Chapter 4:

Lecture #4

Register Transfer and Microoperations

contents

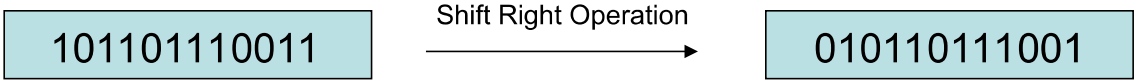
- **Register Transfer Language**
- **Register Transfer**
- **Bus and Memory Transfers**
- **Arithmetic Microoperations**
- **Logic Microoperations**
- **Shift Microoperations**
- **Arithmetic Logic Shift Unit**

4-1 Register Transfer Language (RTL)

- Digital System: An interconnection of hardware modules that do a certain task on the information.
- Registers + Operations performed on the data stored in them = Digital Module
- Modules are interconnected with common data and control paths to form a digital computer system

4-1 Register Transfer Language cont.

- Microoperations: operations executed on data stored in one or more registers.
- For any function of the computer, a sequence of microoperations is used to describe it
- The result of the operation may be:
  - replace the previous binary information of a register or
  - transferred to another register



4-1 Register Transfer Language cont.

- The internal hardware organization of a digital computer is defined by specifying:
  - The set of registers it contains and their function
  - The sequence of microoperations performed on the binary information stored in the registers
  - The control that initiates the sequence of microoperations
- Registers + Microoperations Hardware + Control Functions = Digital Computer

4-1 Register Transfer Language cont.

- Register Transfer Language (RTL) : a symbolic notation to describe the microoperation transfers among registers

Next steps:

- Define symbols for various types of microoperations,
- Describe the hardware that implements these microoperations

4-2 Register Transfer (our first microoperation)

- Computer registers are designated by capital letters (sometimes followed by numerals) to denote the function of the register
  - R1: processor register
  - MAR: Memory Address Register (holds an address for a memory unit)
  - PC: Program Counter
  - IR: Instruction Register
  - SR: Status Register

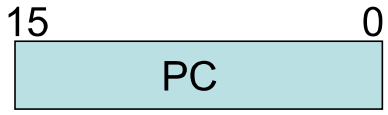
4-2 Register Transfer cont.

- The individual flip-flops in an n-bit register are numbered in sequence from 0 to n-1 (from the right position toward the left position)

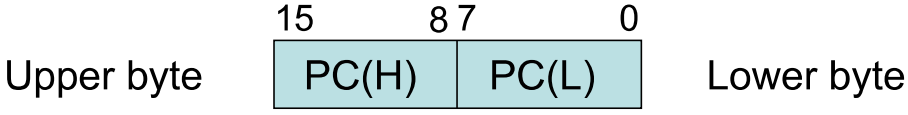
A block diagram of a register

4-2 Register Transfer cont.

Other ways of drawing the block diagram of a register:



Numbering of bits



Partitioned into two parts

4-2 Register Transfer cont.

- Information transfer from one register to another is described by a *replacement operator:* **R2 ← R1**
  - This statement denotes a transfer of the content of register R1 into register R2
- The transfer happens in one clock cycle
- The content of the R1 (source) does not change
- The content of the R2 (destination) will be lost and replaced by the new data transferred from R1
- We are assuming that the circuits are available from the outputs of the source register to the inputs of the destination register, and that the destination register has a parallel load capability

4-2 Register Transfer cont.

- Conditional transfer occurs only under a control condition

- Representation of a (conditional) transfer

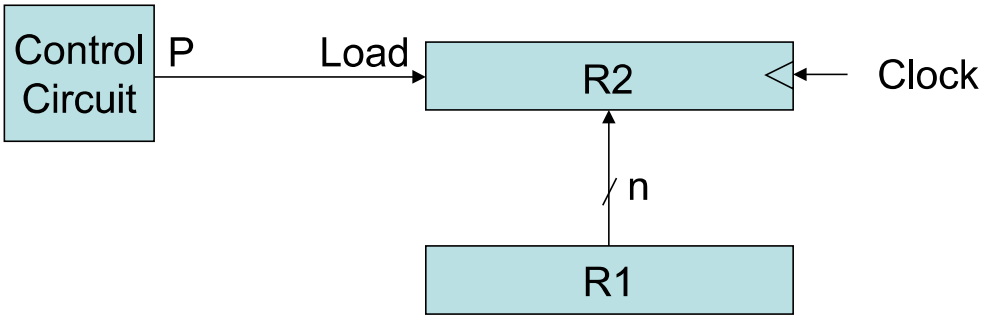
  P: $R2 \leftarrow R1$

- A binary condition (P equals to 0 or 1) determines when the transfer occurs
- The content of R1 is transferred into R2 only if P is 1

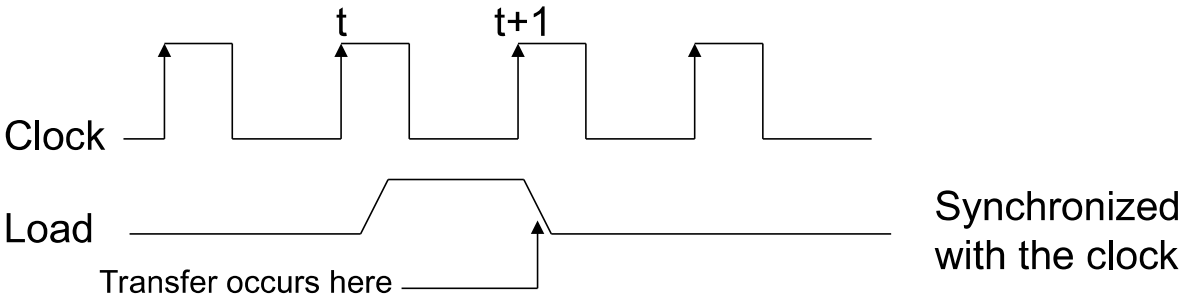
4-2 Register Transfer cont.

Hardware implementation of a controlled transfer: P: R2 ← R1

Block diagram:



Timing diagram



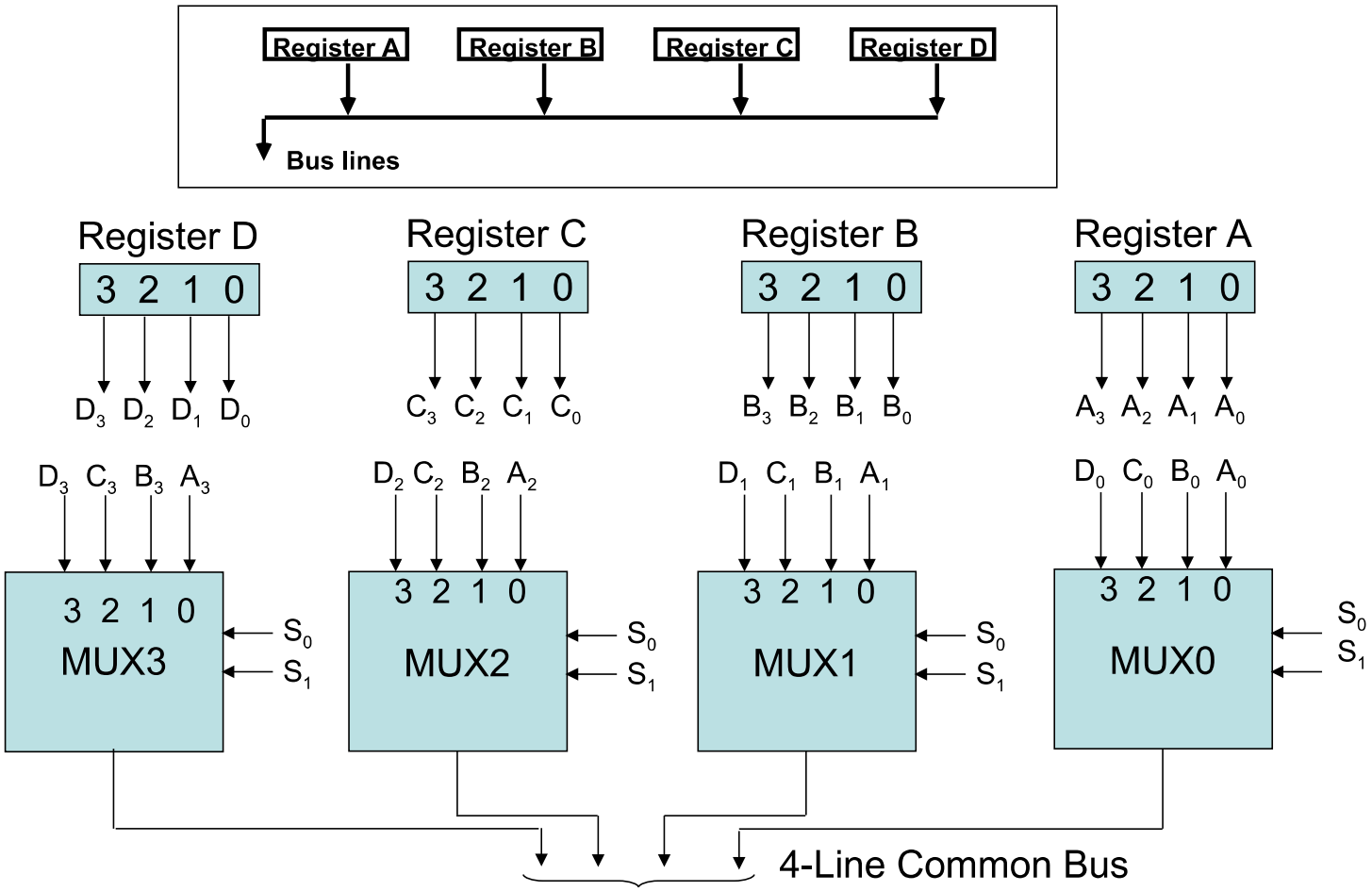
4-2 Register Transfer cont.

Basic Symbols for Register Transfers		
Symbol	Description	Examples
Letters & numerals	Denotes a register	MAR, R2
Parenthesis ( )	Denotes a part of a register	R2(0-7), R2(L)
Arrow ←	Denotes transfer of information	R2 ← R1
Comma ,	Separates two microoperations	R2 ← R1, R1 ← R2

4-3 Bus and Memory Transfers

- Paths must be provided to transfer information from one register to another
- A *Common Bus System* is a scheme for transferring information between registers in a multiple-register configuration
- A bus: set of common lines, one for each bit of a register, through which binary information is transferred one at a time
- Control signals determine which register is selected by the bus during each particular register transfer

4-3 Bus and Memory Transfers



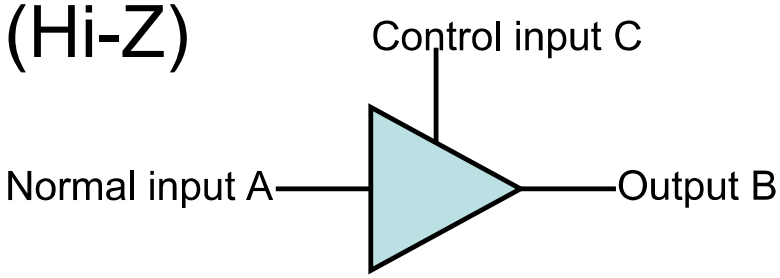
4-3 Bus and Memory Transfers

- The transfer of information from a bus into one of many destination registers is done:
  - By connecting the bus lines to the inputs of all destination registers and then:
  - activating the load control of the particular destination register selected
- We write: R2 ← C to symbolize that the content of register C is *loaded into* the register R2 using the common system bus
- It is equivalent to: BUS ←C, (select C)

  R2 ←BUS (Load R2)

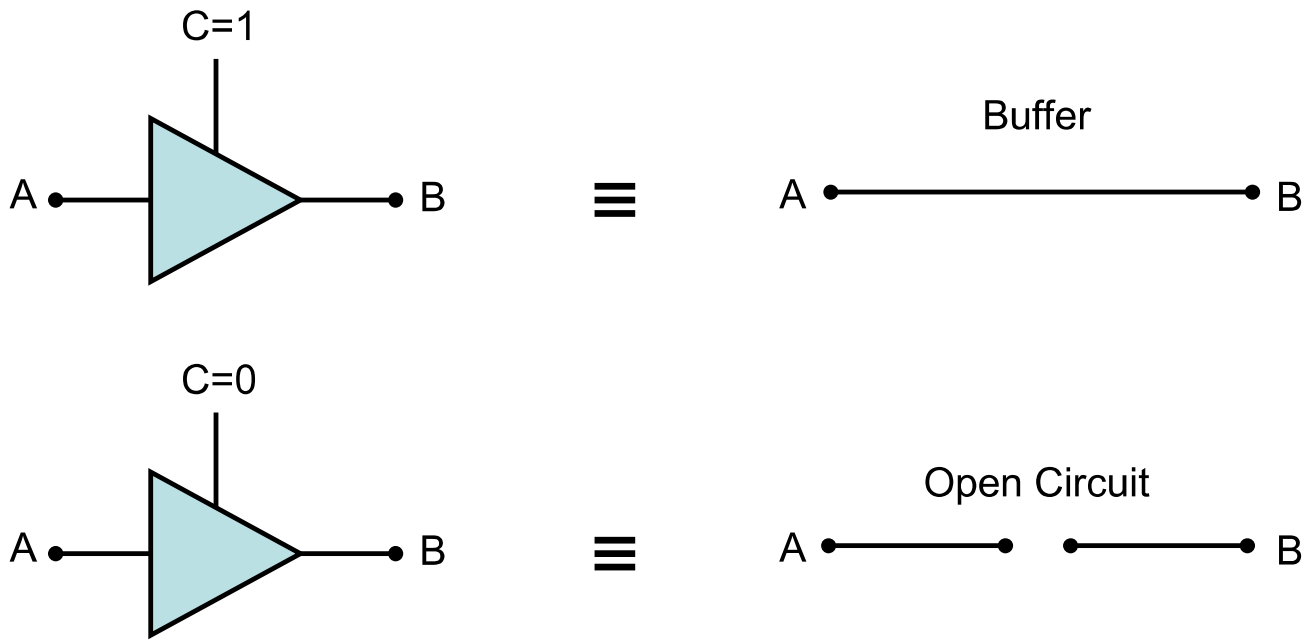
4-3 Bus and Memory Transfers: Three-State Bus Buffers

- A bus system can be constructed with three-state buffer gates instead of multiplexers
- A three-state buffer is a digital circuit that exhibits three states: logic-0, logic-1, and high-impedance (Hi-Z)

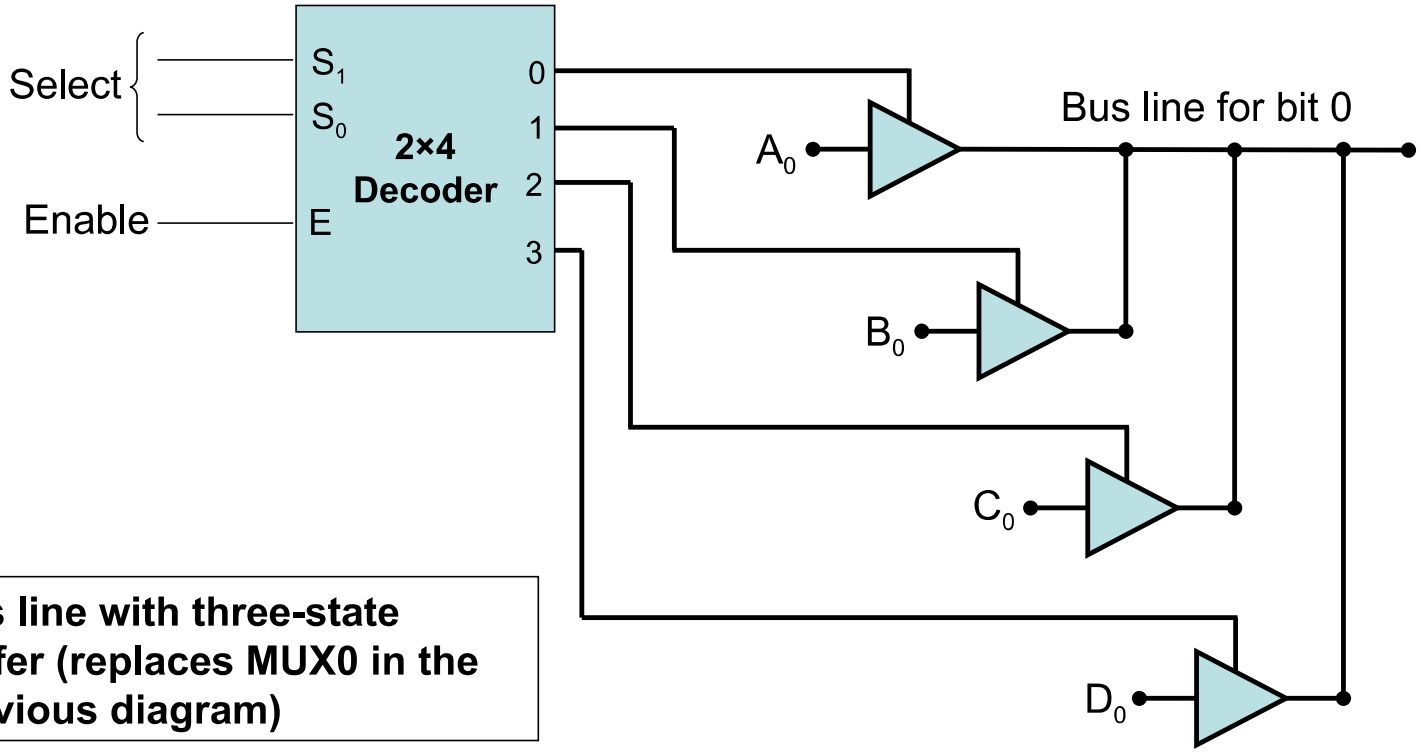


Three-State Buffer

4-3 Bus and Memory Transfers: Three-State Bus Buffers cont.



4-3 Bus and Memory Transfers: Three-State Bus Buffers cont.



Bus line with three-state buffer (replaces MUX0 in the previous diagram)

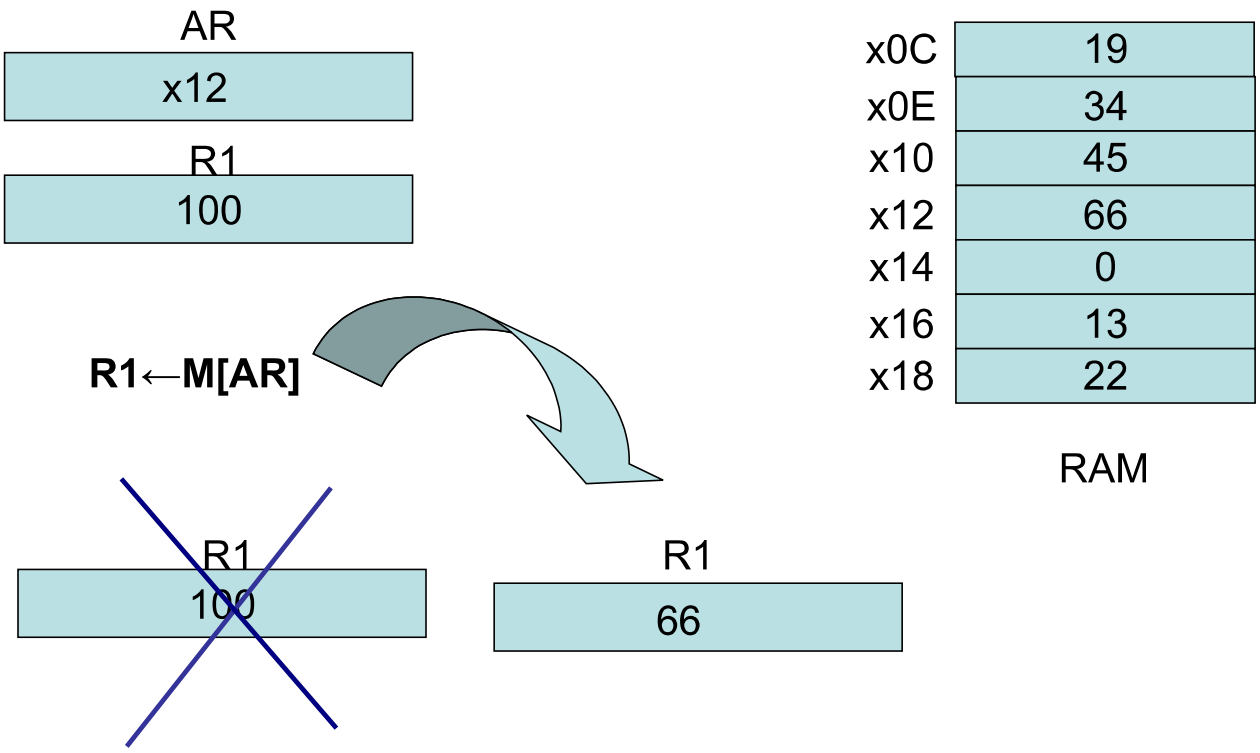
4-3 Bus and Memory Transfers: Memory Transfer

- Memory read : Transfer from memory
- Memory write : Transfer to memory
- Data being read or wrote is called a memory word (called M)- (refer to section 2-7)
- It is necessary to specify the address of M when writing /reading memory
- This is done by enclosing the address in square brackets following the letter M
- Example: M[0016] : the memory contents at address 0x0016

4-3 Bus and Memory Transfers: Memory Transfer cont.

- Assume that the address of a memory unit is stored in a register called the Address Register AR
- Lets represent a Data Register with DR, then:
    - Read: DR ← M[AR]
    - Write: M[AR] ← DR

4-3 Bus and Memory Transfers: Memory Transfer cont.



4-4 Arithmetic Microoperations

- The microoperations most often encountered in digital computers are classified into four categories:
  - Register transfer microoperations
  - Arithmetic microoperations (on numeric data stored in the registers)
  - Logic microoperations (bit manipulations on non-numeric data)
  - Shift microoperations

4-4 Arithmetic Microoperations cont.

- The basic arithmetic microoperations are: addition, subtraction, increment, decrement, and shift
- Addition Microoperation:

$$R3 \leftarrow R1+R2$$

- Subtraction Microoperation:

R3 ←R1-R2 or :

1's complement

$$R3 \leftarrow R1+\overline{R2}+1$$

4-4 Arithmetic Microoperations cont.

- One's Complement Microoperation:

$$R2 \leftarrow \overline{R2}$$

- Two's Complement Microoperation:

$$R2 \leftarrow \overline{R2}+1$$

- Increment Microoperation:

$$R2 \leftarrow R2+1$$

- Decrement Microoperation:

$$R2 \leftarrow R2-1$$

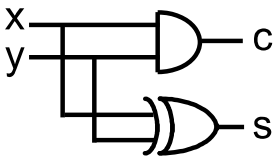
Half Adder/Full Adder

Half Adder

x	y	c	s
0	0	0	0
0	1	0	1
1	0	0	1
1	1	1	0

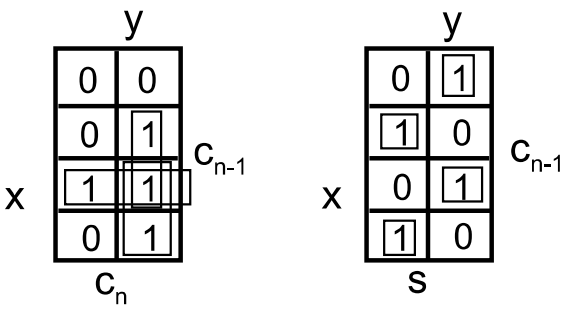
$c = xy$

$s = xy' + x'y$
$= x \oplus y$

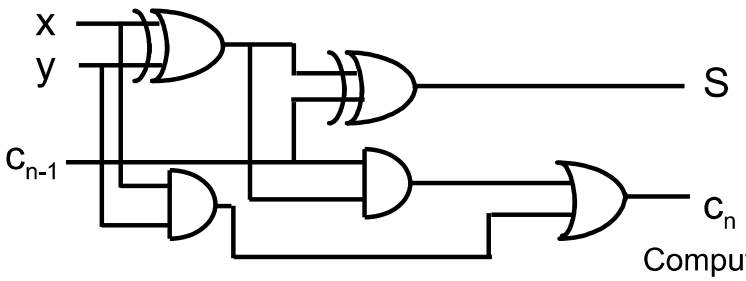


Full Adder

x	y	c_{n-1}	c_n	s
0	0	0	0	0
0	0	1	0	1
0	1	0	0	1
0	1	1	1	0
1	0	0	0	1
1	0	1	1	0
1	1	0	1	0
1	1	1	1	1

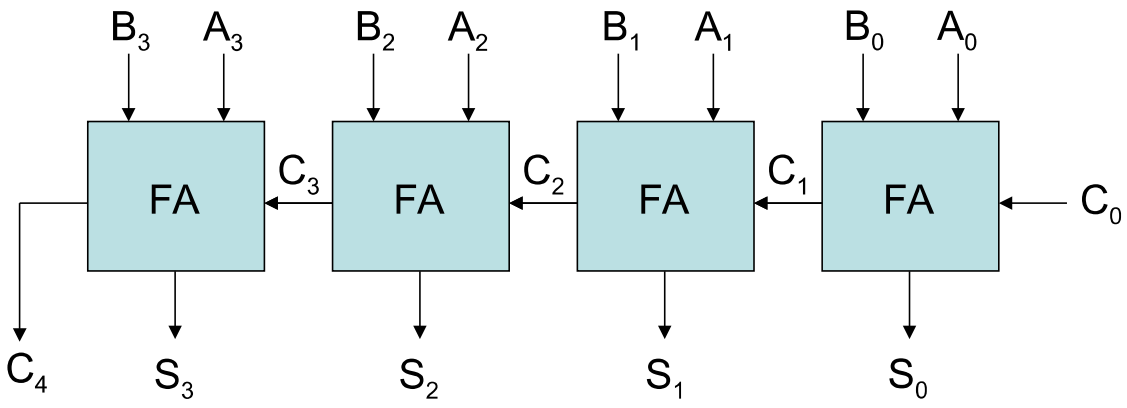


$c_n = xy + xc_{n-1} + yc_{n-1}$
$= xy + (x \oplus y)c_{n-1}$



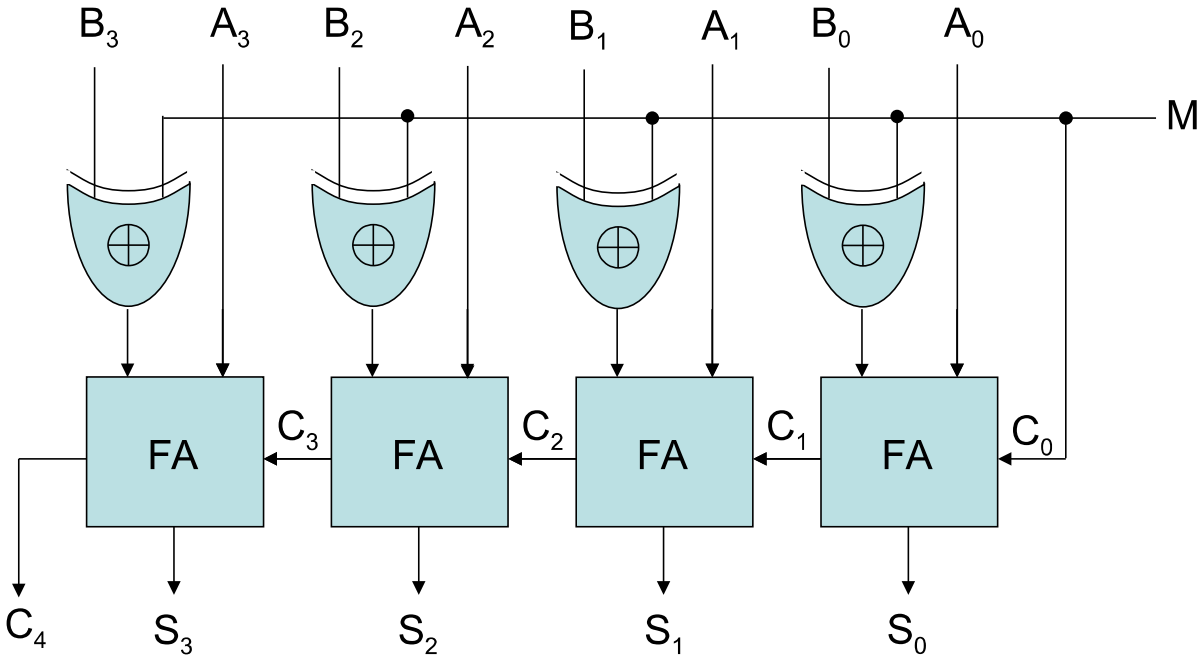
$s = x'y'c_{n-1} + x'yc'_{n-1} + xy'c'_{n-1} + xyc_{n-1}$
$= x \oplus y \oplus c_{n-1} = (x \oplus y) \oplus c_{n-1}$

4-4 Arithmetic Microoperations
Binary Adder



4-bit binary adder
(connection of FAs)

4-4 Arithmetic Microoperations
Binary Adder-Subtractor



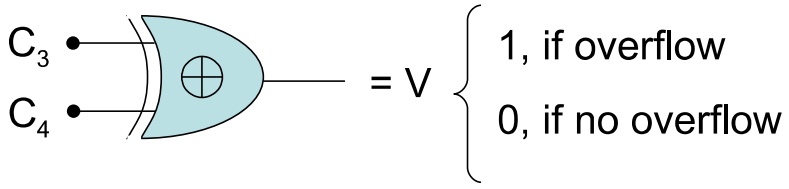
4-bit adder-subtractor

4-4 Arithmetic Microoperations
Binary Adder-Subtractor

- For unsigned numbers, this gives A – B if A≥B or the 2's complement of (B – A) if A < B

  (example: 3 – 5 = -2= 1110)
- For signed numbers, the result is A – B provided that there is no overflow. (example : -3 – 5= -8)

```
 1101
 1011  +
------
 1000
```

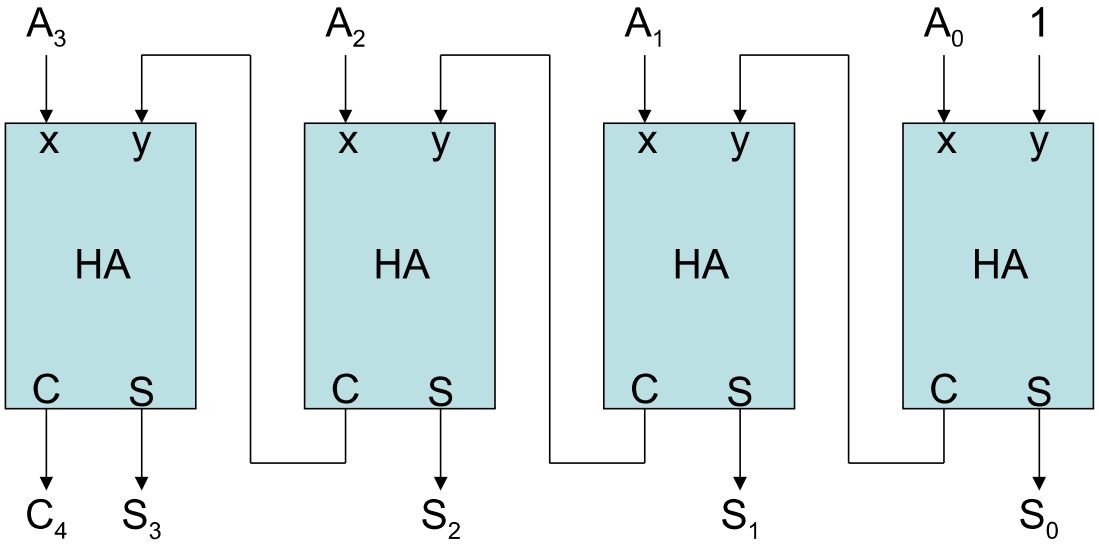


Overflow detector for signed numbers

4-4 Arithmetic Microoperations
Binary Adder-Subtractor cont.

- What is the range of unsigned numbers that can be represented in 4 bits?
- What is the range of signed numbers that can be represented in 4 bits?
- Repeat for n-bit?!

4-4 Arithmetic Microoperations
Binary Incrementer



4-bit Binary Incrementer

4-4 Arithmetic Microoperations
Binary Incrementer

- Binary Incrementer can also be implemented using a counter
- A binary decrementer can be implemented by adding 1111 to the desired register each time!

4-4 Arithmetic Microoperations
Arithmetic Circuit

- This circuit performs seven distinct arithmetic operations and the basic component of it is the parallel adder
- The output of the binary adder is calculated from the following arithmetic sum:
  - $D = A + Y + C_{in}$

4-4 Arithmetic Microoperations
Arithmetic Circuit cont.

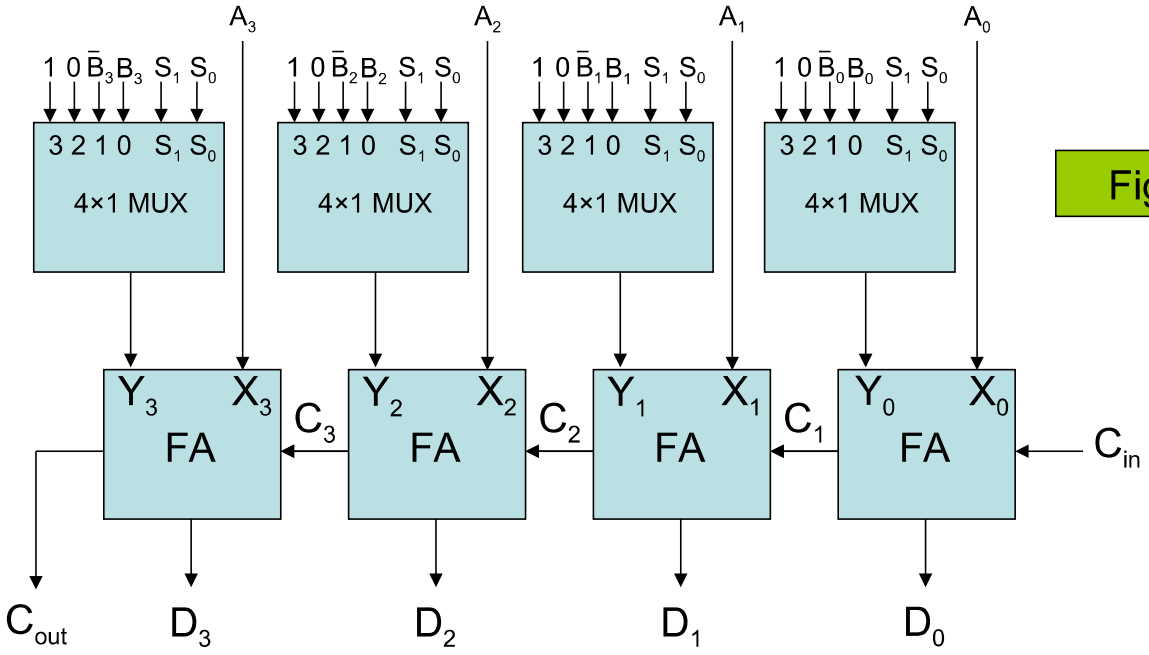
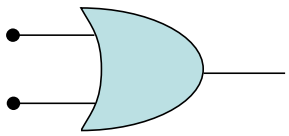


Figure A

4-bit Arithmetic Circuit

4-5 Logic Microoperations
The four basic microoperations

OR Microoperation

- Symbol: $\vee$, +
- Gate: 
- Example: $100110_2 \vee 1010110_2 = 1110110_2$

OR

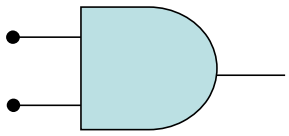
OR

P+Q: R1←R2+R3, R4←R5 $\vee$R6

ADD

4-5 Logic Microoperations
The four basic microoperations
cont.

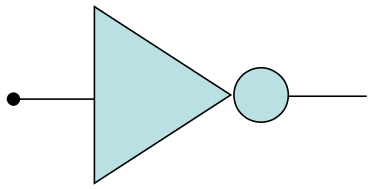
AND Microoperation

- Symbol: ^
- Gate: 
- Example: 100110_2 ^ 1010110_2 = 0000110_2

4-5 Logic Microoperations
The four basic microoperations
cont.

Complement (NOT) Microoperation

- Symbol: -
- Gate:

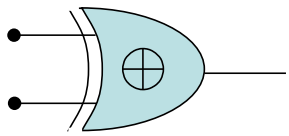


- Example: $\overline{1010110_2} = 0101001_2$

4-5 Logic Microoperations
The four basic microoperations
cont.

XOR (Exclusive-OR) Microoperation

- Symbol: $\oplus$
- Gate:



- Example: $100110_2 \oplus 1010110_2 = 1110000_2$

4-5 Logic Microoperations
Other Logic Microoperations

Selective-set Operation

- Used to force selected bits of a register into logic-1 by using the OR operation

- Example: $0100_2 \vee 1000_2 = 1100_2$

In a processor register

Loaded into a register from memory to perform the selective-set operation

4-5 Logic Microoperations
Other Logic Microoperations cont.

Selective-complement (toggling) Operation

- Used to force selected bits of a register to be complemented by using the XOR operation

- Example: $0001_2 \oplus 1000_2 = 1001_2$

In a processor register

Loaded into a register from memory to perform the selective-complement operation

4-5 Logic Microoperations
Other Logic Microoperations cont.

Insert Operation

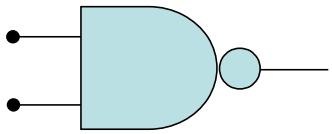
- Step1: mask the desired bits
- Step2: OR them with the desired value

- Example: suppose R1 = 0110 1010, and we desire to replace the leftmost 4 bits (0110) with 1001 then:
  - Step1: 0110 1010 ^ 0000 1111
  - Step2: 0000 1010 ˅ 1001 0000

✂→ R1 = 1001 1010

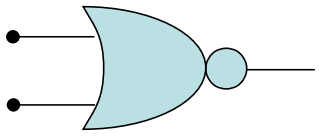
4-5 Logic Microoperations
Other Logic Microoperations cont.

NAND Microoperation

- Symbols: ^ and -
- Gate: 
- Example: 100110_2 ^ 1010110_2 = 1111001_2

4-5 Logic Microoperations
Other Logic Microoperations cont.

NOR Microoperation

- Symbols: $\downarrow$ and $-$
- Gate: 
- Example: $100110_2 \downarrow 1010110_2 = 0001001_2$

4-5 Logic Microoperations

Other Logic Microoperations cont.

Set (Preset) Microoperation

- Force all bits into 1's by ORing them with a value in which all its bits are being assigned to logic-1
- Example: $100110_2 \vee 111111_2 = 111111_2$

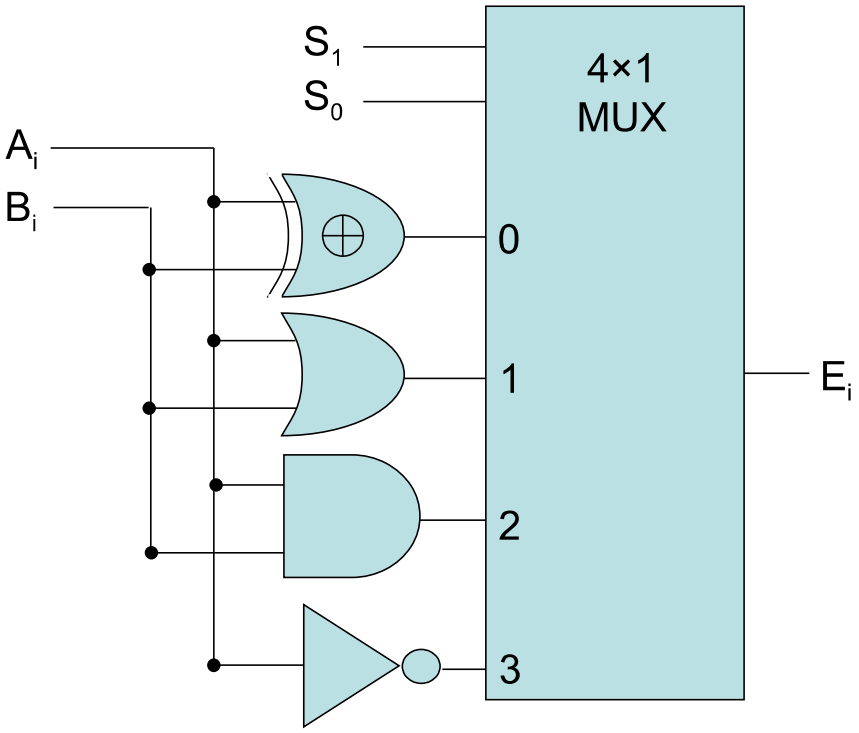
Clear (Reset) Microoperation

- Force all bits into 0's by ANDing them with a value in which all its bits are being assigned to logic-0
- Example: $100110_2 \wedge 000000_2 = 000000_2$

4-5 Logic Microoperations Hardware Implementation

- The hardware implementation of logic microoperations requires that logic gates be inserted for each bit or pair of bits in the registers to perform the required logic function
- Most computers use only four (AND, OR, XOR, and NOT) from which all others can be derived.

4-5 Logic Microoperations Hardware Implementation cont.



S_1	S_0	Output	Operation
0	0	$E = A \oplus B$	XOR
0	1	$E = A \vee B$	OR
1	0	$E = A \wedge B$	AND
1	1	$E = \overline{A}$	Complement

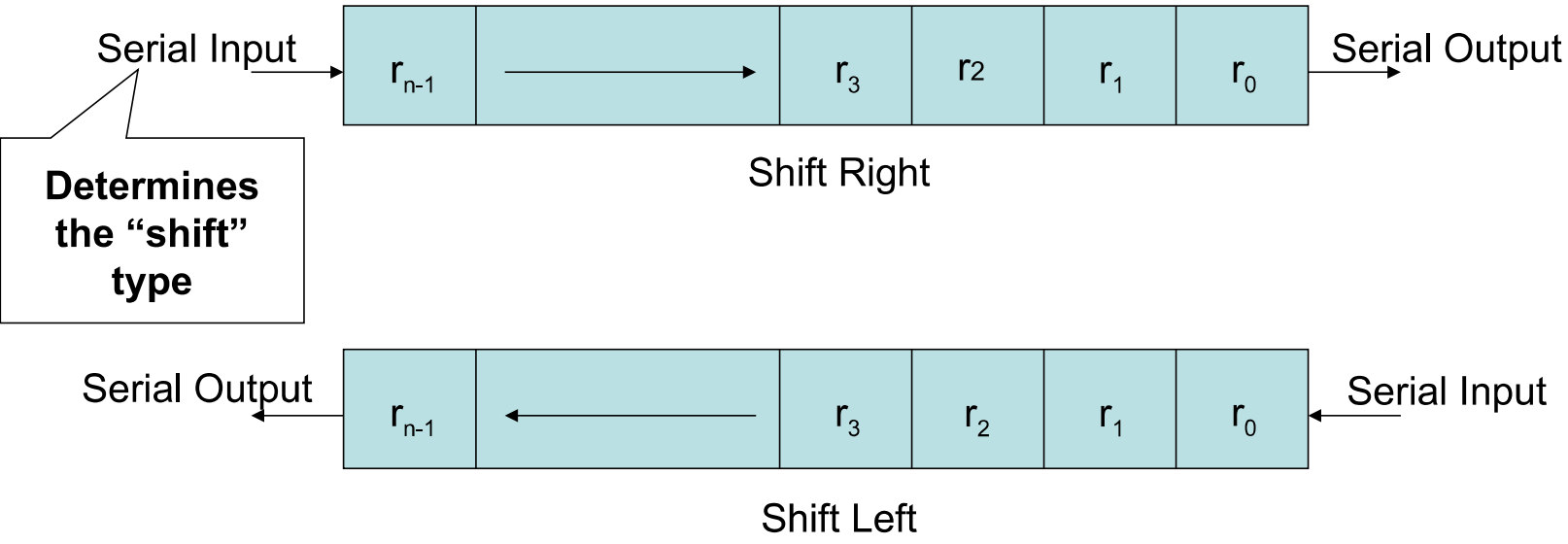
This is for one bit i

Figure B

4-6 Shift Microoperations

- Used for serial transfer of data
- Also used in conjunction with arithmetic, logic, and other data-processing operations
- The contents of the register can be shifted to the left or to the right
- As being shifted, the first flip-flop receives its binary information from the serial input
- Three types of shift: Logical, Circular, and Arithmetic

4-6 Shift Microoperations cont.



**Note that the bit ri is the bit at position (i) of the register

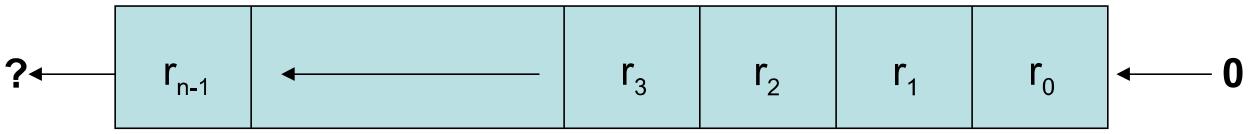
4-6 Shift Microoperations: Logical Shifts

- Transfers 0 through the serial input
- Logical Shift Right: R1←shr R1

The same

- Logical Shift Left: R2←shl R2

The same



Logical Shift Left

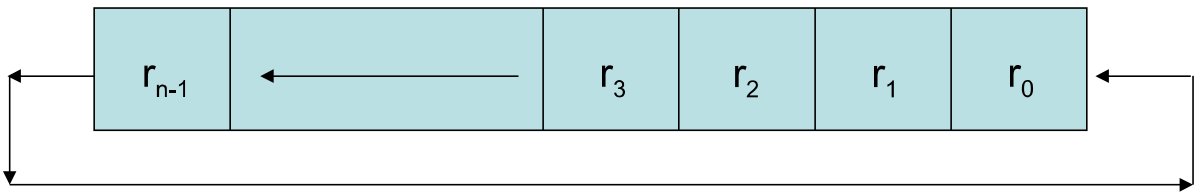
4-6 Shift Microoperations:
Circular Shifts (Rotate Operation)

- Circulates the bits of the register around the two ends without loss of information
- Circular Shift Right: R1 ← cir R1

The same

- Circular Shift Left: R2 ← cil R2

The same



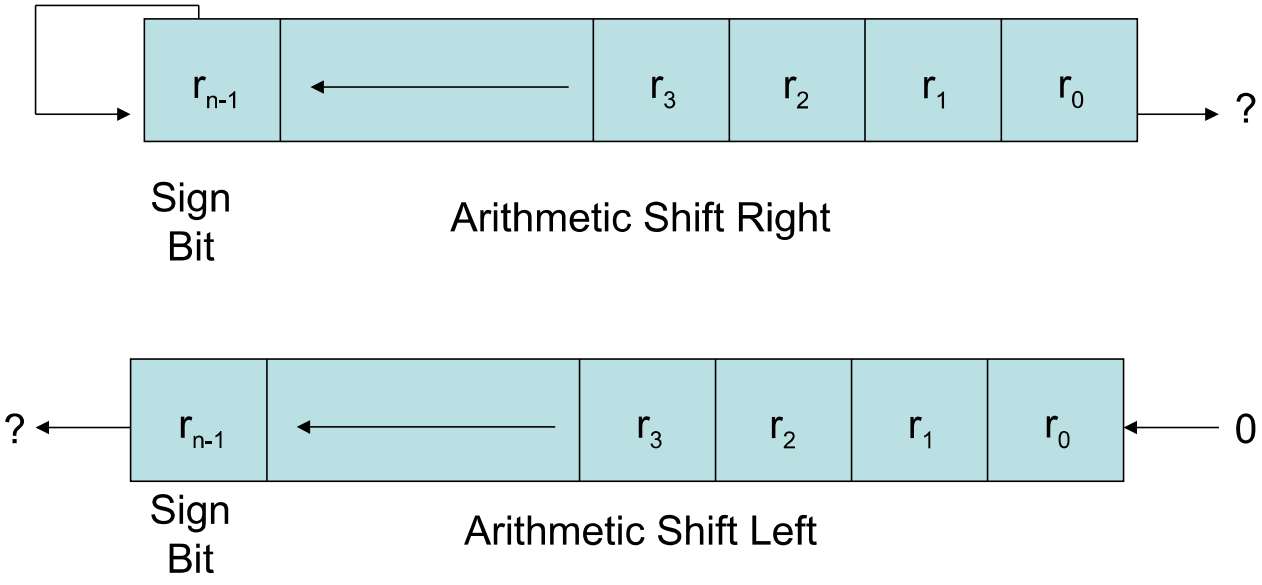
Circular Shift Left

4-6 Shift Microoperations
Arithmetic Shifts

- Shifts a signed binary number to the left or right
- An arithmetic shift-left multiplies a signed binary number by 2: ashl (00100): 01000
- An arithmetic shift-right divides the number by 2

  ashr (00100) : 00010
- An overflow may occur in arithmetic shift-left, and occurs when the sign bit is changed (sign reversal)

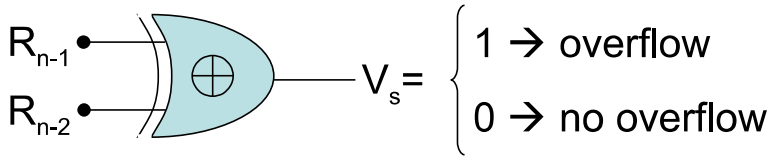
4-6 Shift Microoperations
Arithmetic Shifts cont.



4-6 Shift Microoperations
Arithmetic Shifts cont.

- An overflow flip-flop V_s can be used to detect an arithmetic shift-left overflow

$$V_s = R_{n-1} \oplus R_{n-2}$$



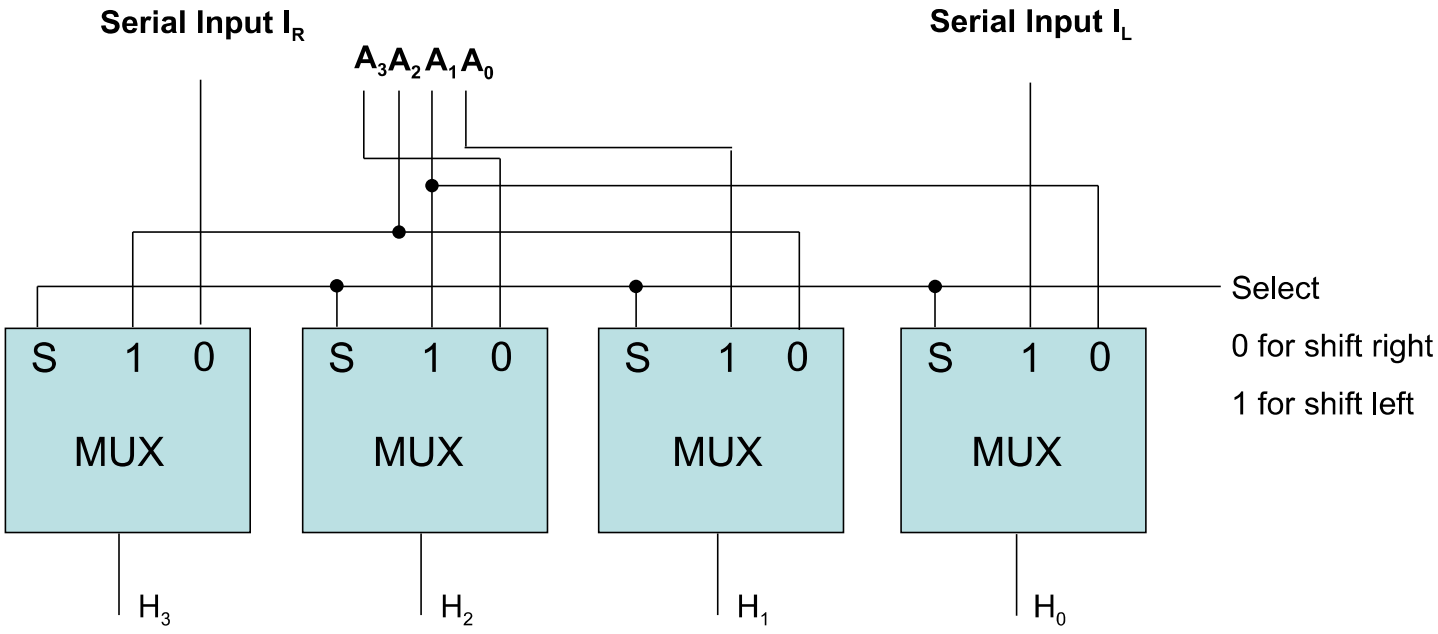
4-6 Shift Microoperations cont.

- Example: Assume R1=11001110, then:
  - Arithmetic shift right once : R1 = 11100111
  - Arithmetic shift right twice : R1 = 11110011
  - Arithmetic shift left once : R1 = 10011100
  - Arithmetic shift left twice : R1 = 00111000
  - Logical shift right once : R1 = 01100111
  - Logical shift left once : R1 = 10011100
  - Circular shift right once : R1 = 01100111
  - Circular shift left once : R1 = 10011101

4-6 Shift Microoperations Hardware Implementation cont.

- A possible choice for a shift unit would be a bidirectional shift register with parallel load (refer to Fig 2-9). Has drawbacks:
  - Needs two pulses (the clock and the shift signal pulse)
  - Not efficient in a processor unit where multiple number of registers share a common bus
- It is more efficient to implement the shift operation with a combinational circuit

4-6 Shift Microoperations Hardware Implementation cont.



4-bit Combinational Circuit Shifter

4-7 Arithmetic Logic Shift Unit

- Instead of having individual registers performing the microoperations directly, computer systems employ a number of storage registers connected to a common operational unit called an Arithmetic Logic Unit (**ALU**)

4-7 Arithmetic Logic Shift Unit cont.