Additional Material for the Paper GNN-Based Interactive Property Graph Repairs

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PVLDB Artifact Availability:

The source code, data, and/or other artifacts have been made available at URL_TO_YOUR_ARTIFACTS.

1 TIME COMPLEXITY

Let |V| be the number of nodes of the GRDG, |F| the number of edges, |U| the number of users, $C = |C_i|$ the size of candidates subgraphs per user and T the number of iterations of the algorithm.

Complexity of BUILDCANDIDATESSET. Let Δ be the maximum degree of the GRDG. For user u_i , denote by CC_i the capacity and by D_v the node difficulties. Let $X_i := \min\left\{|V|, \left\lfloor \frac{CC_i}{\min_{v \in V} D_v} \right\rfloor\right\}$ be an upper bound on the number of nodes a candidate subgraphs for u_i can contain. Assume we start from S_i seeds of violations per user and run t_i iterations of 1-exchange local search (add/drop/swap one node) per seed, keeping at most $C_i \leq S_i$ candidate subraphs. The greedy growth step performs at most X_i insertions, checking at most $O(X_i\Delta)$ neighboring nodes to select the one with maximal gain (cost $O(\log n)$), giving $T_{\text{greedy}}(i) = O(X_i\Delta\log n)$. One step of local search scans a 1-exchange neighborhood of size $O(X_i\Delta)$ with cached deltas; over t_i iterations this is $T(i) = O(t_i X_i\Delta)$. Hence the per-seed cost is $T_{\text{seed}}(i) = O(X_i\Delta(\log n + t_i))$. With S_i seeds, the complexity for finding the candidate subgraphs for a user is $T_{\text{user}}(i) = S_i \cdot T_{\text{seed}}(i) = O(S_i X_i\Delta(\log n + t_i))$,

Complexity of SubmodularAssignment. For each user i, let C_i be the set of candidate subgraphs produced by BuildCandidatesSet. The total candidates for all the users are $M = \sum_{i=1}^{N} |C_i|$. and the total nodes accross the candidates are $Y = \sum_{i=1}^{N} \sum_{P \in C_i} |P|$. We can leverage an inverted index from each node v for the list of candidate

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items (i,P) that contain v (of size O(M)). Let $c_{\min} = \min_i c_i$ be the minimum cost among the users, and let X_{sel} be the number of selected candidates; clearly $X_{\text{sel}} \leq \min \left\{ M, |U|, \lfloor B/c_{\min} \rfloor \right\}$.

Computing initial gains $\sum_{v \in P} EQ(D_v, K_i)$ for all (i, P) and building the inverted index costs O(S).

At each iteration of the greedy loop, we extract the current best feasible item in $O(\log M)$ time. Upon choosing (i^\star, P^\star) we (i) remove all other patches of user i^\star (at most $|C_{i^\star}|$ items overall across the run), and (ii) invalidate all candidates that overlap P^\star . Using the inverted index, step (ii) takes $O(\sum_{v \in P^\star} \Gamma_v)$ time, where Γ_v is the number of candidate items containing node v. Because subgraphs are enforced disjoint, each node is invalidated at most once; hence across the whole run $\sum_{\text{selected } P^\star} \sum_{v \in P^\star} \Gamma_v = \sum_v \Gamma_v = Y$. The total number of operations on the lists of candidates is $O(M + X_{\text{sel}})$, so heap work is $O((M + X_{\text{sel}}) \log M)$.

Summing up, $T_{\text{assignment}} = O(Y + (M + X_{\text{sel}}) \log M)$. Under uniform parameters ($|C_i| = L$ candidates per user, each of size at most X), we have M = |U|L and $X \le |U|LX$, giving

$$T_{\text{assignment}} = O(|U|LX + (|U|L + X_{\text{sel}})\log(|U|L)).$$

Complexity of the Final Outer Loop. Let T be the maximum number of Lagrangian iterations. The remaining outer-loop work per iteration is lightweight: (i) computing the current primal value Z is $O(\sum_{i \in U'} |P_i|) \leq O(|V|)$, (ii) the dual quantity UB_t is O(1) once Z and $\sum_{i \in U'} c_i$ are known, (iii) the subgradient update and projection of λ are O(1), and (iv) updating the incumbent $(U^*, \{P_i^*\})$ is O(1).

Hence the worst-case total time (without early stopping) is $T_{\text{total}} = T \cdot (|U| \cdot T_{\text{user}} + T_{\text{assignmnet}} + O(|V|))$. Therefore,

$$O\left(T \cdot \left(|U| SX \Delta \left(\log |V| + t\right) + |U| LX + \left(|U| L + X_{\text{sel}}\right) \log(|U| L) + |V|\right)\right).$$

2 CONSTRAINTS

In this section, we list the constraint used for each dataset, in a datalog-like format.

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2.1 FAERS (Real)

A drug cannot be primary suspect and secondary suspect of the same case

$$\phi_{1} := (Case(X) \land Drug(Y) \land Caze(Z)$$

$$\land (IS_PRIMARY_SUSPECT(X, Y)$$

$$\land IS_SECONDARY_SUSPECT(Y, Z),$$

$$id(X) = id(Y) \rightarrow \bot)$$

A drug cannot be primary suspect of itself

$$\phi_1 := (Drug(X) \land Drug(Y)$$

$$\land (IS_PRIMARY_SUSPECT(X, Y))$$

$$id(X) = id(Y) \rightarrow \bot)$$

A case cannot fall under two different age groups

$$\phi_3 := (Case(X) \land AGE_GROUP(Y) \land AGE_GROUP(z)$$

 $\land (FALLS_UNDER(X, Y) \land FALLS_UNDER(X, Z),$
 $id(Z) \neq id(Y) \rightarrow \bot)$

A drug cannot be prescribed to a child

$$\phi_{3} := (Terapy(X) \land Drug(Y) \land Case(Z) \land AGE_GROUP(W)$$

$$\land (PRESCRIBED(X, Y) \land RECEIVED(Y, Z)$$

$$\land FALLS_UNDER(Z, W)$$

$$W.ageGroup = "Child" \rightarrow \bot)$$

2.2 LDBC Finbench

An account cannot transfer money if an account is blocked

$$\phi_1 := (Account(X) \land Account(Y) \\ \land (Transfer(X, Y), X.isBLocked = True \rightarrow \bot)$$

A guarantor needs to have more than 5M in the bank account

$$\phi_2 := (Person(X) \land Person(Y) \land Account(Z)$$

$$\land (Guarantee(X, Y) \land Own(Y, Z),$$

$$Z.balance < 500000000 \land id(X) \neq id(Y) \rightarrow \bot)$$

A person cannot be guarantor of themselves

$$\phi_3 := (Account(X) \land Account(Y)$$

 $\land (Guarantee(X, Y), id(X) = id(Y) \rightarrow \bot)$

Interest Rates for company need to be greater than 0.2

$$\begin{split} \phi_4 := & (Company(X) \wedge Loan(Y) \\ & \wedge (Apply(X,Y),Y.interestRate < 0.2 \rightarrow \bot) \end{split}$$

2.3 ICIJ (Real)

An officer of a company cannot register the same address that an Entity has registered

```
\begin{split} \phi_1 := & (Officer(X) \land Entity(Y) \land Address(Y) \land Officer(W) \\ & \land officer\_of(X,Y) \land registered\_address(Y,Z) \\ & \land registered\_address(W,Z), \\ & id(X) = id(W) \rightarrow \bot) \end{split}
```

The registered address of an entity must be the same as the one of the address

```
\phi_2 := Address(X) \land Company(Y)
 \land (registered\_address(X, Y),
 X.country\_codes \neq Y.country\_codes \rightarrow \bot)
```

An intermediary cannot be a shareholder in the same company for which they act as an intermediary

```
\begin{split} \phi_1 := & (Entity(X) \land Intermediary(Y) \land Entity(Z) \\ & \land intermediary\_of(Y,X) \land shareholder\_of(Y,Z), \\ & id(X) = id(Z) \rightarrow \bot) \end{split}
```

A shareholder of a company needs to have at least 1700000 dollars

$$\phi_2 := (Officer(X) \land Company(Y) \land shareholder \ of(X,Y), X.networth < 1700000 \rightarrow \bot)$$

2.4 LDBC SNB

A comment can't be created before its post.

```
\phi_1 := (Comment(X) \land Post(Y) \land TO(X, Y)
\land \  \, X.creationTime < Y.creationTime \rightarrow \bot)
```

Under-age people can't be members of a forum with a higher requirement.

```
\phi_2 := (Person(X) \land Forum(Y) \land HAS\_MEMBER(Y, X)\land X.age < Y.ageRequirement \rightarrow \bot)
```

A person must work at an organisation located in the same place they live.

A person can't like their own post.

$$\phi_4 := (Post(X) \land Person(Y) \land CREATED(Y, X)$$
$$\land LIKES(X, Y) \rightarrow \bot)$$

REFERENCES

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