$$\left(\frac{P_C^N}{P_T^N}\right)^{AUT} = \frac{a_C^N}{a_T^N}$$