

Math Prep – Exercise

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Problem Set 3

1. Consider the function $f(x) = 3 + 2x + x^2$. Which is true (use Taylor approximation, or the definition of the little- o and big- O to argue):
 - a. $f(x) = 3 + o(1)$ as $x \rightarrow 0$
 - b. $f(x) = 3 + o(x)$ as $x \rightarrow 0$
 - c. $f(x) = 3 + O(x)$ as $x \rightarrow 0$
 - d. $f(x) = 3 + 2x + o(x)$ as $x \rightarrow 0$
 - e. $f(x) = 6 + o((x - 1))$ as $x \rightarrow 1$
 - f. $f(x) = 6 + O((x - 1))$ as $x \rightarrow 1$
 - g. $f(x) = 6 + 4(x - 1) + O((x - 1)^2)$ as $x \rightarrow 1$
 - i. $f(x) = 6 + 4(x - 1) + o((x - 1))$ as $x \rightarrow 1$
2. Consider the function $f(x) = 3 + 2x + |x|^{1.5}$. Which of the following statements are true:
 - a. $f(x) = 3 + o(1)$ as $x \rightarrow 0$
 - b. $f(x) = 3 + o(x)$ as $x \rightarrow 0$
 - c. $f(x) = 3 + O(x)$ as $x \rightarrow 0$
 - d. $f(x) = 3 + 2x + o(x)$ as $x \rightarrow 0$
 - e. $f(x) = 6 + o((x - 1))$ as $x \rightarrow 1$
 - f. $f(x) = 6 + O((x - 1))$ as $x \rightarrow 1$
 - g. $f(x) = 6 + 3.5(x - 1) + O((x - 1)^2)$ as $x \rightarrow 1$
 - i. $f(x) = 6 + 3.5(x - 1) + o((x - 1))$ as $x \rightarrow 1$
3. Consider the functions $F(x, y) = 2x^2 - 2xy + y^2 - 2x + 2$ and $g(x, y) = 2x$:
 - a. Find the minimum of F in \mathbb{R}^2

- b. Find the minimum of F subject to the constraint $g(x, y) = 4$
- c. Find the minimum of F subject to the constraint $g(x, y) \geq 4$
- d. Find the minimum of F subject to the constraint $g(x, y) \leq 4$

> Solution



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