

201B172

## Jaypee University of Engineering and Technology

### 18B11CI311– Data Structures

B.Tech -3<sup>rd</sup> Semester

#### Tutorial – 5 (Sorting Algorithms)

Consider the following arrays (Contains 8 elements to be sorted in ascending order) -

Array W - 4, 5, 7, 1, 6, 10, 17, 13

Array X - 20, 15, 13, 11, 4, 3, 2, 1

Array Y - 32, 4, 6, 9, 12, 3, 11, 10

Array Z - 5, 8, 12, 17, 19, 23, 41, 50

1. Give the number of swaps in 4<sup>th</sup> pass in bubble sort for array W.
2. What is the time complexity of selection sort for array X and give the output of 4<sup>th</sup> pass.
3. With reference to insertion sort, which of above arrays (W, X, Y, Z) will be worst, average and best case. Justify your answer with algorithmic statements.
4. Array Z is the worst case input instance of quick sort. Justify the statement.
5. Compare quick and merge sort. Use the above arrays (W, X, Y, Z) to give specific time complexity case.
6. What is the worst case time complexity of insertion sort where position of the data to be inserted is calculated using binary search?
7. Consider the array A[] = {6,4,8,1,3} apply the insertion sort to sort the array . Consider the cost associated with each shift is 5 rupees, what is the total cost of the insertion sort when element 1 reaches the first position of the array?
8. Let t1 and t2 be the number of comparisons made by P for the inputs {1, 2, 3, 4, 5} and {4, 1, 5, 3, 2} respectively. Mention the relation between t1 and t2 for the following cases:
  - a. Quick sort using the first element as pivot.
  - b. Bubble sort
  - c. Insertion sort
  - d. Selection sort
9. Give the practical situations where each of the following sorting algorithms should be preferred over other. Also mention which one is stable and in-place along with their time complexity (best, average and worst case).
  - a. Quick sort
  - b. Bubble sort
  - c. Insertion sort
  - d. Selection sort
  - e. Merge sort
10. Apply bubble sort, selection sort, insertion sort, quick sort, and merge sort on following array. Show all the steps.  
15, 6, 2, 5, 9, 10, 45, 32, 9, 3

## Tutorial-5

Array W = 4, 5, 7, 1, 6, 10, 17, 13

Array X = 20, 15, 13, 11, 4, 8, 2, 1

Array Y = 32, 4, 6, 9, 12, 3, 11, 10.

Array Z = 5, 8, 12, 17, 19, 23, 41, 50

- following arrays (contains 8 elements  
to be sorted in ascending order)

- (1) The number of swaps in 4<sup>th</sup> pass in bubble sort  
for array W is 5

for 0<sup>th</sup> pass - number of swaps = 3  
and resultant array.

4 5 1 7 6 10 17 13

for 1<sup>st</sup> pass - swaps = 4

array = 1 4 5 6 7 10 13 17

for 2<sup>nd</sup> pass - swaps = 5

array = 1 4 5 6 7 10 13 17

(Here array sorted)

- (2) Here array X is reverse sorted so in worst case  
time complexity is  $O(n^2)$   
and output of 4<sup>th</sup> pass (starting with pass 0)  
 $\rightarrow 1, 2, 3, 4, 11, 13, 15, 20.$

③ With reference to insertion sort.

Array X → This is worst case as the array is reverse sorted.

Array Z → This is best case as the array is already sorted.

Array W → As most of the elements are already sorted and Array Y sorted only a few swaps and passes are needed, that is why this is an average case.

④ As array Z is already sorted which is the worst case in quick sort.

Array Z: 5, 8, 12, 17, 19, 23, 41, 50.

It is already sorted and takes  $O(n^2)$  time.

⑤ Worst case time complexity will be  $O(n^2)$  because applying binary search to calculate the position of the data to be inserted doesn't reduce the time complexity of insertion sort. This is because insertion of a data at an appropriate position involves two steps:

(1) Calculate the position

(2) Shift the data from the position calculated in step 1 one step right to create a gap where the data will be inserted.

## Insertion Sorting

(7)

$$A[J] = \{6, 4, 8, 1, 3\}$$

$$\text{Step 1} \Rightarrow 4 \ 6 \ 8 \ 1 \ 3$$

$$\text{Step 2} \Rightarrow 1 \ 4 \ 6 \ 8 \ 3$$

Here when the element 1 reaches the first position of the array thus comparisons are only required

$$1 \times 2 = 2 \text{ comparisons}$$

(8)

	Worst Case	Average Case	Best Case	Stable	In-place
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Bubble sort	$N^2$	$N^2$	$N$	Yes	Yes
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Selection sort	$N^2$	$N^2$	$N^2$	No	Yes
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Insertion sort	$N^2$	$N^2$	$N^2$	Yes	Yes
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Quick sort	$N^2$	$N \log N$	$N \log N$	No	Yes
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Merge sort	$N \log N$	$N \log N$	$N \log N$	Yes	No
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Practical situations where each of the following sorting algorithms should be preferred over other:

Selection Sort: Situation when swap operation is very costly.

Insertion Sort: When the sorting applied on the array which is sorted or almost sorted.

Bubble Sort: This gives fastest result on an extremely small or nearly sorted set of data.

Merge Sort: Widely used for external sorting, where random access can be very, very expensive.

Quick Sort: When we don't need a stable sort and average case performance matters more than worst case performance.

(b) Bubble Sort:

$$T_1 = 10$$

$$T_2 = 10$$

$$\therefore T_1 = T_2$$

(c) Selection Sort:

$$T_1 = 10$$

$$T_2 = 10$$

$$\therefore T_1 = T_2$$

(c) Insertion Sort:

$$T_1 = 4$$

$$T_2 = 8$$

$$T_2 > T_1$$

(a)

(10)

Given array: 15 6 2 5 9 10 45 32 9 3

Bubble sort:

15	6	2	5	9	10	45	32	9	3
6	15	2	5	9	10	45	32	9	3
6	2	15	5	9	10	45	32	9	3
6	2	5	15	9	10	45	32	9	3
6	2	5	9	15	10	45	32	9	3
6	2	5	9	10	15	45	32	9	3
6	2	5	9	10	15	32	45	9	3
6	2	5	9	10	15	32	9	45	3
6	2	5	9	10	15	32	9	3	45
2	6	5	9	10	15	32	9	3	45
2	5	6	9	10	15	32	9	3	45
2	5	6	9	10	15	9	32	3	45
2	5	6	9	10	15	9	3	32	45
2	5	6	9	10	9	15	3	32	45
2	5	6	9	10	9	3	15	32	45
2	5	6	9	9	10	3	15	32	45
2	5	6	9	9	8	10	15	32	45
2	5	6	9	8	9	10	15	32	45
2	5	6	3	9	9	10	15	32	45
2	5	3	6	9	9	10	15	32	45
2	3	5	6	9	9	10	15	32	45

Selection Sort.

15	6	2	5	9	10	45	32	9	3
15	6	2	5	9	10	3	32	9	45
15	6	2	5	9	10	3	9	32	45
9	6	2	5	9	10	3	15	32	45
9	8	2	5	9	3	10	15	32	45
3	6	2	5	9	9	10	15	32	45
3	5	2	6	9	9	10	15	32	45
3	2	5	6	9	9	10	15	32	45
2	3	5	6	9	9	10	15	32	45

Insertion Sort:

15	6	2	5	9	10	45	32	9	3
6	15	2	5	9	10	45	32	9	3
6	2	15	5	9	10	45	32	9	3
2	6	15	5	9	10	45	32	9	3
2	6	15	15	9	10	45	32	9	3
2	6	15	15	9	10	45	32	9	3
2	5	6	15	9	10	45	32	9	3
2	5	6	15	9	10	45	32	9	3
2	5	6	9	15	10	45	32	9	3
2	5	6	9	15	10	45	32	9	3
2	5	6	9	10	15	45	32	9	3
2	5	6	9	10	15	32	45	9	3
2	5	6	9	10	15	32	45	9	3
2	5	6	9	9	10	15	32	45	3
2	5	6	9	9	10	15	32	3	45
2	5	6	9	9	10	15	32	3	45

2	5	6	9	9	10	3	15	32	45
2	5	6	9	9	3	10	15	32	48
2	5	6	9	3	9	10	15	32	48
2	5	6	3	9	9	10	15	32	48
2	5	3	6	9	9	10	15	32	48
2	3	5	6	9	9	10	15	32	48

Quick Sort.

15	6	2	5	9	10	45	32	9	3
15	6	2	5	3	10	45	32	9	9
8	6	2	5	15	10	45	32	9	9
3	6	2	5	9	10	45	32	9	15
3	5	2	6	9	10	45	32	9	15
3	2	5	6	9	10	45	32	9	15
2	3	5	6	9	10	45	32	9	15
2	3	5	6	9	10	45	15	9	82
2	3	5	6	9	10	9	15	45	32
2	3	5	6	9	10	9	15	32	45
2	3	5	6	9	10	15	9	32	45
2	3	5	6	9	9	15	10	32	45
2	3	5	6	9	9	10	15	32	45

short span

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spike

gap

gap

gap

gap

## MergeSort:

15	6	2	5	9	10	45	32	9	3
15	6	2	5	9	10	45	32	9	3
6	15	2	5	9	10	45	32	3	9
6	15	2	5	9	10	45	32	9	32
2	5	6	9	15	3	9	10	32	45
2	3	5	6	9	9	10	15	32	45

(5)

For Array in MergeSort.

X - It is worst average

W - It is average

Y - It is average

Z - It is best.

For Array in Quic sort.

X → worst

Y → avg

W → avg

Z → worst.

Case	quick sort	MergeSort
best	$n \log n$	$n \log n$
avg	$n \log n$	$n \log n$
worst	$n^2$	$n \log n$