

Master Project

# Experimental Comparison of Autonomous Vehicles Routing Optimization Algorithms

Author:	Prisca Aeby <sup>1</sup>	prisca.aeby@epfl.ch
Supervisors:	Bastien Rojanawisut <sup>2</sup>	bastien.rojanawisut@bestmile.com
	Boi Faltings <sup>3</sup>	boi.faltings@epfl.ch

July 3, 2017

---

<sup>1</sup> Computer Science, École Polytechnique Fédérale de Lausanne, Switzerland

<sup>2</sup> Scala Backend Software Engineer, BestMile, Switzerland

<sup>3</sup> Artificial Intelligence Laboratory, School of Computer and Communication Sciences, École Polytechnique Fédérale de Lausanne, Switzerland, [liawww.epfl.ch](http://liawww.epfl.ch)

## **Abstract**

Your abstract.

# Contents

<b>1</b>	<b>Introduction</b>	<b>4</b>
<b>2</b>	<b>Related Literature</b>	<b>4</b>
2.1	Public Transport . . . . .	4
2.2	Demand-Adaptive Transit Systems . . . . .	6
2.3	Vehicles Assignment to Routes . . . . .	6
<b>3</b>	<b>Problem Formulation</b>	<b>7</b>
3.1	Circular Route . . . . .	7
3.2	Vehicles . . . . .	7
3.3	Bookings . . . . .	7
3.4	Output Metrics . . . . .	8
<b>4</b>	<b>Methodology</b>	<b>8</b>
4.1	Simulation Framework . . . . .	8
4.1.1	Simulated Vehicles . . . . .	8
4.1.2	Reported Metrics . . . . .	8
4.2	Scheduling . . . . .	8
4.2.1	Vehicles' Activities Schedule . . . . .	8
4.2.2	Headway . . . . .	9
4.2.3	Dynamic Fleet Size . . . . .	9
<b>5</b>	<b>Numerical Experiments</b>	<b>9</b>
5.1	. . . . .	9
5.2	Simulation Settings . . . . .	9
5.3	Graph . . . . .	9
5.4	Optimal Headway . . . . .	9
5.5	. . . . .	9
5.6	Simulated Demand . . . . .	9
5.7	. . . . .	9
<b>6</b>	<b>Conclusion</b>	<b>9</b>

# 1 Introduction

General problem: two types of services, on-demand and fixed-line => explain why we focus on fixed line (all constraints of the platform) Fixed line because now roads are not made for more complex systems

## 2 Related Literature

The scope of vehicle scheduling problems related to our specific case study can range from fixed-line bus services to on-demand systems. In fact, electric shuttles' routes and stops are predefined but timetables can be flexible to respond to the known real-time demand. The set of constraints differs from traditional bus transportation, for example workforce regulations can be eliminated as the shuttles are not human driven but a battery management component needs to be introduced into the planning process. As we will see in this chapter, current research often concentrates on one specific aspect of the scheduling strategy, simplifying some constraints, assessing the system's performance using various types of metrics and considering different inputs. In what follows, we describe in section 2.1 some techniques used in the traditional public transport industry to guarantee a good quality of service. In section 2.2 we describe the concept of Demand-Adaptive Transit Systems. Finally, we detail in section 2.3 an approach proposed by the Urban Transport Systems Laboratory at EPFL (LUTS) for scheduling autonomous vehicles activities.

### 2.1 Public Transport

Within the standard transit organization, policies and standards affect a lot the development of transport strategies and how people interact with the systems. The planning process of a fixed line bus transportation service is mainly composed of three different tasks: route planning, service frequencies and service timing. Route planning consists of defining a sequence of stops composing each route and how those routes are interconnected. Service frequency captures the number of vehicles per unit time which pass a given route (often expressed in vehicles per hour). A common measure used to express the ideal distance between vehicles is the headway, the inverse of the frequency, in other word the fixed interval at which vehicles are coming at a station. The service frequencies set by the transport organization can be chosen based on different policies (see Pine et al. (1998)):

1. **Fixed headway:** the agency establishes a fixed interval at which vehicles come to stations. It is convenient for customers as they have access to an exact schedule, but it is hard to keep the time between vehicles constant as it is vulnerable to external disturbances.
2. **Demand-based headway:** in existing transport services, agencies can adapt the timetables based on the observed demand at the stations (number of passenger boardings/deboardings) in order to reach the desired passenger load in vehicles.
3. **Performance-based headway:** the goal is to find the headway for which performance standards are optimized. Those costs are usually measured during a

service period, for example a day. It may include the service productivity (e.g. the revenue per passenger per hour), the cost effectiveness of the service or the overall effectiveness (e.g. net subsidy per passenger).

All those scheduling strategies suffer from the well-known bunching effect: two or more buses arrive at the same time at a stop with the first one being overcrowded and the other one empty. This phenomenon occurs because of external disruptions in the service (e.g. stochastic passenger arrivals at stops, traffic jams, etc) (see Camps and Romeu (2016)) slowing down one of the bus which pick up passengers who would have taken the next bus.

Several corrective measures based on different strategies have been developed to overcome this problem. There are mainly two different holding approaches to mitigate bus bunching as described in van Oort et al. (2010):

- **Headway-Based Holding:** vehicles arriving with a shorter headway at a stop (or holding point) wait to restore the headway distribution. If they arrive with a longer headway, it is possible to speed up the buses by skipping stations. The analytical study Cortés et al. (2010) proved the efficiency of using headway holding strategy and bus skipping (considering the extra waiting time of passenger whose station has been skipped) with the two-dimensional objective function composed of the regularization of bus headways on the one hand and the level of service with respect to a circle route scenario.
- **Schedule-Based Holding:** in the case of fixed timetables, schedule-based holding involves holding a vehicle at a stop if it is ahead of its schedule and dispatch it immediately otherwise.

Zhao et al. (2016) proposed a method using boarding limits at stations to control buses which does not involve bus accelerating or waiting at stations and thus does not influence the customers' travel time and does not disturb the traffic. They do not consider schedule and a priori target headway. However, they proved that their self-adjusting control stabilizes the headway spontaneously in a short time.

As stated by He (2015), the majority of earlier studies conducted on maintaining a balanced headway uses arrival time of the current bus at the current stop and arrival times of the preceding buses but does not take advantage of real time information like the vehicles' geolocation. Later methods proposed new approaches assuming availability of locations and even real-time arrivals of passengers to each bus stop. For example, Daganzo and Pilachowski (2011) proposed a solution taking into account the distance between the current bus and the preceding and following buses to adjust the speed of the current bus. It includes holding buses at stations, accelerating or decelerating.

The studies carried out within the traditional fixed-line bus services handle situations where the demand is consistently strong over the territory and where the fleet is composed of high-capacity vehicles. When the demand is weaker, it is complicated to operate an economical and frequent transit system as the resources are shared by few people and are very costly (e.g. driver salaries, fuel expenses, etc.). The autonomous fleets are composed of vehicles with lower capacity, but it is easier to dynamically adapt their scheduling strategy at low cost and have access to real-time information.

## 2.2 Demand-Adaptive Transit Systems

Demand-Adaptive System (DAS), or Demand-Responsive Transit (DRT), is a personalized type of transportation displaying features from both fixed-line services and on-demand systems. In such systems, passengers are picked up and dropped off on-demand at predetermined stops, and unrequested stops are skipped. There are still compulsory stops, which are served within a predefined time window, but the routes are adapted based on the requested stops. A method to determine the time windows at the compulsory stops has been proposed by Crainic et al. (2010). Li et al. (2007) depicted the advantages to substitute fixed-line bus services to DRT services in two cities in California with low demand density.

Gabriel et al. (2008) address the issues of evaluating DAS services in comparison to traditional transit services and fully on-demand systems. The transit systems' evaluation denotes the part of the planning process dedicated to the study of the behaviour and the performance of the line under various conditions with respect to demands, policies and costs. They mention the main steps of transit lines' evaluation in order to tune operating parameters impacting the system performance under different scenarios for cost-benefit analyzes: 1) the scenario, parameters and policies are specified, as well as the demand to serve 2) the line is designed 3) the operation of the line is simulated (during a specified time-horizon) 4) results are collected and performance measures are computed. The importance of demand generation in step 1) differs from one system to the other: whilst in fixed lines transits static methods are often used to simulate an average demand, dynamic methods are used to simulate the time-dependent stop-to-stop requests in on-demand systems. The performance measurements in step 4) vary as well from one system to the other: in fixed-lines the service quality is mainly represented by the buses' punctuality and the constant interarrival times whereas for on-demand systems it is expressed by the specific users' waiting time and journey time. Gabriel et al. (2008) propose a framework for evaluating DAS lines including the scenario input, the optimization modules for the design and operation of the line and the simulation module which yield the statistical information about the performance.

## 2.3 Vehicles Assignment to Routes

Bongiovanni et al. (2016) present an optimization approach for the autonomous vehicles scheduling within a transit system composed of circular routes. They separate the planning process in two main tasks: line planning and vehicle scheduling. Line planning corresponds to defining the routes and the required headway on each route over the planning horizon. Vehicle scheduling refers to computing a general assignment plan for each vehicle for each time period over the planning horizon of one day. It means that each vehicle is assigned to a specific route or to a recharging station for each time period. The underlying assumption is that the vehicles will not transfer between routes and charging stations too often which makes the time discretization of the planning horizon possible. They focus on the vehicle scheduling task which takes as input the predefined routes, frequencies, fleet size and battery model. They present the scheduling problem as a mixed-integer linear programming (MILP) with battery constraints and the goal of the objective function being to maximize the total battery charge levels at the end of the planning horizon.

Parameter	Signification
4	5
7	8

Table 1: My table

### 3 Problem Formulation

In this section we formulate the mathematical model describing the autonomous vehicles circular line system. All the variables are listed in Table 1. In addition to traditional bus transit system descriptions, we introduce the concept of battery stations and we include dynamic bookings from one station to an other station on the loop. As we have access to information during the service horizon time  $T$ , we denote a discrete timestamp  $t$  which takes value between  $[0, T]$  at fixed sampling *interval*.

#### 3.1 Circular Route

The circular line in this transportation system is a route which starts at a certain station, traverses other stations once and terminates at the starting station. The route is represented by set of stations  $S = \{1, \dots, n\}$  and a set of directed edges  $E$  linking each station  $s \in S$  to its following station. If the station  $s \in S$  has a charging station the boolean variable  $C^s$  is set to 1. The maximum speed of an edge, representing the traffic at time  $t$ , is expressed as  $speed_t^e$ .

#### 3.2 Vehicles

Each vehicle composing the fleet  $v \in V$  moving on the circular closed line is characterized by a capacity  $c^v$ , a maximum charge  $q^v$ , a recharge rate  $\alpha^v$ , a battery consumption rate  $\beta^v$  and a maximum speed  $s^v$ . The battery level of vehicle  $v$  at the timestamp  $t$  is  $I_t^v \in [0, q^v]$ . The battery change between The edge it is currently traversing is  $e_t^v$  and the distance to the next vehicle in front of it on the loop is given by  $next_t^v$ . The occupancy of the vehicle is expressed as  $o_t^v \in [0, c^v]$ . The vehicle is travelling either at its maximum speed or at the limitation of the current edge. Its current speed is therefore  $\max\{s^v, speed_t^e\}$ . When a vehicle is charging at a station the boolean variable  $x_t^v$  is set to 1 and it can not carry any passengers  $o_t^v = 0$ .

#### 3.3 Bookings

The set  $B$  represents the users' bookings made during the service horizon. A booking  $b_{i,j} \in B$  requests a trip from station  $i$  to  $j$  at time  $t^b$  for a group of  $n^b$  persons. If the booking has been satisfied, the boolean variable  $D_b$  is set to 1 and we know that it has been executed by vehicle  $v^b \in V$ . The pickup time of booking  $b$  at station  $i$  is  $p^b$  and drop-off time at station  $j$  is  $d^b$ . The waiting time  $w^b$  equals  $p^b - t^b$  and the journey time  $\Delta^b$  is  $d^b - p^b$ .

### 3.4 Output Metrics

At the end of the service horizon  $T$ , some metrics can be derived in order to evaluate the performance of the overall system dispatching the vehicles to serve the requests.

#### Energy

The total energy consumed by a vehicle  $v$  is the difference

#### Occupancy

#### Waiting Time

#### Journey Time

#### Completed Bookings Percentage

Travel time, booking time,

## 4 Methodology

concentrates on respecting the fixed headway (which is first computed) but not optimising the real costs taking everything into account like battery management, etc

### 4.1 Simulation Framework

graph explaining framework

#### 4.1.1 Simulated Vehicles

start: spread on the line, battery is full starting location they cannot take over other vehicles, need to follow the loop unless when they go to charge they don't compute the headway and go max speed

#### 4.1.2 Reported Metrics

Logs fetched from database - vehicle logs - journey logs output graph

### 4.2 Scheduling

Why we don't follow exactly luts: adapt the vehicles on the fly on one fixed route

#### 4.2.1 Vehicles' Activities Schedule

when they arrive at station, if they can they pick up the booking (based on booking size) they drop off bookings that finish here they wait based on headway computation  
\*battery\* check if it is under threshold finish to drop off everybody and go to charging station



### 4.2.2 Headway

compute headway based on fleetorchestrationservice

### 4.2.3 Dynamic Fleet Size

how choose vehicles to send to charge and which ones to activate

## 5 Numerical Experiments

Real environment

### 5.1

### 5.2 Simulation Settings

speed

### 5.3 Graph

Unless stated, charging locations at same place

### 5.4 Optimal Headway

### 5.5

### 5.6 Simulated Demand

### 5.7

## 6 Conclusion

## References

- Bongiovanni, C., Kaspi, M., and Geroliminis, N. (2016). Scheduling autonomous vehicles activities. Technical report, Urban Transport Systems Laboratory EPFL.
- Camps, J. M. and Romeu, M. E. (2016). Headway adherence. detection and reduction of the bus bunching effect. *AET papers repository*.
- Cortés, C. E., Sáez, D., Milla, F., Núñez, A., and Riquelme, M. (2010). Hybrid predictive control for real-time optimization of public transport systems' operations based on evolutionary multi-objective optimization. *Transportation Research Part C: Emerging Technologies*, 18(5):757–769.
- Crainic, T. G., Errico, F., Malucelli, F., and Nonato, M. (2010). Designing the master schedule for demand-adaptive transit systems. *Annals of Operations Research*, 194(1):151–166.

- Daganzo, C. F. and Pilachowski, J. (2011). Reducing bunching with bus-to-bus cooperation. *Transportation Research Part B: Methodological*, 45(1):267–277.
- Gabriel, T., Fausto, C., Malucelli, E. F., and Nonato, M. (2008). A proposal for the evaluation of demand-adaptive transit systems. *Annals of Operations Research*.
- He, S.-X. (2015). An anti-bunching strategy to improve bus schedule and headway reliability by making use of the available accurate information. *Computers & Industrial Engineering*, 85:17 – 32.
- Li, Y., Wang, J., and Chen, J. (2007). *Design of a Demand-responsive Transit System*. California PATH working paper. California PATH Program, Institute of Transportation Studies, University of California at Berkeley.
- Pine, R., Niemeyer, J., and Chisholm, R. (1998). *Transit Scheduling: Basic and Advanced Manuals*. Report (Transit Cooperative Research Program). National Academy Press.
- van Oort, N., Wilson, N., and van Nes, R. (2010). Reliability improvement in short headway transit services. *Transportation Research Record: Journal of the Transportation Research Board*, 2143:67–76.
- Zhao, S., Lu, C., Liang, S., and Liu, H. (2016). A self-adjusting method to resist bus bunching based on boarding limits. *Mathematical Problems in Engineering*, 2016:1–7.