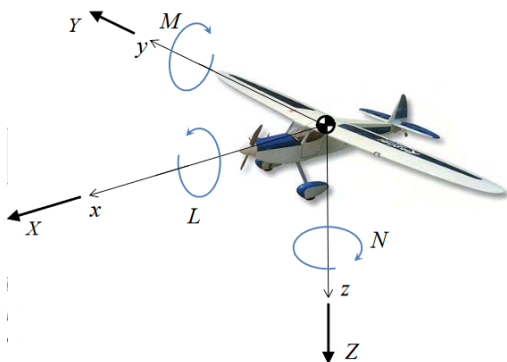


## Nomenclature



$\mathbf{V}_B^E$  = velocity in inertial frame written in body coordinate system

$$\mathbf{F}_B^{aero} = X\mathbf{e}_x + Y\mathbf{e}_y + Z\mathbf{e}_z = [X; Y; Z]$$

$$\mathbf{M}_B^{aero} = \mathbf{G}_B^{aero} = L\mathbf{e}_x + M\mathbf{e}_y + N\mathbf{e}_z = [L; M; N]$$

$$\mathbf{V}_B^E = u^E\mathbf{e}_x + v^E\mathbf{e}_y + w^E\mathbf{e}_z = [u^E; v^E; w^E]$$

$$V_g = |\mathbf{V}_B^E| = \sqrt{(u^E)^2 + (v^E)^2 + (w^E)^2}$$

$$\boldsymbol{\omega}_B^E = p^E\mathbf{e}_x + q^E\mathbf{e}_y + r^E\mathbf{e}_z = [p; q; r]$$

## Four Control Surfaces

**Rudder:**  $+\delta_r$  = towards -y = negative moment & positive force

**Elevator:**  $+\delta_e$  = down = negative moment & negative force

**Aileron:**  $+\delta_a$  = right (+y) down = negative moment

**Throttle:**  $+\delta_t$  = no moment, positive force.

## Wind

**Background Wind:**  $\mathbf{V}^E = \mathbf{V} + \mathbf{W}$  **Wind Angles:**

$$V = |\mathbf{V}_B|$$

$$a = \arctan \frac{w}{u}, \beta = \arcsin \frac{v}{V}$$

$$u = V \cos \beta \cos \alpha, v = V \sin \beta, w = V \cos \beta \sin \alpha$$

$\alpha$  = angle of attack,  $\beta$  = sideslip angle

## Euler Angles

$$R_E^B(\phi, \theta, \psi) = R_{v_2}^B(\phi) R_{v_1}^{v_2}(\theta) R_E^{v_1}(\psi)$$

Body to Inertial Frame Transformation:

$$\mathbf{p}_B = R_E^B \mathbf{p}_E \rightarrow \mathbf{p}_E = R_B^E \mathbf{p}_B$$

$$R_B^E = (R_E^B)^T$$

**Stability Frame:**  $\mathbf{p}_s = R_B^s \mathbf{p}_B$

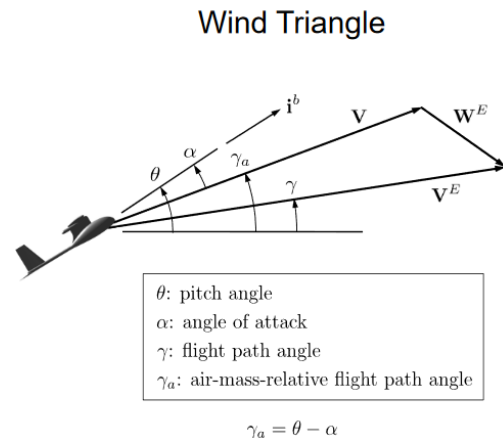
$$R_B^s(\alpha) = \begin{pmatrix} \cos \alpha & 0 & \sin \alpha \\ 0 & 1 & 0 \\ -\sin \alpha & 0 & \cos \alpha \end{pmatrix}$$

**Wind Frame:**  $\mathbf{p}_w = R_s^w(\alpha) \mathbf{p}_s$

$$R_B^w(\alpha, \beta) = R_s^w(\beta) R_B^s(\alpha) = \begin{pmatrix} \cos \beta \cos \alpha & \sin \beta & \cos \beta \sin \alpha \\ -\sin \beta \cos \alpha & \cos \beta & -\sin \beta \sin \alpha \\ -\sin \alpha & 0 & \cos \alpha \end{pmatrix}$$

$$R_w^B(\alpha, \beta) = (R_B^w)^T(\alpha, \beta)$$

## Wind Triangle



## Kinematics and Dynamics

Name	Description
$x_E$	Intertial x (North) position
$y_E$	Intertial y (East) position
$z_E$	Intertial z (Down) position
$\phi$	Roll Angle
$\theta$	Pitch Angle
$\psi$	Yaw Angle
$u^E$	Inertial Velocity along $\hat{i}_B$
$v^E$	Inertial Velocity along $\hat{j}_B$
$w^E$	Inertial Velocity along $\hat{k}_B$
$p$	Angular Velocity along $\hat{i}_B$ (Roll rate)
$q$	Angular Velocity along $\hat{j}_B$ (Pitch rate)
$r$	Angular Velocity along $\hat{k}_B$ (Yaw rate)