

rust-verification

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theory *Definitions*

imports *Main HOL–Library.LaTeXsugar*

begin

We present an imperative programming language with unique references called Unique, aiming at modeling the semantics of mutable references of Rust. In Rust, (mutable) references borrow the ownership, the capacity to observe and modify the content they are referring to, for a certain amount of time. References can borrow not only from a local variable or a heap allocation but also from another reference. The latter case is called reborrowing. Reborrow forms a tree-like relation between references. While the borrow checker of the Rust compiler enforces the reborrow relation to be well-formed (mutable xor alias!) statically, Unique tracks it dynamically. Imagine running an abstract interpreter of Rust with a dynamic borrow checker. At every point of use of unique references, Unique asserts that the reference is in the reborrow relation (the reference is valid) and removes every other reference reborrowed from it so that it is the only valid unique reference to the location. We expect that this dynamic nature of Unique will help us deal with (type-) unsafe portion of Rust. Note that this project is greatly influenced by R. Jung’s Stacked Borrows[1].

1 Definitions and Notations

1.1 Basic data types

type-synonym *vname* = *string*
datatype *ty* = *Tbool* | *Tint* | *Tref ty*
type-synonym *tag* = *nat*
type-synonym *address* = *nat*
datatype *tag-kind* = *Unique*

References consists of the address of the referent and the tag. A unique tag is assigned to each reference on creation.

datatype *val* = *VBool bool* | *VInt int* | *Reference address tag*

1.2 Expressions

datatype *place* = *Var vname* | *Deref place*

Datatype *place* represents an access path to data. It corresponds to `Place` in https://doc.rust-lang.org/nightly/nightly-rustc/rustc_middle/mir/struct.Place.html

datatype *operand* = *Place place* | *Constant val*

Datatype *operand* describes a value inside an rvalue. *Place* denotes the current value at the place, while *Constant* denotes a constant value. *operand* corresponds to `Place` in https://doc.rust-lang.org/nightly/nightly-rustc/rustc_middle/mir/enum.Operand.html, though we simplified the differentiation between a move and a copy (i.e. *Unique* doesn't track the ownership).

datatype
 rvalue = *Use operand*
 | *Box operand*
 | *Ref place*
 | *Reborrow place*
 | *Plus operand operand*
 | *Less operand operand*
 | *Not operand*
 | *And operand operand*

Datatype *rvalue* corresponds to an expression in a usual programming language (as in the previous version of *Unique*). We chose the term *rvalue* because of parity with Rust MIR (https://doc.rust-lang.org/nightly/nightly-rustc/rustc_middle/mir/enum.Rvalue.html)

Note that *rvalue* is *not* recursive. Compound expressions need to be broken apart so that intermediate computation is stored to a variable.

The semantics of the constructs is as follows:

- $Box :: operand \Rightarrow rvalue$ allocates memory in the heap, initializing with the argument (`Box::new` in Rust). Box returns a new unique reference. Note that Box in MIR doesn't initialize the location but only allocates. The semantics will be adapted to MIR's one as we formalize uninitialized memory.
- $Ref :: place \Rightarrow rvalue$ creates a unique reference pointing to the place.
- $Reborrow :: place \Rightarrow rvalue$ creates a new unique reference reborrowing from the argument (`&mut *p` in Rust, although most of the reborrows are automatically inserted by Rust). (TODO: I guess `Use(Copy(mutable ref))` in MIR corresponds to `Reborrow` in Unique.)

1.3 Commands

datatype

```
com = Skip
| Assign place rvalue (- ::= - [1000, 61] 61)
| Seq com com         (-;;/ - [60, 61] 60)
| If rvalue com com    ((IF -/ THEN -/ ELSE -) [0, 0, 61] 61)
| WHILE rvalue com     ((WHILE -/ DO -) [0, 61] 61)
```

type-synonym $gamma = vname \Rightarrow address * tag$

Unique implicitly performs boxing to variables. In other words, every variable behaves as a root reference to a memory cell.

type-synonym $tags = tag\text{-}kind\ list$

type-synonym $borrow\text{-}list = tag\ list$

type-synonym $heap = (val * borrow\text{-}list)\ list$

fun $kill :: tag \Rightarrow borrow\text{-}list \Rightarrow borrow\text{-}list$ **where**

```
kill t [] = [] |
kill t (x # xs) = (if t = x then [x] else
  case kill t xs of
    [] => [] |
    xs => x # xs)
```

The function $kill$ calculates references to be invalidated by the use of the given reference. The following two lemmas show that the used reference will be the “leaf” of the borrow tree.

lemma $[simp]: t \notin set\ ts \implies kill\ t\ ts = []$

$\langle proof \rangle \langle proof \rangle \langle proof \rangle \langle proof \rangle \langle proof \rangle$

lemma $t \in set\ ts \implies \exists ts'. kill\ t\ ts = ts' @ [t]$

$\langle proof \rangle$

fun $kill\text{-}heap :: (address * tag) \Rightarrow heap \Rightarrow heap$ **where**

```
kill-heap (a, t) H = (let (v, ts) = H ! a in H[a := (v, kill t ts)])
```

abbreviation *kill-all* :: (address * tag) list \Rightarrow heap \Rightarrow heap **where**
kill-all refs *H* == foldr *kill-heap* refs *H*

fun *writable* :: heap \Rightarrow (address * tag) \Rightarrow bool **where**
writable *H* (*p*, *t*) \longleftrightarrow *p* < length *H* \wedge *t* \in set (snd (*H* ! *p*))

definition *readable* **where** *readable* = *writable*

Functions *writable* :: (val \times nat list) list \Rightarrow nat \times nat \Rightarrow bool and *readable* :: (val \times nat list) list \Rightarrow nat \times nat \Rightarrow bool determine whether the given reference can be used to write to/read from it. The validity of references is determined by the existence in the current borrow tree. In Unique, we allow only unique references. Thus *readable* is equivalent to *writable*.

definition *allocated* :: heap \Rightarrow address \Rightarrow bool **where**
allocated *H* *a* \longleftrightarrow *a* < length *H*
 <proof><proof><proof><proof><proof><proof><proof>
end
theory *Exp*
 imports *Definitions*
begin

2 Semantics of Expressions

This section presents the big-step semantics of expressions.

inductive *place-sem* ::
 gamma \Rightarrow heap \Rightarrow place \Rightarrow (address * tag) list * val \Rightarrow bool
 ((-; - \vdash - \Downarrow_p -))
where
 Var: $\Gamma \ x = (a, t) \Longrightarrow \Gamma; H \vdash \text{Var } x \Downarrow_p ([], \text{Reference } a \ t) \mid$
 Deref: $\llbracket \Gamma; H \vdash p \Downarrow_p (\text{refs}, \text{Reference } a \ t); \text{allocated } H \ a \rrbracket \Longrightarrow$
 $\Gamma; H \vdash \text{Deref } p \Downarrow_p ((a, t) \# \text{refs}, \text{fst } (H \ ! \ a))$

The relation *place-sem* describes the semantics of places. $\Gamma; H \vdash p \Downarrow_p (\text{refs}, v)$ means that a place expression *p* evaluates to a value *v* under the environment Γ and *H*, where *refs* are the references used to retrieve the value (thus they need to be validated).

inductive *operand-sem* ::
 gamma \Rightarrow heap \Rightarrow operand \Rightarrow (address * tag) list * val \Rightarrow bool
 ((-; - \vdash - \Downarrow_{op} -))
where
 Place: $\Gamma; H \vdash p \Downarrow_p v \Longrightarrow \Gamma; H \vdash \text{Place } p \Downarrow_{op} v \mid$
 Constant: $\Gamma; H \vdash \text{Constant } v \Downarrow_{op} ([], v)$

inductive *rvalue-sem* ::
 gamma * tags * heap * rvalue \Rightarrow tags * heap * val \Rightarrow bool (**infix** \Downarrow 65)
where
 Use: $\llbracket \Gamma; H \vdash op \Downarrow_{op} (\text{refs}, v); \text{list-all } (\text{readable } H) \ \text{refs} \rrbracket$

$$\begin{aligned}
& \Rightarrow (\Gamma, T, H, \text{Use } op) \Downarrow (T, \text{kill-all refs } H, v) \mid \\
\text{Box: } & \llbracket \Gamma; H \vdash op \Downarrow_{op} (refs, v); p = \text{length } H; t = \text{length } T \rrbracket \\
& \Rightarrow (\Gamma, T, H, \text{Box } op) \Downarrow (T @ [\text{Unique}], H @ [(v, [t])], \text{Reference } p \ t) \mid \\
\text{Ref: } & \llbracket \Gamma; H \vdash p \Downarrow_p (refs, \text{Reference } a \ t); \text{list-all (readable } H) \ refs \rrbracket \\
& \Rightarrow (\Gamma, T, H, \text{Ref } p) \Downarrow (T, \text{kill-all refs } H, \text{Reference } a \ t) \mid \\
\text{Reborrow: } & \llbracket \Gamma; H \vdash p \Downarrow_p (refs, \text{Reference } a \ t); \text{list-all (writable } H) \ refs; \\
& \quad \text{writable } H \ (a, t); t' = \text{length } T; \\
& \quad H' = \text{kill-all } ((a, t) \# refs) \ H; H' ! a = (v, ts) \rrbracket \\
& \Rightarrow (\Gamma, T, H, \text{Reborrow } p) \Downarrow (T @ [\text{Unique}], H'[a := (v, ts @ [t'])], \\
& \quad \text{Reference } a \ t') \mid \\
\text{Plus: } & \llbracket \Gamma; H \vdash lhs \Downarrow_{op} (rl, \text{VInt } lhs'); \Gamma; H \vdash rhs \Downarrow_{op} (rr, \text{VInt } rhs'); \\
& \quad \text{list-all (readable } H) \ rl; \text{list-all (readable } H) \ rr \rrbracket \\
& \Rightarrow (\Gamma, T, H, \text{Plus } lhs \ rhs) \Downarrow (T, \text{kill-all } (rr @ rl) \ H, \text{VInt } (lhs' + rhs')) \mid \\
\text{Less: } & \llbracket \Gamma; H \vdash lhs \Downarrow_{op} (rl, \text{VInt } lhs'); \Gamma; H \vdash rhs \Downarrow_{op} (rr, \text{VInt } rhs'); \\
& \quad \text{list-all (readable } H) \ rl; \text{list-all (readable } H) \ rr \rrbracket \\
& \Rightarrow (\Gamma, T, H, \text{Less } lhs \ rhs) \Downarrow (T, \text{kill-all } (rr @ rl) \ H, \text{VBool } (lhs' < rhs')) \\
& \mid \\
\text{Not: } & \llbracket \Gamma; H \vdash op \Downarrow_{op} (refs, \text{VBool } v); \text{list-all (readable } H) \ refs \rrbracket \\
& \Rightarrow (\Gamma, T, H, \text{Not } op) \Downarrow (T, \text{kill-all refs } H, \text{VBool } (\neg v)) \mid \\
\text{And: } & \llbracket \Gamma; H \vdash lhs \Downarrow_{op} (rl, \text{VBool } lhs'); \Gamma; H \vdash rhs \Downarrow_{op} (rr, \text{VBool } rhs'); \\
& \quad \text{list-all (readable } H) \ rl; \text{list-all (readable } H) \ rr \rrbracket \\
& \Rightarrow (\Gamma, T, H, \text{And } lhs \ rhs) \Downarrow (T, \text{kill-all } (rr @ rl) \ H, \text{VBool } (lhs' \wedge rhs'))
\end{aligned}$$

Some TODO notes on the semantics of expressions:

- I don't get the semantics of *Ref* in MIR and how it should behave under the auto-boxing of variables.
- I'm not sure readable/writable checking is correct.

We present the intuition behind the selected rules. First, *Box* rule allocates a new slot at the end of heap, returning a reference pointing to the slot with a fresh tag.

$ \frac{\Gamma; H \vdash op \Downarrow_{op} (refs, v) \quad p = H \quad t = T }{(\Gamma, T, H, \text{Box } op) \Downarrow (T @ [\text{Unique}], H @ [(v, [t])], \text{Reference } p \ t)} $ <p style="text-align: center; margin: 0;">Box</p>

Next, *USE* and *REF* rules allow us to read the content through a place (or give a constant). The validity of the access is checked by *readable* :: (*val* × *nat list*) *list* ⇒ *nat* × *nat* ⇒ *bool*. Moreover, they invalidate all descendant references to establish the uniqueness.

$$\begin{array}{c}
\frac{\Gamma; H \vdash op \Downarrow_{op} (refs, v) \quad list-all (readable H) refs}{(\Gamma, T, H, Use op) \Downarrow (T, kill-all refs H, v)} \text{ USE} \\
\frac{\Gamma; H \vdash p \Downarrow_p (refs, Reference a t) \quad list-all (readable H) refs}{(\Gamma, T, H, Ref p) \Downarrow (T, kill-all refs H, Reference a t)} \text{ REF}
\end{array}$$

Last but not least, REBORROW rule creates a new reference pointing to the same object but with a fresh tag. The newly created reference is writable. Thus the original reference must be valid for writes. Reborrow is considered as the use of the original reference and hence it invalidates former children of the reference. As a result, the reborrow tree will have the original reference and the reborrowing reference as the last two element.

$$\begin{array}{c}
\text{REBORROW RULE:} \\
\Gamma; H \vdash p \Downarrow_p (refs, Reference a t) \\
list-all (writable H) refs \quad writable H (a, t) \\
t' = |T| \quad H' = kill-all ((a, t) \cdot refs) H \quad H'_{[a]} = (v, ts) \\
\hline
(\Gamma, T, H, Reborrow p) \Downarrow (T @ [Unique], H'[a := (v, ts @ [t'])], Reference a t')
\end{array}$$

We can prove that the semantics of expressions is deterministic.

lemma *place-sem-det*: $\Gamma; H \vdash p \Downarrow_p (refs, v) \implies \Gamma; H \vdash p \Downarrow_p (refs', v') \implies (refs', v') = (refs, v)$

<proof>

lemmas *place-sem-det'* = *place-sem-det*[*split-format*(*complete*)]

lemma *operand-sem-det*: $\Gamma; H \vdash op \Downarrow_{op} (refs, v) \implies \Gamma; H \vdash op \Downarrow_{op} (refs', v') \implies (refs', v') = (refs, v)$

<proof>

lemmas *operand-sem-det'* = *operand-sem-det*[*split-format*(*complete*)]

lemma *rvalue-sem-det*: $(\Gamma, T, H, rv) \Downarrow (T', H', v') \implies (\Gamma, T, H, rv) \Downarrow (T'', H'', v'') \implies (T'', H'', v'') = (T', H', v')$

<proof>

The following lemmas are sanity checks of the semantics. We must be able to write through the references retrieved by BOX and REBORROW

lemma *box--writable*: $(\Gamma, T, H, Box e) \Downarrow (T', H', Reference a t) \implies writable H' (a, t)$

<proof>

lemma *reborrow--writable*: $(\Gamma, T, H, Reborrow p) \Downarrow (T', H', Reference a t) \implies writable H' (a, t)$

$\langle proof \rangle$

end

$\langle proof \rangle \langle proof \rangle$

theory *Unique*

imports *Main Definitions Exp Star*

begin

3 Semantics of Commands

This section describes the small-step semantics of commands. The configuration of an execution consists of:

- the variable environment Γ (of type *gamma*);
- the heap H (of type *heap*) which holds the actual data and the reborrow trees for each address; and
- the command to be executed c (of type *com*).

type-synonym *config* = *tags* * *heap* * *com*

inductive *com-sem* :: *gamma* \Rightarrow *config* \Rightarrow *config* \Rightarrow *bool* ((\vdash - \rightarrow -))

where

Assign: $\llbracket \Gamma; H \vdash p \Downarrow_p (refs, \text{Reference } a \ t); \text{list-all } (writable \ H) \ refs; \text{writable } H(a, \ t);$

$H' = \text{kill-all refs } H; (\Gamma, T, H', rv) \Downarrow (T', H'', v); H'' ! a = (-, ts) \rrbracket$

$\implies \Gamma \vdash (T, H, p ::= rv) \rightarrow (T', H''[a := (v, \text{kill } t \ ts)], \text{Skip}) \mid$

SeqL: $\Gamma \vdash (T, H, \text{Skip};; c) \rightarrow (T, H, c) \mid$

SeqR: $\Gamma \vdash (T, H, c1) \rightarrow (T', H', c') \implies \Gamma \vdash (T, H, c1;; c2) \rightarrow (T', H', c';; c2) \mid$

IfTrue: $(\Gamma, T, H, b) \Downarrow (T', H', \text{VBool True})$

$\implies \Gamma \vdash (T, H, \text{IF } b \text{ THEN } c1 \text{ ELSE } c2) \rightarrow (T', H', c1) \mid$

IfFalse: $(\Gamma, T, H, b) \Downarrow (T', H', \text{VBool False})$

$\implies \Gamma \vdash (T, H, \text{IF } b \text{ THEN } c1 \text{ ELSE } c2) \rightarrow (T', H', c2) \mid$

While: $\Gamma \vdash (T, H, \text{WHILE } b \text{ DO } c) \rightarrow (T, H, \text{IF } b \text{ THEN } (c;; \text{WHILE } b \text{ DO } c) \text{ ELSE Skip})$

abbreviation *com-sem-steps* :: *gamma* \Rightarrow *config* \Rightarrow *config* \Rightarrow *bool* ((\vdash - \rightarrow^* -))

where

$\Gamma \vdash \text{cfg} \rightarrow^* \text{cfg}' == \text{star } (\text{com-sem } \Gamma) \ \text{cfg} \ \text{cfg}'$

Figure 1 shows the assignment rules. Other commands are standard.

The ASSIGN rule assigns a value to the the location. To assign through a reference, the reference must be valid for writes. Moreover, the write is considered as a use of the reference; it will invalidate the child references.

The following lemmas show that the execution of the commands is deterministic.

$$\boxed{
\begin{array}{c}
\Gamma; H \vdash p \Downarrow_p (\text{refs}, \text{Reference } a \ t) \quad \text{list-all (writable } H) \text{ refs} \\
\text{writable } H \ (a, t) \quad H' = \text{kill-all refs } H \\
\hline
(\Gamma, T, H', rv) \Downarrow (T', H'', v) \quad H''_{[a]} = (uu, ts) \\
\hline
\Gamma \vdash (T, H, p ::= rv) \rightarrow (T', H''[a := (v, \text{kill } t \ ts)], \text{Skip}) \\
\text{ASSIGN}
\end{array}
}$$

Figure 1: The assignment rule

definition *final* :: *config* \Rightarrow *bool* **where**
final *cfg* \longleftrightarrow (case *cfg* of $(-, -, \text{Skip}) \Rightarrow \text{True} \mid - \Rightarrow \text{False}$)

definition *stuck* :: *gamma* \Rightarrow *config* \Rightarrow *bool* **where**
stuck Γ *cfg* \longleftrightarrow (case *cfg* of
 $(-, -, \text{Skip}) \Rightarrow \text{False} \mid$
 $- \Rightarrow \neg(\exists \text{cfg}'. (\Gamma \vdash \text{cfg} \rightarrow \text{cfg}'))$)

lemma *skip-final-noteq[simp]*: $\Gamma \vdash (T, H, c) \rightarrow (T, H', c') \Longrightarrow c \neq \text{Skip}$
 $\langle \text{proof} \rangle$

lemma *skip-final[simp]*: $\Gamma \vdash (T, H, \text{Skip}) \rightarrow (T', H', c) \Longrightarrow \text{False}$
 $\langle \text{proof} \rangle$

lemma *com-sem-det*: $\Gamma \vdash \text{cfg} \rightarrow \text{cfg}' \Longrightarrow \Gamma \vdash \text{cfg} \rightarrow \text{cfg}'' \Longrightarrow \text{cfg}'' = \text{cfg}'$
 $\langle \text{proof} \rangle$

We show the transitivity of *com-sem-steps*.

lemma *com-seql-trans*:
 $\Gamma \vdash (T, H, c1) \rightarrow^* (T', H', c1') \Longrightarrow \Gamma \vdash (T, H, c1;; c2) \rightarrow^* (T', H', c1';; c2)$
 $\langle \text{proof} \rangle$

4 Code examples

We need to assign a pre-allocated location to each variable to run a program. Currently we initialize those locations with zeros, but they will be uninitialized when we implement uninitialized slots.

abbreviation $\Gamma_0 == \lambda-. \text{undefined}$
fun *preallocate'* :: *vname list* \Rightarrow *gamma* * *tags* * *heap* \Rightarrow *gamma* * *tags* * *heap*
where
preallocate' [] *ret* = *ret* |
preallocate' (*x* # *xs*) (Γ, T, H) =
 (let *t* = *length* *T* in
 let $\Gamma' = \Gamma(x := (t, t))$ in
 let $T' = T @ [\text{Unique}]$ in


```

    let  $H' = H @ [(VInt\ 0, [t])]$  in
    preallocate'  $xs\ (\Gamma', T', H')$ 
fun preallocate ::  $vname\ list \Rightarrow gamma * tags * heap$  where
    preallocate  $xs = preallocate'\ xs\ (\Gamma_0, [], [])$ 

value preallocate ["x", "y"]
value map (fst (preallocate ["x", "y"])) ["x", "y"]

fun prealloc-com-sem ::  $vname\ list \Rightarrow com \Rightarrow config \Rightarrow bool$ 
    ((-; -  $\rightarrow^*$  -)) where
    ( $xs; c \rightarrow^* cfg$ ) =
    (let ( $\Gamma, T, H$ ) = preallocate  $xs$  in ( $\Gamma \vdash (T, H, c) \rightarrow^* cfg$ ))

```

Let Isabelle run Unique programs by generating code for the semantics.

```

code-pred [show-modes] place-sem <proof>
code-pred [show-modes] operand-sem <proof>
code-pred [show-modes] rvalue-sem <proof>
code-pred [show-modes] com-sem <proof>

```

4.1 Invalidating a reference

Consider the following Rust program.

```

1 let mut root = Box::new(42);
2 let mut px = &mut *root; // reborrowing from root
3 *px = 100;
4 let mut py = &mut *root; // another reborrow. invalidates px
5 *py = 200;
6 // *px = 300 // this write is invalid.

```

In line 1, we create a box that contains 42 in the heap. In the following two lines, we reborrow from it and use the reference to write. The interesting part is line 4. In this line, we create a new reference from `root`. As this reborrow asserts that `py` is the unique reference to the box, `px` must be invalidated at this point. Therefore, if we remove the comment in line 6, the program will perform an invalid write (thus rustc will reject the program). Let's execute the program with Unique. The following command is the translation of the program above without the last commented line.

```

definition XY ::  $com$  where
  XY =
    (Var "root") ::= (Use  $\circ$  Constant  $\circ$  VInt) 42;;
    (Var "px") ::= (Reborrow  $\circ$  Var) "root";;
    ((Deref  $\circ$  Var) "px") ::= (Use  $\circ$  Constant  $\circ$  VInt) 100;;
    (Var "py") ::= (Reborrow  $\circ$  Var) "root";;
    ((Deref  $\circ$  Var) "py") ::= (Use  $\circ$  Constant  $\circ$  VInt) 200

```

We can let Isabelle compute the program.

value *preallocate* ["root", "px", "py"]
abbreviation $\Gamma == \Gamma_0("root" := (0, 0), "px" := (1, 1), "py" := (2, 2))$
abbreviation $T == [Unique, Unique, Unique]$
abbreviation $H == [(VInt\ 0, [0]), (VInt\ 0, [1]), (VInt\ 0, [2])]$
lemma *preallocate* ["root", "px", "py"] = $(\Gamma, T, H) \langle proof \rangle$

values $\{(T', H') \mid$
 $T' H' c'. \Gamma \vdash (T, H, XY) \rightarrow^* (T', H', c')\}$

The following shows the tags and the heap at the end of execution.

abbreviation $T_{XY} :: tags$ **where**
 $T_{XY} == [Unique, Unique, Unique, Unique, Unique]$
abbreviation $H_{XY} :: heap$ **where**
 $H_{XY} == [(VInt\ 200, [0, 4]), (Reference\ 0\ 3, [1]), (Reference\ 0\ 4, [2])]$

We can also prove that the program result in the state shown above in theory, but it's really tedious (why can't Isabelle prove it by computing the execution?). The actual proof is left to the reader.

lemma *final-xy*: $\Gamma \vdash (T, H, XY) \rightarrow^* (T_{XY}, H_{XY}, Skip)$
sorry

We show that accessing through **px** after the program will stuck.

lemma *intermediate-xyx*: $\Gamma \vdash (T, H, XY;; ((Deref \circ Var) "px") ::= (Use \circ Constant \circ VInt) 300)$
 $\rightarrow^* (T_{XY}, H_{XY}, ((Deref \circ Var) "px") ::= (Use \circ Constant \circ VInt) 300)$
 $\langle proof \rangle$

lemma *stuck-xyx*: *stuck* Γ
 $(T_{XY}, H_{XY}, ((Deref \circ Var) "px") ::= (Use \circ Constant \circ VInt) 300)$
 $\langle proof \rangle$

lemma $\exists\ cfg. (\Gamma \vdash (T, H, XY;; ((Deref \circ Var) "px") ::= (Use \circ Constant \circ VInt) 300) \rightarrow^* cfg)$
 $\wedge stuck\ \Gamma\ cfg$
 $\langle proof \rangle$

4.2 Swap

The following program swaps the content the given two references pointing to.

fun *swap* :: *place* \Rightarrow *place* \Rightarrow *com* **where**
 $swap\ x\ y =$
 $(Var\ "reborrow-x") ::= Reborrow\ x;;$
 $(Var\ "reborrow-y") ::= Reborrow\ y;;$
 $(Var\ "tmp") ::= (Use \circ Place \circ Deref \circ Deref \circ Var) "reborrow-x";;$
 $((Deref \circ Var) "reborrow-x") ::= (Use \circ Place \circ Deref \circ Deref \circ Var)$
 $"reborrow-y";;$
 $((Deref \circ Var) "reborrow-y") ::= (Use \circ Place \circ Deref \circ Deref \circ Var) "tmp"$

We can see the content swapped during the execution by running it on Isabelle.

values $\{H \mid T \ H \ c.$

$\Gamma_0("reborrow-x" := (0, 0), "reborrow-y" := (1, 1), "tmp" := (2, 2), "a" := (3, 3), "b" := (4, 4)) \vdash$

$([Unique, Unique, Unique],$

$[(VInt\ 0, [0]), (VInt\ 0, [1]), (VInt\ 0, [2]), (VInt\ 10000, [3]), (VInt\ 20000, [4])],$

$swap\ (Var\ "a")\ (Var\ "b")) \rightarrow^* (T, H, c)\}$

Proving the correctness of *swap* would need a Hoare Logic. The road continues...

end

References

- [1] R. Jung, H. Dang, J. Kang, and D. Dreyer. Stacked borrows: an aliasing model for rust. *Proc. ACM Program. Lang.*, 4(POPL):41:1–41:32, 2020.