



School of Computer Science and Engineering

Winter Semester 2023-24

Continuous Assessment Test – I

SLOT E1+TE1

Programme Name & Branch: B.Tech & Computer Science and Engineering

Course Name & Code: Cryptography and Network Security & BCSE309L

Class Number (s): Applicable to all

Faculty Name (s): Applicable to all

Exam Duration: 90 Min.

Maximum Marks: 50

General instruction(s):

Answer All the Questions and calculator is allowed

Q. No.	Question	Max Marks																																																		
1.	<p>a) Find GCD, variables S and T by construct a table for the following inputs using Extended Euclidean Algorithm. 291, 41.</p> <p>∴ We use the following table:</p> <table><tr><th>q</th><th>r₁</th><th>r₂</th><th>r</th><th>s₁</th><th>s₂</th><th>s</th><th>t₁</th><th>t₂</th><th>t</th></tr><tr><td>6</td><td>291</td><td>42</td><td>39</td><td>1</td><td>0</td><td>1</td><td>0</td><td>1</td><td>-6</td></tr><tr><td>1</td><td>42</td><td>39</td><td>3</td><td>0</td><td>1</td><td>-1</td><td>1</td><td>-6</td><td>7</td></tr><tr><td>13</td><td>39</td><td>3</td><td>0</td><td>1</td><td>-1</td><td>14</td><td>-6</td><td>7</td><td>-97</td></tr><tr><td></td><td>3</td><td>0</td><td></td><td>-1</td><td>14</td><td></td><td>7</td><td>-97</td><td></td></tr></table> <div><div>↑</div><div>gcd</div></div> <div><div>↑</div><div>s</div></div> <div><div>↑</div><div>t</div></div> <p>gcd (291, 42) = 3 → (291)(-1) + (42)(7) = 3</p>	q	r ₁	r ₂	r	s ₁	s ₂	s	t ₁	t ₂	t	6	291	42	39	1	0	1	0	1	-6	1	42	39	3	0	1	-1	1	-6	7	13	39	3	0	1	-1	14	-6	7	-97		3	0		-1	14		7	-97		5
q	r ₁	r ₂	r	s ₁	s ₂	s	t ₁	t ₂	t																																											
6	291	42	39	1	0	1	0	1	-6																																											
1	42	39	3	0	1	-1	1	-6	7																																											
13	39	3	0	1	-1	14	-6	7	-97																																											
	3	0		-1	14		7	-97																																												
	<p>b) Find the remainder for $2^{20} + 3^{30} + 4^{40} + 5^{50} + 6^{60} \bmod 7$ using Fermat's Little Theorem.</p> <p>Find $2^{20} + 3^{30} + 4^{40} + 5^{50} + 6^{60} \bmod 7$.</p> <p>[Solution: $2^{20} + 3^{30} + 4^{40} + 5^{50} + 6^{60} \equiv 0 \bmod 7$]</p> <p>By Fermat's Little Theorem, $2^6 \equiv 3^6 \equiv 4^6 \equiv 5^6 \equiv 6^6 \equiv 1 \bmod 7$. Thus, $2^{20} + 3^{30} + 4^{40} + 5^{50} + 6^{60} \equiv 2^2 + 3^0 + 4^4 + 5^2 + 6^0 \equiv 4 + 1 + 2^8 + 25 + 1 \equiv 4 + 1 + 4 + 4 + 1 \equiv 14 \equiv 0 \bmod 7$.</p>	5																																																		

2. A hoard of gold pieces comes into the possession of a band of 15 pirates. When they come to divide up the coins, they find that 3 are left over. Their discussion of what to do with these extra coins becomes animated, and by the time some semblance of order returns there remain only 7 pirates capable of making an effective claim on the hoard. When, however, the hoard is divided between these seven it is found that 2 pieces are left over. There ensues an unfortunate repetition of the earlier disagreement, but this does at least have the consequence that the 4 pirates who remain are able to divide up the hoard evenly between them. What is the minimum number of gold pieces which could have been in the hoard?

$$x \equiv 3 \pmod{15}$$

$$x \equiv 2 \pmod{7}$$

$$x \equiv 0 \pmod{4}$$

$$\text{GCD}(15, 7)$$

$$\text{GCD}(15, 4)$$

$$\text{GCD}(7, 4)$$

$$= 1$$

1) $M = m_1 \times m_2 \times m_3$
 $M = 15 \times 7 \times 4$
 $M = 420$

2) $M_1 = M / m_1$
 $= 420 / 15 = 28$
 $M_2 = 420 / 7 = 60$
 $M_3 = 420 / 4 = 105$

$$m_1^{-1} = 28^{-1} \pmod{15}$$

$$= 28 \times ? \pmod{15} = 1$$

$$= 28 \times 7 \pmod{15} = 1$$

$$= 196 \pmod{15} = 1$$

$$m_1^{-1} = 7$$

$$m_2^{-1} = 60^{-1} \pmod{7}$$

$$= 60 \times ? \pmod{7} = 1$$

$$= 60 \times 2 \pmod{7} = 1$$

$$= 120 \pmod{7} = 1$$

$$m_2^{-1} = 2$$

$$x = [(3 \times 28 \times 7) + (2 \times 60 \times 2)] \text{ mod } 420$$

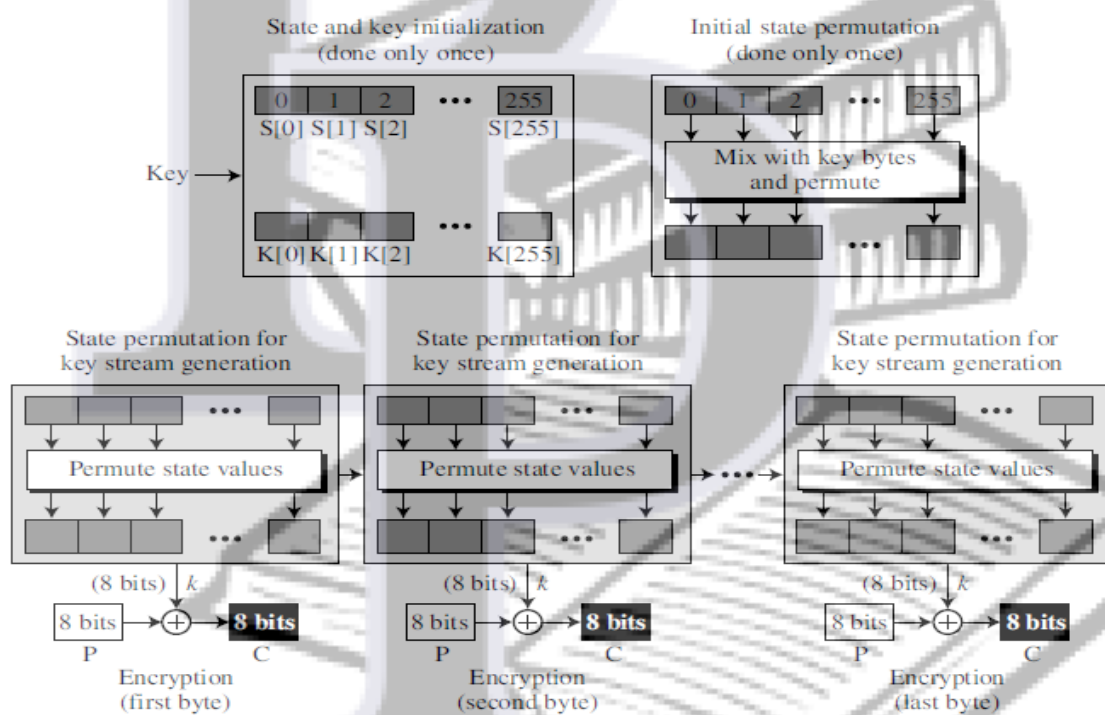
$$x = [588 + 240] \text{ mod } 420$$

$$x = 828 \text{ mod } 420$$

$$x = 408$$

3. Draw an architecture of RC4 algorithm and discuss the process of initialization, initial state permutation, key stream generation and encryption in detail.

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Architecture – 2

Initialization process - 2

Initial state permutation - 2

Key stream generation - 2

Encryption - 2

4. a) Explain the DES feistel structure in detail with neat diagram.

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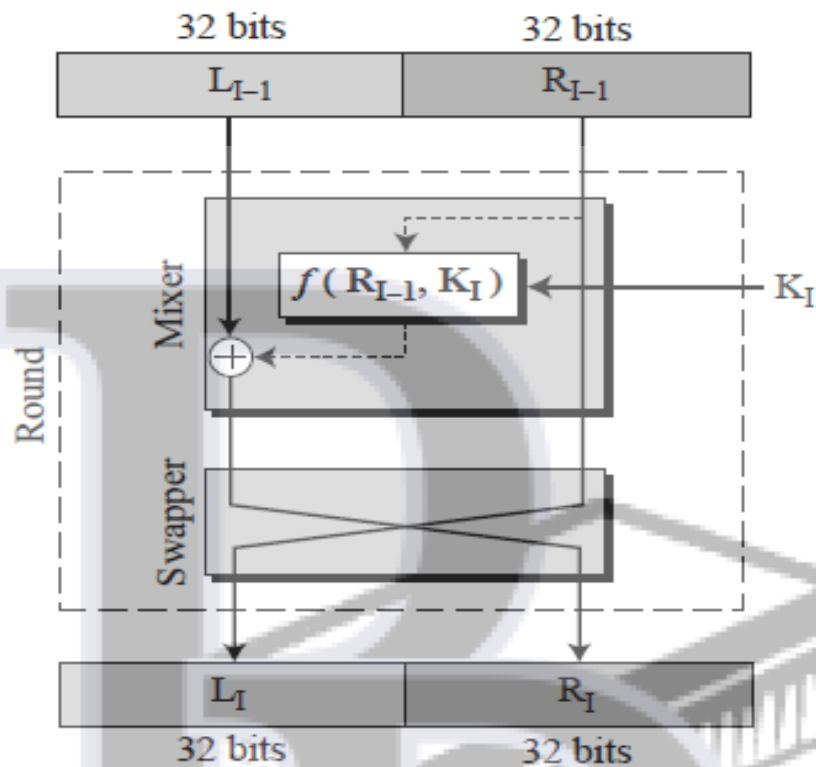


Fig. 6.4 A round in DES (encryption site)

b) Answer the following questions about S-boxes in DES:

- Show the result of passing the input 111111 through S-box 2.
- Show the result of passing the input 000000 through S-box 7.

S-box 2 Table

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
0	15	01	08	14	06	11	03	04	09	07	02	13	12	00	05	10
1	03	13	04	07	15	02	08	14	12	00	01	10	06	09	11	05
2	00	14	07	11	10	04	13	01	05	08	12	06	09	03	02	15
3	13	08	10	01	03	15	04	02	11	06	07	12	00	05	14	09

S-box 7 Table

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
0	4	11	2	14	15	00	08	13	03	12	09	07	05	10	06	01
1	13	00	11	07	04	09	01	10	14	03	05	12	02	15	08	06
2	01	04	11	13	12	03	07	14	10	15	06	08	00	05	09	02
3	06	11	13	08	01	04	10	07	09	05	00	15	14	02	03	12

i)

Input: 1 1111 1 → 3, 15 → Output: 09 (1001)

ii)

Input: 0 0000 0 → 0, 0 → Output: 04 (0100)

5. Find the third round key of AES 128 using the following second round key which is given in hexadecimal, S-Box table and round constant 04.

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Second Round Key

56	C7	76	A0
08	1A	43	3A
20	B1	55	F7
07	8F	69	FA

S-Box Table

		Y															
		0	1	2	3	4	5	6	7	8	9	A	B	C	D	E	F
X	0	63	7C	77	7B	F2	6B	6F	C5	30	01	67	2B	FE	D7	AB	76
	1	CA	82	C9	7D	FA	59	47	F0	AD	D4	A2	AF	9C	A4	72	C0
	2	B7	FD	93	26	36	3F	F7	CC	34	A5	E5	F1	71	D8	31	15
	3	04	C7	23	C3	18	96	05	9A	07	12	80	E2	EB	27	B2	75
	4	09	83	2C	1A	1B	6E	5A	A0	52	3B	D6	B3	29	E3	2F	84
	5	53	D1	00	ED	20	FC	B1	5B	6A	CB	BE	39	4A	4C	58	CF
	6	D0	EF	AA	FB	43	4D	33	85	45	F9	02	7F	50	3C	9F	A8
	7	51	A3	40	8F	92	9D	38	F5	BC	B6	DA	21	10	FF	F3	D2
	8	CD	0C	13	EC	5F	97	44	17	C4	A7	7E	3D	64	5D	19	73
	9	60	81	4F	DC	22	2A	90	88	46	EE	B8	14	DE	5E	0B	DB
	A	E0	32	3A	0A	49	06	24	5C	C2	D3	AC	62	91	95	E4	79
	B	E7	C8	37	6D	8D	D5	4E	A9	6C	56	F4	EA	65	7A	AE	08
	C	BA	78	25	2E	1C	A6	B4	C6	E8	DD	74	1F	4D	BD	8B	8A
	D	70	3E	B5	66	48	03	F6	0E	61	35	57	B9	86	C1	1D	9E
	E	E1	F8	98	11	69	D9	8E	94	9B	1E	87	E9	CE	55	28	DF
	F	8C	A1	89	0D	BF	E6	42	68	41	99	2D	0F	B0	54	BB	16

PAJAMA PADHAI

Second Round Key = 56 C7 76 A0

08 1A 43 3A

20 B1 55 F7

07 8F 69 FA

↑ ↑ ↑ ↑
W4 W5 W6 W7

Find

$$g(W7) = g(A0 \ 3A \ F7 \ FA)$$

1) Rotword one byte circular shift
= 3A F7 FA A0

2) Sub word = 80 68 2D E0

3) EX OR with RC
= 80 68 2D E0 XOR

04 00 00 00

$$g(W7) = 84 68 2D E0$$

$$4) W_8 = W_4 \oplus g(W_7)$$

$$= \begin{array}{cccc} 56 & 08 & 20 & 07 \\ 84 & 68 & 2D & E0 \end{array}$$

$$W_8 = \begin{array}{cccc} D2 & 60 & 0D & E7 \end{array}$$

$$5) W_9 = W_5 \oplus W_8$$

$$= \begin{array}{cccc} C7 & 1A & B1 & 8F \\ D2 & 60 & 0D & E7 \end{array}$$

$$W_9 = \begin{array}{cccc} 15 & 7A & BC & 68 \end{array}$$

$$6) W_{10} = W_6 \oplus W_9$$

$$= \begin{array}{cccc} 76 & 43 & 85 & 69 \\ 15 & 7A & BC & 68 \end{array}$$

$$W_{10} = \begin{array}{cccc} 63 & 39 & E9 & 01 \end{array}$$

$$7) W_{11} = W_7 \oplus W_{10}$$

$$= \begin{array}{cccc} A0 & 3A & F7 & FA \\ 63 & 39 & E9 & 01 \end{array}$$

$$W_{11} = \begin{array}{cccc} C3 & 03 & 1E & FB \end{array}$$

Round 3 key:

D2 60 0D E7 15 7A BC 68 63 39 E9 01 C3 03 1E FB