$$\left(\frac{P_C^S}{P_T^S}\right)^{AUT} = \frac{a_C^S}{a_T^S}$$