Python Course 1: Introduction to Python

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Introduction

- Objectives:
 - ► Learn Python basics
 - Get an introduction to popular optimization and data science libraries
- Prerequisites: Familiarity with basic programming concepts (variables, data types, control structures, and functions) in any programming language
- Pedagogical approach: Learn fundamental Python concepts by solving an optimization problem

Plan

- Introduction
- Python fundamentals
- Data science and optimization libraries:
 - Manipulating data with pandas
 - Visualizing data with Matplotlib
 - ► Formulating and solving optimization models with Pyomo
- Additional topics (if time permits)

Creating a virtual environment

- Use a virtual environment to keep your project's dependencies isolated.
- To create the environment, in a terminal, navigate to your project folder and run:

```
python -m venv venv
```

- To activate the environment:
 - venv\Scripts\activate (Windows)
 - source venv/bin/activate (macOS/Linux)
- When activated, (venv) appears at the prompt.
- To exit the environment, type deactivate.

Getting started with Python

Strings:

```
"Hello, world!"  # Double quotes
'Hello, world!'  # Single quotes
"That's fine!"  # Double quotes with a single quote inside
```

Printing:

```
print("Hello, world!")
```

Arithmetic:

Comments:

```
# This is a comment
```

Transportation problem

A motivating example for learning Python

Goal: Distribute goods from suppliers to customers at minimal cost.

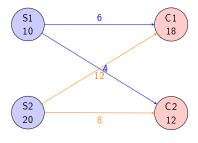
Given:

- Supplier capacities
- Customer demands
- Shipping costs

Constraints:

- Supply limits per supplier
- Demand requirements per customer

Objective: Minimize total transportation cost



Transportation problem

Data representation

Typical data for the transportation problem:

- Suppliers: List with supply amounts
- Customers: List with demand amounts
- Cost Matrix: Table of shipping costs from each supplier to each customer

Example:

Suppliers

S1: 10 units

S2: 20 units

Customers

- C1: 18 units
- C2: 12 units

Cost Matrix

	C1	C2
S1	5	7
S2	4	6

Variables and data types

Concepts

- A variable is a name (identifier) that refers to an object (the value) stored in memory.
- Each object has a data type, which determines what kind of data it represents (e.g. integer, string).
- The name (the variable) and the content (the object/value) are separate:
 - ▶ Variable: The label or identifier (e.g. x)
 - ▶ Object/Value: The data assigned to the variable (e.g. 42 or "hello")
 - ▶ Data type: The kind of the object/value (e.g. int, str)
- In Python, every value is represented as an object.

Variables and data types

Dynamic typing in Python

- No type declaration is needed when defining a variable.
- For example, you simply assign a value without: x = 10 (no need to specify that it is an integer)
- Variables can be reassigned to values of different types:

```
x = 10 # x is an integer (int)
x = "hello" # now x is a string (str)
```

• This is different from languages like Java or C++, where the type must be specified.

Variables and data types

Example

The input data from our transportation problem can be stored in variables:

```
# Suppliers
s1 = 10
s2 = 20
# Customers
c1 = 18
c2 = 12
# Cost matrix
s1_c1 = 5
s1_c2 = 7
s2_c1 = 4
s2_c2 = 6
```

Printing strings with variables

Examples

 You can print the value of a variable by passing it as an argument to the print function:

```
print(s1) # Output: 10
```

 You can print multiple variables by passing them as separate arguments:

 You can include variable values inside a string using an f-string (formatted string literal):

```
print(f"s1: {s1}, s2: {s2}") # Output: s1: 10, s2: 20
```

The type function

- Use the type function to determine the type of any object.
- It can be called directly on a value:

```
print(type(23.54))  # Output: <class 'float'>
print(type("Customer"))  # Output: <class 'str'>
```

Or on a variable:

• The output is always in the form <class 'type'>.

Python basic data types

Examples:

- int: Integer numbersx = 42
- float: Decimal numbersy = 3.14
- str: Text strings
 name = "test"
- bool: Boolean values flag = True

- list: Ordered collection nums = [1, 2, 3]
- tuple: Immutable collection coords = (10, 20)
- dict: Key-value pairs
 info = {"S1": 35, "S2": 25}
- set: Unordered unique items
 unique = {2, 4, 6}

Remarks

- There are many other built-in data types.
- You can also define your own data types (using object-oriented programming).

Lists

Concept and syntax

- A list is a built-in Python data structure that stores an ordered collection of items.
- Lists can contain elements of any type (integers, strings, other lists, etc.).
- You can access elements in a list by their position, starting from 0.

General syntax:

```
my_list = [element1, element2, element3, ...]
```

Remark

Python lists can mix types, e.g. mixed = [1, "hello", 3.14, [2, 3]]

Lists

Access elements

- Access elements by index: my_list[0] (first element)
- Lists are 0-indexed (the first item is at position 0)
- Access the last element with my_list[-1]
- Access a range of elements (a slice) with my_list[start:stop] (from start up to but not including stop)

Example:

Lists

Useful functions on lists

- len(x): Returns the number of elements in the list x.
- sorted(x): Returns a new sorted list with the same elements as x (the original list is unchanged).
- sum(x): Returns the sum of all elements in the list (works with numbers).
- min(x): Returns the smallest element in the list.
- max(x): Returns the largest element in the list.

```
suppliers = [10, 20]
customers = [18, 12]

print(len(suppliers))  # Output: 2
print(sorted(customers))  # Output: [12, 18]
print(customers)  # Output: [18, 12]
print(sum(suppliers))  # Output: 30
print(min(customers))  # Output: 12
print(max(customers))  # Output: 18
```

Methods

What is a method?

- A **method** is a function that is associated with a specific object (like a list or a string).
- You call a method using the "dot notation":

```
object.method(arguments)
```

• The method can use or change the contents of the object it belongs to.

Examples with strings:

```
my_string = "hello world"
print(my_string.upper())  # Output: "HELLO WORLD"
print(my_string.replace("o", "O"))  # Output: "hello wOrld"
print(my_string.split())  # Output: ['hello', 'world']
```

Methods

Common list methods

- Lists in Python have several useful methods for modifying their contents:
 - append(x): Adds element x to the end of the list.
 - ▶ insert(i, x): Inserts element x at position i.
 - pop([i]): Removes and returns the element at position i (last element if i is omitted).
 - remove(x): Removes the first occurrence of element x.
 - extend(iterable): Adds all elements from another iterable to the end of the list
 - sort(): Sorts the list in place.
 - reverse(): Reverses the elements of the list in place.
- Elements of a list can also be changed or accessed using the [] (index) operator.

Note

These methods modify the list directly (in place).

Methods

Examples of common list methods

```
lst = [10, 20, 30]
                       # [10, 20, 30, 40]
1st.append(40)
                       # [10, 15, 20, 30, 40]
lst.insert(1, 15)
lst.pop()
                       # [10, 15, 20, 30]
lst.remove(15)
                       # [10, 20, 30]
                    # [10, 20, 30, 50, 60]
lst.extend([50, 60])
                       # [10, 20, 30, 50, 60]
lst.sort()
lst.reverse()
                       # [60, 50, 30, 20, 10]
lst[0] = 99
                        # [99, 50, 30, 20, 10]
```

Note

All these methods modify the list 1st directly.

Mutability

Concept

- Objects in Python can be *mutable* (can be changed after creation) or *immutable* (cannot be changed after creation).
 - ► Mutable objects: list, dict, set
 - ▶ Immutable objects: int, float, str, tuple
- Mutable objects can have their contents changed after they are created, while immutable objects cannot be changed—any operation that seems to modify them actually creates a new object.

Mutability

Examples

```
# Mutable example (list)
mixed = [1, "hello", 3.14, [2, 3]]
mixed[0] = 42
mixed.pop()
print(mixed) # Output: [42, 'hello', 3.14]
# Immutable example (str)
s = "hello"
# s[0] = "H" # This would raise an error
s = "Hello" # A new string object is assigned to s
# Immutable example (int)
x = 10
x = x + 5 \# A new int object is assigned to x
```

Concept and syntax

- A dictionary is a built-in Python data structure that stores data as key-value pairs.
- Each **key** is unique and is used to access its corresponding **value**.
- Dictionaries are useful for representing mappings, such as supplier to supply amounts, or customer to demand amount.

General syntax:

```
my_dict = {key1: value1, key2: value2, ...}
```

- Access a value by its key: my_dict[key1]
- Keys can be of any immutable type (e.g., strings, numbers, tuples).

Example: suppliers and customers

```
supply_by_sup = {"S1": 10, "S2": 20}
demand_by_cust = {"C1": 18, "C2": 12}

print(supply_by_sup["S2"]) # Output: 20
print(demand_by_cust["C1"]) # Output: 18
print(len(supply_by_sup)) # Output: 2
```

- In {"S1": 10, "S2": 20}, "S1" and "S2" are the keys, whereas 10 and 20 are the values.
- The len of a dictionary in Python corresponds to the number of key-value pairs it contains.

Example: cost matrix

- A tuple (such as a pair ("S1", "C2")) can be used as a dictionary key because it is immutable.
- A list cannot be used as a key, because lists are mutable.

Common dictionary methods

- Dictionaries in Python have several useful methods for accessing and working with their contents:
 - keys(): Returns a view of all the keys in the dictionary.
 - values(): Returns a view of all the values in the dictionary.
 - items(): Returns a view of all key-value pairs as tuples.
 - get(key, default): Returns the value for key if it exists; otherwise returns default (or None if default is not provided).
 - pop(key): Removes the item with the specified key and returns its value.

Examples of common dictionary methods

Dictionary views vs. lists

- Methods like mydict.keys(), mydict.values(), and mydict.items()
 return dictionary view objects.
- A dictionary view is **not exactly a list**, but you can loop over it like a list.
- If you need a real list (for example, to index or modify it), use list(dict_view).

```
list(supply_by_sup.keys()) # ['S1', 'S2', 'S3']
list(demand_by_cust.values()) # [18, 12]
list(cost_by_sup_cust.items())
# [(('S1', 'C1'), 5), (('S1', 'C2'), 7)]
```

Goal: Assign flow from suppliers to customers in order of increasing unit cost, without violating supply or demand.

Pseudo code:

- Initialize empty flow dictionary.
- ② Sort all (supplier, customer) pairs by their unit cost (ascending).
- For each (supplier, customer) pair in sorted order:
 - supply ← supplier's current available units.
 - **b** demand ← customer's current required units.
 - Set quantity to the smaller of supply and demand.
 - **1** Assign quantity from supplier to customer in the flow dictionary.
 - Subtract quantity from supplier's supply and customer's demand.

Goal: Assign flow from suppliers to customers in order of increasing unit cost, without violating supply or demand.

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 - Set quantity to the smaller of supply and demand.
 - **1** Assign quantity from supplier to customer in the flow dictionary.
 - Subtract quantity from supplier's supply and customer's demand.

Initialize empty flow dictionary

- Create a dictionary to store the final solution: the quantity shipped from each supplier to each customer.
- The keys will be (*supplier*, *customer*) pairs, and the values are quantities shipped.

```
flow_by_sup_cust = {}
```

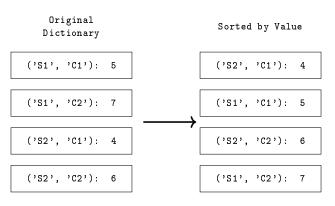
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 - Subtract quantity from supplier's supply and customer's demand.

Sort all (supplier, customer) pairs by their unit cost

We want to sort the supplier-customer pairs by cost:



This can be done with the help of the sorted function.

The sorted() function

General syntax

 sorted() is a built-in function that returns a new sorted list from an iterable.

```
sorted(iterable, key=None, reverse=False)
```

- Parameters: (Parameters marked as optional have a default value and can be omitted.)
 - ▶ iterable: The sequence (e.g., list, tuple, dict, etc.) to sort.
 - key (optional): A function that tells Python what to sort by.
 - reverse (optional): If True, sorts in descending order.
- sorted() always returns a new list and does not modify the original data.

The sorted() function

Example: Sorting shipments

• Applying sorted directly to cost_by_sup_cust returns a list of the dictionary's keys, sorted in ascending (lexicographic) order:

```
sorted(cost_by_sup_cust)
# [('S1', 'C1'), ('S1', 'C2'), ('S1', 'C3'),
# ('S2', 'C1'), ('S2', 'C2'), ('S2', 'C3')]
```

• To include both the keys and values in the result, sort the dictionary's items:

```
sorted(cost_by_sup_cust.items())
# [(('S1', 'C1'), 4), (('S1', 'C2'), 6), (('S1', 'C3'), 8),
# (('S2', 'C1'), 5), (('S2', 'C2'), 4), (('S2', 'C3'), 3)]
```

Defining a function

General syntax:

```
def function_name(arg1, arg2, ...):
    # Code block
    return value
```

Example:

```
def get_cost(cost_tuple):
    cost = cost_tuple[1]
    return cost
```

- The function get_cost takes one argument: cost_tuple.
- The variable cost is assigned the 2nd element of the tuple (the cost).
- The function returns the cost.
- For example: get_cost((('S1', 'C1'), 4)) returns 4.

The sorted() function

Example: Sorting shipments by cost

To sort by cost, we pass our function get_cost to the key parameter:

```
def get_cost(cost_tuple):
    cost = cost_tuple[1]
    return cost

...

sorted_costs = sorted(cost_by_sup_cust.items(), key=get_cost)
# [(('S2', 'C3'), 3), (('S1', 'C1'), 4), (('S2', 'C2'), 4),
# (('S2', 'C1'), 5), (('S1', 'C2'), 6), (('S1', 'C3'), 8)]
```

Lambda Expressions

- A lambda expression is an anonymous function—a function without a name.
- General syntax: lambda x, y, ...: f(x, y, ...) (for example: lambda x, y: x + y)
- When a function is simple and only used once, a lambda expression makes the code shorter and clearer.

Goal: Assign flow from suppliers to customers in order of increasing unit cost, without violating supply or demand.

Pseudo code:

- Initialize empty flow dictionary.
- ② Sort all (supplier, customer) pairs by their unit cost (ascending).
- **Tor each** (supplier, customer) pair in sorted order:
 - supply ← supplier's current available units.
 - **o** demand ← customer's current required units.
 - Set quantity to the smaller of supply and demand.
 - **1** Assign quantity from supplier to customer in the flow dictionary.
 - Subtract quantity from supplier's supply and customer's demand.

Iterating over the sorted shipments

• We want to iterate over each pair of sorted_costs.

Iteration 1	Iteration 2	Iteration 3	Iteration 4
('S2', 'C1'): 4	('S2', 'C1'): 4	('S2', 'C1'): 4	('S2', 'C1'): 4
('S1', 'C1'): 5	('S1', 'C1'): 5	('S1', 'C1'): 5	('S1', 'C1'): 5
('S2', 'C2'): 6	('S2', 'C2'): 6	('S2', 'C2'): 6	('S2', 'C2'): 6
('S1', 'C2'): 7	('S1', 'C2'): 7	('S1', 'C2'): 7	('S1', 'C2'): 7

• This can be done with the help of a for loop.

The for loop

General syntax

 A for loop lets you repeat actions for each item in a sequence (like a list, tuple, or dictionary).

```
for variable in sequence:
    # code to execute for each item
```

• The loop ends automatically after all items are processed.

Remark

The code inside the for loop must be indented. Python uses indentation to determine which lines belong inside the loop.

The for loop

Unpacking values

```
for s_c_cost in sorted_costs:
    print(s_c_cost) # 1st output: (("S1", "C1"), 4)

for s_c, cost in sorted_costs:
    print(s_c) # 1st output: ("S1", "C1")
    print(cost) # 1st output: 4

for (s, c), cost in sorted_costs:
    print(s) # 1st output: S2
    print(c) # 1st output: C3
    print(cost) # 1st output: 3
```

- The loop visits each item in sorted_costs one at a time.
- You can unpack multiple values directly in the loop header.
- You can use the unpacked values (e.g, s, c and cost) inside the loop body.

Goal: Assign flow from suppliers to customers in order of increasing unit cost, without violating supply or demand.

Pseudo code:

- 1 Initialize empty flow dictionary.
- 2 Sort all (supplier, customer) pairs by their unit cost (ascending).
- For each (supplier, customer) pair in sorted order:
 - supply ← supplier's current available units.
 - **b** demand ← customer's current required units.
 - Set quantity to the smaller of supply and demand.
 - **1** Assign quantity from supplier to customer in the flow dictionary.
 - Subtract quantity from supplier's supply and customer's demand.

Assigning supply and demand

• The current supply of supplier s is given by the value for key s in the dictionary supply_by_sup:

```
supply = supply_by_sup[s]
```

 The current demand of customer c is given by the value for key c in the dictionary demand_by_cust:

```
demand = demand_by_cust[c]
```

Goal: Assign flow from suppliers to customers in order of increasing unit cost, without violating supply or demand.

Pseudo code:

- Initialize empty flow dictionary.
- ② Sort all (supplier, customer) pairs by their unit cost (ascending).
- For each (supplier, customer) pair in sorted order:
 - supply ← supplier's current available units.
 - **o** demand ← customer's current required units.
 - Set quantity to the smaller of supply and demand.
 - **1** Assign quantity from supplier to customer in the flow dictionary.
 - Subtract quantity from supplier's supply and customer's demand.

Deciding how much to ship at each step

- At each step, we want to ship as many units from supplier s to customer c as possible, without exceeding either the supplier's supply or the customer's demand.
- Setting quantity to the smaller value ensures that neither limit is violated.
- In other words, quantity = min(supply, demand).
- This is equivalent to the following decision process:
 - ► If supply > demand:
 - ★ quantity ← demand
 - ► Else if supply < demand:
 - ★ quantity ← supply
 - ► Else:
 - ★ quantity ← supply (or demand, they are equal)

Conditional statements

The if, elif, and else statements

```
if condition1:
    # if condition1 is True
elif condition2:
    # if condition2 is True (and condition1 is False)
elif condition3:
    # if condition3 is True (and previous are False)
    # ...
else:
    # if none of the above conditions are True
```

- if checks the first condition.
- You can have zero, one, or many elif blocks to check additional conditions in order.
- else is optional, and runs if none of the above conditions are True.

Conditional statements

Example: deciding how much to ship at each step

- Decision process:
 - ► If supply > demand:
 - * quantity ← demand
 - ► Else if supply < demand:
 - **★** quantity ← supply
 - Else:
 - **★** quantity ← supply (or demand, they are equal)
- This decision process can be translated in Python as follows:

```
if supply > demand:
    quantity = demand
elif supply < demand:
    quantity = supply
else:
    quantity = supply # or demand</pre>
```

Goal: Assign flow from suppliers to customers in order of increasing unit cost, without violating supply or demand.

Pseudo code:

- Initialize empty flow dictionary.
- ② Sort all (supplier, customer) pairs by their unit cost (ascending).
- For each (supplier, customer) pair in sorted order:
 - supply ← supplier's current available units.
 - **b** demand ← customer's current required units.
 - Set quantity to the smaller of supply and demand.
 - **1** Assign *quantity* from *supplier* to *customer* in the flow dictionary.
 - Subtract quantity from supplier's supply and customer's demand.

Storing the shipment plan

• Record the assigned quantity of shipment in flow_by_sup_cust to keep track of how much is shipped from each supplier to each customer:

```
flow_by_sup_cust = {} # Defined previously
# ... some logic ...

for (s, c), cost in sorted_costs:
    # ... determine quantity to ship ...
    flow_by_sup_cust[(s, c)] = quantity
```

Goal: Assign flow from suppliers to customers in order of increasing unit cost, without violating supply or demand.

Pseudo code:

- Initialize empty flow dictionary.
- ② Sort all (supplier, customer) pairs by their unit cost (ascending).
- For each (supplier, customer) pair in sorted order:
 - supply ← supplier's current available units.
 - **o** demand ← customer's current required units.
 - Set quantity to the smaller of supply and demand.
 - **1** Assign quantity from supplier to customer in the flow dictionary.
 - Subtract quantity from supplier's supply and customer's demand.

Greedy heuristic for the transportation problem Updating supply and demand

• Subtract quantity from the supply of supplier s:

```
supply_by_sup[s] -= quantity
```

Subtract quantity from the demand of customer c:

```
demand_by_cust[c] -= quantity
```

 After each shipment, these updates keep track of what each supplier still has and what each customer still needs.

Printing the solution

 Print the shipment plan (how much is shipped from each supplier to each customer):

```
print(f"Shipment plan: {flow_by_sup_cust}")
# Shipment plan: {('S2', 'C1'): 18, ('S1', 'C1'): 0,
# ('S2', 'C2'): 2, ('S1', 'C2'): 10}
```

Print the remaining supply for each supplier:

```
print(f"supply_by_sup: {supply_by_sup}")
# Remaining supply: {'S1': 0, 'S2': 0}
```

• Print the remaining demand for each customer:

```
print(f"demand_by_cust: {demand_by_cust}")
# Remaining demand: {'C1': 0, 'C2': 0}
```

Creating a function

• To reuse our greedy heuristic, we can put it inside a function:

We can then call the function with different input data:

Returning remaining supply and demand

- In addition to the shipment plan, we can return the remaining supply and the remaining demand.
- Python lets you return more than one value from a function (as a tuple).

• You can assign each return value to a different variable:

Adding an optional verbose parameter

- To control whether the solution is printed, we can add an optional verbose parameter (default: False).
- Optional arguments should always appear after positional arguments in the function definition.

```
def greedy_solve(supply_by_sup, demand_by_cust,
                 cost_by_sup_cust, verbose=False):
   # ... greedy heuristic ...
   if verbose:
        print(f"Shipment plan: {flow_by_sup_cust}")
        print(f"Remaining supply: {supply_by_sup}")
        print(f"Remaining demand: {demand_by_cust}")
   return flow_by_sup_cust
greedy_solve(sup, dem, costs)
                                          # No output
greedy_solve(sup, dem, costs, verbose=True) # Prints solution
```

Modifying arguments

Example

 What are the values of sup and dem after calling greedy_solve in the following example?

Modifying arguments

Example

 What are the values of sup and dem after calling greedy_solve in the following example?

• Output of print(f"sup={sup}") and print(f"dem={dem}"):

```
sup={'S1': 0, 'S2': 0}
dem={'C1': 0, 'C2': 0}
```

• The dictionaries were modified! Why?

Mutable vs immutable arguments in functions

- The type of object you pass to a function—mutable or immutable—affects how it can be changed.
- Immutable objects (e.g., int, float, str, tuple):
 - The function cannot change the original object.
 - ▶ If "modified", a **new object** is created and the original remains unchanged.
- Mutable objects (e.g., list, dict, set):
 - ► The function can change the original object.
 - ► Changes made inside the function are visible outside the function.

Mutable vs immutable arguments in functions

Example: Direct modification

```
def greedy_solve(supply_by_sup, demand_by_cust,
                 cost_by_sup_cust):
   # ... some logic ...
    for (s, d), c in sorted(cost_by_sup_cust.items()):
        # ... determine quantity ...
        supply_by_sup[s] -= quantity # MODIFIES sup
        demand_by_cust[d] -= quantity # MODIFIES dem
   # . . .
    return flow_by_sup_cust, supply_by_sup, \
        demand_by_cust
greedy_solve(sup, dem, costss)
```

• The lines marked above directly modify the dictionaries sup and dem passed as arguments.

Mutable vs immutable arguments in functions

Example: Making copies

```
def greedy_solve(supply_by_sup, demand_by_cust,
                 cost_by_sup_cust):
    rem_sup = supply_by_sup.copy()
    rem_dem = demand_by_cust.copy()
    # ... some logic ...
    for (s, d), c in sorted(cost_by_sup_cust.items()):
        supply = rem_sup[s]
        demand = rem dem[d]
        # ... determine quantity ...
        rem_sup[s] -= quantity
        rem_dem[d] -= quantity
    # . . .
    return flow_by_sup_cust, rem_sup, rem_dem
```

- To avoid modifying the original arguments, make a copy of the dictionaries inside the function before modifying them.
- Now, the original dictionaries remain unchanged after the function call.

Modules

- Putting the greedy heuristic in a function lets us use it multiple times in the same script with different data.
- What if we want to reuse greedy_solve in other programs, without copying the code each time?
- We can make any function or variable reusable by putting it in a module (a separate .py file), and then import it when needed.

Creating a module

```
# File: mymodule.py

def my_function(arg1, arg2):
    # ... implementation ...
```

Importing from a module

Modules

Example: Moving greedy_solve to greedy.py

• Place the greedy_solve function in its own file, greedy.py, to make it reusable.

Now, import and use it in any script:

```
# File: myscript.py

from greedy import greedy_solve

# Use the function as needed
greedy_solve(sup, dem, costs)
```

What is pandas?

Pandas is a popular Python library for working with structured data:

- Efficiently loads, manipulates, and analyzes tabular data (like spreadsheets, CSV files, or SQL tables).
- The main data structure is the DataFrame, which looks like a table.
 Pandas also provides the Series, for one-dimensional data.
- Great for data cleaning, exploration, and preparation.

Installation:

pip install pandas

Import pandas:

import pandas as pd

Reading CSV files with pandas

Example: Loading data for the transportation problem

```
costs_df = pd.read_csv("data/costs.csv")
```

pd.read_csv loads a CSV file into a DataFrame.

rows

		supplier	customer	cost
S	0	S1	C1	5
	1	S1	C2	7
	3	S2	C1	4
	4	S2	C2	6

- The row labels are called the index (accessible with .index).
- The column labels are called columns (accessible with .columns).

Inspecting DataFrames

- head(n) shows the first n rows (n is optional, default is 5).
- tail(n) shows the last n rows (n is optional, default is 5).
- df['supplier'] (single square brackets) returns a Series, not a DataFrame.
- df[['col']] (double square brackets) returns a DataFrame, even for one column.
- Double brackets are required to select multiple columns: df[['col1','col2']].

Accessing data with loc

The loc method allows you to select rows and columns by label.

```
# Select a single row by index label
costs_df.loc[0]

# Select specific rows and columns by label
costs_df.loc[0, 'cost']

# Select multiple rows and columns by label
costs_df.loc[[0, 3], ['supplier', 'cost']]
```

- loc[index, columns] selects data by label, not position.
- Useful for precise data selection, filtering, and subsetting.

Basic statistics with DataFrames

 describe() gives count, mean, std deviation, min, max, and percentiles:

 You can also use mean(), std(), min(), max(), and median() directly.

```
costs_df['cost'].mean() # Mean
costs_df['cost'].std() # Standard deviation
costs_df['cost'].min() # Minimum value
costs_df['cost'].max() # Maximum value
print(costs_df['cost'].median()) # Median
```

Filtering rows with boolean conditions

- Use boolean expressions inside [] to select rows.
- Combine conditions with & (and), | (or), and surround each condition with parentheses.
- The result is a filtered DataFrame.

Converting DataFrames to dictionaries

```
# Convert supply and demand DataFrames to dict
supply_df.set_index('supplier').to_dict()['supply']
demand_df.set_index('customer').to_dict()['demand']

# Convert costs DataFrame to a dictionary
costs_df.set_index(
    ['supplier', 'customer']).to_dict()['cost']
```

- The set_index method sets one or more columns as the dictionary keys.
- The to_dict() method converts the DataFrame (or Series) to a Python dictionary.

Matplotlib

What is Matplotlib?

Matplotlib is a popular Python library for creating visualizations such as graphs and charts.

- Lets you turn data into plots: line charts, bar charts, heatmaps, and more.
- Integrates well with pandas and plain Python lists.
- The main module for plotting is matplotlib.pyplot, commonly imported as plt.

Installation:

```
pip install matplotlib
```

Import Matplotlib:

```
import matplotlib.pyplot as plt
```

Matplotlib

The plot function

```
plt.plot(x, y, ...)
```

- Creates a line plot.
- x: Sequence of positions or labels.
- y: Sequence of numeric values.
- Common options: marker, linestyle, color.
- plt.show() renders and displays the current figure.

Example:

Matplotlib

Adding labels, titles, and legends

- plt.xlabel("...") sets the label for the x-axis.
- plt.ylabel("...") sets the label for the y-axis.
- plt.title("...") sets the plot title.
- plt.legend() shows a legend for labeled artists (e.g., lines or bars with label=).

Example:

Matplotlib

The bar function

```
plt.bar(x, height, ...)
```

- Creates a bar chart.
- x: Sequence of labels or positions.
- height: Sequence of numeric values.
- Additional options: color, label, etc.

Example:

Matplotlib

Saving a plot to a file

- Use plt.savefig("filename.png") to save the current plot to an image file.
- You can specify the file format by changing the extension (e.g., .png, .jpg, .pdf, .svg).
- plt.savefig must be called before plt.show().

Example: Saving a line plot

What is Pyomo?

- Pyomo is a Python-based, open-source optimization modeling language.
- It allows you to define mathematical models for linear, integer, and nonlinear optimization problems.
- Pyomo provides a high-level, readable, and flexible interface for expressing variables, constraints, and objectives.
- Pyomo models can be solved by a variety of external solvers (e.g., GLPK, CBC, Gurobi, CPLEX).

Installation:

```
pip install pyomo
```

Import Pyomo:

```
from pyomo.environ import *
```

Transportation problem: sets, parameters and variables

- Sets:
 - ► I: set of suppliers
 - ► *J*: set of customers
- Parameters:
 - \triangleright s_i : supply available at supplier $i \in I$
 - ▶ d_i : demand required at customer $i \in J$
 - $ightharpoonup c_{ij}$: cost per unit shipped from supplier i to customer j
- Decision variables:
 - $\triangleright x_{ij}$: quantity shipped from supplier i to customer j

Transportation problem: objective function and constraints

Objective function:

$$\text{Minimize } Z = \sum_{i \in I} \sum_{j \in J} c_{ij} x_{ij}$$

- Constraints:
 - Supply capacity:

$$\sum_{i \in J} x_{ij} \le s_i \qquad \forall i \in I$$

Demand satisfaction:

$$\sum_{i \in I} x_{ij} \ge d_j \qquad \forall j \in J$$

► Non-negativity:

$$x_{ij} \geq 0$$
 $\forall i \in I, \ \forall j \in J$

Basic building blocks in Pyomo

- ConcreteModel: The main object that holds sets, parameters, variables, constraints, and objectives.
- **Set**: Represents a finite collection of elements (e.g., suppliers, customers).
- Var: Decision variables whose values are determined by the optimization solver.
- Constraint: Mathematical conditions that must be satisfied.
- Objective: The function to be minimized or maximized.

Defining a Pyomo model

- A ConcreteModel in Pyomo is a container for sets, parameters, variables, constraints, and objectives.
- ConcreteModel() creates a model where all components are fully specified when the script runs.

```
model = ConcreteModel()
```

Pyomo Defining sets

- Sets represent index collections for variables and constraints.
- The initialize argument fills the set from Python objects.

```
model.S = Set(initialize=supply.keys())  # Suppliers
model.C = Set(initialize=demand.keys())  # Customers
```

• S and C are user-defined names for sets.

Defining variables

- Variables represent the decisions to be made (e.g., how much to ship from each supplier to each customer).
- In the code:

```
model.x = Var(model.S, model.C, domain=NonNegativeReals)
```

- model.x[i,j] is the amount shipped from supplier i to customer j.
- ullet NonNegativeReals ensures variables are ≥ 0 .

Defining the objective function

• Minimize the total transportation cost:

- costs[(i, j)] * model.x[i, j] is computed for every supplier i
 and customer j.
- for i in model.S for j in model.C loops over all supplier-customer pairs.
- The expression inside sum(...) is called a Python generator expression—it produces terms one at a time, making this both concise and memory efficient.

Defining the constraints

• Each supplier's total shipment does not exceed its available supply.

• Each customer's demand is satisfied.

Choosing and configuring a solver

- Pyomo uses external solvers (like GLPK, CBC, Gurobi, CPLEX) to find optimal solutions.
- You can choose a solver by name:

```
solver = SolverFactory("cbc")
```

 Replace "cbc" with the name of your solver (e.g., "gurobi", "cplex").

Solving the model

• Once the solver is configured, you can solve the model:

```
results = solver.solve(model, tee=True)
```

- solve() runs the optimization and returns the results.
- The tee argument controls whether to display solver output in the console.

Extracting the results

 After solving, you can access the optimal variable values and objective value:

```
flows_opt = {}
for i in model.S:
    for j in model.C:
        flows_opt[(i, j)] = value(model.x[i, j])

opt_cost = value(model.obj)
```

 value() extracts the numerical value from a Pyomo variable or expression.