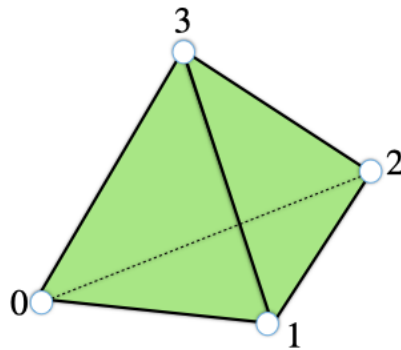


## 1 Ejemplo 1

Consideramos el 3-símplice  $(0,1,2,3)$



```
[80]: sc=SimplicialComplex([(0,1,2,3)])
```

## 2 Conjunto de todas sus caras

```
[81]: sc.face_set
```

```
[81]: {(0,),  
      (0, 1),  
      (0, 1, 2),  
      (0, 1, 2, 3),  
      (0, 1, 3),  
      (0, 2),  
      (0, 2, 3),  
      (0, 3),  
      (1,),  
      (1, 2),  
      (1, 2, 3),  
      (1, 3),  
      (2,),  
      (2, 3),  
      (3,)}
```

## 3 Dimensión

```
[82]: sc.dimension
```

```
[82]: 3
```

## 4 Conjunto de vértices

```
[83]: sc.n_faces(0)
```

```
[83]: {(0,), (1,), (2,), (3,)}
```

## 5 Conjunto de aristas

```
[84]: sc.n_faces(1)
```

```
[84]: {(0, 1), (0, 2), (0, 3), (1, 2), (1, 3), (2, 3)}
```

## 6 Conjunto de 2-símplices

```
[85]: sc.n_faces(2)
```

```
[85]: {(0, 1, 2), (0, 1, 3), (0, 2, 3), (1, 2, 3)}
```

## 7 Conjunto de 3-símplices

```
[86]: sc.n_faces(3)
```

```
[86]: {(0, 1, 2, 3)}
```

## 8 Característica de Euler

```
[87]: sc.Euler_characteristic
```

```
[87]: 1
```

## 9 Estrella de la arista (0,1)

```
[88]: sc.st((0,1))
```

```
[88]: {(0, 1), (0, 1, 2), (0, 1, 2, 3), (0, 1, 3)}
```

## 10 Link de la arista (0,1)

```
[89]: sc.lk((0,1))
```

```
[89]: {(2,), (2, 3), (3,)}
```

## 11 Número de componentes conexas

```
[90]: sc.connected_components()
```

```
[90]: 1
```

```
[ ]:
```

## 12 Ejemplo 2

Borde del tetraedro (triangula la 2-esfera)

```
[91]: sc1=SimplicialComplex(list(sc.skeleton(2)))
```

## 13 Conjunto de todas sus caras

```
[92]: sc1.face_set
```

```
[92]: {(0,),  
      (0, 1),  
      (0, 1, 2),  
      (0, 1, 3),  
      (0, 2),  
      (0, 2, 3),  
      (0, 3),  
      (1,),  
      (1, 2),  
      (1, 2, 3),  
      (1, 3),  
      (2,),  
      (2, 3),  
      (3,)}
```

## 14 Dimensión

```
[93]: sc1.dimension
```

```
[93]: 2
```

## 15 Estrella del vértice 0

```
[94]: sc1.st((0,))
```

```
[94]: {(0,), (0, 1), (0, 1, 2), (0, 1, 3), (0, 2), (0, 2, 3), (0, 3)}
```

## 16 Link del vértice 0

```
[95]: sc1.lk((0,))
```

```
[95]: {(1,), (1, 2), (1, 3), (2,), (2, 3), (3,)}
```

## 17 Característica de Euler

```
[96]: sc1.Euler_characteristic
```

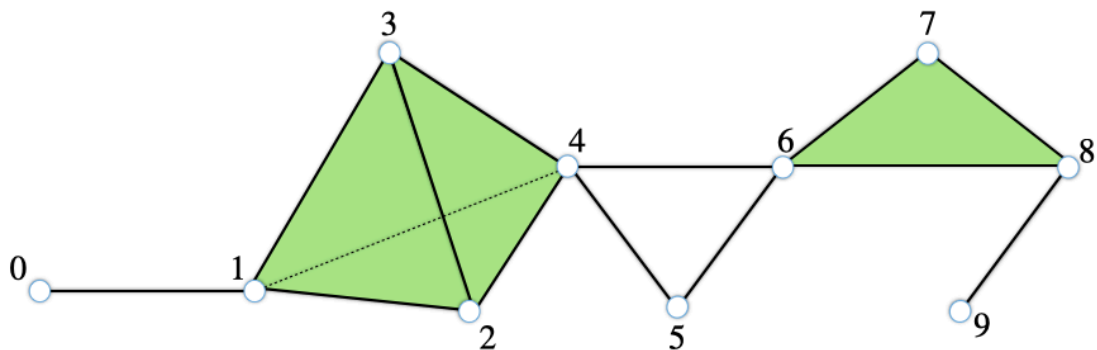
```
[96]: 2
```

## 18 Número de componentes conexas

```
[97]: sc1.connected_components()
```

```
[97]: 1
```

## 19 Ejemplo 3



Símplices maximales:  $(0,1)$ ,  $(1,2,3,4)$ ,  $(4,5)$ ,  $(5,6)$ ,  $(4,6)$ ,  $(6,7,8)$ ,  $(8,9)$

```
[98]: sc=SimplicialComplex([(0,1),(1,2,3,4),(4,5),(5,6),(4,6),(6,7,8),(8,9)])
```

## 20 Conjunto de todas sus caras

```
[99]: sc.face_set
```

```
[99]: {(0,),  
      (0, 1),  
      (1,),  
      (1, 2),  
      (1, 2, 3),  
      (1, 2, 3, 4),  
      (1, 2, 4),  
      (1, 3),  
      (1, 3, 4),  
      (1, 4),  
      (2,),  
      (2, 3),  
      (2, 3, 4),  
      (2, 4),  
      (3,),  
      (3, 4),  
      (4,),  
      (4, 5),  
      (4, 6),  
      (5,),  
      (5, 6),
```

```
(6,),  
(6, 7),  
(6, 7, 8),  
(6, 8),  
(7,),  
(7, 8),  
(8,),  
(8, 9),  
(9,)]}
```

## 21 Dimensión

```
[100]: sc.dimension
```

```
[100]: 3
```

## 22 1-esqueleto

```
[103]: sc.skeleton(1)
```

```
[103]: {(0,),  
        (0, 1),  
        (1,),  
        (1, 2),  
        (1, 3),  
        (1, 4),  
        (2,),  
        (2, 3),  
        (2, 4),  
        (3,),  
        (3, 4),  
        (4,),  
        (4, 5),  
        (4, 6),  
        (5,),  
        (5, 6),  
        (6,),  
        (6, 7),  
        (6, 8),  
        (7,),  
        (7, 8),  
        (8,),  
        (8, 9),
```

```
(9,))}
```

## 23 Estrella del vértice 4

```
[104]: sc.st((4,))
```

```
[104]: {(1, 2, 3, 4),  
        (1, 2, 4),  
        (1, 3, 4),  
        (1, 4),  
        (2, 3, 4),  
        (2, 4),  
        (3, 4),  
        (4,),  
        (4, 5),  
        (4, 6)}
```

## 24 Link del vértice 4

```
[105]: sc.lk((4,))
```

```
[105]: {(1,), (1, 2), (1, 2, 3), (1, 3), (2,), (2, 3), (3,), (5,), (6,)}
```

## 25 Característica de Euler

```
[106]: sc.Euler_characteristic
```

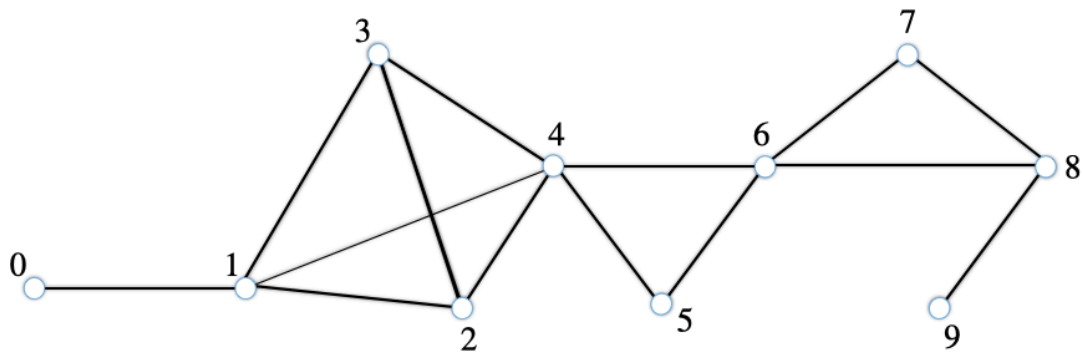
```
[106]: 0
```

## 26 Número de componentes conexas

```
[107]: sc.connected_components()
```

```
[107]: 1
```

## 27 Ejemplo 4



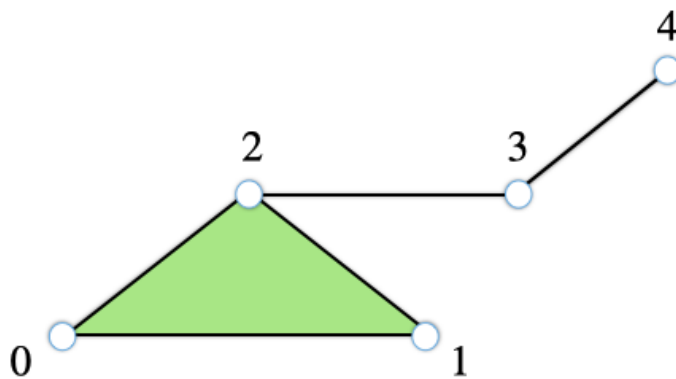
```
[108]: sc1=SimplicialComplex(list(sc.skeleton(1)))
```

## 28 Característica de Euler

```
[109]: sc1.Euler_characteristic
```

```
[109]: -4
```

## 29 Ejemplo 5



Símplices maximales:  $(0,1,2), (2,3), (3,4)$

```
[110]: sc=SimplicialComplex([(0,1,2),(2,3),(3,4)])
```



### 30 Conjunto de todos sus símlices

```
[111]: sc.face_set
```

```
[111]: {(0,),  
        (0, 1),  
        (0, 1, 2),  
        (0, 2),  
        (1,),  
        (1, 2),  
        (2,),  
        (2, 3),  
        (3,),  
        (3, 4),  
        (4,)}
```

### 31 Dimensión

```
[112]: sc.dimension
```

```
[112]: 2
```

### 32 1-esqueleto

```
[113]: sc.skeleton(1)
```

```
[113]: {(0,), (0, 1), (0, 2), (1,), (1, 2), (2,), (2, 3), (3,), (3, 4), (4,)}
```

### 33 Estrella del vértice 2

```
[116]: sc.st((2,))
```

```
[116]: {(0, 1, 2), (0, 2), (1, 2), (2,), (2, 3)}
```

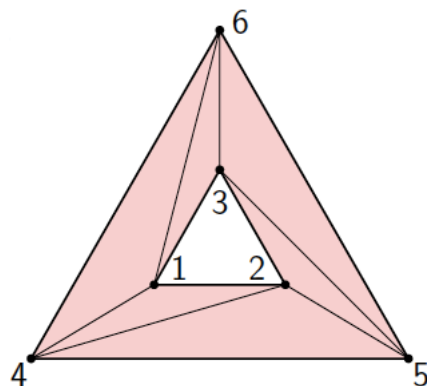
### 34 Link del vértice 2

```
[117]: sc.lk((2,))
```

```
[117]: {(0,), (0, 1), (1,), (3,)}
```

## 35 Ejemplo 6

Triangulación del anillo cerrado



Símplices maximales:  $(1,2,4)$ ,  $(1,3,6)$ ,  $(1,4,6)$ ,  $(2,3,5)$ ,  $(2,4,5)$ ,  $(3,5,6)$

```
[118]: sc=SimplicialComplex([(1,2,4),(1,3,6),(1,4,6),(2,3,5),(2,4,5),(3,5,6)])
```

## 36 Lista de todas sus caras

```
[119]: sc.face_set
```

```
[119]: {(1,),  
        (1, 2),  
        (1, 2, 4),  
        (1, 3),  
        (1, 3, 6),  
        (1, 4),  
        (1, 4, 6),  
        (1, 6),  
        (2,),  
        (2, 3),  
        (2, 3, 5),  
        (2, 4),  
        (2, 4, 5),  
        (2, 5),  
        (3,),  
        (3, 5),  
        (3, 5, 6),  
        (3, 6),  
        (4,),  
        (4, 5),  
        (4, 6),
```

```
(5, ),  
(5, 6),  
(6, )}
```

## 37 Dimensión

```
[120]: sc.dimension
```

```
[120]: 2
```

## 38 1-esqueleto

```
[121]: sc.skeleton(1)
```

```
[121]: {(1, ),  
        (1, 2),  
        (1, 3),  
        (1, 4),  
        (1, 6),  
        (2, ),  
        (2, 3),  
        (2, 4),  
        (2, 5),  
        (3, ),  
        (3, 5),  
        (3, 6),  
        (4, ),  
        (4, 5),  
        (4, 6),  
        (5, ),  
        (5, 6),  
        (6, )}
```

## 39 Estrella de la arista (1,4)

```
[122]: sc.st((1,4))
```

```
[122]: {(1, 2, 4), (1, 4), (1, 4, 6)}
```

## 40 Link de la arista (1,4)

```
[123]: sc.lk((1,4))
```

```
[123]: {(2,), (6,)}
```

## 41 Característica de Euler

```
[124]: sc.Euler_characteristic
```

```
[124]: 0
```

## 42 Ejemplo 7

1-esqueleto del anillo

```
[125]: sc1=SimplicialComplex(list(sc.skeleton(1)))
```

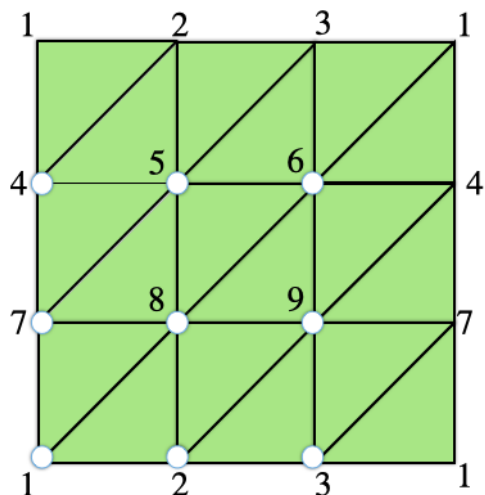
## 43 Característica de Euler

```
[126]: sc1.Euler_characteristic
```

```
[126]: -6
```

## 44 Ejemplo 8

El toro



Símplices maximales: (1,2,4), (2,4,5), (2,3,5), (3,5,6), (1,3,6), (1,4,6), (4,5,7), (5,7,8), (5,6,8), (6,8,9), (4,6,9), (4,7,9), (1,7,8), (1,2,8), (2,8,9), (2,3,9), (3,7,9), (1,3,7)

```
[127]: sc=SimplicialComplex([(1,2,4), (2,4,5), (2,3,5), (3,5,6), (1,3,6), (1,4,6),
    ↳ (4,5,7), (5,7,8), (5,6,8), (6,8,9), (4,6,9), (4,7,9), (1,7,8), (1,2,8),
    ↳ (2,8,9), (2,3,9), (3,7,9), (1,3,7) ])
```

## 45 Dimensión

```
[128]: sc.dimension
```

```
[128]: 2
```

## 46 Conjunto de vértices

```
[129]: sc.n_faces(0)
```

```
[129]: {(1,), (2,), (3,), (4,), (5,), (6,), (7,), (8,), (9,)}
```

## 47 Conjunto de aristas

```
[130]: sc.n_faces(1)
```

```
[130]: {(1, 2),
    (1, 3),
```

```
(1, 4),
(1, 6),
(1, 7),
(1, 8),
(2, 3),
(2, 4),
(2, 5),
(2, 8),
(2, 9),
(3, 5),
(3, 6),
(3, 7),
(3, 9),
(4, 5),
(4, 6),
(4, 7),
(4, 9),
(5, 6),
(5, 7),
(5, 8),
(6, 8),
(6, 9),
(7, 8),
(7, 9),
(8, 9)}
```

## 48 Estrella del vértice 1

```
[131]: sc.st((1,))
```

```
[131]: {(1,),
(1, 2),
(1, 2, 4),
(1, 2, 8),
(1, 3),
(1, 3, 6),
(1, 3, 7),
(1, 4),
(1, 4, 6),
(1, 6),
(1, 7),
(1, 7, 8),
(1, 8)}
```

## 49 Link del vértice 1

```
[132]: sc.lk((1,))
```

```
[132]: {(2,),  
        (2, 4),  
        (2, 8),  
        (3,),  
        (3, 6),  
        (3, 7),  
        (4,),  
        (4, 6),  
        (6,),  
        (7,),  
        (7, 8),  
        (8,)}
```

## 50 Característica de Euler

```
[133]: sc.Euler_characteristic
```

```
[133]: 0
```

## 51 Número de componentes conexas

```
[134]: sc.connected_components()
```

```
[134]: 1
```

## 52 Ejemplo 8

1-esqueleto del toro

```
[135]: sc1=SimplicialComplex(list(sc.skeleton(1)))
```

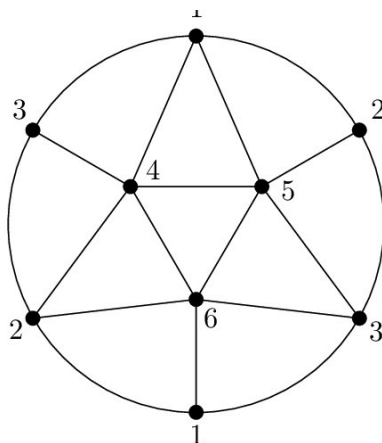
## 53 Característica de Euler

```
[136]: sc1.Euler_characteristic
```

```
[136]: -18
```

## 54 Ejemplo 9

Triangulación del plano proyectivo



Símplices maximales:  $(1,2,6)$ ,  $(2,3,4)$ ,  $(1,3,4)$ ,  $(1,2,5)$ ,  $(2,3,5)$ ,  $(1,3,6)$ ,  $(2,4,6)$ ,  $(1,4,5)$ ,  $(3,5,6)$ ,  $(4,5,6)$

```
[137]: sc=SimplicialComplex([(1,2,6), (2,3,4), (1,3,4), (1,2,5), (2,3,5), (1,3,6),  
→(2,4,6), (1,4,5), (3,5,6), (4,5,6)])
```

## 55 Dimensión

```
[138]: sc.dimension
```

```
[138]: 2
```

## 56 Conjunto de aristas

```
[140]: sc.n_faces(1)
```

```
[140]: {(1, 2),  
        (1, 3),  
        (1, 4),  
        (1, 5),  
        (1, 6),  
        (2, 3),  
        (2, 4),  
        (2, 5),  
        (2, 6),  
        (3, 4),  
        (3, 5),
```



```
(3, 6),  
(4, 5),  
(4, 6),  
(5, 6)}
```

## 57 Estrella del vértice 1

```
[141]: sc.st((1,))
```

```
[141]: {(1,),  
        (1, 2),  
        (1, 2, 5),  
        (1, 2, 6),  
        (1, 3),  
        (1, 3, 4),  
        (1, 3, 6),  
        (1, 4),  
        (1, 4, 5),  
        (1, 5),  
        (1, 6)}
```

## 58 Link del vértice 1

```
[142]: sc.lk((1,))
```

```
[142]: {(2,), (2, 5), (2, 6), (3,), (3, 4), (3, 6), (4,), (4, 5), (5,), (6,)}
```

## 59 Característica de Euler

```
[143]: sc.Euler_characteristic
```

```
[143]: 1
```

## 60 Componentes conexas

```
[144]: sc.connected_components()
```

```
[144]: 1
```

## 61 Ejemplo 10

1-esqueleto del plano proyectivo

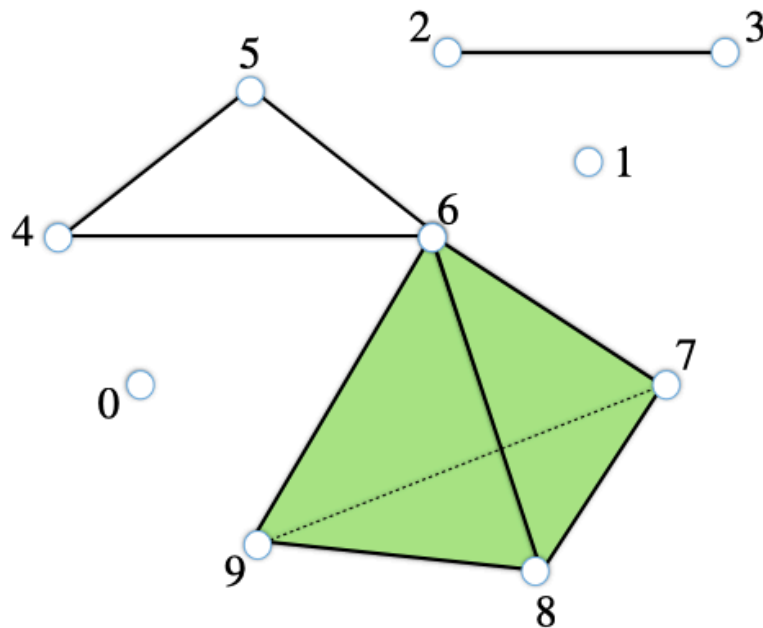
```
[145]: sc1=SimplicialComplex(list(sc.skeleton(1)))
```

## 62 Característica de Euler

```
[146]: sc1.Euler_characteristic
```

```
[146]: -9
```

## 63 Ejemplo 11



Símplices maximales:  $(0,)$ ,  $(1,)$ ,  $(2,3)$ ,  $(4,5)$ ,  $(5,6)$ ,  $(4,6)$ ,  $(6,7,8,9)$

```
[147]: sc=SimplicialComplex([(0,), (1,), (2,3), (4,5), (5,6), (4,6), (6,7,8,9)])
```

## 64 Conjunto de todas las caras

```
[148]: sc.face_set
```

```
[148]: {(0,),  
        (1,),  
        (2,),  
        (2, 3),  
        (3,),  
        (4,),  
        (4, 5),  
        (4, 6),  
        (5,),  
        (5, 6),  
        (6,),  
        (6, 7),  
        (6, 7, 8),  
        (6, 7, 8, 9),  
        (6, 7, 9),  
        (6, 8),  
        (6, 8, 9),  
        (6, 9),  
        (7,),  
        (7, 8),  
        (7, 8, 9),  
        (7, 9),  
        (8,),  
        (8, 9),  
        (9,)}
```

## 65 Dimensión

```
[149]: sc.dimension
```

```
[149]: 3
```

## 66 Conjunto de vértices

```
[150]: sc.n_faces(0)
```

```
[150]: {(0,), (1,), (2,), (3,), (4,), (5,), (6,), (7,), (8,), (9,)}
```

## 67 Conjunto de aristas

```
[151]: sc.n_faces(1)
```

```
[151]: {(2, 3),  
        (4, 5),  
        (4, 6),  
        (5, 6),  
        (6, 7),  
        (6, 8),  
        (6, 9),  
        (7, 8),  
        (7, 9),  
        (8, 9)}
```

## 68 Conjunto de 2-símplices

```
[154]: sc.n_faces(2)
```

```
[154]: {(6, 7, 8), (6, 7, 9), (6, 8, 9), (7, 8, 9)}
```

## 69 Conjunto de 3-símplices

```
[153]: sc.n_faces(3)
```

```
[153]: {(6, 7, 8, 9)}
```

## 70 Estrella del vértice 6

```
[155]: sc.st((6,))
```

```
[155]: {(4, 6),  
        (5, 6),  
        (6,),  
        (6, 7),  
        (6, 7, 8),  
        (6, 7, 8, 9),  
        (6, 7, 9),  
        (6, 8),  
        (6, 8, 9),  
        (6, 9)}
```

## 71 Link del vértice 6

```
[156]: sc.lk((6,))
```

```
[156]: {(4,), (5,), (7,), (7, 8), (7, 8, 9), (7, 9), (8,), (8, 9), (9,)}
```

## 72 Característica de Euler

```
[157]: sc.Euler_characteristic
```

```
[157]: 3
```

## 73 Número de componentes conexas

```
[159]: sc.connected_components()
```

```
[159]: 4
```