

#### Creating and Evaluating **Stochastic Regression Models** TECO on the Basis of Heterogeneous Sensor Networks

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#### Motivation



Given is a heterogeneous network of sensors – the network contains "good" **and** "bad" sensors.

- good calibrated and high precision of the measurements
- bad uncalibrated and low precision of the measurements

#### Interesting Questions:

- Can we use the bad sensors in order to predict the values of the good ones?
- Can we identify the weak parts of the network?

#### Our approach to the problems:

- Use of stochastic regression models.
- Formal evaluation of the models through the use of proper scoring rules, verification rank histograms and predictive performance checks.
- Analyzing the relevance of each predictor for the final prediction through the use of a feature importance technique.

## **Data**

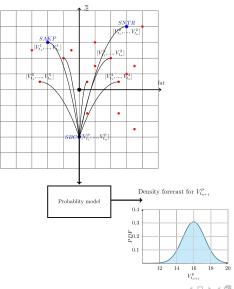


- Heterogeneous Network of air pollution sensors in Stuttgart.
  - LU-BW (Landesanstalt für Umwelt, Messungen und Naturschutz Baden-Württemberg) - 3 Sensors of high quality.
    - Station names: SBC, SNTR, SAKP
  - luftdaten.info Public data from cheap DIY sensors.
- Considered period: the year of 2018.
- Challenges:
  - Noisy data.
  - Holes in the data.
  - Station SAKP provides air pollution values only for the last four months of the considered year.
  - The DIY sensors provide values for each minute of the day, the LUBW sensors - for thirty-minute intervals



### **General View**







## Goals and not goals



#### Goals:

- Investigate how the considered models perform on the data.
- Show that the use of stochastic regression models is a feasible approach to predicting air pollution values in heterogeneous networks of sensors.
- Show that the unreliable parts of the network can be identified through the use of feature importance technique\*.

#### Not goals:

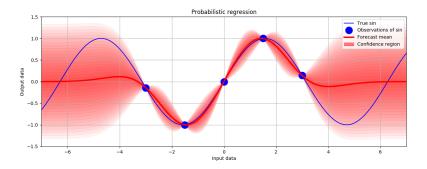
Build the best possible model for predicting air pollution values.



# **Stochastic Regression Models**



- lacktriangle Regression: feature vector  $\mapsto$  a real value
- Stochastic Regression: feature vector → a probability distribution

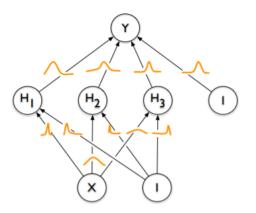




### **Concrete Models**



Bayesian Neural Networks

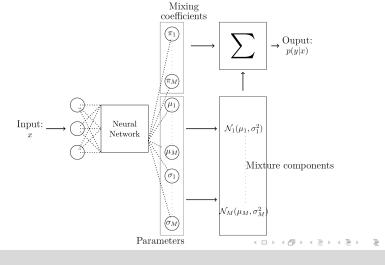




#### **Concrete Models**



Mixture Density Networks



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#### **Concrete Models**



#### Empirical model

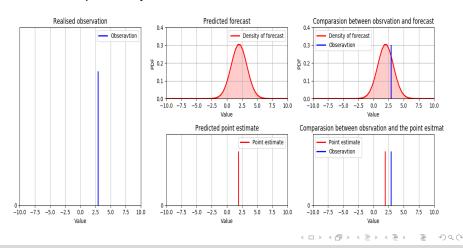
- Past observations are treated as values of a random variable. From that a distribution for a predicted future value is implied.
- We use this model as a baseline.

We hope to achieve better results than the empirical model with the other two models.

# **Evaluation of probability distributions**



 We do not compare point estimate with a realized real value but rather a probability distribution with a real value.



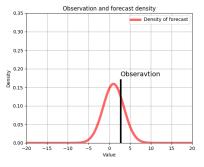
# **Proper Scoring Rules**

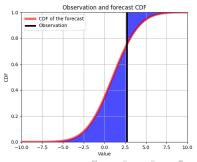


#### Continuous Rank Probability Score

 CRPS compares a distribution with an observation, where both are represented as cumulative distribution functions.

$$CRPS(F, y) = \int_{-\infty}^{\infty} (F(x) - \mathbb{1}\{y \le x\})^2 dx$$

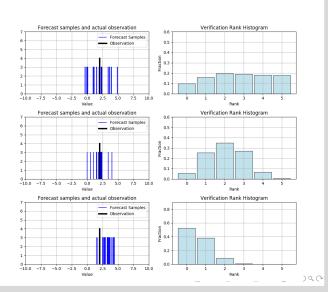




# **Verification Rank Histograms**



Does the observation behave like a random sample from the forecast distribution?



## Feature importance



- Assess the relative importance of all features used by a model.
  - Important: Importance is relative only to the model itself.
- Random shuffling of each predictor/feature in the test set one at a time and observing the increase/decrease in mean the CRPS value compared to the unpermuted features.

# **Training**



Approach

Based on the data and the examined types of models there are several orthogonal considerations to make when it comes to training:

- Target LUBW-Station SAKP, SBC, SNTR
- Integration period one day, twelve hours, one hour
- Use of the other two LUBW station yes or no
- Predicted air pollution value PM10 or PM2.5
- Used model BNN or MDN (two types of MDNs)

We wanted to investigate every possible combination.

- Challenges:
  - BNNs are very hard to train.
  - A lot of possible ways to train several different models.





Results presented here: representative sample of all results.



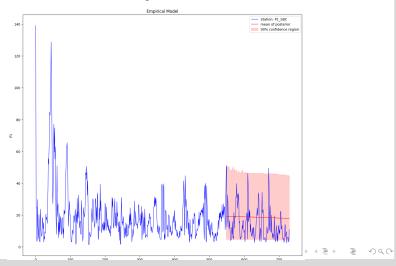
Results presented here: representative sample of all results.

 Plots showing how exactly the built models predict the values of their train and test sets.



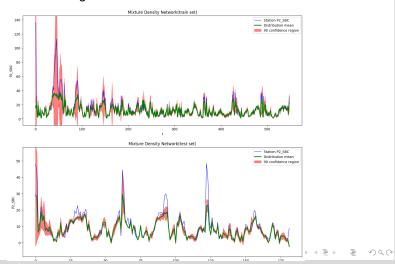


#### Empirical Model, twelve hour averaged data



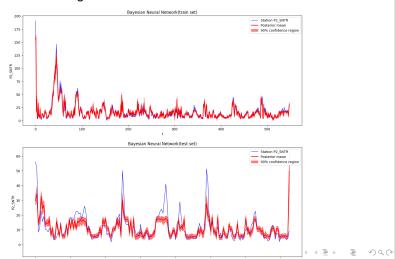


#### MDN, twelve hour averaged data





#### BNN, twelve hour averaged data





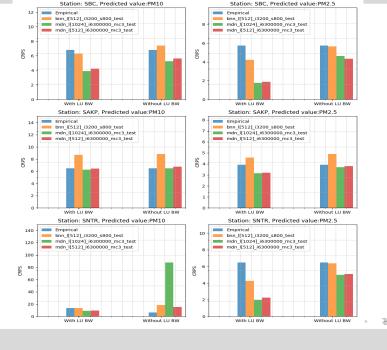
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Plots of the models modeling their respective test and train sets.



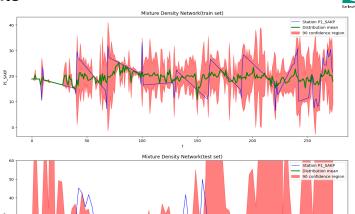
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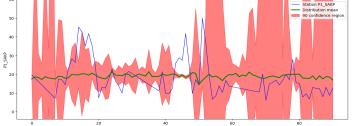
- Plots of the models modeling their respective test and train sets.
- Plots comparing the built models with respect their CRPS score across LUBW Station, use of LUBW data and predicted air pollution value.



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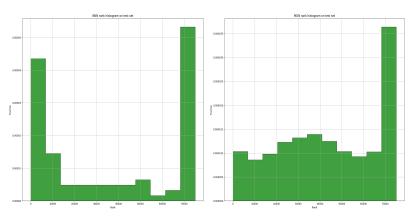
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- Two rank histograms reflecting the results of all built models.





BNN (one day average) and MDN (one hour average), Rank Histograms





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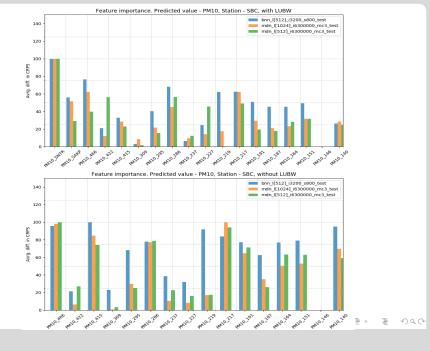




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- Two rank histograms reflecting the results of all built models.
- Feature importance data.





#### Conclusion



#### The results show:

- Stochastic regression models are a viable approach for predicting values in the investigated sensor network.
- Few sensors have consistently low feature importance for the built models.
- There is clearly room for improvement of the models.



Thank you for your attention.



# Questions?