac{9}{\sqrt{181}} \rangle$
- (b) $\langle -\frac{10}{\sqrt{19}}, -\frac{9}{\sqrt{19}} \rangle$
- (c) $\langle -\frac{10}{\sqrt{181}}, -\frac{9}{\sqrt{181}} \rangle$
- (d) $\langle -\frac{10}{\sqrt{19}}, \frac{9}{\sqrt{19}} \rangle$

11. Which vector is perpendicular to $\langle \frac{2}{3}, -\frac{17}{2} \rangle$

- (a) $\langle -9, -\frac{17}{18} \rangle$
- (b) $\langle -9, -17 \rangle$
- (c) $\langle -9, -\frac{6}{17} \rangle$
- (d) $\langle 9, \frac{18}{3} \rangle$

12. Which vector is parallel to $\langle \frac{2}{3}, -\frac{17}{2} \rangle$

- (a) $\langle 4, -51 \rangle$
- (b) (2, -25)
- (c) $\langle -51, 4 \rangle$
- (d) $\langle 25, -2 \rangle$

13. What is the radian angle between $\langle 5,1 \rangle$ and $\langle 2,-3 \rangle$

- (a) 1.580
- (b) 1.080
- (c) 1.180
- (d) 1.480

- 14. If vector \vec{x} has magnitude 9 and makes an angle of 3.4 radians with the positive x axis, find the components of x and write as $a\hat{i} + b\hat{j}$.
 - (a) $-9.20\hat{i} + 3.20\hat{j}$
 - (b) $-2.30\hat{i} 8.70\hat{j}$
 - (c) $8.70\hat{i} + 2.30\hat{j}$
 - (d) $-8.70\hat{i} 2.30\hat{j}$
- 15. Write the complex number -3 + 9i in polar form.
 - (a) $9.49e^{1.89i}$
 - (b) $9.59e^{1.79i}$
 - (c) $9.29e^{1.81i}$
 - (d) $9.49e^{1.33i}$
- 16. Divide 10 9i by 2 4i, and express your answer in the form a + bi.
 - (a) $-\frac{4}{5} + \frac{29}{10}i$
 - (b) $-\frac{4}{5} \frac{29}{10}i$
 - (c) $\frac{14}{5} + \frac{11}{10}i$
 - (d) $\frac{14}{5} \frac{11}{10}i$
- 17. Simplify the product $\sqrt{7}e^{-i\pi/3} \cdot 3e^{i\pi/5}$.
 - (a) $3\sqrt{7}e^{2\pi i/15}$
 - (b) $3\sqrt{7}e^{\pi i/15}$
 - (c) $3\sqrt{7}e^{-2\pi i/15}$
 - (d) $3\sqrt{7}e^{-\pi i/15}$
- 18. Solve the equation $z^2 2z + 5 = 0$ for z and express your answers in rectangular form.
 - (a) $1 \pm 2i^2$
 - (b) $1 \pm \sqrt{5}i$
 - (c) $1 \pm 2i$
 - (d) $1 \pm 3i$

19. If z = 2 + i is one root of a quadratic equation $x^2 + bx + c$ with real coefficients, what is bc?

- (a) 4
- (b) -20
- (c) 8
- (d) -10

20. If $z^4 = 16e^{2\pi i/5}$, find all values of z in polar form.

(a)
$$z = 2e^{2\pi i/5}, 2e^{4\pi i/5}, 2e^{6\pi i/5}, 2e^{8\pi i/5}$$

(b)
$$z = 2, 2e^{\pi i/2}, 2e^{\pi i}, 2e^{3\pi i/2}$$

(c)
$$z = 2e^{\pi i/10}, 2e^{3\pi i/5}, 2e^{11\pi i/10}, 2e^{8\pi i/5}$$

(d)
$$z = 2e^{\pi i/10}, 2e^{3\pi i/10}, 2e^{5\pi i/10}, 2e^{7\pi i/10}$$

21. Factor $z^2 + 9$ into a product of two binomials.

(a)
$$(z + 3\sqrt{i})(z - 3\sqrt{i})$$

(b)
$$(z+3)(z-3)$$

(c)
$$(z+3i)(z+3i)$$

(d)
$$(z+3i)(z-3i)$$

22. (Bonus): By multiplying two complex numbers, prove the addition identities for sin and cos.

KEY

- 1. D
- 2. A
- 3. C
- 4. D
- 5. C
- 6. C
- 7. D
- 8. A
- 9. C
- 10. A
- 11. C
- 12. A
- 13. C
- 14. D
- 15. A
- 16. C
- 17. C
- 18. C
- 19. B
- 20. C
- 21. D

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