REPORT ON INVESTMENT MANAGEMENT

TOPIC: Planning a Client's Wealth Over a 5-year Horizon

CAPSTONE PROJECT BY THE UNIVERSITY OF GENEVA

Submitted by

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CERTIFICATES



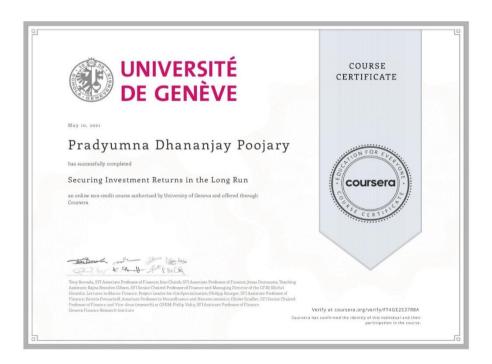
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PROBLEM STATEMENT

Planning your client's wealth over a 5-year horizon by initially preparing a client profile, discussing the investment policy, reporting and rebalancing asset allocation and the final reporting using portfolio asset allocation and investment valuation models and techniques.

Material used to prepare the client profile:

Client name: JOHN LAM

John Lam is a successful 54-year-old commercial lawyer with his own firm. He's married and has two children (aged 19 and 22). He works hard and values the success this has bought him. John lives in an average suburban house and drives a top of the range VW Passat estate; he dresses well but not flashily and his idea of partying is lunch with friends at a restaurant by the lake. John keeps a low profile but acts as a mentor to a number of young lawyers and takes part as a member of various committees in the legal life of the city, but never appears as a spokesperson. His business is successful and the need for detailed attention is less. His goal is now to spend more time with family, friends and children.

John made his money through hard work and he doesn't believe in a free lunch. His total wealth amounts to USD 8mio. He is willing to help his children out in their future entrepreneurial activities, but expects them to make their own way until then. His expenses are covered by his salary and he wishes to grow his wealth through investments but does not think he could stomach to see his portfolio lose more than one third of its value in the process.

You have been working with John for eight years. You have been recommending an investment strategy annually. Five years ago, you suggested the following asset allocation, which was in line with his risk profile at that time: 60% equities, 35% bonds, and 5% cash. John, however, chose to be more aggressive to take advantage of a recent rally in emerging markets and lost almost 40% of his invested assets. Two years ago, you proposed a more conservative strategy. John followed your advice but soon expressed dissatisfaction with missed market trend opportunities and low returns. Last year, when you recommended again a more aggressive strategy with an allocation of 50% equities, 40% bonds, and 10% cash, he actually desired a much more conservative position to respond to a recent concern about decelerating growth in developed countries, requesting 30% equities, 30% bonds, and 40% cash.

Currently, John has the idea that he should go out of consumer equity investments and be more in IT equity investments, which have come into fashion following the latest virtual reality boom and the new wave of social media IPOs. Although he is not an expert in new technologies, John has been an occasional reader of IT magazines ever since he bought shares in several new tech firms. He is confident that their stock price will go past their all-time high which was reached 6 years ago. John has made some good calls over the past decade. He invested in three different successful companies, making decent returns and never keeping his positions open for more than a year. Being a hard worker, John regularly revisits his past fruitful trades and finds that he nearly always had a feeling whether the trades were going to end up being winners or losers. "If only I was able to listen more to my intuition..." he often says. When he talks to you about investments he made, he turns into a storyteller for a moment. Whether big gains or losses, his face lights up as he revisits past trades and remembers the excitement of watching his positions change in value.

Introduction

The purpose of this Investment Policy Statement is to establish a clear understanding between the client and the wealth manager as to the investment goals and policies applicable to the investor's investment portfolio.

This Investment Policy Statement will:

- Establish reasonable objectives and guidelines in the investment of the investor's assets
- Set forth a target portfolio indicative of the risk levels, allocations and return targets that the client's money will typically be invested to achieve. The customized investment strategy and target portfolio allocation illustrated for you are approximate based on individual cash requirements, re-balancing tolerance, economic and market conditions.

This has been developed from an evaluation of many key factors which impact the investor's specific situation, risk tolerance and investment objectives. This is not a contract, but rather a summary of the investment philosophy that the financial representative will seek to pursue on behalf of the investor.

Client's Investment Goals

- Mr. John wants to help out his children in their future entrepreneurial activities.
- His expenses are covered by his salary but he wishes to grow his wealth through investments so that he can spend more time with his family, friends and children.
- Triggering emotions ("When he talks to you about investments he made, he turns into a storyteller for a moment. Whether big gains or losses, his face lights up as he revisits past trades and remembers the excitement of watching his positions change in value.")
- He does not have any incoming expense in the near future.

Cognitive Biases and Risk Tolerance

Recency bias ("Five years ago, you suggested the following asset allocation, which was in line with his risk profile at that time: 60% equities, 35% bonds, and 5% cash. John, however, chose to be more aggressive to take advantage of a recent rally in emerging markets and lost almost 40% of his invested assets. Two years ago, you proposed a more conservative strategy. John followed your advice but soon expressed dissatisfaction with missed market trend opportunities and low returns. Last year, when you recommended again a more aggressive strategy with an allocation of 50% equities, 40% bonds, and 10% cash, he actually desired a much more conservative position to respond to a recent concern about decelerating growth in developed countries, requesting 30% equities, 30% bonds, and 40% cash. Currently, John has the idea that he should go out of consumer equity investments and be

more in IT equity investments, which have come into fashion following the latest virtual reality boom and the new wave of social media IPOs.")

- ❖ Disposition effect ("Although he is not an expert in new technologies, John has been an occasional reader of IT magazines ever since he bought shares in several new tech firms. He is confident that their stock price will go past their all-time high which was reached 6 years ago. John has made some good calls over the past decade. He invested in three different successful companies, making decent returns and never keeping his positions open for more than a year.")
- ❖ Hindsight bias ("Being a hard worker, John regularly revisits his past fruitful trades and finds that he nearly always had a feeling whether the trades were going to end up being winners or losers. "If only I was able to listen more to my intuition..." he often says.")
- Mr. John Lam is susceptible to fear in financial markets as he demands for a more conservative position in his portfolio in response to a recent concern about decelerating growth in developed countries.

Mr. John Lam experiences the Recency bias which occurs while defining the investment universe.

One can overcome this bias using the following methods:

- Don't rely solely on readily available data
- · Get out of your comfort zone and
- Do some extensive research

He also experiences the Disposition bias which occurs while adjusting and rebalancing the portfolio over time.

One can overcome this bias using the following methods:

- Stick to your original and carefully designed strategy
- Your buy and sell orders should be dictated by this strategy only

Investment Profile

Mr John Lam seems to be a balanced investor corresponding to his requests to take advantage of recent market rallies by deviating from the advised investment strategy and his tendency to shift his equity investments into the IT sector which have come in fashion following the latest virtual reality boom and the new wave of social media IPOs but nevertheless maintaining a conservative position in response to a recent concern about decelerating growth in developed countries.

Age and Retirement Horizon

The following data can be inferred from the profile of Mr. John Lam:

He is currently 54 years old. He intends to now spend more time with his family, friends and children.

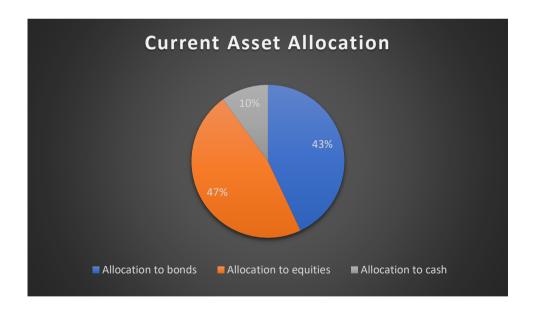
It is critically important to keep the financial representative updated if the retirement objectives begin to change for any reason.

Asset Allocation

Asset classification is depicted below for the portfolio(s) in this report. The ratios depicted for Stocks, Bonds, Cash, and Other, are reflective of current value for the portfolio(s) shown and are subject to change along with changes to the portfolio value.

Portfolio asset allocations are defined as follows:

- Stocks: Individual equities, along with equity portions of mutual funds and ETFs.
- Bonds: Individual bonds, along with fixed income portions of mutual funds and ETFs.
- Cash: Cash, Money Market funds, along with portions of mutual funds and ETFs allocated to cash. Other: Non-Traded REITs/DPPs, Variable Annuities and any other custom allocation.



To construct portfolios, we need 3 main types of information on financial assets:

- The anticipated (or expected) returns
- The risk associated to those returns which can be measured using the standard deviation of the returns
- The dependence between the returns of the different asset classes.

The following set of data has been used to compute the monthly and yearly returns over the past 11 years:

	DATE	WORLD BONDS INDEX	WORLD BONDS INDEX	WORLD EQUITIES INDEX	WORLD EQUITIES INDEX	3-MONTHS CASH USD	3-MONTHS CASH
		price	(holding) return	price	(holding) return	price	(holding) return
1	01-01- 2050	100		100		100	
2	01-02- 2050	98.5374677	-1.46%	102.7858681	2.79%	100.7010138	0.70%
3	01-03- 2050	98.60465116	0.07%	101.7153902	-1.04%	101.4284099	0.72%
4	01-04- 2050	97.23514212	-1.39%	102.1575178	0.43%	102.1859571	0.75%
5	01-05- 2050	98.52196382	1.32%	103.6309396	1.44%	102.9472732	0.75%
6	01-06- 2050	96.4444444	-2.11%	101.2627599	-2.29%	103.6633626	0.70%
7	01-07- 2050	98.38242894	2.01%	101.0650245	-0.20%	104.3869898	0.70%
8	01-08- 2050	102.8630491	4.55%	110.6843787	9.52%	105.0955414	0.68%
9	01-09- 2050	99.40568475	-3.36%	108.0461558	-2.38%	105.7777108	0.65%
10	01-10- 2050	101.2919897	1.90%	110.9061494	2.65%	106.4975691	0.68%
11	01-11- 2050	102.1395349	0.84%	106.9441695	-3.57%	107.1872762	0.65%
12	01-12- 2050	103.0645995	0.91%	111.5902453	4.34%	107.8958278	0.66%
13	01-01- 2051	104.3255814	1.22%	114.5891991	2.69%	108.6081483	0.66%
14	01-02- 2051	102.9457364	-1.32%	109.3820313	-4.54%	109.2601666	0.60%
15	01-03- 2051	101.3643411	-1.54%	103.1439732	-5.70%	109.9951004	0.67%
16	01-04- 2051	100.3617571	-0.99%	94.59327901	-8.29%	110.7111898	0.65%
17	01-05- 2051	100.0516796	-0.31%	96.52862215	2.05%	111.4611993	0.68%
18	01-06- 2051	103.374677	3.32%	106.6442338	10.48%	112.1885953	0.65%
19	01-07- 2051	105.2713178	1.83%	105.62526	-0.96%	112.931067	0.66%
20	01-08- 2051	108.5684755	3.13%	105.590722	-0.03%	113.6660008	0.65%
21	01-09- 2051	107.7209302	-0.78%	94.90957492	-10.12%	114.3632458	0.61%
22	01-10- 2051	108.9250646	1.12%	86.81938817	-8.52%	115.0755663	0.62%
23	01-11- 2051	113.7932817	4.47%	92.14552035	6.13%	115.7577356	0.59%
24	01-12- 2051	115.6795866	1.66%	92.08371541	-0.07%	116.4436739	0.59%
25	01-01- 2052	116.8217054	0.99%	93.21781598	1.23%	117.1069988	0.57%
26	01-02- 2052	119.7416021	2.50%	96.43813648	3.45%	117.6761015	0.49%
27	01-03- 2052	119.777778	0.03%	103.9815716	7.82%	118.2866619	0.52%
28	01-04- 2052	115.4263566	-3.63%	101.3045691	-2.57%	118.8595334	0.48%
29	01-05- 2052	117.2041344	1.54%	104.1686023	2.83%	119.4324049	0.48%
30	01-06- 2052	117.0542636	-0.13%	103.9409743	-0.22%	119.986432	0.46%
31	01-07- 2052	115.8294574	-1.05%	99.43527245	-4.33%	120.5593035	0.48%
32	01-08- 2052	118.3049096	2.14%	102.2690091	2.85%	121.1246372	0.47%
33	01-09- 2052	120.5943152	1.94%	102.2645656	0.00%	121.6635887	0.44%
34	01-10- 2052	125.3126615	3.91%	104.8795611	2.56%	122.1987713	0.44%
35	01-11- 2052	126.625323	1.05%	105.9657932	1.04%	122.6849584	0.40%

36	01-12- 2052	128.6046512	1.56%	100.8652693	-4.81%	123.1447631	0.37%
37	01-01- 2053	135.2918863	5.20%	108.1311881	7.20%	123.5706479	0.35%
38	01-02- 2053	132.8888372	-1.78%	105.8946973	-2.07%	123.9550748	0.31%
39	01-03- 2053	132.1498708	-0.56%	104.0563031	-1.74%	124.3771907	0.34%
40	01-04- 2053	130.749354	-1.06%	97.18565317	-6.60%	124.7804621	0.32%
41	01-05- 2053	131.6847545	0.72%	99.86487742	2.76%	125.1912712	0.33%
42	01-06- 2053	135.7260465	3.07%	103.6392207	3.78%	125.5719293	0.30%
43	01-07- 2053	139.5245478	2.80%	101.1207701	-2.43%	125.9488185	0.30%
44	01-08- 2053	142.7750904	2.33%	100.1191664	-0.99%	126.3068632	0.28%
45	01-09- 2053	146.7700258	2.80%	102.3158677	2.19%	126.62345	0.25%
46	01-10- 2053	148.2428424	1.00%	100.7911437	-1.49%	126.9438058	0.25%
47	01-11- 2053	144.2168475	-2.72%	98.34015342	-2.43%	127.2603927	0.25%
48	01-12- 2053	141.9275969	-1.59%	99.48051528	1.16%	127.6033619	0.27%
49	01-01- 2054	142.7750904	0.60%	100.4092053	0.93%	127.9425621	0.27%
50	01-02- 2054	144.4924031	1.20%	100.7634729	0.35%	128.2403045	0.23%
51	01-03- 2054	148.4455814	2.74%	102.8385841	2.06%	128.5644292	0.25%
52	01-04- 2054	150.9177778	1.67%	109.4179832	6.40%	128.8772472	0.24%
53	01-05-	154.1314729	2.13%	113.3947074	3.63%	129.2051408	0.25%
54	2054 01-06-	155.1487855	0.66%	116.0597933	2.35%	129.5254966	0.25%
55	2054 01-07-	154.9235659	-0.15%	114.4623576	-1.38%	129.8646968	0.26%
56	2054 01-08-	156.1457881	0.79%	116.990705	2.21%	130.203897	0.26%
57	2054 01-09-	160.0396899	2.49%	121.5933558	3.93%	130.5280217	0.25%
58	2054 01-10-	162.0394832	1.25%	119.6753826	-1.58%	130.867222	0.26%
59	2054 01-11- 2054	160.852093	-0.73%	121.9995314	1.94%	131.1951155	0.25%
60	01-12-	160.4229974	-0.27%	117.5497772	-3.65%	131.5418535	0.26%
61	2054 01-01-	161.4603618	0.65%	120.960158	2.90%	131.8885916	0.26%
62	2055 01-02-	163.7713178	1.43%	129.4720726	7.04%	132.2051785	0.24%
63	2055 01-03-	160.6791214	-1.89%	126.0528049	-2.64%	132.5782987	0.28%
64	2055 01-04-	160.7080103	0.02%	120.7583831	-4.20%	132.9740323	0.30%
65	2055 01-05-	162.0803618	0.85%	124.7138996	3.28%	133.4149927	0.33%
66	2055 01-06-	159.9968992	-1.29%	124.9130489	0.16%	133.8672596	0.34%
67	2055 01-07-	162.6340052	1.65%	123.9215441	-0.79%	134.3534467	0.36%
68	2055 01-08-	165.034522	1.48%	127.49694	2.89%	134.8509403	0.37%
69	2055 01-09-	163.8082687	-0.74%	129.7782697	1.79%	135.3597407	0.38%
70	2055 01-10-	163.9554005	0.09%	125.6242098	-3.20%	135.9137678	0.41%
71	2055 01-11-	167.56677	2.20%	129.2513118	2.89%	136.4904082	0.42%
72	2055 01-12-	164.9704393	-1.55%	122.9807354	-4.85%	137.123582	0.46%
73	2055 01-01-	165.5143669	0.33%	124.929611	1.58%	137.7567557	0.46%
74	2056 01-02-	168.5002067	1.80%	122.9676069	-1.57%	138.3635473	0.44%

75	01-03- 2056	173.609354	3.03%	123.9162927	0.77%	139.0457167	0.49%
76	01-04- 2056	184.2222222	6.11%	128.5512597	3.74%	139.7165794	0.48%
77	01-05- 2056	186.9565891	1.48%	134.5709808	4.68%	140.4062865	0.49%
78	01-06- 2056	191.9687339	2.68%	135.6697354	0.82%	141.0696114	0.47%
79	01-07- 2056	194.1951421	1.16%	135.7533538	0.06%	141.7480119	0.48%
80	01-08- 2056	193.5796899	-0.32%	140.7242086	3.66%	142.4226435	0.48%
81	01-09- 2056	188.0610853	-2.85%	138.766446	-1.39%	143.0595862	0.45%
82	01-10- 2056	190.8613437	1.49%	140.7866194	1.46%	143.7153733	0.46%
83	01-11- 2056	192.651938	0.94%	139.4103485	-0.98%	144.352316	0.44%
84	01-12- 2056	195.1421705	1.29%	145.0442935	4.04%	145.011872	0.46%
85	01-01- 2057	197.0217571	0.96%	148.3076351	2.25%	145.6638902	0.45%
86	01-02- 2057	194.4878553	-1.29%	151.1878264	1.94%	146.2593751	0.41%
87	01-03- 2057	194.2746253	-0.11%	152.0286565	0.56%	146.8812422	0.43%
88	01-04- 2057	193.2636176	-0.52%	154.609518	1.70%	147.4842649	0.41%
89	01-05- 2057	192.4126098	-0.44%	156.563039	1.26%	148.1174387	0.43%
90	01-06- 2057	192.771938	0.19%	156.2715863	-0.19%	148.7393058	0.42%
91	01-07- 2057	194.0347804	0.66%	158.1909732	1.23%	149.3837862	0.43%
92	01-08- 2057	198.5001034	2.30%	153.3835179	-3.04%	150.0395734	0.44%
93	01-09- 2057	198.0347804	-0.23%	152.8189923	-0.37%	150.6802849	0.43%
94	01-10- 2057	199.8124031	0.90%	159.3384043	4.27%	151.339841	0.44%
95	01-11- 2057	202.9092506	1.55%	159.9154524	0.36%	151.9767836	0.42%
96	01-12- 2057	205.8487855	1.45%	167.9713031	5.04%	152.6288019	0.43%
97	01-01- 2058	204.1540568	-0.82%	165.694215	-1.36%	153.2883579	0.43%
98	01-02- 2058	198.5775711	-2.73%	167.3399232	0.99%	153.8913805	0.39%
99	01-03- 2058	196.8568475	-0.87%	169.1348923	1.07%	154.5622432	0.44%
100	01-04- 2058	195.6737468	-0.60%	164.3490485	-2.83%	155.2180304	0.42%
101	01-05- 2058	194.921137	-0.38%	171.1243653	4.12%	155.9039686	0.44%
102	01-06- 2058	198.6610853	1.92%	181.3246052	5.96%	156.5597558	0.42%
103	01-07- 2058	202.02	1.69%	190.7149176	5.18%	157.2343874	0.43%
104	01-08- 2058	198.623876	-1.68%	196.4270277	3.00%	157.9127878	0.43%
105	01-09- 2058	199.4905426	0.44%	184.1811652	-6.23%	158.5836505	0.42%
106	01-10- 2058	204.3429457	2.43%	195.6346722	6.22%	159.2733577	0.43%
107	01-11- 2058	207.3854264	1.49%	187.5456973	-4.13%	159.9442204	0.42%
108	01-12- 2058	204.2331783	-1.52%	190.1479683	1.39%	160.6414653	0.44%
109	01-01- 2059	204.6325065	0.20%	189.1697939	-0.51%	161.350017	0.44%
110	01-02- 2059	206.6642377	0.99%	197.8996417	4.61%	161.9907285	0.40%
111	01-03- 2059	208.6319897	0.95%	208.4244586	5.32%	162.7105868	0.44%
112	01-04- 2059	206.4047028	-1.07%	216.5889729	3.92%	163.400294	0.42%
113	01-05- 2059	210.0969509	1.79%	218.9141315	1.07%	164.1050767	0.43%

114	01-06- 2059	210.2228941	0.06%	213.4082399	-2.52%	164.7797083	0.41%
115	01-07- 2059	209.6057881	-0.29%	222.0585087	4.05%	165.4769532	0.42%
116	01-08- 2059	210.2575711	0.31%	215.8198446	-2.81%	166.181736	0.43%
117	01-09- 2059	218.2309561	3.79%	192.9976611	-10.57%	166.8601364	0.41%
118	01-10- 2059	230.3202584	5.54%	186.5131911	-3.36%	167.5309991	0.40%
119	01-11- 2059	234.9567959	2.01%	213.6120346	14.53%	168.1453285	0.37%
120	01-12- 2059	232.5546253	-1.02%	220.4366338	3.19%	168.7709645	0.37%
121	01-01- 2060	235.9501292	1.46%	232.2637981	5.37%	169.4003694	0.37%
122	01-02- 2060	233.1614987	-1.18%	237.3665437	2.20%	169.9807787	0.34%
123	01-03- 2060	224.8213437	-3.58%	228.7174868	-3.64%	170.629028	0.38%
124	01-04- 2060	226.3796899	0.69%	241.3717467	5.53%	171.2584329	0.37%
125	01-05- 2060	226.3602584	-0.01%	251.051492	4.01%	171.91422	0.38%
126	01-06- 2060	222.2790181	-1.80%	239.6708988	-4.53%	172.5511627	0.37%
127	01-07- 2060	218.7122997	-1.60%	253.6208408	5.82%	173.2257943	0.39%
128	01-08- 2060	223.6181912	2.24%	248.9769867	-1.83%	173.9117326	0.40%
129	01-09- 2060	225.7271318	0.94%	251.5713807	1.04%	174.5939019	0.39%
130	01-10- 2060	229.2837726	1.58%	246.503577	-2.01%	175.3062224	0.41%
131	01-11- 2060	228.7541085	-0.23%	257.790251	4.58%	176.0147741	0.40%
132	01-12- 2060	226.7203618	-0.89%	267.4885782	3.76%	176.7685524	0.43%
133	01-01- 2061	227.3852713	0.29%	287.2485892	7.39%	177.544944	0.44%

RISK RETURN TRADE-OFF

The risk-return trade-off states that the potential return rises with an increase in risk. Using this principle, individuals associate low levels of uncertainty with low potential returns, and high levels of uncertainty or risk with high potential returns. According to the risk-return trade-off, invested money can render higher profits only if the investor will accept a higher possibility of losses.

The risk-return trade-off is the trading principle that links high risk with high reward. The appropriate risk-return trade-off depends on a variety of factors including an investor's risk tolerance, the investor's years to retirement and the potential to replace lost funds. Time also plays an essential role in determining a portfolio with the appropriate levels of risk and reward. For example, if an investor has the ability to invest in equities over the long term, that provides the investor with the potential to recover from the risks of bear markets and participate in bull markets, while if an investor can only invest in a short time frame, the same equities have a higher risk proposition.

Investors use the risk-return trade-off as one of the essential components of each investment decision, as well as to assess their portfolios as a whole. At the portfolio level, the risk-return trade-off can include assessments of the concentration or the diversity of holdings and whether the mix presents too much risk or a lower-than-desired potential for returns.

When an investor considers high-risk-high-return investments, the investor can apply the risk-return trade-off to the vehicle on a singular basis as well as within the context of the portfolio as a whole.

That said, the risk-return trade-off also exists at the portfolio level. For example, a portfolio composed of all equities presents both higher risk and higher potential returns. Within an all-equity portfolio, risk and reward can be increased by concentrating investments in specific sectors or by taking on single positions that represent a large percentage of holdings. For investors, assessing the cumulative risk-return trade-off of all positions can provide insight on whether a portfolio assumes enough risk to achieve long-term return objectives or if the risk levels are too high with the existing mix of holdings.

The following metrics have been calculated for Mr. John Lam using the given data over the past 11 years:

	in percentages	in USD terms
Average (expected) yearly return	9.07%	7,25,341
Volatility of yearly return	7.29%	5,83,522
Lowest expected return in 68% of the time	1.77%	1,41,819
Highest expected return in 68% of the time	16.36%	13,08,863

STRATEGIC ASSET ALLOCATION

Strategic asset allocation is a portfolio strategy. The investor sets target allocations for various asset classes and rebalances the portfolio periodically. The portfolio is rebalanced to the original allocations when they deviate significantly from the initial settings due to differing returns from the various assets.

In strategic asset allocation, the target allocations depend on several factors: the investor's risk tolerance, time horizon, and investment objectives. Also, the allocations may change over time as the parameters change. Strategic asset allocation is compatible with a buy-and-hold strategy as opposed to tactical asset allocation, which is more suited to an active trading approach. Strategic and tactical asset allocation styles are based on modern portfolio theory, which emphasizes diversification to reduce risk and improve portfolio returns.

The reduction of risk due to diversification is really at the heart of the portfolio construction.

TACTICAL ASSET ALLOCATION

Tactical asset allocation is an active management portfolio strategy that shifts the percentage of assets held in various categories to take advantage of market pricing anomalies or strong market sectors. This strategy allows portfolio managers to create extra value by taking advantage of certain situations in the marketplace. It is a moderately active strategy since managers return to the portfolio's original asset mix once reaching the desired short-term profits.

Tactical asset allocation is the process of taking an active stance on the strategic asset allocation itself and adjusting long-term target weights for a short period to capitalize on the market or economic opportunities. For example, assume that data suggests that there will be a substantial increase in demand for commodities over the next 18 months. It may be prudent for an investor to shift more capital into that asset class to take advantage of the opportunity.

Tactical shifts may also come within an asset class. Assume the 45% strategic allocation of stocks consists of 30% large-cap and 15% small-cap holdings. If the outlook for small-cap stocks does not look favourable, it may be a wise tactical decision to shift the allocation within stocks to 40% large-cap and 5% small-cap for a short time until conditions change.

Usually, tactical shifts range from 5% to 10%, though they may be lower. In practice, it is unusual to adjust any asset class by more than 10% tactically. This large adjustment would show a fundamental problem with the construction of the strategic asset allocation.

Tactical asset allocation is different from rebalancing a portfolio. During rebalancing, trades are made to bring the portfolio back to its desired strategic asset allocation. Tactical asset allocation adjusts the strategic asset allocation for a short time, with the intention of reverting to the strategic allocation once the short-term opportunities disappear.

FED MODEL

The model can be used as valuation tool to help allocating between equities and bonds.

Chairman Alan Greenspan in 1997 stated:

"...changes in this ratio [P/E of S&P 500 index] have often been inversely related to changes in the long term treasury yields, but this year's stock price gains were not matched by a significant decline in interest rates. As a result, the yield on ten-year treasury notes now exceeds the ratio of twelve month ahead earnings to prices by the largest amount since 1991, when earnings were depressed by the economic slowdown."

Designing a Tactical Asset Allocation for Mr. John Lam using the FED valuation model as a valuation tool on the given set of data:

	DATE	WORLD BONDS INDEX	WORLD BONDS INDEX	WORLD BONDS INDEX	WORLD EQUITIES INDEX	WORLD EQUITIES INDEX
		price	yield	(holding) return	price	P/E ratio
1	01-01- 2050	100	7.5416		100	14.793
2	01-02- 2050	98.5374677	7.6786	-1.46%	102.7858681	15.617
3	01-03- 2050	98.60465116	7.8368	0.07%	101.7153902	15.446
4	01-04- 2050	97.23514212	7.8159	-1.39%	102.1575178	15.091
5	01-05- 2050	98.52196382	7.7562	1.32%	103.6309396	11.61
6	01-06- 2050	96.4444444	7.6266	-2.11%	101.2627599	12.176
7	01-07- 2050	98.38242894	7.4302	2.01%	101.0650245	13.299
8	01-08- 2050	102.8630491	7.4484	4.55%	110.6843787	14.926
9			7.5198	-3.36%	108.0461558	15.902
10			7.5483	1.90%	110.9061494	15.62
11	01-11- 102.1395349 2050		7.6323	0.84%	106.9441695	15.728
12	01-12- 2050	103.0645995	7.6618	0.91%	111.5902453	15.589
13	01-01- 2051	104.3255814	8.0249	1.22%	114.5891991	16.007
14	01-02- 2051	102.9457364	8.3679	-1.32%	109.3820313	17.448
15	01-03- 2051	101.3643411	8.6251	-1.54%	103.1439732	16.572
16	01-04- 2051	100.3617571	8.5903	-0.99%	94.59327901	15.171
17	01-05- 2051	100.0516796	8.4862	-0.31%	96.52862215	12.08
18	01-06- 2051	103.374677	8.3588	3.32%	106.6442338	12.304
19	01-07- 2051	105.2713178	8.3552	1.83%	105.62526	13.454
20	01-08- 2051	108.5684755	8.6884	3.13%	105.590722	15.039
21	01-09- 2051	107.7209302	8.9134	-0.78%	94.90957492	14.697
22	01-10- 2051	108.9250646	8.7913	1.12%	86.81938817	13.251
23	01-11- 2051	113.7932817	8.5809	4.47%	92.14552035	11.908
24	01-12- 2051	115.6795866	8.2524	1.66%	92.08371541	13.015
25	01-01- 2052	116.8217054	8.2635	0.99%	93.21781598	13.202

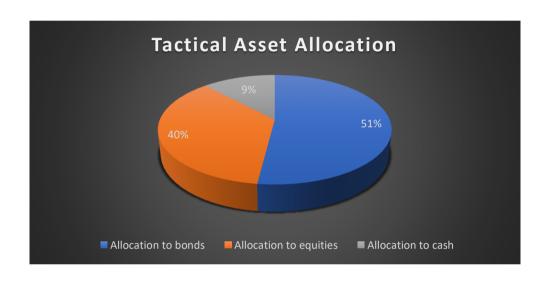
26	01-02- 2052	119.7416021	7.9137	2.50%	96.43813648	13.833
27	01-03- 2052	119.7777778	8.0614	0.03%	103.9815716	15.205
28	01-04- 2052	115.4263566	7.953	-3.63%	101.3045691	15.943
29	01-05- 2052	117.2041344	7.9875	1.54%	104.1686023	14.394
30	01-06- 2052	117.0542636	8.0939	-0.13%	103.9409743	14.055
31	01-07- 2052	115.8294574	8.0873	-1.05%	99.43527245	16.195
32	01-08- 2052	118.3049096	7.8818	2.14%	102.2690091	15.898
33	01-09- 2052	120.5943152	7.661	1.94%	102.2645656	16.141
34	01-10- 2052	125.3126615	7.5329	3.91%	104.8795611	16.196
35	01-11- 2052	126.625323	7.5023	1.05%	105.9657932	16.413
36	01-12- 2052	128.6046512	7.3929	1.56%	100.8652693	16.663
37	01-01- 2053	135.2918863	7.1701	5.20%	108.1311881	15.786
38	01-02- 2053	132.8888372	7.2827	-1.78%	105.8946973	16.842
39	01-03- 2053	132.1498708	7.4083	-0.56%	104.0563031	16.257
40	01-04- 2053	130.749354	7.2746	-1.06%	97.18565317	15.826
41	01-05- 2053	131.6847545	7.2616	0.72%	99.86487742	14.273
42	01-06- 2053	135.7260465	7.3193	3.07%	103.6392207	14.833
43	01-07- 2053	139.5245478	7.1898	2.80%	101.1207701	14.664
44	01-08- 2053	142.7750904	7.038	2.33%	100.1191664	15.159
45	01-09- 2053	146.7700258	6.9375	2.80%	102.3158677	14.572
46	01-10- 2053	148.2428424	7.0169	1.00%	100.7911437	15.409
47	01-11- 2053	144.2168475	6.921	-2.72%	98.34015342	15.462
48	01-12- 2053	141.9275969	6.9536	-1.59%	99.48051528	16.046
49	01-01- 2054	142.7750904	6.7611	0.60%	100.4092053	16.455
50	01-02- 2054	144.4924031	6.5398	1.20%	100.7634729	16.621
51	01-03- 2054	148.4455814	6.3081	2.74%	102.8385841	16.875
52	01-04- 2054	150.9177778	6.2768	1.67%	109.4179832	17.472
53	01-05- 2054	154.1314729	6.3688	2.13%	113.3947074	16.767
54	01-06- 2054	155.1487855	6.2293	0.66%	116.0597933	16.911
55	01-07- 2054	154.9235659	5.9772	-0.15%	114.4623576	17.268
56	01-08- 2054	156.1457881	5.7663	0.79%	116.990705	18.767
57	01-09- 2054	160.0396899	5.5506	2.49%	121.5933558	19.313
58	01-10- 2054	162.0394832	5.3092	1.25%	119.6753826	19.21
59	01-11- 2054	160.852093	5.4252	-0.73%	121.9995314	19.226
60	01-12- 2054	160.4229974	5.2932	-0.27%	117.5497772	19.16
61	01-01- 2055	161.4603618	5.1231	0.65%	120.960158	18.872
62	01-02- 2055	163.7713178	5.2959	1.43%	129.4720726	19.443
63	01-03- 2055	160.6791214	5.8047	-1.89%	126.0528049	19.48
64	01-04-	160.7080103	5.9994	0.02%	120.7583831	19.454

65	01-05- 2055	162.0803618	6.2216	0.85%	124.7138996	16.712
66	01-06- 2055	159.9968992	6.4294	-1.29%	124.9130489	16.73
67	01-07- 2055	162.6340052	6.4943	1.65%	123.9215441	17.162
68	01-08- 2055	165.034522	6.6935	1.48%	127.49694	17.432
69	01-09- 2055	163.8082687	6.8317	-0.74%	129.7782697	17.773
70	01-10- 2055	163.9554005	6.9512	0.09%	125.6242098	17.493
71	01-11- 2055	167.56677	7.0442	2.20%	129.2513118	17.135
72	01-12- 2055	164.9704393	6.9785	-1.55%	122.9807354	16.698
73	01-01- 2056	165.5143669	7.0215	0.33%	124.929611	15.908
74	01-02- 2056	168.5002067	6.8869	1.80%	122.9676069	15.819
75	01-03- 2056	173.609354	6.7484	3.03%	123.9162927	15.52
76	01-04- 2056	184.222222	6.4927	6.11%	128.5512597	15.011
77	01-05- 2056	186.9565891	6.2186	1.48%	134.5709808	14.363
78	01-06- 2056	191.9687339	5.9695	2.68%	135.6697354	14.773
79	01-07- 2056	194.1951421	5.9296	1.16%	135.7533538	14.944
80	01-08- 2056	193.5796899	6.0608	-0.32%	140.7242086	15.678
81	01-09- 2056	188.0610853	5.7752	-2.85%	138.766446	15.734
82	01-10- 2056	190.8613437	5.754	1.49%	140.7866194	15.853
83	01-11- 2056	192.651938	5.6523	0.94%	139.4103485	15.719
84	01-12- 2056	195.1421705	5.4175	1.29%	145.0442935	15.557
85	01-01-	197.0217571	5.3796	0.96%	148.3076351	16.224
86	2057 01-02-	194.4878553	5.4719	-1.29%	151.1878264	16.354
87	2057 01-03-	194.2746253	5.786	-0.11%	152.0286565	16.806
88	2057 01-04- 2057	193.2636176	5.7395	-0.52%	154.609518	16.35
89	01-05-	192.4126098	5.7565	-0.44%	156.563039	15.055
90	2057 01-06- 2057	192.771938	5.8531	0.19%	156.2715863	15.398
91	01-07- 2057	194.0347804	5.8138	0.66%	158.1909732	16.777
92	01-08-	198.5001034	5.6549	2.30%	153.3835179	16.28
93	2057 01-09-	198.0347804	5.582	-0.23%	152.8189923	16.533
94	2057 01-10-	199.8124031	5.3643	0.90%	159.3384043	16.814
95	2057 01-11-	202.9092506	5.1063	1.55%	159.9154524	17.13
96	2057 01-12-	205.8487855	5.0851	1.45%	167.9713031	17.232
97	2057 01-01-	204.1540568	5.1454	-0.82%	165.694215	17.134
98	2058 01-02-	198.5775711	4.9842	-2.73%	167.3399232	17.543
99	2058 01-03-	196.8568475	5.168	-0.87%	169.1348923	17.947
100	2058 01-04-	195.6737468	5.2522	-0.60%	164.3490485	17.573
	2058 01-05-	194.921137	5.1663	-0.38%	171.1243653	16.912
101						
101	2058 01-06- 2058	198.6610853	5.0269	1.92%	181.3246052	18.308

104	01-08- 2058	198.623876	4.8734	-1.68%	196.4270277	19.896
105	01-09- 2058	199.4905426	4.7405	0.44%	184.1811652	19.838
106	01-10- 2058	204.3429457	4.6514	2.43%	195.6346722	19.213
107	01-11- 2058	207.3854264	4.5022	1.49%	187.5456973	19.607
108	01-12- 2058	204.2331783	4.4088	-1.52%	190.1479683	18.261
109	01-01- 2059	204.6325065	4.2144	0.20%	189.1697939	18.623
110	01-02- 2059	206.6642377	4.2286	0.99%	197.8996417	18.525
111	01-03- 2059	208.6319897	4.1638	0.95%	208.4244586	20.227
112	01-04- 2059	206.4047028	4.1516	-1.07%	216.5889729	21.024
113	01-05- 2059	210.0969509	4.1767	1.79%	218.9141315	21.696
114	01-06- 2059	210.2228941	3.9701	0.06%	213.4082399	21.092
115	01-07- 2059	209.6057881	4.0445	-0.29%	222.0585087	20.537
116	01-08- 2059	210.2575711	3.8794	0.31%	215.8198446	22.017
117	01-09- 2059	218.2309561	3.4644	3.79%	192.9976611	20.476
118	01-10- 2059	230.3202584	3.3283	5.54%	186.5131911	19.036
119	01-11- 2059	234.9567959	3.4119	2.01%	213.6120346	18.386
120	01-12- 2059	232.5546253	3.3348	-1.02%	220.4366338	20.992
121	01-01- 2060	235.9501292	3.3944	1.46%	232.2637981	21.342
122	01-02- 2060	233.1614987	3.6862	-1.18%	237.3665437	22.716
123	01-03- 2060	224.8213437	3.6957	-3.58%	228.7174868	22.323
124	01-04- 2060	226.3796899	3.616	0.69%	241.3717467	23.438
125	01-05- 2060	226.3602584	3.7613	-0.01%	251.051492	24.094
126	01-06- 2060	222.2790181	4.0237	-1.80%	239.6708988	23.484
127	01-07- 2060	218.7122997	4.0944	-1.60%	253.6208408	23.431
128	01-08- 2060	223.6181912	4.3049	2.24%	248.9769867	24.305
129	01-09- 2060	225.7271318	4.3383	0.94%	251.5713807	22.981
130	01-10- 2060	229.2837726	4.4441	1.58%	246.503577	22.937
131	01-11- 2060	228.7541085	4.2685	-0.23%	257.790251	22.249
132	01-12- 2060	226.7203618	4.4159	-0.89%	267.4885782	23.768
133	01-01- 2061	227.3852713	4.7087	0.29%	287.2485892	24.296

Using the above set of data and applying the FED model as a valuation tool, it can be inferred that the allocation to bonds has to be increased by decreasing the allocation to equities in Tactical Asset Allocation (TAA) since the earnings yield of the long term government bond comes up to be 6.1634% whereas the earnings yield of the stock market is 5.8038%.

[John Lam]'s TAA	Max. pos. deviation for SAA	Max. neg. deviation from SAA
51%	+9%	-9%
40%	+11%	-11%
9%	+5%	-5%
100%		



	in percentages	in USD terms
Average (expected) yearly return	6.16%	4,95,800
Volatility of yearly return	8.22%	6,12,957
Lowest expected return in 68% of the time	-2.06%	-1,17,157
Highest expected return in 68% of the time	14.38%	11,08,757

Three additional years of data corresponding to the three years since the meeting with the client Mr. John have been added to the "Data" sheet. The three years data is as follows:

DATE	WORLD	WORLD	WORLD	WORLD	WORLD	WORLD	3-MONTHS	3-MONTHS
	BONDS INDEX	BONDS INDEX	BONDS INDEX	EQUITIES	EQUITIES	EQUITIES	CASH USD	CASH USD
				INDEX	INDEX	INDEX		
	price	yield	(holding) return	price	P/E ratio	(holding) return		(holding) return
01-	220.6163307	4.6891	-2.98%	272.4366095	25.039	-5.16%	178.2987223	0.42%
02-								
2061								
01-	221.412093	4.5106	0.36%	274.4931388	24.48	0.75%	179.1391852	0.47%
03-								
2061 01-	225 0771050	4.3484	1.66%	288.2089896	24.299	5.00%	179.979648	0.47%
01-	225.0771059	4.5464	1.00%	200.2009090	24.299	3.00%	1/3.3/3046	0.47%
2061								
01-	218.1672351	4.5494	-3.07%	278.6298288	23.909	-3.32%	180.8577997	0.49%
05-								
2061								
01-	220.9585013	4.3415	1.28%	273.9055879	24.187	-1.70%	181.7058003	0.47%
06-								
2061	225 2420044	4.4270	1.040/	200 5450005	22.050	2.440/	102 507721	0.400/
01- 07-	225.2428941	4.4279	1.94%	280.5158895	23.958	2.41%	182.587721	0.49%
2061								
01-	222.4825323	4.3634	-1.23%	271.346338	24.093	-3.27%	183.4922549	0.50%
08-								
2061								
01-	222.4287855	4.3935	-0.02%	281.7889502	23.497	3.85%	184.4043267	0.50%
09-								
2061	240 2055020	4 202	4.250/	254 0225505	22.00	6.200/	405.2504520	0.530/
01- 10-	219.3955039	4.293	-1.36%	264.0325506	23.88	-6.30%	185.3691629	0.52%
2061								
01-	218.586615	4.2552	-0.37%	260.1883233	21.868	-1.46%	186.3189236	0.51%
11-								3.32/
2061								
01-	221.5324548	3.9563	1.35%	244.4991578	22.498	-6.03%	187.2988354	0.53%
12-								
2061	222 1727 121	2 22 44	0.500/	245 5540555		2 222/	100.0505=1=	2.500/
01- 01-	229.4735401	3.9241	3.58%	246.6649566	22.33	0.89%	188.2636717	0.52%
2062								
01-	231.2180879	3.9245	0.76%	252.3063748	21.56	2.29%	189.0777522	0.43%
02-								
2062								
01-	230.7753488	3.6601	-0.19%	229.6869761	21.333	-8.97%	189.9106773	0.44%
03-								
2062	224 4404205	2.0024	4.050/	242 4042200	10.440	7.630/	100 6200722	0.200/
01- 04-	221.4181395	3.9034	-4.05%	212.1812299	19.448	-7.62%	190.6380733	0.38%
2062								
01-	223.0516796	4.0421	0.74%	232.8984096	20.558	9.76%	191.3353183	0.37%
05-								
2062	1							
01-	221.448062	3.9227	-0.72%	226.7469996	21.359	-2.64%	191.9534165	0.32%
206-								
2062 01-	219.2751421	3.9646	-0.98%	221.2471673	20.816	-2.43%	192.5526703	0.31%
07-	213.2/31421	3.3040	-0.36%	221.24/10/3	20.610	-2.43/0	132.3320703	0.31%
2062								
01-	224.8084755	3.8357	2.52%	217.2609502	20.444	-1.80%	193.1406173	0.31%
-80								
2062								
01-	232.9102842	3.6754	3.60%	203.9852072	20.293	-6.11%	193.6946444	0.29%
09-								
2062	235.0245478	3.6218	0.91%	186.2185067	17.444	-8.71%	194.1996759	0.26%
10-	233.0243478	3.0218	0.51/0	100.210300/	17.444	-0./1/0	137.1330/33	0.20%
2062								
01-	238.2948837	3.6015	1.39%	193.761134	19.965	4.05%	194.6142539	0.21%
11-								
2062	ĺ			ĺ	1			Ì

01-	232.6312145	3.8415	-2.38%	199.4073996	21.449	2.91%	194.9534542	0.17%
12-	252.0512145	3.0413	2.3070	155.4075550	21.443	2.5170	154.5554542	0.1770
2062								
01-	227.2018088	3.7708	-2.33%	202.6871013	21.764	1.64%	195.2587344	0.16%
01-	2271202000	5.7,00	2.0070	202.007.1015	22.701	2.0.70	13512507511	0.2075
2063								
01-	223.2168475	3.8344	-1.75%	195.4013888	21.081	-3.59%	195.5187879	0.13%
02-								
2063								
01-	224.0795866	4.0589	0.39%	198.0848546	20.815	1.37%	195.8089926	0.15%
03-								
2063								
01-	223.9214987	3.9629	-0.07%	202.996732	21.457	2.48%	196.0916594	0.14%
04-								
2063								
01-	232.8141602	4.0088	3.97%	196.96772	20.854	-2.97%	196.385633	0.15%
05-								
2063								
01-	238.7176744	3.7963	2.54%	192.6583398	20.124	-2.19%	196.6682999	0.14%
06-								
2063								
01-	249.24677	3.6642	4.41%	181.1381805	18.391	-5.98%	196.9547356	0.15%
07-								
2063								
01-	252.8481654	3.4058	1.44%	162.8309897	16.409	-10.11%	197.2411714	0.15%
08-								
2063								
01-	257.617416	3.194	1.89%	166.9604085	16.632	2.54%	197.5125316	0.14%
09-								
2063								
01-	257.9408269	3.27	0.13%	152.6206509	15.816	-8.59%	197.7876606	0.14%
10-								
2063								
01-	258.6313695	3.2619	0.27%	161.3502967	15.913	5.72%	198.0401764	0.13%
11-								
2063								
01-	257.0839793	3.2012	-0.60%	167.9971562	16.039	4.12%	198.2738477	0.12%
12-								
2063								
01-	271.4941085	3.1296	5.61%	160.0091698	16.145	-4.75%	198.4924434	0.11%
01-								
2064								

The updated summary statistics for the Strategic Asset Allocation by including the above additional 3 years of data are as follows:

Average (expected) yearly return	5.93%	\$4,74,059
Volatility of yearly return	9.01%	\$7,20,291
Lowest expected return in 68% of the time	-3.08%	-\$2,46,232
Highest expected return in 68% of the time	14.93%	\$11,94,351

VS

Previous summary statistics excluding the additional 3 years of data:

Average (expected) yearly return	9.07%	\$7,25,341
Volatility of yearly return	7.29%	\$5,83,522
Lowest expected return in 68% of the time	1.77%	\$1,41,819
Highest expected return in 68% of the time	16.36%	\$13,08,863

From the above set of summary statistics, it can be inferred that:

- The average yearly returns decreased due to the net fall in the return of the equity index for the last 3 years.
- The yearly volatilities increased due to the net fall in the return of the equity index for the last 3 years.
- The asset class responsible for these changes is the equities asset class.

Since we had already predicted the overvaluation of the equities asset class in our previous meeting using the FED valuation model, we had thus developed an optimal tactical asset allocation for Mr. John Lam considering the above factors and reducing the allocation to equities, hence optimizing the returns.

Summary statistics of Total Asset Allocation devised for Mr. John Lam:

Average (expected) yearly return	6.16%	4,95,800
Volatility of yearly return	8.22%	6,12,957
Lowest expected return in 68% of the time	-2.06%	-1,17,157
Highest expected return in 68% of the time	14.38%	11,08,757

VS
Summary statistics of Strategic Asset Allocation without TAA:

Average (expected) yearly return	5.93%	4,74,059
Volatility of yearly return	9.01%	7,20,291
Lowest expected return in 68% of the time	-3.08%	-2,46,232
Highest expected return in 68% of the time	14.93%	11,94,351

VALUE-AT-RISK

Value at risk (VaR) is a statistic that measures and quantifies the level of financial risk within a firm, portfolio, or position over a specific time frame. This metric is most commonly used by investment and commercial banks to determine the extent and occurrence ratio of potential losses in their institutional portfolios. Risk managers use VaR to measure and control the level of risk exposure. One can apply VaR calculations to specific positions or whole portfolios or to measure firm-wide risk exposure.

VaR modelling determines the potential for loss in the entity being assessed and the probability of occurrence for the defined loss. One measures VaR by assessing the amount of potential loss, the probability of occurrence for the amount of loss, and the timeframe.

HISTORICAL APPROACH (For Asymmetric distributions)

- From a history of portfolio loss returns, compute the 99th percentile of the distribution of these historical returns.
- In other words, find the loss return so that only 1% of the historical loss returns are larger than this number.

VARIANCE-COVARIANCE APPROACH (For Symmetric distributions)

- This method assumes that stock returns are normally distributed. In other words, it requires that we estimate only two factors—an expected (or average) return and a standard deviation—which allow us to plot a normal distribution curve.
- The idea behind the variance-covariance is similar to the ideas behind the historical method—except that we use the familiar curve instead of actual data.

VaR (
$$a_1, a_2, ..., a_n, \alpha$$
) = - $\mu + z_{\alpha} \sigma$

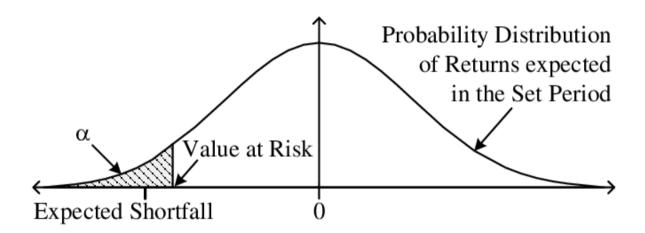
WHERE μ is the average of the portfolio returns

σ is the standard deviation of the returns

 α is the confidence level and z_α is the quantile of gaussian distribution

EXPECTED SHORTFALL

Expected shortfall (ES) is a risk measure—a concept used in the field of financial risk measurement to evaluate the market risk or credit risk of a portfolio. The "expected shortfall at q% level" is the expected return on the portfolio in the worst of cases. ES is an alternative to value at risk that is more sensitive to the shape of the tail of the loss distribution.



- The Expected Shortfall is the average of the losses that are beyond the 99^{th} percentile of the loss distribution assuming α =99% .
- Suppose the VaR is equal to \$1 million, then the Expected Shortfall is the average of the losses that exceed \$1 million.

HISTORICAL APPROACH

- From a history of portfolio loss returns, compute the sum of the loss returns that are above VaR.
- \circ Then divide this sum by the total number of portfolio loss returns times (1- α).

VARIANCE-COVARIANCE APPROACH

- o This method assumes that stock returns are normally distributed.
- The idea behind the variance-covariance is similar to the ideas behind the historical method—except that we use the familiar curve instead of actual data.

ES
$$(a_1, a_2, ..., a_n, \alpha) = -\mu + \sigma \phi(z_{\alpha}) / (1-\alpha)$$

WHERE μ is the average of the portfolio returns

σ is the standard deviation of the returns

 α is the confidence level and z_α is the quantile of gaussian distribution

 $\varphi(\,z_{\alpha})$ is the density of the gaussian distribution

RISK MANAGEMENT

Risk management: Variance-covariance approach:

Risk management: Variance- covariance approach	In Percentages	In USD terms
Average return (μ)	0.50%	39,868
Standard deviation of returns (σ)	2.14%	1,71,429
Value-at-risk (95%)	-3.04%	-2,42,990
Phi	0.1023	
Expected shortfall (95%)	-3.89%	-3,10,756

- The Value-at-risk calculated here indicates that there is a 5% chance of losing more than -2.80% in returns or \$2,24,351.
- The Expected Shortfall calculated here indicates that the average return might be -3.60% in the 5% of worst months.

Risk management: Historical approach

Risk management: Historical approach	In Percentages	In USD terms
Value-at-risk (95%)	-3.21%	-2,56,969
Sum of returns that are below the VaR	-42.64%	
Expected shortfall (95%)	-5.08%	-4,06,112

- The Value-at-risk calculated here indicates that there is a 5% chance of losing more than -2.90% in returns or \$2,32,263.
- The Expected Shortfall calculated here indicates that the average return might be -3.32% in the 5% of worst months.

The risk management quantities computed through the variance-covariance and historical approaches are not equal.

It can be inferred that the returns of the SAAs (and our client's TAA) are not normally distributed (otherwise, both approaches would have yielded the same numbers).

Three additional years of data have been added to the "Data" sheet for devising an appropriate Tactical Asset Allocation strategy. The three years data is as follows:

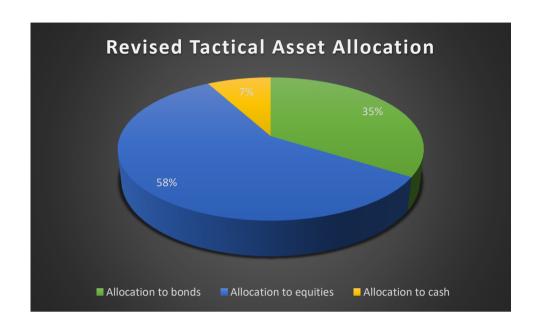
DATE	WORLD BONDS INDEX	WORLD BONDS INDEX	WORLD BONDS INDEX	WORLD EQUITIES	WORLD EQUITIES	WORLD EQUITIES	3-MONTHS CASH USD	3-MONTHS CASH USD
	price	yield	(holding)	INDEX price	INDEX P/E ratio	(holding)		(holding)
01- 02-	220.6163307	4.6891	-2.98%	272.4366095	25.039	-5.16%	178.2987223	return 0.42%
01- 03-	221.412093	4.5106	0.36%	274.4931388	24.48	0.75%	179.1391852	0.47%
01- 04-	225.0771059	4.3484	1.66%	288.2089896	24.299	5.00%	179.979648	0.47%
01- 05-	218.1672351	4.5494	-3.07%	278.6298288	23.909	-3.32%	180.8577997	0.49%
01- 06-	220.9585013	4.3415	1.28%	273.9055879	24.187	-1.70%	181.7058003	0.47%
01- 07-	225.2428941	4.4279	1.94%	280.5158895	23.958	2.41%	182.587721	0.49%
2061 01- 08- 2061	222.4825323	4.3634	-1.23%	271.346338	24.093	-3.27%	183.4922549	0.50%
01- 09- 2061	222.4287855	4.3935	-0.02%	281.7889502	23.497	3.85%	184.4043267	0.50%
01- 10- 2061	219.3955039	4.293	-1.36%	264.0325506	23.88	-6.30%	185.3691629	0.52%
01- 11- 2061	218.586615	4.2552	-0.37%	260.1883233	21.868	-1.46%	186.3189236	0.51%
01- 12- 2061	221.5324548	3.9563	1.35%	244.4991578	22.498	-6.03%	187.2988354	0.53%
01- 01- 2062	229.4735401	3.9241	3.58%	246.6649566	22.33	0.89%	188.2636717	0.52%
01- 02- 2062	231.2180879	3.9245	0.76%	252.3063748	21.56	2.29%	189.0777522	0.43%
01- 03- 2062	230.7753488	3.6601	-0.19%	229.6869761	21.333	-8.97%	189.9106773	0.44%
01- 04- 2062	221.4181395	3.9034	-4.05%	212.1812299	19.448	-7.62%	190.6380733	0.38%
01- 05- 2062	223.0516796	4.0421	0.74%	232.8984096	20.558	9.76%	191.3353183	0.37%
01- 06- 2062	221.448062	3.9227	-0.72%	226.7469996	21.359	-2.64%	191.9534165	0.32%
01- 07- 2062	219.2751421	3.9646	-0.98%	221.2471673	20.816	-2.43%	192.5526703	0.31%
01- 08- 2062	224.8084755	3.8357	2.52%	217.2609502	20.444	-1.80%	193.1406173	0.31%
01- 09- 2062	232.9102842	3.6754	3.60%	203.9852072	20.293	-6.11%	193.6946444	0.29%

101- 235.0245478 3.6218 0.991% 186.2185067 17.444 -8.71% 194.1996759 0.26% 2062 238.2948837 3.6015 1.39% 193.761134 19.965 4.05% 194.6142539 0.21% 2062 227.2018088 3.7708 -2.38% 199.4073996 21.449 2.91% 194.9534542 0.17% 12.2062 227.2018088 3.7708 -2.33% 202.6871013 21.764 1.64% 195.2587344 0.16% 01-2063 223.2168475 3.8344 -1.75% 195.4013888 21.081 -3.59% 195.5187879 0.13% 02-2063 01-224.0795866 4.0589 0.39% 198.0848546 20.815 1.37% 195.8089926 0.15% 03-2063 01-223.214987 3.9629 -0.07% 202.996732 21.457 2.48% 196.0916594 0.14% 04-2063 232.8141602 4.0088 3.97% 196.96772 20.854 -2.97% 196.385633 0.15% 0.5263 0.1-224.074744 3.7963 2.54% 192.6583398 20.124 -2.19% 196.6682999 0.14% 0.6662099 0.14% 0.6662099 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15% 0.15%									
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01-	2063								
	01-	271.4941085	3.1296	5.61%	160.0091698	16.145	-4.75%	198.4924434	0.11%
2064	01-								
	2064								

Using the above set of data and applying the FED model as a valuation tool, it can be inferred that the allocation to equities has to be increased by decreasing the allocation to bonds in Tactical Asset Allocation (TAA) since the earnings yield of the long-term government bond comes up to be 3.9056% whereas the earnings yield of the stock market is 4.7990%.

The recent collapse of the equity market increased the risk of your portfolio beyond our previous estimates. This translates into a jump in the yearly volatility of the returns of portfolio of nearly 1%. On the other hand, this fall in the price of equities opens the door for attractive investment opportunities and I would like to suggest the following adjustments to your portfolio.

TACTICAL ASSET ALLOCATION



Summary Statistics:

	in percentages	in USD terms
Average (expected) yearly return	5.69%	4,55,232
Volatility of yearly return	10.55%	8,43,835
Lowest expected return in 68% of the time	-4.86%	-3,88,603
Highest expected return in 68% of the time	16.24%	12,99,067

Risk management: Variance-covariance approach

	in percentages	in USD terms
Average return (μ)	0.46%	36,719
Standard deviation of returns (σ)	2.71%	2,16,573
Value-at-risk (95%)	-4.01%	-3,20,626
Phi	0.1023	
Expected shortfall (95%)	-5.08%	-4,06,236

Risk management: Historical approach

	in percentages	in USD terms
Value-at-risk (95%)	-4.62%	-3,69,820
Sum of returns that are below the VaR	-42.02%	
Expected shortfall (95%)	-5.00%	-4,00,208

Two additional years of data corresponding to the two years since the meeting with the client Mr. John have been added to the "Data" sheet. The two years data is as follows:

DATE	WORLD BONDS INDEX	WORLD BONDS INDEX	WORLD BONDS INDEX	WORLD EQUITIES INDEX	WORLD EQUITIES INDEX	WORLD EQUITIES INDEX	3-MONTHS CASH USD	3-MONTHS CASH USD
	price	yield	(holding) return	price	P/E ratio	(holding) return		(holding) return
01- 02- 2064	274.6984496	2.998	1.18%	156.440843	16.34	-2.23%	198.6733502	0.09%
01- 03- 2064	280.4414987	2.9241	2.09%	152.0304743	15.189	-2.82%	198.8768703	0.10%
01- 04- 2064	279.9020155	3.039	-0.19%	152.8234358	15.195	0.52%	199.0653149	0.09%
01- 05- 2064	285.3536951	2.7619	1.95%	164.6015197	15.528	7.71%	199.2575284	0.10%
01- 06- 2064	295.3397416	2.5086	3.50%	174.8132723	16.222	6.20%	199.4384352	0.09%
01- 07- 2064	292.7466667	3.0425	-0.88%	176.6151087	17.216	1.03%	199.6118042	0.09%
01- 08- 2064	282.3012403	3.3009	-3.57%	177.8990762	16.978	0.73%	199.7776354	0.08%
01- 09- 2064	280.0940052	3.3416	-0.78%	183.9282901	16.68	3.39%	199.9283911	0.08%
01- 10- 2064	298.1754522	3.4103	6.46%	187.5143909	17.293	1.95%	200.0904534	0.08%
01- 11- 2064	291.4880103	3.3792	-2.24%	195.2795967	17.258	4.14%	200.244978	0.08%
01- 12- 2064	299.0484238	3.3677	2.59%	199.6081647	16.813	2.22%	200.4070403	0.08%
01- 01- 2065	311.9760207	3.2119	4.32%	209.3123493	17.052	4.86%	200.5653337	0.08%
01- 02- 2065	313.3260465	3.2012	0.43%	213.2149479	17.595	1.86%	200.7123205	0.07%
01- 03- 2065	313.6301292	3.0624	0.10%	218.3526356	17.58	2.41%	200.870614	0.08%
01- 04- 2065	318.6463049	3.4139	1.60%	215.8053023	16.969	-1.17%	201.0213696	0.08%

01-	303.915969	3.5924	-4.62%	210.3993892	17.009	-2.50%	201.183432	0.08%
05-								
2065								
01-	306.5497674	3.6458	0.87%	210.3844429	15.755	-0.01%	201.3492632	0.08%
06-								
2065								
01-	307.8798966	3.5456	0.43%	213.3785492	16.072	1.42%	201.5414767	0.10%
07-								
2065								
01-	306.3193798	3.3459	-0.51%	207.947793	15.682	-2.55%	201.7600724	0.11%
08-								
2065								
01-	313.3128165	3.2899	2.28%	208.9140507	15.077	0.46%	201.9975125	0.12%
09-								
2065								
01-	316.2424806	3.1917	0.94%	214.6705958	15.354	2.76%	202.2688727	0.13%
10-								
2065								
01-	326.6466667	3.2047	3.29%	217.2498414	15.216	1.20%	202.5553085	0.14%
11-								
2065								
01-	338.7039276	3.0668	3.69%	230.1466757	15.673	5.94%	202.8907398	0.17%
12-								
2065								
01-	342.2689922	3.1066	1.05%	234.6032971	15.6	1.94%	203.2525534	0.18%
01-								
2066								

PERFORMANCE RATIOS

SHARPE RATIO

The Sharpe ratio was developed by Nobel laureate William F. Sharpe and is used to help investors understand the return of an investment compared to its risk.1 2 The ratio is the average return earned in excess of the risk-free rate per unit of volatility or total risk. Volatility is a measure of the price fluctuations of an asset or portfolio.

Subtracting the risk-free rate from the mean return allows an investor to better isolate the profits associated with risk-taking activities. The risk-free rate of return is the return on an investment with zero risk, meaning it's the return investors could expect for taking no risk. The yield for a U.S. Treasury bond, for example, could be used as the risk-free rate.

Generally, the greater the value of the Sharpe ratio, the more attractive the risk-adjusted return.

Sharpe Ratio =
$$\frac{R_p - R_f}{\sigma_p}$$

R_p = Return of portfolio

R_f = Risk-Free rate

 σ_n = Standard deviation of portfolio's excess return

SORTINO RATIO

The Sortino ratio is a variation of the Sharpe ratio that differentiates harmful volatility from total overall volatility by using the asset's standard deviation of negative portfolio returns—downside deviation—instead of the total standard deviation of portfolio returns. The Sortino ratio takes an asset or portfolio's return and subtracts the risk-free rate, and then divides that amount by the asset's downside deviation. The ratio was named after Frank A. Sortino.

The Sortino ratio is a useful way for investors, analysts, and portfolio managers to evaluate an investment's return for a given level of bad risk. Since this ratio uses only the downside deviation as its risk measure, it addresses the problem of using total risk, or standard deviation, which is important because upside volatility is beneficial to investors and isn't a factor most investors worry about.

Sortino Ratio =
$$\frac{\langle R \rangle - R_f}{\sigma_d}$$

Where,

< R > = Expected Return

R_f = The Risk Free Rate of Return

 σ_d = Standard Deviation of Negative Asset Returns

MAR RATIO

MAR ratio is a measurement of returns adjusted for risk that can be used to compare the performance of commodity trading advisors, hedge funds, and trading strategies. The MAR ratio is calculated by dividing the compound annual growth rate (CAGR) of a fund or strategy since its inception by its most significant drawdown. The higher the ratio, the better the risk-adjusted returns.

For example, if Fund A has registered a compound annual growth rate (CAGR) of 30% since inception, and has had a maximum drawdown of 15% in its history, its MAR ratio is 2. If Fund B has a CAGR of 35% and a maximum drawdown of 20%, its MAR ratio is 1.75. While Fund B has a higher absolute growth rate, on a risk-adjusted basis, Fund A would be deemed to be superior because of its higher MAR ratio.

$$\label{eq:market} \text{Mar Ratio} = \frac{\text{Compound Annual Rate of Return}}{\text{Maximum Drawdown}}$$

Summary statistics of Mr. John Lam (before devising an efficient asset allocation strategy) if original asset allocation of 30% bond, 30% equities and 40% cash was followed:

	in percentages	in USD terms
Average (expected) yearly return	2.87%	2,29,576
Volatility of yearly return	7.39%	5,90,918
Lowest expected return in 68% of the time	-4.52%	-3,61,343
Highest expected return in 68% of the time	10.26%	8,20,494

Risk management: Variance-covariance approach

Risk management: Variance-covariance approach	in percentages	in USD terms
Average return (μ)	0.23%	18,489
Standard deviation of returns (σ)	1.56%	1,24,426
Value-at-risk (95%)	-2.34%	-1,86,814
Phi	0.1023	
Expected shortfall (95%)	-2.95%	-2,35,999

Risk management: Historical approach

Risk management: Historical approach	in percentages	in USD terms
Value-at-risk (95%)	-2.54%	-2,03,002
Sum of returns that are below the VaR	-8.46%	-6,76,864
Expected shortfall (95%)	-2.82%	-2,25,621

Performance ratios

Performance ratios	
Average monthly excess return	0.01%
Standard deviation of monthly (excess) returns	1.60%
Sharpe ratio	0.003
Standard deviation of returns below the mean	1.03%
Sortino ratio	0.005
CAGR	2.66%
Biggest drawdown	-3.35%
MAR	0.795

Final summary statistics of Mr. John Lam's portfolio after designing an appropriate Strategic and Tactical Asset Allocation plan for his wealth over the span of 5 -years:

	in percentages	in USD terms
Average (expected) yearly return	4.40%	3,52,054
Volatility of yearly return	12.45%	9,96,244
Lowest expected return in 68% of the time	-8.05%	-6,44,190
Highest expected return in 68% of the time	16.85%	13,48,298

Risk management: Variance-covariance approach

Risk management: Variance- covariance approach	in percentages	in USD terms
Average return (μ)	0.34%	27,185
Standard deviation of returns (σ)	2.31%	1,84,936
Value-at-risk (95%)	-3.47%	-2,77,959
Phi	0.1023	
Expected shortfall (95%)	-4.39%	-3,51,064

Risk management: Historical approach

Risk management: Historical approach in percentages in USD terms

Value-at-risk (95%)	-3.53%	-2,82,672
Sum of returns that are below the VaR	-12.27%	
Expected shortfall (95%)	-4.09%	-3,27,164

Performance ratios

Performance ratios

Average monthly excess return	0.11%
Standard deviation of monthly (excess) returns	2.36%
Sharpe ratio	0.048
Standard deviation of returns below the mean	1.48%
Sortino ratio	0.077
CAGR	3.83%
Biggest drawdown	-5.08%
MAR	0.753

The tactical asset allocation recommended allowed to dampen the impact of the recent equity market crash since the initial asset allocation has a MAR ratio that is lower than the actual portfolio. This was caused by a reduction in risk which translates into smaller drawdowns.

REFERENCES

The data sets used in the project were extracted from the Capstone Project in Coursera which was included in the minor specialization course on Investment Management offered by the University of Geneva.