

# Experimental Comparison of Autonomous Vehicles Scheduling Algorithms

With Battery Management in a Fixed Line Service

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Master Thesis, Computer Science

1. The Problem: Autonomous Vehicles in a Fixed Line Transportation Service
2. Model Outline
3. Numerical Experiments

# The Problem: Autonomous Vehicles in a Fixed Line Transportation Service

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## The Problem

Scheduling autonomous vehicles' activities in a circular line transportation service with dynamic bookings

## Goals

- Run simulations as close as possible to **real world** conditions
- Get insights about strategical choices to improve the:
  - **passengers level of service**
  - **vehicles operating costs**

## How

- Propose a **dynamic fleet size** scheduling strategy making use of **demand forecasting**
- Test how the system's performance metrics react to different **scenarios** and **scheduling strategies**

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# Model Outline

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Loop

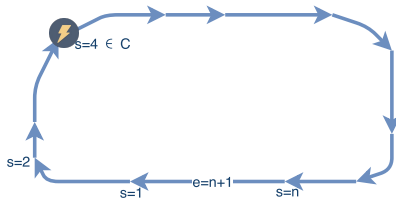


Figure 1: Example of a circular route

- Set of stations  $S = 1, \dots, n$
- Set of charging stations  $C \in S$
- Stop  $s$  is mandatory or optional
- Speed of edge  $e$  at time  $t$ :  $speed_t^e$



## Vehicles

- Vehicles fleet:  $V$
- Vehicle  $v \in V$ :
  - Capacity:  $c^v$
  - Maximum battery:  $q^v$  Recharging rate:  $\alpha^v$  Consumption rate:  $\beta^v$
  - Maximum speed:  $s^v$

## Dynamic Information at time $t$

- Battery level:  $I_t^v$
- Number of passengers in vehicle:  $o_t^v$
- Distance to the next vehicle on the loop:  $next_t^v$
- Stopping duration:  $wait_t^v$
- Indicator if vehicle is charging:  $x_t^v$

# AUTONOMOUS VEHICLES TRANSPORTATION MODEL

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## Bookings

- Booking from stop  $i$  to  $j$ :  $b_{i,j}$ , made at time  $t^b$  for  $n^b$  passengers
- If it has been satisfied  $D_b = 1$ :
  - Pickup time:  $p^d$
  - Drop-off time:  $d^d$
  - Satisfied by vehicle  $v^d$
  - Waiting time:  $w^b = p^b - t^b$
  - Journey time:  $\rho^b = d^b - p^b$
- Set of bookings which have been satisfied:  $B^* \in B$

## Demand

$dem_{t^*}$ : the number of bookings which have been made between  $t^*$  and  $t^* + 1h$ , so the number of bookings with  $t^* \leq t^{*b} < (t^* + 1h)$

$t^*$  is a discrete hourly timestamp

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# VEHICLES OUTPUT METRICS

Metrics at the end of the scheduling horizon of one day (midnight to midnight)

## Battery

- *battery<sup>v</sup>*: sum of the battery changes over the scheduling horizon when the vehicle is not charging
- *batteryCost* =  $\sum_{v \in V} \text{battery}^v$

## Occupancy

- *avgOccupancy<sup>v</sup>*: average occupancy of vehicle *v*
  - *loadFactor<sup>v</sup>*: doesn't consider time a vehicle is going to charge.
- Passenger-battery over seat-battery:

$$\frac{\sum_{b \in B^*} \text{battery}^b * n^b}{\text{battery}^v * c^v}$$

# CUSTOMERS' LEVEL OF SERVICE OUTPUT METRICS

## Waiting Time

- $avgWaitingTime = \frac{\sum_{b \in B^*} w^b}{|B^*|}$
- $stabilityWaitingTime = \max_{b^+ \in B^*} w^{b^+} - \min_{b^- \in B^*} w^{b^-}$

## Journey Time



- $avgJourneyTime = \frac{\sum_{b \in B^*} \rho^b}{|B^*|}$

## Completed Bookings Percentage

- $completedBookings = \frac{|B^*|}{|B|}$

# Numerical Experiments

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## Testing Environment

- Scheduling Horizon  $H = 1$  hour
- Demands  $dem_0 = 27$
- Fleet size  $|V| = 5$
- Heterogeneous fleet  $\forall v \in V$ .
  - $c^v = 10$
  - battery  $q^v = 1$ , charging/consumption rates = 1
  - Maximum speed  $s^v = 20\text{km/h}$
- Delphi Graph:  $S = 1, \dots, 32$
- Each simulation run 3 times, average reported
- **Reporting** application fetches vehicles' logs every second





## Vehicles

- Simulated concurrently following an actor model, each vehicle being an actor
- Actor step: position + battery updated every  $1000/\textit{rate}$  [ms]
- Trade-off between:
  - complexity of computation: if *rate* is **too high** => actor system has too many unhandled messages
  - precision: if *rate* is **too low** => vehicles skip stops
- *rate* = 3

# SIMULATION SETTINGS

## Time Synchronization

- Synchronize simulated time which is accelerated  $r$  times in the different applications, using the system clock
- $simTime = startTimestamp + (currentSystemTime - startTimestamp) * r + shiftDuration$

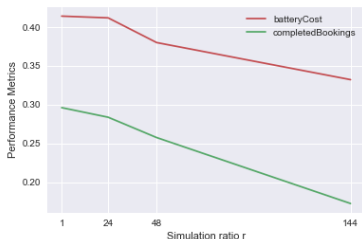


Figure 2: Performance metrics at growing simulation ratio

Table 1: Difference to  $r = 1$

	$r = 24$	$r = 144$
<i>batteryCost</i>	0.5%	21%
<i>completedBookings</i>	4%	52%

=>  $r = 24$  is a reasonable choice!

## Time Consistency Between Applications

Difference between  $simTime^b$  at which `World Simulator` sends booking  $b$  and the reported time in the logs from `Reporting` is not more than 55 seconds and on average 5 seconds

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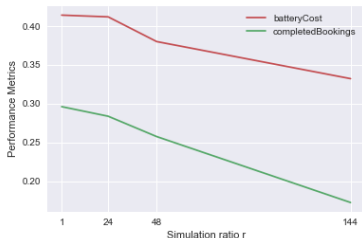


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## Goal

Maintain equal distance between vehicles to avoid bus bunching effect

## Strategy

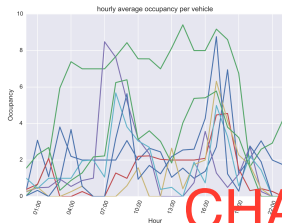
- *default*: default waiting time in seconds at a station
- When a vehicle  $v$  arrives at a station it waits  $wait_{simTime}^v = \text{default} * \text{ratio}$ , with *ratio* computed as follows:
  - Ideal distance:  $\text{ideal} = \text{len} / |V^*|$ ,  $V^*$  being the set of active vehicles on the line
  - $\text{ratio} = \text{next}_{simTime}^v / \text{ideal}$
  - Bounded by *waitMin* and *waitMax*

## Testing Scenario

- Delphi Site:  $S = 1, \dots, 32$
- Scheduling horizon:  $H = 1$  day (midnight to midnight)
- Week-day bookings from Samira (generated analyzing traffic info from HERE map)
- Heterogeneous fleet size  $|V| = 8$
- Speed of edges at any time  $\text{speed}_t^e = 20\text{km/h}$
- Charging stations: 10 at the same place on the loop

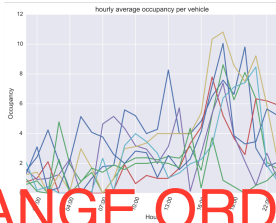
## Constant $wait_t^V$

default = 20 [s], ratio = 1



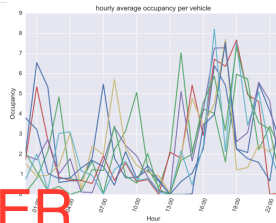
## Optional Stops

default = 20 [s], average: 24 [s]



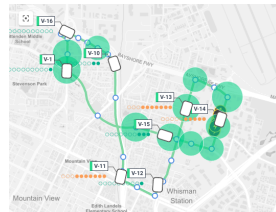
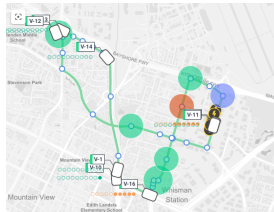
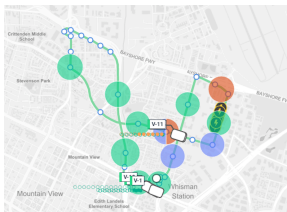
## Adapting $wait_t^V$

default = 20 [s], average: 35 [s]



# CHANGE ORDER

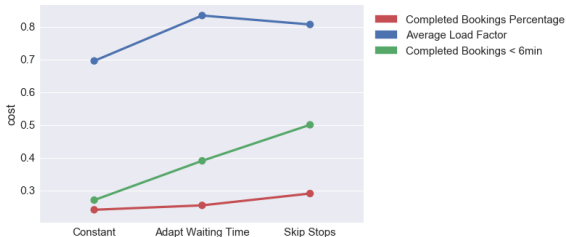
simTime = 6:00 am



# PERFORMANCE METRICS COMPARISON FOR HEADWAY



## AVG LOAD FACTOR



## Incentives

- Demand **varies** through the scheduling horizon
- System gathers real-life data and build prediction models through a machine learning pipeline  
=> reasonable to assume that demand can be predicted
- Demand high and not enough vehicles => passengers can't board in and **increase waiting time**
- Demand low and too many vehicles => vehicles **running empty** (not efficient)
- Need to find the right moment to send vehicles to charge

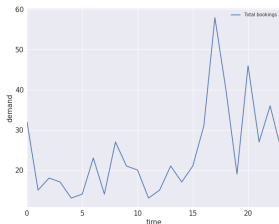


## Strategy

- Decide how many vehicles need to be active at each hour of the scheduling horizon based on the demand.
- Need to decide:
  - How the fleet is **rescheduled** when the number of vehicles needed on the line changes  
=> send the vehicles with the lowest battery level to charge, reactivate the ones with the highest battery level
  - What is the **demand**  
=> number of bookings made within an hour
  - What is the **balance** between quality of service VS cost of the running vehicles  
=> define cost function

# DEMAND AND SIMULATIONS

Demand distribution through the day



Demand Frequency



## Generating Data

- Simulations with scheduling horizon  $H = 1h$  => no battery management's noise
- $\forall dem \in D = \{13, 15, 21, 23, 25, 27, 31, 36, 40, 46, 58\}$  simulate with fleet size  $|V| \in [2, 10]$
- Gather all **performance metrics**
- Time between two consecutive bookings:  $1h/dem$
- **Clean** the data: replace values lower than 5th quantiles and higher than 95th quantiles



# DYNAMIC FLEET SIZE

**Data:** Scheduling horizon  $H$ , maximum fleet size  $V^{max}$ , optimal fleet size function  $optFleet(dem)$

**Result:** Optimal fleet size at each hour  $t^*$  of the scheduling horizon  $H$

$precFleetSize = 0$ ;

**for** each hour  $t^* \in T^*$  **do**

$optFleet_{t^*} = \min(optFleet(dem_{t^*}), V^{max})$ ;

$\Delta_{t^*} = optFleet_{t^*} - precFleetSize$ ;

**if**  $\Delta_{t^*} > 0$  **then**

        | create increase fleet size event by  $\Delta_{t^*}$

**end**

**else**

        | create decrease fleet size event by  $-\Delta_{t^*}$

**end**

$precFleetSize = optFleet_{t^*}$ ;

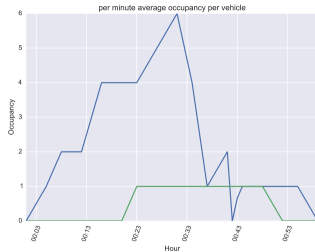
**end**

**Algorithm 1:** Dynamic Fleet Size Algorithm

# EXTREME SIMULATION EXAMPLES

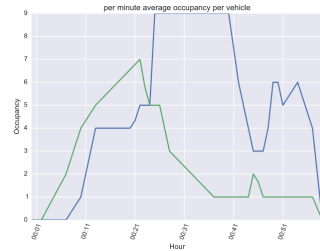
$dem = 13$

$|V| = 2$ ,  $WT = 14$ ,  $CBP = 0.61$



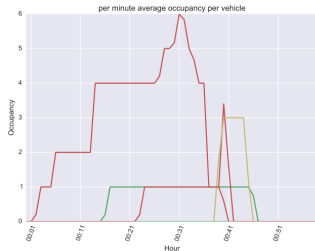
$dem = 58$

$|V| = 2$ ,  $WT = 12$ ,  $CBP = 0.31$

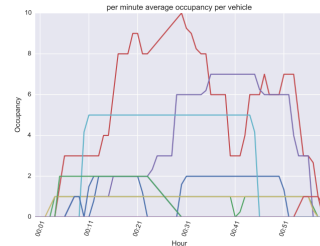


Texte  
Texte

$|V| = 10$ ,  $WT = 6$ ,  $CBP = 0.69$

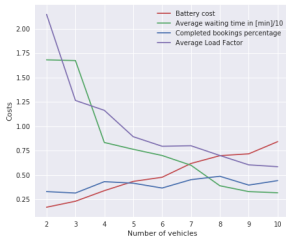


$|V| = 10$ ,  $WT = 5$ ,  $CBP = 0.51$



# FLEET SIZE' IMPACT ON PERFORMANCE METRICS

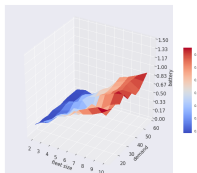
Averages over all demands  $\in D$



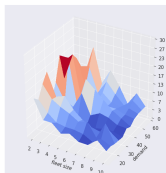
	$ V =2$	$ V $	Difference (in times)
<i>batteryCost</i>	0.17	0.84	4.95
<i>avgWaitingTime</i>	16.8	3.18	-13.62
<i>avgJourneyTime</i>	27	20	-6.54
<i>completedBookings</i>	0.33	0.44	1.34
<i>avgLoadFactor</i>	0.21	0.06	-3.67

Correlation Coeff	Dem	$ V $
<i>batteryCost</i>	-0.09	0.9
<i>avgWaitingTime</i>	0.24	-0.48
<i>completedBookings</i>	-0.39	0.25
<i>avgLoadFactor</i>	0.5	-0.5

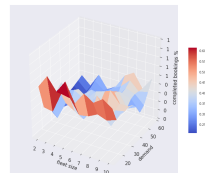
*batteryCost*



*avgWaitingTime*



*completedBookings*



# OPTIMAL NUMBER OF VEHICLES: TWO STRATEGIES

completedbookingsratio

1<sup>st</sup> strategy: Cost Function

$$cost_{dem,|V|} = \frac{batteryCost + avgWaitingTime}{e^{completedBookings}}$$

*batteryCost* and *avgWaitingTime* normalized by feature scaling  $(x - min)/(max - min)$  for each group of same *dem*

- optimal fleet size for *dem*:  $|V|$  which minimizes the cost function:

$$\min_{V \in [2,10]} (cost_{dem,|V|})$$

=> For *dem* = 13 we obtain *optFleet* = 3, which grows linearly to *dem* = 58 with *optFleet* = 8 ( $R^2 = 0.85$ )

## 2<sup>nd</sup> strategy: Level of Service Constraint

- Find function describing waiting time:  $avgWait_{dem,|V|}$
- Optimal fleet size: minimum  $|V|$  such that  $avgWait_{dem,|V|}$  is under an acceptable threshold (6 minutes)

### Function $avgWait_{dem,|V|}$

- Add dummy variables for each group of same  $dem$  to overcome multicollinearity
- **Linear regression**:  $avgWaitingTime \sim (dem, |V|, dummyVar) \Rightarrow R^2 = 0.53$  (plot of residuals ok)

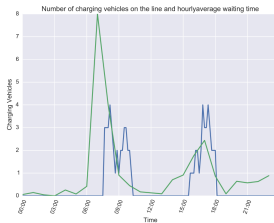
=>  $optFleet$  between 6 and 8

We compare the simulation results with 8 vehicles always active and adaptive stopping time at stations without skipping stops.

# DYNAMIC FLEET SIZE EXPERIMENTS

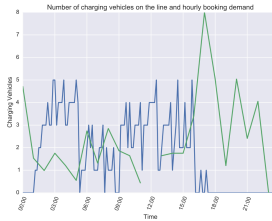
## 8 Vehicles Active

No dynamic fleet size



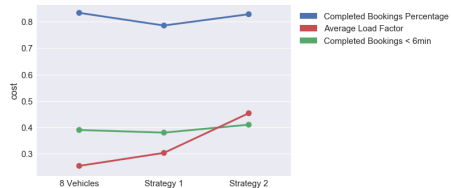
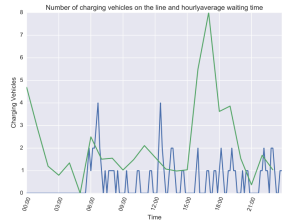
## Strategy 1: Cost Function

Fleet size between 3 and 8



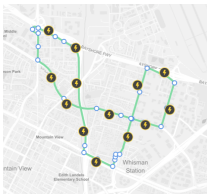
## Strategy 2: Max WT 6min

Fleet size between 3 and 8



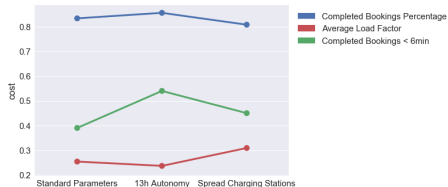
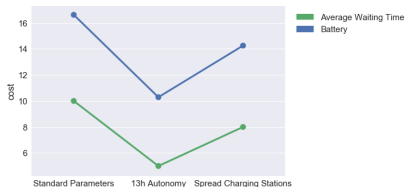
# BATTERY MANAGEMENT EXPERIMENTS

## Charging Stations' Position



## Better Autonomy

Increase battery autonomy from 8 hours to 13 hours



# IMPROVEMENT OF PERFORMANCE PARAMETERS BASED ON SCHEDULING STRATEGIES

Difference in percentage to 8 vehicles always active with adaptive stopping times at stations.

Dispatching Strategy	Battery	Waiting Time	Load Factor	Completed Bookings	Completed < 6min
Reference: Constant 8 vehicles	16.61	10	0.25	0.83	0.47
Optional Stops	43	-66	13.26	-3	28
adaptVehicles	-11	-22	19	-5	2
adaptVehicles2	-0.2	-35	55	0	4
Spread Charging Stations	-15	-22	19	-3	17
13h Autonomy	-47	-66	-7	2	29



Thank you!  
Questions?