# Assignment\_06 - STAT 689

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```
# import third-party modules
library("HRW")
library("tidyverse")
library("mgcv")
library("nlme")
```

Read in our data

```
fram <- read.csv("/Users/panders2/Documents/schools/tamu/stat_689/homework/semiparametric-regression/hw
names(fram) <- tolower(names(fram))
# check that we have 1615 observations
dim(fram)</pre>
```

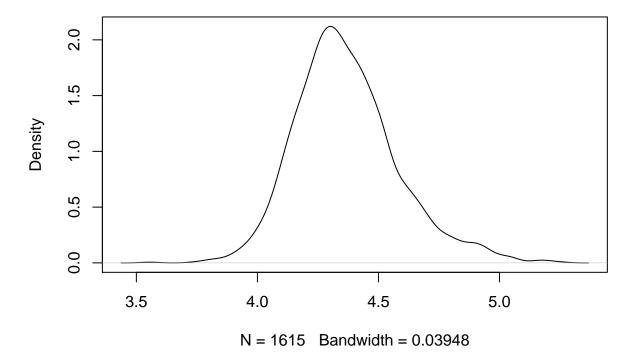
```
## [1] 1615 10
```

Create new variables for the systolic blood pressure readings and the two cholesterol measurements.

```
# systolic blood pressure first
fram$lsbp <- log(((fram$sbp21 + fram$sbp22 + fram$sbp31 + fram$sbp32) / 4) - 50)
# cholesterol measurements second
fram$lcholest <- log((fram$cholest2 + fram$cholest3) / 2)</pre>
```

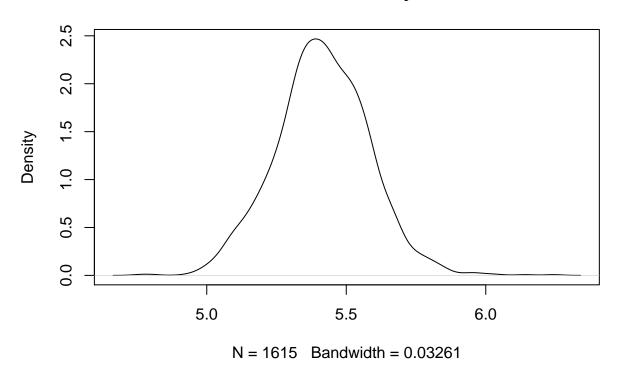
Im guessing that we conducted the transformations to take the variables to normality. Checking that here. plot(density(fram\$lsbp), main="Blood Pressure Density Plot")

## **Blood Pressure Density Plot**





### **Cholesterol Density Plot**



Keep only the variables that we will be working with directly and make sure everything seems reasonable.

```
fram2 <- fram %>%
  dplyr::select(chd, age, smoker, lsbp, lcholest)
head(fram2)
```

```
##
     chd age smoker
                         1sbp 1cholest
## 1
          56
                   0 4.317488 5.654242
          38
                   1 4.241327 5.451038
          54
                   1 4.347047 5.654242
## 3
       0
## 4
          42
                   1 4.185860 5.541264
       0
## 5
       0
          47
                   1 4.454347 5.583496
## 6
          43
                   1 4.269697 5.298317
```

# Question 1

Fit a multiple linear regression of LSBP on lcholest and smoker via "lm" function. Produce estimates, standard errors, and p-values.

##

```
## Call:
## lm(formula = lsbp ~ smoker + lcholest, data = fram2)
##
## Residuals:
##
                  1Q
                       Median
                                    3Q
  -0.79148 -0.14009 -0.02043
                              0.10915
##
                                        0.93289
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept)
               3.55569
                           0.17029
                                    20.880 < 2e-16 ***
## smoker
               -0.03796
                           0.01251
                                    -3.034 0.00246 **
                0.15540
                           0.03140
                                     4.949 8.22e-07 ***
## lcholest
## ---
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.2107 on 1612 degrees of freedom
## Multiple R-squared: 0.02036,
                                    Adjusted R-squared: 0.01915
## F-statistic: 16.75 on 2 and 1612 DF, p-value: 6.299e-08
```

### Question 2

Conduct web research on whether smokers have higher or lower blood pressure on average compared with non-smokers.

WebMD indicates that individuals who smoke tend to have higher blood pressure than those who do not. This is not consistent with my findings from Question 1, which indicate that participants who smoke have lower blood pressure than those who do not, conditional on our transformed cholesterol variable. There is nothing in the documentation to indicate that smoker is not encoded with '1' as the positive class. This result is suspicious, and suggests that we need to check our data or revisit our model specification.

## Question 3

The model produces the expectation of LSBP given smoking status conditional on cholesterol.

# Question 4

Recreate the same model as in Question 1, but also include an interaction amongst the independent variables.

```
## -0.79151 -0.14039 -0.02046 0.10916 0.93280
##
## Coefficients:
##
                  Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                   3.55075
                             0.33525 10.591
                  -0.03130
                             0.38907 -0.080
                                              0.9359
## smoker
                   0.15632
                                      2.525
## lcholest
                             0.06191
                                               0.0117 *
## smoker:lcholest -0.00123
                             0.07184 -0.017
                                               0.9863
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.2108 on 1611 degrees of freedom
## Multiple R-squared: 0.02036,
                                  Adjusted R-squared: 0.01854
## F-statistic: 11.16 on 3 and 1611 DF, p-value: 2.993e-07
```

The smoking indicator is still negatively associated with our blood pressure variable, but is no longer significant in the presence of the interaction term.

#### Question 5

Run a semiparametric ANCOVA with mgcv, the semiparametric version of an ANCOVA without an interaction.

```
##
## Family: gaussian
## Link function: identity
##
## Formula:
## lsbp ~ factor(smoker) + s(lcholest, k = 23, bs = "cr")
## Parametric coefficients:
##
                  Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                   4.39713
                             0.01100 399.735 < 2e-16 ***
## factor(smoker)1 -0.03799
                              0.01251 -3.036 0.00244 **
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Approximate significance of smooth terms:
                               F p-value
                edf Ref.df
## s(lcholest) 1.064 1.126 22.27 1.73e-06 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## R-sq.(adj) = 0.0192 Deviance explained = 2.04\%
## -REML = -214.85 Scale est. = 0.044402 n = 1615
```

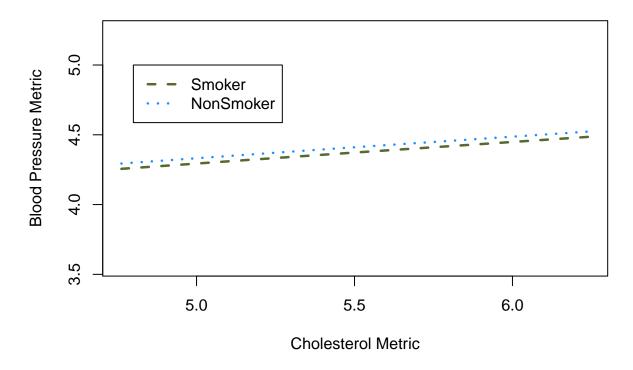
### Question 6

For the data in part 5, display a plot of the two lines, but without the data

, col=c(lineColors[1], lineColors[2])

```
# first, generate the data required for plotting
ng <- 1000
# x var
x_var <- seq(from=min(fram2$lcholest)</pre>
              , to=max(fram2$lcholest)
              , len=ng
# y prediction variables
f_hat_smoker <- predict(semi_mod</pre>
                         , newdata=data.frame(
                          smoker=rep('1', ng)
                          , lcholest=x_var
                         , se.fit=TRUE
f_hat_nosmoke <- predict(semi_mod</pre>
                          , newdata=data.frame(
                             smoker=rep('0', ng)
                             , lcholest=x_var
                            se.fit=TRUE
lineColors <- c("darkolivegreen", "dodgerblue")</pre>
plot(fram2$lcholest, fram2$lsbp, type="n"
     , xlab="Cholesterol Metric"
     , ylab = "Blood Pressure Metric"
     , main="Blood Presure by Cholesterol ANCOVA comparison"
lines(x_var, f_hat_smoker$fit, lty=2, lwd=2.5, col=lineColors[1])
lines(x_var, f_hat_nosmoke$fit, lty=3, lwd=2.5, col=lineColors[2])
legend(4.8, 5
       , c("Smoker", "NonSmoker")
       , lty=c(2,3)
       , lwd=rep(2.5, 2)
```

# **Blood Presure by Cholesterol ANCOVA comparison**



### Question 7

Display a plot of the two lines, but split into two separate graphics, and with pointwise 95% confidence intervals.

```
plot_with_bands <- function(mod_pred, range_var, color_vec, color_idx, lty, title="NULL") {</pre>
  # create a regression fit with 95% pointwise confidence intervals for the line
  upper <- mod_pred$fit + (1.96 * mod_pred$se.fit)</pre>
  lower <- mod_pred$fit - (1.96 * mod_pred$se.fit)</pre>
  fit <- mod_pred$fit
  plot(fram2$lcholest, fram2$lsbp, type="n"
       , xlab="Cholesterol Metric"
       , ylab = "Blood Pressure Metric"
       , main=title
         )
  lines(range_var, fit, lty=2, lwd=2.5, col=color_vec[color_idx])
  polygon(x=c(range_var,rev(range_var))
        , y=c(upper
        , rev(lower))
        , col="gray"
          border=NA
          density=75
```

# 

# Blood Pressure Metric 5. 4.0 4.5 5.0

5.0

5.5

Cholesterol Metric

6.0

Non-Smoker

```
par(mfrow=c(1,1)) # reset
```

### Question 8

Run the semiparametric version of ANCOVA but with an interaction.

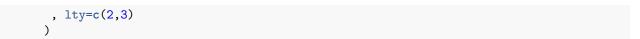
```
##
                             Estimate Std. Error t value Pr(>|t|)
                            0.3664545 0.0218837 16.746
## (Intercept)
                                                           <2e-16 ***
                                                           0.932
## factor(smoker)1
                           -0.0330055 0.3891394 -0.085
## lcholest
                            0.7444406 0.0044560 167.063
                                                          <2e-16 ***
## factor(smoker)1:lcholest -0.0009226  0.0718517  -0.013
                                                           0.990
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Approximate significance of smooth terms:
##
                edf Ref.df
                               F p-value
## s(lcholest) 1.015 1.091 94.01 <2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Rank: 25/26
## R-sq.(adj) = 0.0186
                         Deviance explained = 2.05%
## GCV = 0.044542 Scale est. = 0.044429 n = 1615
```

From the above results, it does not appear that there is any sort of interaction present between *smoker* and *lcholest*. The estimate for this term is negligibly small, and the p-value is very large, indicating a lack of significance.

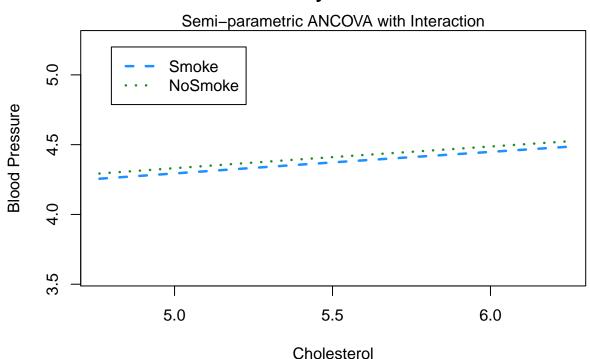
### Question 9

Display the fits of the above regressions, but without the data points.

```
x_vec <- seq(from=min(fram2$lcholest), to=max(fram2$lcholest), len=ng)
fHat_smoke <- predict(semi_mod2, newdata=data.frame(</pre>
                        lcholest=x_vec
                        , smoker=rep('1', ng)
fHat_nosmoke <- predict(semi_mod2, newdata=data.frame(</pre>
                        lcholest=x_vec
                        , smoker=rep('0', ng)
                         )
                       )
plot(fram2$lcholest, fram2$lsbp, type='n'
     , xlab="Cholesterol"
     , ylab="Blood Pressure"
      main="Cholesterol by Blood Pressure"
mtext("Semi-parametric ANCOVA with Interaction")
col_vec <- c("dodgerblue", "forestgreen")</pre>
lines(x_vec, fHat_smoke, col=col_vec[1], lwd=2.5, lty=2)
lines(x_vec, fHat_nosmoke, col=col_vec[2], lwd=2.5, lty=3)
legend(4.8, 5.2, c("Smoke", "NoSmoke")
       , col=col vec
       , lwd=rep(2.5, 2)
```



### **Cholesterol by Blood Pressure**



# Question 10

What does the interaction mean in the case when the factors are binary?

When we have a binary factor for our ANCOVA model, this indicates that the interaction term's coefficient is reflecting what happens to our outcome variable for that factor's non-reference class only. In this case, we are seeing the results of smoker = 1 interacting with lcholest.

# Question 11

Run an analysis of whether our two regression lines are significantly different.

```
# First, fit the null model - this is run on both the smokers and non-smokers
contrast_mod1 <- mgcv::gam(lsbp ~ s(lcholest), data=fram2)

# indicator of the smoke varible taking positive class
smoke_ind <- as.numeric(fram2$smoker==1)
# now, fit the alternative model
contrast_mod2 <- mgcv::gam(lsbp ~ s(lcholest, smoke_ind), data=fram2)

# run the final test
anova(contrast_mod1, contrast_mod2, test="F")</pre>
```

## Analysis of Deviance Table

```
##
## Model 1: lsbp ~ s(lcholest)
## Model 2: lsbp ~ s(lcholest, smoke_ind)
## Resid. Df Resid. Dev Df Deviance F Pr(>F)
## 1 1613 71.988
## 2 1612 71.579 1 0.40861 9.2021 0.002456 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

It appears that there is a significant difference between the two fits, for smoker and non-smoker.

### Question 12

Ignore the smokers, and run native code using lime to fit LSBP vs. age.

```
fram_ns <- fram2[which(fram2$smoker==0), ]
x <- fram_ns$age
y <- fram_ns$lsbp

numIntKnots <- 23
intKnots <- quantile(unique(x), seq(0, 1, length=numIntKnots+2))[-c(1, numIntKnots+2)]
a <- 1.01 * min(x) - 0.01*max(x)
b <- 1.01 * max(x) - 0.01*min(x)
Z <- HRW::ZOSull(x, range.x=c(a, b), intKnots=intKnots)

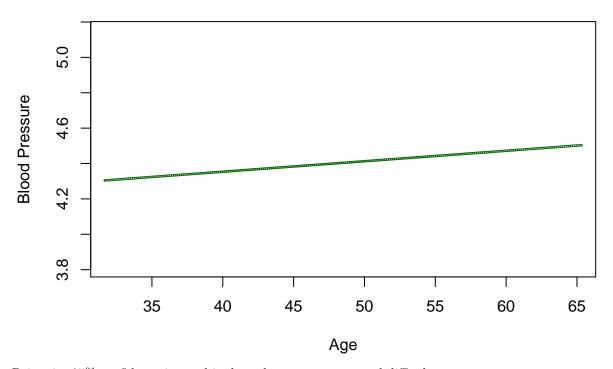
dummyID <- factor(rep(1, length(x)))

# prep is finally over - run the model
mm_fit <- nlme::lme(y ~ x, random=list(dummyID=pdIdent(~ -1 + Z)))</pre>
```

### Question 13

Display the fit without data points. Also provide a confidence band.

# **Blood Pressure by Age Mixed Model Fit**



Pointwise 95% confidence interval is there, but very narrow and difficult to see.

# Question 14

Is the fit of our mixed model statistically significant?

```
anova(mm_fit)
## numDF denDF F-value p-value
```

```
## (Intercept) 1 365 151345.51 <.0001
## x 1 365 22.13 <.0001
```

The F-test indicates that the fit of our model is significant.

### Question 15

Test whether the fit is linear or quadratic vs. the need to do a semiparametric fit.

```
mm_fit2 <- nlme::lme(y ~ x + x**2, random=list(dummyID=pdIdent(~ -1+Z)))</pre>
summary(mm_fit2)
## Linear mixed-effects model fit by REML
   Data: NULL
##
          AIC
                    BIC
                          logLik
##
     -56.9505 -41.35091 32.47525
##
## Random effects:
   Formula: ~-1 + Z | dummyID
   Structure: Multiple of an Identity
##
                     Z1
                                                Z3
##
                                  Z2
## StdDev: 4.758371e-07 4.758371e-07 4.758371e-07 4.758371e-07 4.758371e-07
                     Z6
                                  Z7
                                                Z8
## StdDev: 4.758371e-07 4.758371e-07 4.758371e-07 4.758371e-07 4.758371e-07
##
                    Z11
                                  Z12
                                               Z13
                                                            Z14
## StdDev: 4.758371e-07 4.758371e-07 4.758371e-07 4.758371e-07 4.758371e-07
                    Z16
                                 Z17
                                               Z18
                                                            Z19
## StdDev: 4.758371e-07 4.758371e-07 4.758371e-07 4.758371e-07 4.758371e-07
##
                    Z21
                                 Z22
                                               Z23
                                                            Z24
## StdDev: 4.758371e-07 4.758371e-07 4.758371e-07 4.758371e-07 4.758371e-07
           Residual
## StdDev: 0.216513
##
## Fixed effects: y \sim x + x^2
                  Value Std.Error DF t-value p-value
## (Intercept) 4.116889 0.06056931 365 67.96989
               0.005920 0.00125849 365 4.70377
## x
  Correlation:
##
     (Intr)
## x - 0.982
##
## Standardized Within-Group Residuals:
           Min
                        Q1
                                   Med
                                                 Q3
                                                            Max
## -2.33683136 -0.63763354 -0.09383609 0.52774344 3.04425398
## Number of Observations: 367
## Number of Groups: 1
```