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1. Let  $f(x) = \sqrt{x}$ . What is the equation of the tangent line to  $f$  at the point  $(4, 2)$ ?

(a)  $y = -\frac{1}{2}x + 3$

(b)  $y = \frac{1}{2}x$

(c)  $y = 2x - 6$

(d)  $y = \frac{1}{4}x + 1$

2. What is the derivative of  $s(t) = \sec \sqrt{t}$  ?

(a)  $\sec \frac{1}{2\sqrt{t}} \tan \frac{1}{2\sqrt{t}}$

(b)  $\frac{\sec \sqrt{t} \tan \sqrt{t}}{2\sqrt{t}}$

(c)  $\sec \sqrt{t} \tan \sqrt{t}$

(d)  $\tan^2 \sqrt{t}$

3. If  $f, g$ , and  $h$  are nonzero differentiable functions, then the derivative of  $\frac{fg}{h}$  is

(a)  $\frac{fg'h' - fgh'}{h^2}$

(b)  $\frac{fgh' - fg'h - f'gh}{h^2}$

(c)  $\frac{f'gh + fg'h + fgh'}{h^2}$

(d)  $\frac{fg'h + f'gh - fgh'}{h^2}$

(e)  $\frac{fg' + f'g}{h'}$

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4. The line tangent to the curve  $y = \sqrt{16 - x}$  at the point  $(0, 4)$  has slope

- (a) 4
- (b)  $1/8$
- (c)  $-1/8$
- (d) -8
- (e) 8

5. At what point(s) on the curve  $x^2 - y^2 + x = 2$  is the tangent line vertical?

- (a)  $(-2, 0)$  only
- (b)  $(1, \sqrt{2})$  only
- (c)  $(1, 0)$  and  $(-2, 0)$
- (d) The tangent line is never vertical
- (e)  $(1, 0)$  only

6. If  $y = 6 \cos(3x)$  then what is  $y'$  ?

- (a)  $18 \sin(x)$
- (b)  $18 \sin(3x)$
- (c)  $-18 \sin(3x)$
- (d)  $-6 \sin(3x)$

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7. What is the value of

$$\lim_{\Delta x \rightarrow 0} \frac{2(x + \Delta x)^2 - 2x^2}{\Delta x}$$

(a)  $4x$

(b)  $4$

(c)  $2$

(d) Does not exist

(e)  $2x$

8. If  $w(t) = \sqrt{t^2 - 1}$  what is the value of  $w'(4)$  ?

(a)  $\frac{2}{\sqrt{15}}$

(b)  $\frac{1}{\sqrt{15}}$

(c)  $\frac{1}{2\sqrt{15}}$

(d)  $\frac{4}{\sqrt{15}}$

9. At which  $x$  value does the graph of  $y = 3x^2 - 10x + 15$  have a horizontal tangent line?

(a)  $-\frac{3}{5}$

(b)  $\frac{5}{3}$

(c)  $-\frac{5}{3}$

(d)  $\frac{3}{5}$

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10. Find  $\frac{dy}{dx}$  if  $x^2 + 4xy + 2y^2 = 16$

(a)  $\frac{-2(x+y)}{x+2y}$

(b)  $\frac{-2(x+y)}{2x+y}$

(c)  $\frac{-x+2y}{x+y}$

(d)  $\frac{-x-2y}{2x+2y}$

11. At which  $x$  value(s) does the graph of  $y = 2x^3 - 24x + 16$  have a horizontal tangent line?

(a) 2

(b) 1

(c) 2 and -2

(d) 1 and -1

12. If  $h(x) = f(x^2 + 1)$  then which of the following is true?

(a)  $h'(x) = f'(2x)$

(b)  $h'(x) = 2xf'(2x)$

(c)  $h'(x) = 2xf'(x^2 + 1)$

(d)  $h'(x) = f'(x^2 + 1)$

13. If  $f(x) = 10x^2 - 5$ , what is the average rate of change of  $f(x)$  over the interval

$$-1 \leq x \leq 2$$

(a) 30

(b) 20

(c)  $\frac{20}{3}$

(d) 10

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14. If  $h(x) = f(x)g(x)$  and  $f(5) = 3, f'(5) = -1, g(5) = -\frac{1}{2}, g'(5) = 2$ , then what is the value of  $h'(5)$  ?

(a)  $\frac{13}{2}$

(b)  $-\frac{9}{2}$

(c)  $\frac{9}{2}$

(d) -2

15. If  $f(x) = \sin(x^2 + 1)$  then find  $f''(x)$

(a)  $-4x^2 \sin(x^2 + 1) + 2 \cos(x^2 + 1)$

(b)  $4x^2 \sin(x^2 + 1) - 2 \cos(x^2 + 1)$

(c)  $-4x^2 \sin(x^2 + 1) - 2 \cos(x^2 + 1)$

(d)  $4x^2 \sin(x^2 + 1) + 2 \cos(x^2 + 1)$

16. The height (in feet) of a ball thrown vertically upward is given by

$$s(t) = -16t^2 + 32t + 64$$

where  $t$  is in seconds. What is the velocity of the ball at time  $t = 3$  seconds?

(a) 64ft/s

(b) -16ft/s

(c) 16ft/s

(d) -64ft/s

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17. At which point on the graph is the slope of the tangent line closest to the average rate of change of  $f(x)$  between points  $X$  and  $Y$ ?

(a) B

(b) C

(c) D

(d) E

(e) A

18. Let  $f(x) = x^3 - 6x^2 + 10$ . At which point(s) on the graph of  $f$  is the tangent line parallel to the line  $15x - y = 11$  ?

(a)  $(2, -6)$  and  $(-2, -22)$

(b)  $(5, -15)$  and  $(-1, 3)$

(c)  $(5, -15)$  and  $(2, -6)$

(d)  $(2, -6)$  and  $(-2, 22)$