








Logic Gates






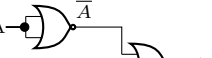
Type	Gate	Truth Table	Boolean Logic															
not		<table><tr><th>in</th><th>out</th></tr><tr><td>0</td><td>1</td></tr><tr><td>1</td><td>0</td></tr></table>	in	out	0	1	1	0	$Y = \overline{A}$									
in	out																	
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and		<table><tr><th>A</th><th>B</th><th>out</th></tr><tr><td>0</td><td>0</td><td>0</td></tr><tr><td>0</td><td>1</td><td>0</td></tr><tr><td>1</td><td>0</td><td>0</td></tr><tr><td>1</td><td>1</td><td>1</td></tr></table>	A	B	out	0	0	0	0	1	0	1	0	0	1	1	1	$Y = AB$
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or		<table><tr><th>A</th><th>B</th><th>out</th></tr><tr><td>0</td><td>0</td><td>0</td></tr><tr><td>0</td><td>1</td><td>1</td></tr><tr><td>1</td><td>0</td><td>1</td></tr><tr><td>1</td><td>1</td><td>1</td></tr></table>	A	B	out	0	0	0	0	1	1	1	0	1	1	1	1	$Y = A + B$
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nor		<table><tr><th>A</th><th>B</th><th>out</th></tr><tr><td>0</td><td>0</td><td>1</td></tr><tr><td>0</td><td>1</td><td>0</td></tr><tr><td>1</td><td>0</td><td>0</td></tr><tr><td>1</td><td>1</td><td>0</td></tr></table>	A	B	out	0	0	1	0	1	0	1	0	0	1	1	0	$Y = \overline{A + B}$
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A	B	out																
0	0	1																
0	1	0																
1	0	0																
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Logic Identities

- $A + B = B + A$
- $AB = BA$
- $A + (B + C) = (A + B) + C$
- $A(BC) = (AB)C$
- $A(B + C) = AB + AC$
- $(A + B)(C + D) = AC + AD + BC + BD$
- $\overline{1} = 0$
- $\overline{0} = 1$
- $A \cdot 0 = 0$
- $A \cdot 1 = A$
- $A + 0 = A$
- $A + 1 = 1$
- $A + A = A$
- $AA = A$
- $\overline{\overline{A}} = A$
- $A + \overline{A} = 1$
- $A\overline{A} = 0$
- $\overline{A + B} = \overline{A} \cdot \overline{B}$
- $\overline{A \cdot B} = \overline{A} + \overline{B}$
- $A + \overline{A}B = A + B$
- $A \oplus B = \overline{A}B + A\overline{B} = (A + B)(\overline{AB})$
- $\overline{A \oplus B} = AB + \overline{A} \cdot \overline{B}$

Boolean Math

Commutative Rules
$A \cdot B = B \cdot A$ $A + B = B + A$
Associative Rules
$(A \cdot B) \cdot C = A \cdot (B \cdot C)$ $(A + B) + C = A + (B + C)$
Distributive Rules
$A \cdot (B + C) = A \cdot B + A \cdot C$ $(A + B) \cdot (A + C) = A + (B \cdot C)$
Absorption Rules
$A \cdot (A + B) = A$ $A + (A \cdot B) = A$

Logic Gate	NAND Eq.	NOR Eq.
	 $\overline{AA} = \overline{A}$	 $\overline{A + A} = \overline{A}$
	 $\overline{\overline{AB}} = AB$	 $\overline{\overline{AB}} = AB$

De Morgan's Theorem

$\overline{A \cdot B} = \overline{A} + \overline{B}$
 $\overline{A \cdot B \cdot C} = \overline{A} + \overline{B} + \overline{C}$
 $\overline{A + B} = \overline{A} \cdot \overline{B}$
 $\overline{A + B + C} = \overline{A} \cdot \overline{B} \cdot \overline{C}$