

# HW15

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5/12/2021

## 1

Find the equation of the regression line for the given points. Round any final values to the nearest hundredth, if necessary.

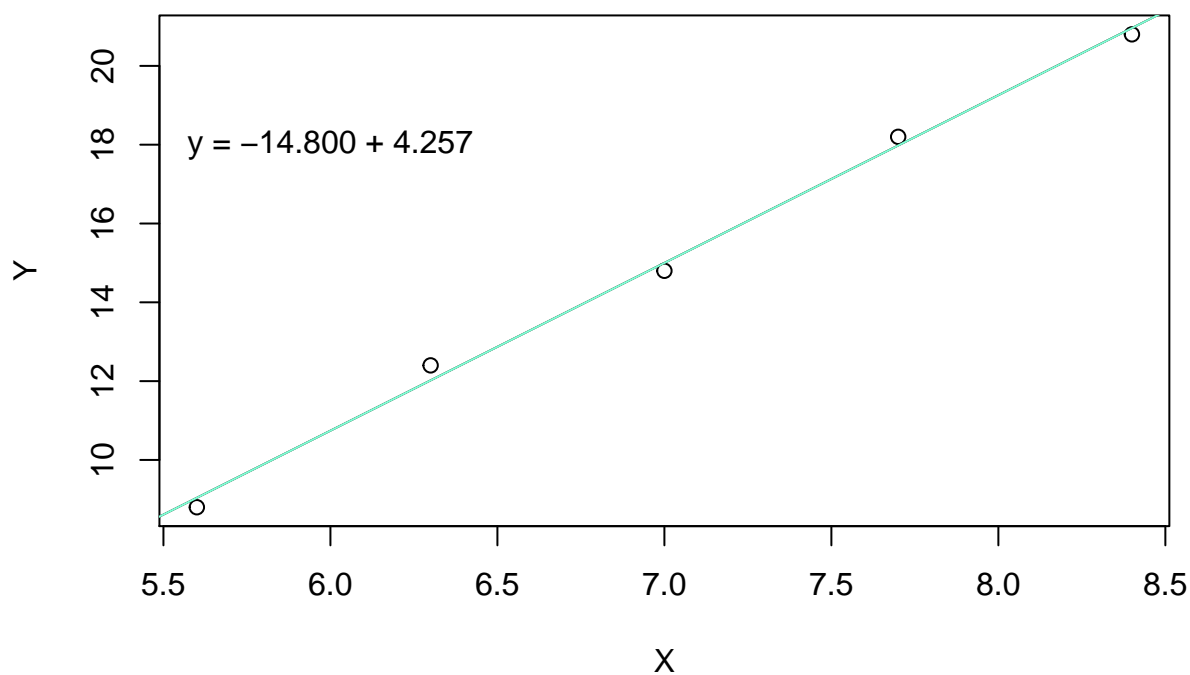
( 5.6, 8.8 ), ( 6.3, 12.4 ), ( 7, 14.8 ), ( 7.7, 18.2 ), ( 8.4, 20.8 )

```
x = c(5.6, 6.3, 7, 7.7, 8.4)
y = c(8.8, 12.4, 14.8, 18.2, 20.8)
reg <- lm(y~x)
reg
```

```
##
## Call:
## lm(formula = y ~ x)
##
## Coefficients:
## (Intercept)          x
##      -14.800       4.257
```

```
# Equation of the line based on coefficients: -14.800 + 4.257x
plot(x,y, xlab="X", ylab="Y", main = "Regression Line of Points")
abline(reg)
lines(c(5,9), -14.800 + 4.257*c(5,9), col="aquamarine")
text(6, 18, labels = "y = -14.800 + 4.257")
```

## Regression Line of Points



Rounded to the nearest hundreth the equation of the regression line is:

$$y = -14.80 + 4.26x$$

**2**

Find all local maxima, local minima, and saddle points for the function given below. Write your answer(s) in the form ( x, y, z ). Separate multiple points with a comma.

$$f(x, y) = 24x - 6xy^2 - 8y^3$$

$$f_x = 24 - 6y^2$$

$$f_y = -12xy - 24y^2$$

$$-6y^2 + 24 = 0$$

$$-12xy - 24y^2 = 0$$

$$y = \sqrt{\frac{24}{6}} \pm 2$$

$$x = -2y = 4$$

```
fz <- function(x,y){
  z = 24*x-6*x*y^2-8*y^3
  print(paste("x =", x, ",", "y=", y, ",", "z=", z))
}
fz(-4,2)
```

```
## [1] "x = -4 , y= 2 , z= -64"
```

The points separated with a comma in the format (x,y,z) are -4, 2, and -64.

### 3

A grocery store sells two brands of a product, the “house” brand and a “name” brand. The manager estimates that if she sells the “house” brand for  $x$  dollars and the “name” brand for  $y$  dollars, she will be able to sell  $81 - 21x + 17y$  units of the “house” brand and  $40 + 11x - 23y$  units of the “name” brand.

Step 1. Find the revenue function  $R(x, y)$ .

$$\begin{aligned} R(x, y) &= (81 - 21x + 17y)x + (40 + 11x - 23y)y \\ &= 81x - 21x^2 + 17xy + 40y + 11xy - 23y^2 \\ &= 81x + 40y + 28xy - 21x^2 - 23y^2 \end{aligned}$$

Step 2. What is the revenue if she sells the “house” brand for \$2.30 and the “name” brand for \$4.10?

$$R(2.3, 4.1) = 81 * 2.3 + 40 * 4.1 + 28 * 2.3 * 4.1 - 21 * (2.3)^2 - 23 * (4.1)^2 = 116.62$$

### 4

A company has a plant in Los Angeles and a plant in Denver. The firm is committed to produce a total of 96 units of a product each week. The total weekly cost is given by  $C(x, y) = \frac{1}{6}x^2 + \frac{1}{6}y^2 + 7x + 25y + 700$ , where  $x$  is the number of units produced in Los Angeles and  $y$  is the number of units produced in Denver. How many units should be produced in each plant to minimize the total weekly cost?

Given:  $C(x, y) = \frac{1}{6}x^2 + \frac{1}{6}y^2 + 7x + 25y + 700$

Where  $x$  is the units produced in LA and  $y$  units produced in Denver, we solve using the total units needed, 96, as shown:

$$\begin{aligned} &\frac{1}{6}(96 - y)^2 + \frac{1}{6}y^2 + 7(96 - y) + 25y + 700 \\ &= \frac{1}{6}(y^2 - 192y + 9216) + \frac{1}{6}y^2 + 18y + 25y + 1372 \\ &= \frac{1}{3}y^2 - 14y + 2908 \end{aligned}$$

Then find the minimum value:

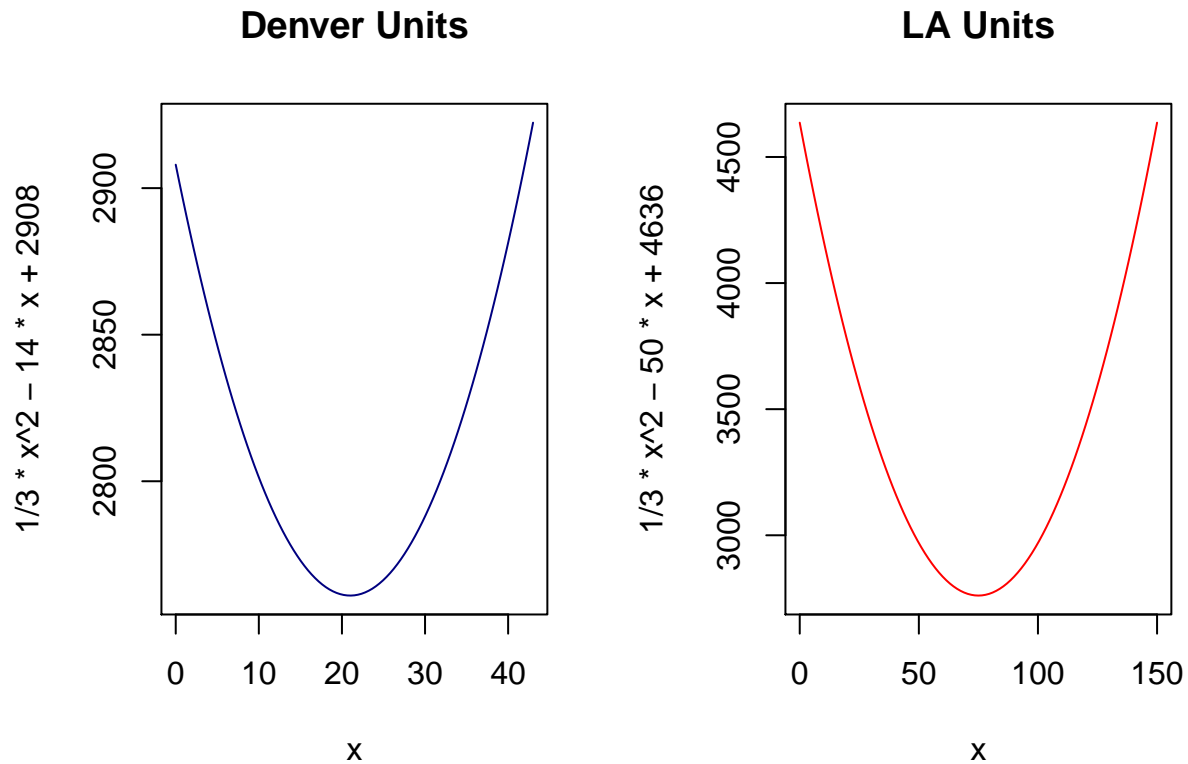
$$z = \frac{d}{dy}(\frac{1}{3}y^2 - 14y + 2908) = \frac{2}{3}y - 14 = 0 \implies y = 21$$

Substitute

$$x = 96 - y = 96 - 21 = 75$$

We can also confirm this with the equations and local minima on plots of each location’s unit production as shown below:

```
par(mfrow=c(1,2))
curve(1/3*x^2-14*x+2908 , from = 0, to = 43, col="navy", main = "Denver Units")
curve(1/3*x^2-50*x+4636 , from = 0, to = 150, col="red", main = "LA Units")
```



It looks like our local minima are confirmed. Thus, for LA and Denver we have 75 units and 21 units respectively.

5

Evaluate the double integral on the given region.

$$\int \int_R (e^{8x+3y}) dA, R : 2 \leq x \leq 4 \text{ and } 2 \leq y \leq 4$$

Write your answer in exact form without decimals.

We have one form as:

```
1/24*((exp(32)+exp(16))*(exp(12) - exp(6)))
```

```
## [1] 5.341561e+17
```

It could also be left in fractional form without decimals as mentioned:

$$\int_2^4 \int_2^4 (e^{8x+3y}) dy dx \int_2^4 \left(\frac{1}{3}e^{8x+3y}\right)\bigg|_2^4 dx$$

$$\begin{aligned}
& \int_2^4 \left( \left( \frac{1}{3} e^{8x+12} \right) - \left( \frac{1}{3} e^{8x+6} \right) \right) dx \\
& \int_2^4 \frac{1}{3} e^{8x+6} (e^6 - 1) dx \\
& \frac{1}{24} e^{38} (e^6 - 1) - \frac{1}{24} e^{22} (e^6 - 1) \\
& \frac{1}{24} (e^6 - 1) (e^{38} - e^{22}) \\
& \frac{1}{24} (e^{22} - e^{28} - e^{38} + e^{44})
\end{aligned}$$

Without any decimals we have  $\frac{1}{24}(e^{22} - e^{28} - e^{38} + e^{44})$