A Topology on a set $X$ is a collection of subsets $\mathcal{T} \subseteq \mathcal{P}(X)$, satisfying the following properties: