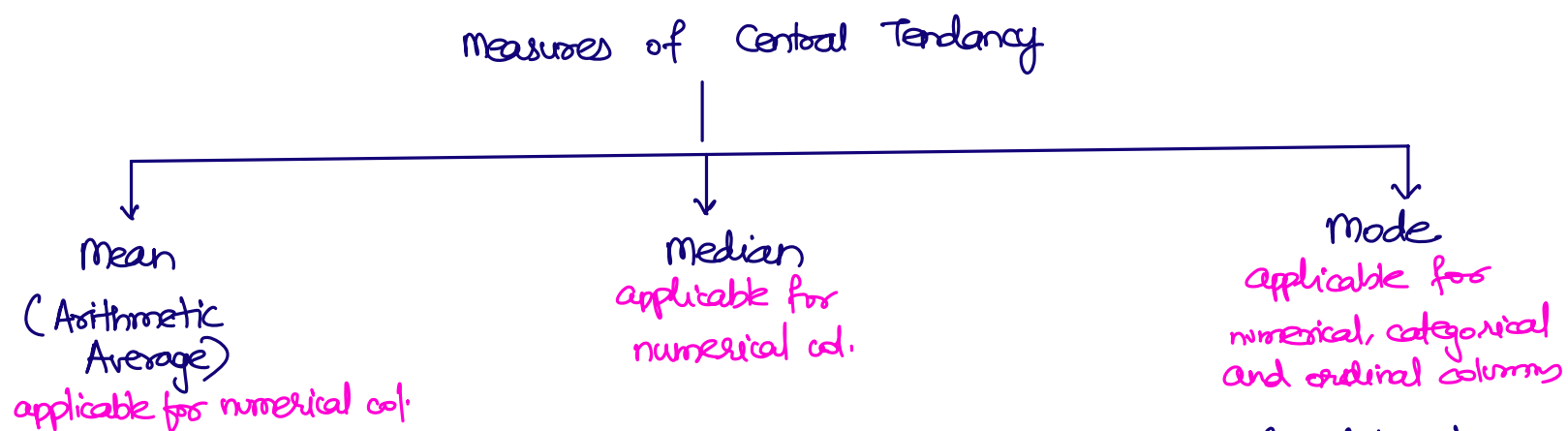


Descriptive Statistics

Measures of Central Tendency :

These are statistical tools used to summarize the data based on the central point of the data.



@ Mean: The sum of all data points divided by number of data pts

$$\text{mean} = \frac{\sum_{i=1}^n x_i}{n}$$

n no. of records

eg: [2, 3, 4, 5]

$$\text{mean} = \frac{2+3+4+5}{4} = 3.5$$

@ Median: It's the middle value of the dataset when it's ordered from smallest to largest.

Calc. median

① Order the data in ascending order.

② Identify the middle position

- if no. of records is odd, the median value is at $\left(\frac{n+1}{2}\right)^{\text{th}}$ position.

eg: [3, 1, 4, 1, 5]

→ [1, 1, 3, 4, 5]

Here,
the middle position will be $\frac{5+1}{2} = 3^{\text{rd}}$ position $\Rightarrow 3 //$

- if no. of records is even, the median value is the avg of $\left(\frac{n}{2}\right)^{\text{th}}$ position value and $\left(\frac{n}{2}+1\right)^{\text{th}}$ position value.

eg: [3, 1, 4, 1]

→ [1, 1, 3, 4]

Here,
middle position $\left(\frac{4}{2}\right) = 2^{\text{nd}}$ & $\left(\frac{4}{2}+1\right) = 3^{\text{rd}}$

$$\text{median} = \frac{1+3}{2} = \underline{\underline{2}}$$

③ Mode → most frequent data. / data with highest frequency (count)

steps:

- ① Count the frequency of each unique value
- ② Identify the value with highest frequency.

eg [1, 2, 2, 3, 3, 3, 4]

1 → 1 4 → 1
2 → 2
3 → 3

∴ mode = 3 //

Note: if all unique data has same frequency, in that case, sort the data in ascending order and return the first value

eg: $[1, 2, 3, 4] \rightarrow \underline{1}$

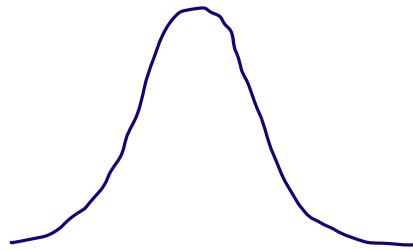
$[1, 2, 2, 3, 3] \rightarrow$
 $\begin{matrix} 1 \rightarrow 1 \\ 2 \rightarrow 2 \\ 3 \rightarrow 2 \end{matrix} \rightarrow \text{sort} \rightarrow 2 //$

Data Distributions

This concept is applicable only for numerical columns

① Normal Distribution | Gaussian Distribution | Bell curve

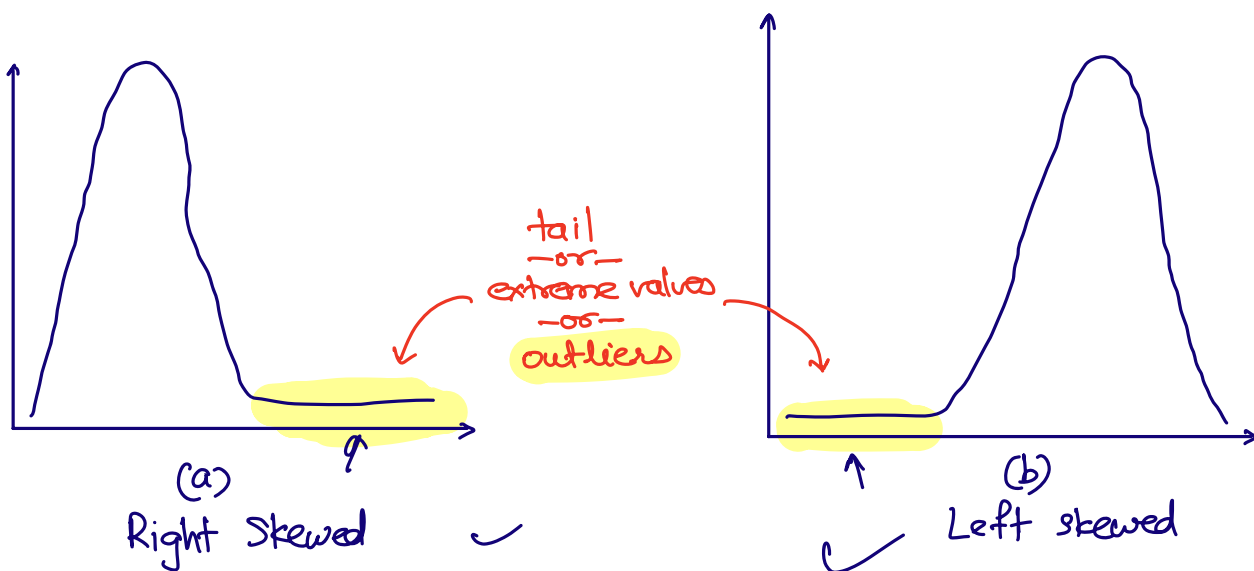
GENERALIZED
DATA



if data column forms a bell curve, chances are data is generalized.

(the data may represent the population)

② Skewed distribution.



Quartiles

Quartiles are the values that divide the dataset into 4 equal parts.

25%	50%	75%	100%
Q_1	Q_2	Q_3	Q_4
First Quartile	Second Quartile (median)	Third Quartile	Maximum

consider a dataset $D = \{12, 15, 7, 23, 10, 8, 14, 18, 5, 20\}$

To calc quartiles

step 1: Arrange the data in ascending order

$\{ \underset{1}{5}, \underset{2}{7}, \underset{3}{8}, \underset{4}{10}, \underset{5}{12}, \underset{6}{14}, \underset{7}{15}, \underset{8}{18}, \underset{9}{20}, \underset{10}{23} \}$

step 2: Identify the median

$$\text{median} = 13 \Rightarrow Q_2$$

step 3: Calc first quartile (Q_1)

Q_1 is the median of the lower half of the dataset

$$Q_1 = 8 //$$

step 4: Calc third quartile (Q_3)

Q_3 is the median of the upper half of the dataset

$$Q_3 = 18 //$$

step 5: Calc fourth quartile (Q_4)

Q_4 is the max value

$$Q_4 = 23 //$$

Outliers

Outliers are those extreme values that affect the general tone of the domain.

To identify & remove an outlier, you can use Tukey's Method
— or —
1.5 IQR rule.

Tukey's Method	1.5 IQR rule
----------------	--------------

↳ Inter Quartile Range

$$IQR = Q3 - Q1$$

Algo:

① Calc IQR

$$IQR = Q3 - Q1$$

② Calc the valid range of the given column.

$$\text{lowerRange} = Q1 - (1.5 * IQR)$$

$$\text{upperRange} = Q3 + (1.5 * IQR)$$

