Assignment 05 - STAT 689

Philip Anderson: panders2@tamu.edu February 7, 2018

```
# import third-party modules
library("mgcv")
Import our data
fossil <- read.csv("C:/Users/Philip/Schools/TAMU/STAT 689/homework/semiparametric-regression/misc/fossi
names(fossil) <- tolower(names(fossil))</pre>
summary(fossil)
##
         age
                     strontium.ratio
## Min. : 91.79 Min.
                             :0.7072
## 1st Qu.:103.62 1st Qu.:0.7073
## Median :109.37 Median :0.7074
## Mean
          :108.62 Mean
                            :0.7074
                     3rd Qu.:0.7074
## 3rd Qu.:115.41
## Max. :123.00
                     Max.
                             :0.7075
Fit GAM's with 4, 8, and 23 knots
fossil_mod <- function(knots=8) {</pre>
  mod <- mgcv::gam(strontium.ratio ~ s(age, k=knots, bs="cr")</pre>
                    , data=fossil )
 return(mod)
gam4 <- fossil_mod(knots=4)</pre>
gam8 <- fossil_mod(knots=8)</pre>
gam23 <- fossil_mod(knots=23)</pre>
```

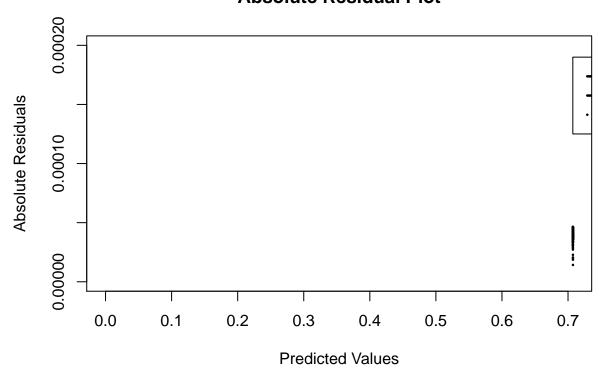
Question 1

For each of the three models, plot the absolute fitted residuals against the predicted values.

```
plot(1, type="n"
    , xlim=c(min(gam23$residuals), max(gam4$fitted.values))
    , ylim=c(0, 0.00020)
    , xlab="Predicted Values"
    , ylab="Absolute Residuals"
    , main="Absolute Residual Plot"
    )

line_plotter <- function(gam_obj, lty=1, knots=8){
    age_ord <- order(fossil$age)
    x <- fitted(gam_obj)[age_ord]
    y <- abs(gam_obj$residuals)[age_ord]
    gam_obj_abs <- mgcv::gam(y ~ s(x, k=knots, bs="cr"))
    lines(x, fitted(gam_obj_abs), lwd=2.5, lty=lty)
}</pre>
```

Absolute Residual Plot



Question 2

Give the ratio of the maximum fitted absolute residual to the minimum absolute fitted residual.

```
ratio_finder <- function(mod_obj, precision=2) {
    # find the ratio of the max value of abs(resid) to the min value
    ratio <- round(max(abs(mod_obj$residuals)) / min(abs(mod_obj$residuals)), precision)
    return(ratio)
}

pasteO("GAM with 4 knots ratio is: ", ratio_finder(mod_obj=gam4))</pre>
```

[1] "GAM with 4 knots ratio is: 89.82"

```
paste0("GAM with 8 knots ratio is: ", ratio_finder(mod_obj=gam8))

## [1] "GAM with 8 knots ratio is: 771.81"

paste0("GAM with 23 knots ratio is: ", ratio_finder(mod_obj=gam23))

## [1] "GAM with 23 knots ratio is: 320.81"
```

Question 3

All three of the ratios dramatically exceed our rule of thumb value of 3.

```
## K Ratio
## 1 4 89.82
## 2 8 771.81
## 3 23 320.81
```

Question 4

The failure of our results to fall within the bounds of the residual ratio heuristic indicates that our model fails to capture the non-constant variance present in our single predictor variable. It indicates that our model is widely missing in making at least one prediction, which is the consequence of heteroscedacticity. I have included more extensive residual plots in the Appendix of this document, which more thoroughly demonstrate the problem.

Question 5

Give a verbal description of what K is.

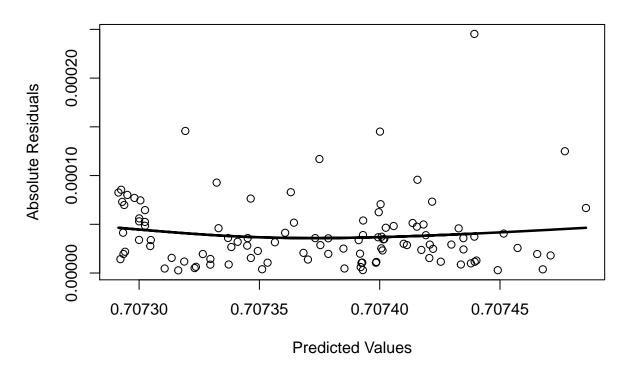
K is the number of basis dimensions, or knots, with which our smoothed regression line will be fit. These are the points at which our fitted line will be permitted to deviate from linearity. It is selected through identifying the unique quantiles of the x variable, with a forumula such as:

$$knot\ location = \frac{k}{K-1}$$

Appendix

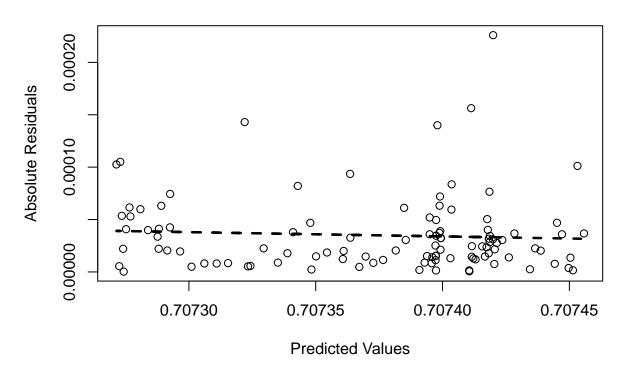
Question 1 expounded

GAM with 4 Knots Hetereoscedacticity Eval.



hs_plotter(gam_obj=gam8, knots=8, title_prompt="GAM with 8 Knots Hetereoscedacticity Eval.", lty=2)

GAM with 8 Knots Hetereoscedacticity Eval.



hs_plotter(gam_obj=gam23, knots=23, title_prompt="GAM with 23 Knots Hetereoscedacticity Eval.", lty=3)

GAM with 23 Knots Hetereoscedacticity Eval.

