

# AOS Math 10, Spring 2024

## Derivatives Test (#14)

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**May 10, 2024**

**Student Signature**

**Class**

**Date**

**Print Name:**

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**Instructions:** Questions 1-14 are multiple choice. For each problem, circle the letter of the best answer. You **must show all work** for credit. Partial credit may be awarded as appropriate. Each question is valued at 3 points.

1. Let  $f(x) = x^3 - 6x^2 + 10$ . At which point(s) on the graph of  $f$  is the tangent line parallel to the line  $15x - y = 11$  ?

- (a)  $(5, -15)$  and  $(2, -6)$
- (b)  $(2, -6)$  and  $(-2, 22)$
- (c)  $(2, -6)$  and  $(-2, -22)$
- (d)  $(5, -15)$  and  $(-1, 3)$

2. The line tangent to the curve  $y = \sqrt{16 - x}$  at the point  $(0, 4)$  has slope

- (a)  $-4$
- (b)  $4$
- (c)  $\frac{1}{8}$
- (d)  $\frac{-1}{8}$

3. If  $f$  and  $h$  are nonzero differentiable functions, then the derivative of  $\frac{f}{h}$  is

- (a)  $\frac{f'h + fh'}{h^2}$
- (b)  $\frac{fh' - f'h}{h^2}$
- (c)  $\frac{f'}{h'}$
- (d)  $\frac{f'h - fh'}{h^2}$

4. What is the value of

$$\lim_{\Delta x \rightarrow 0} \frac{2(x + \Delta x)^2 - 2x^2}{\Delta x}$$

- (a)  $2$
- (b)  $2x$
- (c)  $4x$
- (d)  $4$

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5. If  $y(x) = \frac{\sin(2x)}{x^2}$  find  $y'(x)$

(a)  $\frac{x^2 \cos(2x) - \sin(2x)}{x^3}$

(b)  $\frac{2 \cos(2x)}{x}$

(c)  $\frac{x^2 \sin(2x) + 2 \cos(2x)}{x^4}$

(d)  $\frac{2x \cos(2x) - 2 \sin(2x)}{x^3}$

6. At which  $x$  value does the graph of  $y = 3x^2 - 10x + 15$  have a horizontal tangent line?

(a)  $\frac{-3}{5}$

(b)  $\frac{5}{3}$

(c)  $\frac{3}{5}$

(d)  $\frac{-5}{3}$

7. Let  $f(x) = \sqrt{x}$ . What is the equation of the tangent line to  $f$  at the point  $(4, 2)$ ?

(a)  $y = -\frac{1}{2}x + 3$

(b)  $y = \frac{1}{2}x$

(c)  $y = 2x - 6$

(d)  $y = \frac{1}{4}x + 1$

8. What is the derivative of  $s(t) = \cos(t^2 + 1)$  ?

(a)  $-\sin(2t)$

(b)  $-2t \sin(t^2 + 1)$

(c)  $\cos(2t)$

(d)  $-(t^2 + 1) \sin(t^2 + 1)$

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9. If  $h(x) = f(x^2 + 1)$  then which of the following is true?

(a)  $h'(x) = 2xf'(2x)$

(b)  $h'(x) = f'(x^2 + 1)$

(c)  $h'(x) = f'(2x)$

(d)  $h'(x) = 2xf'(x^2 + 1)$

10. Calculate  $\frac{d}{dt}(\ln(e^{2t}) - 2t)$

(a) 0

(b)  $\frac{2}{e^{2t}} - 2$

(c)  $\frac{1}{2t} - 2$

(d)  $\frac{1}{2e^{2t}} - 2$

11. If  $w(t) = \sqrt{t^2 - 1}$  what is the value of  $w'(4)$  ?

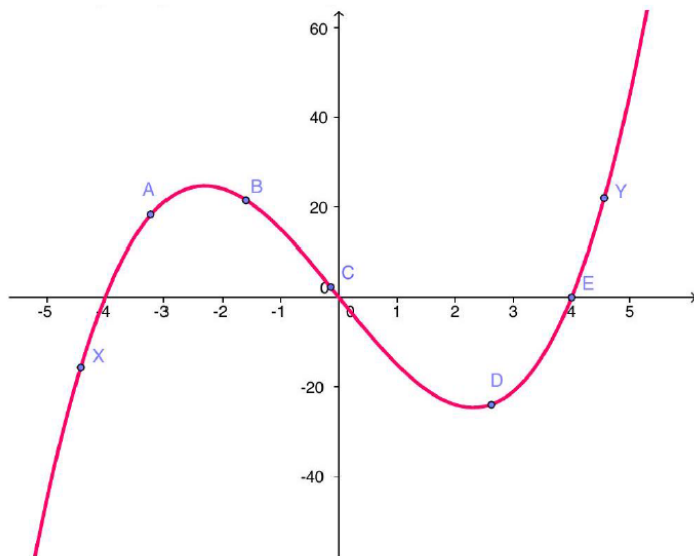
(a)  $\frac{2}{\sqrt{15}}$

(b)  $\frac{1}{2\sqrt{15}}$

(c)  $\frac{1}{\sqrt{15}}$

(d)  $\frac{4}{\sqrt{15}}$

12. The graph of a continuous differentiable function  $f$  is shown below.



Using the above graph, select the one true statement below.

- (a)  $f'(X) < f'(Y) < f'(C)$
  - (b)  $f'(A) < f'(B) < f'(C)$
  - (c)  $f'(X) < f'(B) < f'(E)$
  - (d)  $f'(C) < f'(D) < f'(Y)$
13. If  $y = 6 \ln(3x)$  then what is  $y'$  ?

- (a)  $\frac{18}{x}$
- (b)  $\frac{1}{3x}$
- (c)  $\frac{6}{x}$
- (d)  $\frac{2}{x}$

14. If  $f(x) = \sin(2x + 1)$  and  $g(x) = f'(x)$ , find  $g'(x)$

- (a)  $g'(x) = 2 \sin(2x + 1)$
- (b)  $g'(x) = -4 \sin(2x + 1)$
- (c)  $g'(x) = 4 \sin(2x + 1) \cos(2x + 1)$
- (d)  $g'(x) = -4x \cos(2x + 1)$

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**Free Response Section:** Selected values of  $f, g, f', g'$  are given in the table below.

$x$	0	1	2	3	4
$f(x)$	$\frac{1}{2}$	$\frac{1}{3}$	1	-1	3
$g(x)$	-2	1	$-\frac{1}{2}$	2	$-\frac{1}{3}$
$f'(x)$	$\frac{3}{2}$	$\frac{5}{3}$	$\frac{1}{4}$	0	$-\frac{4}{5}$
$g'(x)$	-1	$\frac{2}{3}$	-4	-3	$-\frac{1}{3}$

Using the values in the table, evaluate the following derivatives. **You must show the symbolic derivative as the first part of your answer for credit!**

15.  $\frac{d}{dx} (f(x) + g(x))$  at  $x = 4$

16.  $\frac{d}{dx} (f(x)g(x))$  at  $x = 1$

17.  $\frac{d}{dx} \left( \frac{f(x)}{g(x)} \right)$  at  $x = 0$

18.  $\frac{d}{dx} (f(g(x)))$  at  $x = 3$

19.  $\frac{d}{dx} (g(x + f(x)))$  at  $x = 3$

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**KEY**

1. D
2. D
3. D
4. C
5. D
6. B
7. D
8. B
9. D
10. A
11. D
12. D
13. C
14. B