

CAS 741: SRS

Aqueous Speciation Diagram Generator

Steven Palmer

`palmes4`

October 6, 2017

Revision History

Table 1: Revision History

Date	Developer(s)	Change
10.5.2017	S. Palmer	First revision of document

Reference Material

This section records information for easy reference.

Table of Units

Throughout this document SI (Système International d'Unités) is employed as the unit system. In addition to the basic units, several derived units are used as described below. For each unit, the symbol is given followed by a description of the unit and the SI name.

symbol	unit	SI
m	length	metre
kg	mass	kilogram
s	time	second
°C	temperature	centigrade
mol	amount of substance	mole
l	volume	litre ($l = 10^{-3} \cdot \text{m}^3$)
Pa	pressure	pascal ($\text{Pa} = \text{kg m}^{-1} \text{s}^{-2}$)
bar	pressure	bar ($\text{bar} = 10^5 \cdot \text{Pa}$)

Table of Symbols

The table that follows summarizes the symbols used in this document along with their units. The choice of symbols was made to be consistent with chemistry literature. The symbols are listed in alphabetical order.

symbol	unit	description
A	–	reactant species in a chemical equation
B	–	product species in a chemical equation
K	–	equilibrium constant
R	–	an arbitrary reversible reaction
\overline{RK}_{in}	–	the input set of all pairs of reactions and associated equilibrium constants
\overline{S}	–	a set of aqueous solute species in a chemical system
\overline{S}_{in}	–	the input set of all aqueous solute species in the chemical system
\overline{T}_{in}	–	the input set of total concentrations of chemical elements
X	–	arbitrary chemical species
x	–	arbitrary chemical element

x_{tot}	mol/l	total concentration of an arbitrary chemical element x
$[X]$	mol/l	concentration of the arbitrary chemical species X
$\{X\}$	–	activity of the arbitrary chemical species X
z_X	–	charge number of an arbitrary aqueous solute X

Abbreviations and Acronyms

symbol	description
A	Assumption
DD	Data Definition
GD	General Definition
GS	Goal Statement
IM	Instance Model
LC	Likely Change
PS	Physical System Description
R	Requirement
SATP	Standard Ambient Temperature and Pressure
SRS	Software Requirements Specification
SpecGen	The Aqueous Speciation Diagram Generator program
T	Theoretical Model

Contents

Revision History	i
Reference Material	ii
Table of Units	ii
Table of Symbols	ii
Abbreviations and Acronyms	iii
1 Introduction	1
1.1 Purpose of Document	1
1.2 Scope of Requirements	1
1.3 Characteristics of Intended Reader	1
1.4 Organization of Document	1
2 General System Description	2
2.1 System Context	2
2.2 User Characteristics	2
2.3 System Constraints	2
3 Specific System Description	2
3.1 Problem Description	3
3.1.1 Terminology and Definitions	3
3.1.2 Physical System Description	3
3.1.3 Goal Statements	3
3.2 Solution Characteristics Specification	4
3.2.1 Assumptions	4
3.2.2 Theoretical Models	4
3.2.3 General Definitions	9
3.2.4 Data Definitions	10
3.2.5 Instance Models	12
3.2.6 Data Constraints	13
3.2.7 Properties of a Correct Solution	13
4 Requirements	14
4.1 Functional Requirements	14
4.2 Nonfunctional Requirements	14
5 Likely Changes	15
6 Traceability Matrices and Graphs	15

1 Introduction

1.1 Purpose of Document

The purpose of this document is to describe the requirements for the Aqueous Speciation Diagram Generator program (herein referred to as SpecGen), a software product that will produce a speciation diagram given a set of chemical reactions and element totals that define a chemical system as inputs. The goals and theoretical models used in the SpecGen code are provided, with an emphasis on explicitly identifying assumptions and unambiguous definitions. This document is intended to be used as a reference to provide all information necessary to understand and verify the transformation of inputs to outputs. The SRS is abstract: the contents describe the problem being solved, but not how to solve it.

This document will be used as a starting point for subsequent development phases, including writing the design specification and the software verification and validation plan. The design document will show how the requirements are to be realized, including decisions on the numerical algorithms and programming environment. The verification and validation plan will show the steps that will be used to increase confidence in the software documentation and the implementation. Although the SRS fits in a series of documents that follow the so-called waterfall model, the actual development process is not constrained in any way. Even when the waterfall model is not followed, as [Parnas and Clements \(February 1986\)](#) point out, the most logical way to present the documentation is still to "fake" a rational design process.

1.2 Scope of Requirements

[Note: Think about what should actually go here for revision 1. Major assumptions? — SP] The scope of the requirements includes collecting all input parameters that describe a chemical system. Given the appropriate inputs, the code for SpecGen is intended to use the data to produce a speciation diagram in the pH range 0 to 14.

1.3 Characteristics of Intended Reader

Reviewers of this documentation should have an understanding of first year undergraduate physical chemistry.

1.4 Organization of Document

The organization of this document follows the template for an SRS for scientific computing software proposed by [Smith and Lai \(2005\)](#) and [Koothoor \(2013\)](#), with some aspects taken from [Robertson and Robertson \(1999\)](#). The presentation follows the standard pattern of presenting goals, theories, definitions, and assumptions. For readers that would like a more bottom up approach, they can start reading the data definitions in Sec:DataDefi and trace back to find any additional information they require.

The goal statements are refined to the theoretical models, and the theoretical models to the instance models. The data definitions are used to support the definitions of the different models.

2 General System Description

This section identifies the interfaces between the system and its environment, describes the user characteristics and lists the system constraints.

2.1 System Context

- User Responsibilities:
 - Ensure that the input data is correct.
 - Ensure that the input data is sufficient to specify a chemical system that has a unique speciation solution.
- SpecGen Responsibilities:
 - Detect data type mismatch, such as a string of characters instead of a floating point number.
 - Determine if the inputs satisfy the required physical and software constraints.
 - Solve the system of equations arising from the input data to generate the output data.
 - Generate a plot of the output data.

2.2 User Characteristics

The end user of SpecGen should have an understanding of first year undergraduate physical chemistry.

2.3 System Constraints

There are no system constraints.

3 Specific System Description

This section first presents the problem description, which gives a high-level view of the problem to be solved. This is followed by the solution characteristics specification, which presents the assumptions, theories, definitions and finally the instance models.

3.1 Problem Description

Chemical speciation refers to the stable (equilibrium) distribution of chemical species in a given chemical system. Speciation diagrams, which plot species concentrations against an independently varied parameter of the system, are useful tools for displaying speciation data in a concise and easy to use format. The production of speciation diagrams requires solving a set of non-linear equations which arise from the chemical reactions of the species present in a chemical system. As the number of reactions taking place in a system increases, producing speciation diagrams can quickly become a tedious undertaking when done manually.

SpecGen will produce a speciation diagram given a set of chemical reactions, equilibrium constants, and element totals that define a chemical system. SpecGen will be specific to speciation of ions in aqueous systems under varying pH, which is of particular importance in the fields of aqueous process engineering and hydrometallurgy. The diagram generated by SpecGen will plot speciation of all aqueous species (excluding H^+ and OH^-) across the pH range 0 to 14.

3.1.1 Terminology and Definitions

This subsection provides a list of terms that are used in the subsequent sections and their meaning, with the purpose of reducing ambiguity and making it easier to correctly understand the requirements:

Activity: the “effective concentration” of a species in a chemical system

Equilibrium: the state of a chemical system in which species concentrations are stable

SATP: standard ambient temperature pressure ($T = 25^\circ\text{C}$, $P = 1 \text{ bar}$)

3.1.2 Physical System Description

The physical system of SpecGen includes the following elements: [I don’t think I need a diagram here. It’s just water with dissolved solutes. —SP]

PS1: An unspecified volume of liquid water containing dissolved chemical species under equilibrium conditions.

3.1.3 Goal Statements

Given a set of chemical species present in an aqueous chemical system, a set of reversible reactions and associated equilibrium constants that the species are subject to, and the total concentrations of all elements present in the species set (excluding O and H), the goal statements are:

GS1: Calculate the equilibrium concentrations of all chemical species present in the system over the pH range 0 to 14.

GS2: Generate a plot of the equilibrium concentrations of all chemical species present in the system versus pH.

3.2 Solution Characteristics Specification

The instance models that govern SpecGen are presented in § 3.2.5. The information to understand the meaning of the instance models and their derivation is also presented, so that the instance models can be verified.

3.2.1 Assumptions

This section simplifies the original problem and helps in developing the theoretical model by filling in the missing information for the physical system. The numbers given in the square brackets refer to the theoretical model [T], general definition [GD], data definition [DD], instance model [IM], or likely change [LC], in which the respective assumption is used.

- A1: All generated speciation diagrams will cover the pH range 0 to 14. [IM1]
- A2: All generated speciation diagrams are at SATP conditions. It follows that all user supplied equilibrium constants are assumed to be values measured under SATP conditions. [GD1, LC1]
- A3: The chemical system is assumed to be a single-solvent solution, where the solvent is liquid water at SATP. The chemical species in all of the user supplied equations are assumed to be aqueous solutes or water. [IM1, LC2]
- A4: The activity of liquid water is assumed to be 1.0. [IM1, LC3]
- A5: The activities of all aqueous solute species are assumed to be equal to their concentration. [IM1, LC3]
- A6: All chemical equations supplied by the user are assumed to be reversible (finite equilibrium constant). [DD1]

3.2.2 Theoretical Models

This section focuses on the general equations and laws that SpecGen is based on.

Number	T1
Label	Equational representation of reversible chemical reactions
Equation	$\alpha_1 A_1 + \cdots + \alpha_n A_n \rightleftharpoons \beta_1 B_1 + \cdots + \beta_m B_m$
Description	<p>The above equation represents a reversible chemical reaction where:</p> <p>n is the number of reactants</p> <p>m is the number of products</p> <p>A_i is the i^{th} reactant species</p> <p>α_i is the stoichiometric coefficient of the i^{th} reactant</p> <p>B_j is the j^{th} product species</p> <p>β_j is the stoichiometric coefficient of the j^{th} product</p>
Source	Wikipedia (2016)
Ref. By	T4, T5

Number	T2
Label	Conservation of mass (concentration balance)
Equation	$x_{tot} = \sum \{X : \bar{S} \mid x \in X \bullet \#x\langle X \rangle \cdot [X]\}$
Description	<p>The total dissolved concentration of an element in an aqueous solution is equal to the sum of the concentrations of all species which contain that element. This is captured in the above equation, where:</p> <p>x is a chemical element</p> <p>x_{tot} is the total dissolved concentration of x in a solution</p> <p>X is an aqueous species in solution</p> <p>\bar{S} is a set of all aqueous species in a solution</p> <p>$\#x\langle X \rangle$ is the number of occurrences of x in X</p> <p>$[X]$ is the concentration of X in solution</p>
Source	–
Ref. By	DD2

Number	T3
Label	Charge neutrality of aqueous solutions
Equation	$\sum\{X : \bar{S} \cdot z_X \cdot [X]\} = 0$
Description	<p>Aqueous solutions must be electrically neutral, and thus the concentration of positive charge from dissolved solutes must balance with the concentration of negative charge from dissolved solutes. This is reflected in the equation above, where:</p> <p>X is an aqueous species in solution</p> <p>\bar{S} is a set of all aqueous species a solution</p> <p>z_X is the charge number of X</p> <p>$[X]$ is the concentration of X</p>
Source	–
Ref. By	DD3

Number	T4
Label	Law of mass action (forward)
Equation	$r_+ = k_+ \prod_{i=1}^n \{A_i\}^{\alpha_i}$
Description	<p>The law of mass action describes the forward and backward reaction rates for a chemical reaction. For a chemical reaction expressed in the equational form given in T1, the equation above expresses the law of mass action in the forward direction, where:</p> <p>r_+ is the forward reaction rate (mol s^{-1}).</p> <p>k_+ is the forward rate constant (mol s^{-1}).</p> <p>n is the number of reactants.</p> <p>A_i is the i^{th} reactant species.</p> <p>$\{A_i\}$ is the activity of A_i.</p> <p>α_i is the stoichiometric coefficient of the i^{th} reactant.</p>
Source	Wikipedia (2017a)
Ref. By	T6

Number	T5
Label	Law of mass action (backward)
Equation	$r_- = k_- \prod_{j=1}^m \{B_j\}^{\beta_j}$
Description	<p>The law of mass action describes the forward and backward reaction rates for a chemical reaction. For a chemical reaction expressed in the equational form given in T1, the equation above expresses the law of mass action in the backward direction, where:</p> <p>r_- is the backward reaction rate (mols^{-1}).</p> <p>k_- is the backward rate constant (mols^{-1}).</p> <p>m is the number of products.</p> <p>B_j is the j^{th} product species.</p> <p>$\{B_j\}$ is the activity of B_j.</p> <p>β_j is the stoichiometric coefficient of the j^{th} product.</p>
Source	Wikipedia (2017a)
Ref. By	T6

Number	T6
Label	Chemical equilibrium
Equation	$k_+ \prod_{i=1}^n \{A_i\}^{\alpha_i} = k_- \prod_{j=1}^m \{B_j\}^{\beta_j}$
Description	<p>When a chemical reaction is in equilibrium, the forward and reverse reaction rates are the same. Using T4 and T5, this idea is expressed in the equation above, where:</p> <p>k_+ is the forward rate constant (mol s^{-1}).</p> <p>n is the number of reactants.</p> <p>A_i is the i^{th} reactant species.</p> <p>$\{A_i\}$ is the activity of A_i.</p> <p>α_i is the stoichiometric coefficient of the i^{th} reactant.</p> <p>k_- is the backward rate constant (mol s^{-1}).</p> <p>m is the number of products.</p> <p>B_j is the j^{th} product species.</p> <p>$\{B_j\}$ is the activity of B_j.</p> <p>β_j is the stoichiometric coefficient of the j^{th} product.</p>
Source	Wikipedia (2017a)
Ref. By	T7

Number	T7
Label	Equilibrium equation
Equation	$K = \frac{r_+}{r_-} = \frac{\prod_{j=1}^m \{B_j\}^{\beta_j}}{\prod_{i=1}^n \{A_i\}^{\alpha_i}}$
Description	<p>The ratio of the forward and backward rate constants for a reaction forms a new constant called the equilibrium constant. Using T6, we can relate the equilibrium constant to the activities of the products and reactants. This is shown in the equation above, where:</p> <p>K is the equilibrium constant.</p> <p>r_+ is the forward reaction rate (mol s^{-1}).</p> <p>k_+ is the forward rate constant (mol s^{-1}).</p> <p>n is the number of reactants.</p> <p>A_i is the i^{th} reactant species.</p> <p>$\{A_i\}$ is the activity of A_i.</p> <p>α_i is the stoichiometric coefficient of the i^{th} reactant.</p> <p>r_- is the backward reaction rate (mol s^{-1}).</p> <p>k_- is the backward rate constant (mol s^{-1}).</p> <p>m is the number of products.</p> <p>B_j is the j^{th} product species.</p> <p>$\{B_j\}$ is the activity of B_j.</p> <p>β_j is the stoichiometric coefficient of the j^{th} product.</p>
Sources	Wikipedia (2017a)
Ref. By	GD1, DD1

3.2.3 General Definitions

This section collects the laws and equations that will be used in deriving the data definitions, which in turn are used to build the instance models.

Number	GD1
Label	Water dissociation equilibrium
SI Units	–
Equation	$K_{H_2O} : 10^{-14} = \{H^+\} \cdot \{OH^-\}$
Description	<p>This is the equilibrium equation for the dissociation of water. The equation arises from T7 using the value of 10^{-14} for the equilibrium constant at SATP, where:</p> <p>$\{H^+\}$ is the activity of H^+</p> <p>$\{OH^-\}$ is the activity of OH^-</p>
Source	Wikipedia (2017b)
Ref. By	DD1

3.2.4 Data Definitions

This section collects and defines all the data needed to build the instance models. The dimension of each quantity is also given.

[Note: The definitions here need rethinking – not clear enough as they are. Reminder: type system. —SP]

Number	DD1
Label	Set of equilibria
Symbol	\overline{K}
SI Units	–
Equation	$\overline{K} = \left\{ (R, K_R) : \overline{R}\overline{K}_{in} \bullet K_R = \frac{\prod_{j=1}^m \{B_j\}^{\beta_j}}{\prod_{i=1}^n \{A_i\}^{\alpha_i}} \text{ with reaction } R \right\} \cup K_{H_2O}$
Description	<p>By A6, all of the input reactions are reversible with finite equilibrium constants. Thus, we can express the input reactions as a set of equilibria via T7. The equilibrium equation for the dissociation of water (GD1) is added to this set since it is not supplied by the user.</p> <p>[The “equation” needs revision to state this more clearly – doesn’t look like a set of equations. I’m leaving out the description of variables for now as it is going to change anyway. —SP]</p>
Sources	–
Ref. By	IM1

Number	DD2
Label	Set of mass balance equations
Symbol	\overline{M}
SI Units	–
Equation	$\overline{M} = \{x_{tot} : \overline{T}_{in} \bullet \sum \{X : \overline{S}_{in} \mid x \in X \bullet \#x\langle X \rangle \cdot [X]\} = x_{tot}\}$
Description	<p>Instantiation of T2 using the input sets \overline{T}_{in} and \overline{S}_{in} yields a set of mass (concentration) balance equations.</p> <p>[The “equation” needs revision to state this more clearly – doesn’t look like a set of equations. I’m leaving out the description of variables for now as it is going to change anyway. —SP]</p>
Sources	–
Ref. By	IM1

Number	DD3
Label	Charge balance equation
Symbol	C
SI Units	–
Equation	$C : \sum \{X : \bar{S}_{in} \cdot z_X \cdot [X]\} = 0$
Description	<p>Instantiation of T3 using the input set \bar{S}_{in} yields the charge balance equation.</p> <p>[As with the previous DD's, the “equation” needs revision to state this more clearly. —SP]</p>
Sources	–
Ref. By	IM1

3.2.5 Instance Models

This section transforms the problem defined in § 3.1 into one which is expressed in mathematical terms. It uses concrete symbols defined in § 3.2.4 to replace the abstract symbols in the models identified in § 3.2.2 and § 3.2.3.

The goal GS1 is solved by IM1.

Number	IM1
Label	System of non-linear equations to find equilibrium concentrations
Input	\bar{K}, \bar{M}, C
Output	$\{X : \bar{S}_{in} \mid X \neq OH^- \wedge X \neq H^+ \cdot \{[X] \text{ for } 0 \leq pH \leq 14\}\},$ when the system of non-linear equations $\bar{K} \cup \bar{M} \cup C$ is satisfied
Description	<p>The union of \bar{K} (DD1), \bar{M} (DD2), and C (DD3) makes up the system of non-linear equations that must be solved. By A3, all activities in the system of equations $\bar{K} \cup \bar{M} \cup C$ are either that of water or that of an aqueous solute species. By A4, all instances of $\{H_2O\}$ can be replaced with 1.0. By A5, all activities of aqueous solute species can be replaced by their concentrations. This results in a non-linear system of equations where the set of unknowns is the set \bar{S}_{in}. By A1, the system is solved on the pH range 0 to 14.</p>
Sources	–
Ref. By	–

3.2.6 Data Constraints

Tables 2 and 4 show the data constraints on the input and output variables, respectively. The column for physical constraints gives the physical limitations on the range of values that can be taken by the variable. The column for software constraints restricts the range of inputs to reasonable values. The constraints are conservative, to give the user of the model the flexibility to experiment with unusual situations. The column of typical values is intended to provide a feel for a common scenario. The uncertainty column provides an estimate of the confidence with which the physical quantities can be measured. This information would be part of the input if one were performing an uncertainty quantification exercise.

The specification parameters in Table 2 are listed in Table 3.

[There is a line break between table captions and tables and I can't figure out why. It's really bothering me. Will fix later. :-(—SP]

Table 2: Input Variables

Input	Physical Constraints	Software Constraints	Typical Value	Uncertainty
x_{tot}	—	$x_{tot_{\min}} \leq x_{tot}$	0.1 mol/l	1%
R	—	—	—	—
K	—	—	10^{-4}	2.5%

* The user will supply a set of each input variable.

** There must be an accompanying equilibrium constant for every equation supplied by the user.

*** The set of pairs (R, K) is \overline{RK}_{in} .

**** The set of x_{tot} is \overline{T}_{in} .

Table 3: Specification Parameter Values

Var	Value
$x_{tot_{\min}}$	0 mol l ⁻¹

3.2.7 Properties of a Correct Solution

A correct solution must satisfy the system of non-linear equations described by IM1.

Table 4: Output Variables

Output	Physical Constraints
$\{X : \bar{S}_{in} \mid X \neq OH^- \wedge X \neq H^+ \bullet \{[X] \text{ for } 0 \leq pH \leq 14\}\}$	$[X] \geq 0$

4 Requirements

This section provides the functional requirements, the business tasks that the software is expected to complete, and the nonfunctional requirements, the qualities that the software is expected to exhibit.

The goal GS2 is solved by R6.

4.1 Functional Requirements

R1: SpecGen will take the following inputs:

1. RK_{in} : the set of all pairs of reactions and associated equilibrium constants
2. T_{in} : the set of total concentrations of chemical elements

R2: SpecGen will derive S_{in} (the set of all aqueous solute species in the chemical system) from the set of reactions in R1.

R3: SpecGen will ensure that the inputs do not violate the constraints specified in § 3.2.6.

R4: SpecGen will provide the water dissociation equilibrium.

R5: SpecGen will calculate equilibrium concentrations for all species in S_{in} (excluding H^+ and OH^-) via IM1.

R6: SpecGen will generate a speciation diagram of all species in S_{in} (excluding H^+ and OH^-) in the pH range 0 to 14 using the results of the calculation in R5.

4.2 Nonfunctional Requirements

[Using Drasil boilerplate here. Is this sufficient or should it be more precise? —SP] SpecGen is small in size and relatively simple, so performance is not a priority. Any reasonable implementation will be very quick and use minimal storage. Rather than performance, the non-functional requirement priorities are correctness, understandability, reusability, maintainability, and portability.

5 Likely Changes

LC1: Generation of diagrams under non-SATP conditions [A2]

LC2: Consideration of gas and solid equilibria [A3]

LC3: Calculation using true activity, with user supplied activity coefficients for more accurate speciation [A4, A5]

6 Traceability Matrices and Graphs

The purpose of the traceability matrices is to provide easy references on what has to be additionally modified if a certain component is changed. Every time a component is changed, the items in the column of that component that are marked with an “X” may have to be modified as well. Table 5 shows the dependencies of theoretical models, general definitions, data definitions, and instance models with each other. Table 6 shows the dependencies of instance models, requirements, and data constraints on each other. Table 7 shows the dependencies of theoretical models, general definitions, data definitions, instance models, and likely changes on the assumptions.

	T1	T2	T3	T4	T5	T6	T7	GD1	DD1	DD2	DD3	IM1
T1												
T2												
T3												
T4	X											
T5	X											
T6				X	X							
T7						X						
GD1							X					
DD1							X	X				
DD2		X										
DD3			X									
IM1									X	X	X	

Table 5: Traceability Matrix Showing the Connections Between TM, GD, DD, IM

	GD1	GD1	§ 3.2.6
R1			
R2			
R3			X
R4	X		
R5		X	
R6			

Table 6: Traceability Matrix Showing the Connections Between Requirements and Instance Models

	A1	A2	A3	A4	A5	A6
T1						
T2						
T3						
T4						
T5						
T6						
T7						
GD1		X				
DD1						X
DD2						
DD3						
IM1	X		X	X	X	
LC1		X				
LC2			X			
LC3				X	X	

Table 7: Traceability Matrix Showing the Connections Between Assumptions and Other Items

References

- Nirmitha Koothoor. A document driven approach to certifying scientific computing software. Master's thesis, McMaster University, Hamilton, Ontario, Canada, 2013.
- David L. Parnas and P.C. Clements. A rational design process: How and why to fake it. *IEEE Transactions on Software Engineering*, 12(2):251–257, February 1986.
- Suzanne Robertson and James Robertson. *Mastering the Requirements Process*, chapter Volere Requirements Specification Template, pages 353–391. ACM Press/Addison-Wesley Publishing Co, New York, NY, USA, 1999.
- W. Spencer Smith and Lei Lai. A new requirements template for scientific computing. In J. Ralyté, P. Ågerfalk, and N. Kraiem, editors, *Proceedings of the First International Workshop on Situational Requirements Engineering Processes – Methods, Techniques and Tools to Support Situation-Specific Requirements Engineering Processes, SREP'05*, pages 107–121, Paris, France, 2005. In conjunction with 13th IEEE International Requirements Engineering Conference.
- Wikipedia. Reversible reaction — wikipedia, the free encyclopedia, 2016. URL https://en.wikipedia.org/w/index.php?title=Reversible_reaction&oldid=748515123. [Online; accessed 6-October-2017].
- Wikipedia. Chemical equilibrium — wikipedia, the free encyclopedia, 2017a. URL https://en.wikipedia.org/w/index.php?title=Chemical_equilibrium&oldid=799947211. [Online; accessed 6-October-2017].
- Wikipedia. Self-ionization of water — wikipedia, the free encyclopedia, 2017b. URL https://en.wikipedia.org/w/index.php?title=Self-ionization_of_water&oldid=800970044. [Online; accessed 6-October-2017].