

S-Parameter Simulation with ADS

1) Objective:

To setup and execute S-parameter simulation, to display simulation data, and to use SNP files in ADS

2) Theory:

The abbreviation (S) has been derived from the word scattering. The scattering matrix provides a complete description of the network as seen at its (N) ports. The scattering matrix relates the voltage waves incident on the ports to those reflected from the ports.

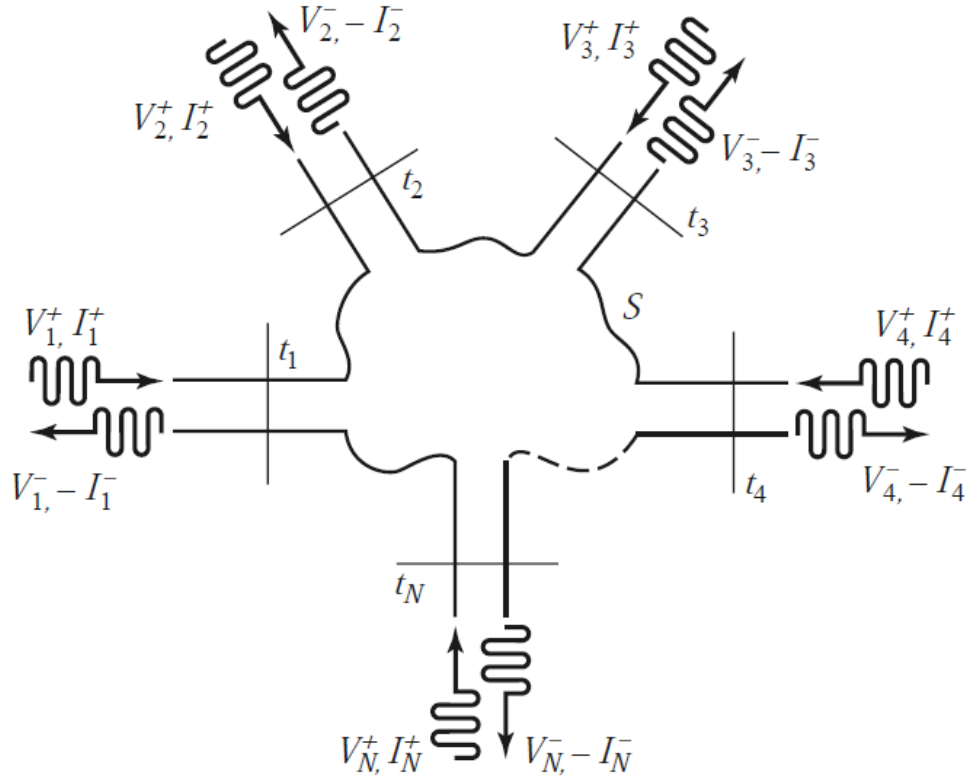


Figure 1: An N-port Microwave Network

Consider the N-port network shown in figure 1, where the voltages with positive superscripts denote the amplitude of the voltage wave incident on a port, and voltages with negative superscripts represent the amplitude of the voltage wave reflected from a port. The scattering matrix, or S-matrix, is defined in relation to these incident and reflected voltage waves as:

$$[V^-] = [S][V^+]$$

The above equation can be expanded to give the following expression:

$$\begin{bmatrix} V_1^- \\ \vdots \\ V_N^- \end{bmatrix} = \begin{bmatrix} S_{11} & \cdots & S_{1N} \\ \vdots & \ddots & \vdots \\ S_{N1} & \cdots & S_{NN} \end{bmatrix} \begin{bmatrix} V_1^+ \\ \vdots \\ V_N^+ \end{bmatrix}$$

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A specific element of the scattering matrix can be determined as:

$$S_{ij} = \left. \frac{V_i^-}{V_j^+} \right|_{V_k^+ = 0 \text{ for } k \neq j}$$

The value (S_{ij}) is found by driving port (j) with an incident wave of voltage (V_j^+) and measuring the reflected wave amplitude (V_i^-) coming out of port (i). The incident waves on all ports except the j^{th} port are set to zero, which means that all ports should be terminated in matched loads to avoid reflections.

(S_{ii}) is the reflection coefficient seen looking into port (i) when all other ports are terminated in matched loads.
(S_{ij}) is the transmission coefficient from port (j) to port (i) when all other ports are terminated in matched loads.

The total voltage and current on a transmission line in terms of the incident and reflected voltage wave amplitudes are given by:

$$V = V_0^+ + V_0^-$$

$$I = \frac{1}{Z_0}(V_0^+ - V_0^-)$$

In the above equation, Z_0 is the characteristic impedance of the line. The incident and reflected voltage wave amplitudes in terms of the total voltage and current are given by:

$$V_0^+ = \frac{V + Z_0 I}{2}$$

$$V_0^- = \frac{V - Z_0 I}{2}$$

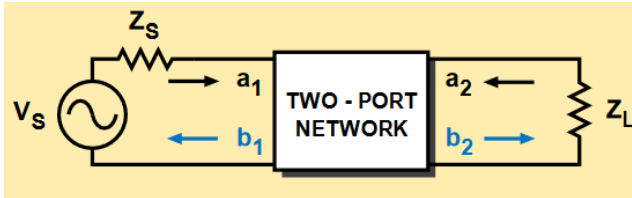


Figure 2: Incident and Reflected Waves

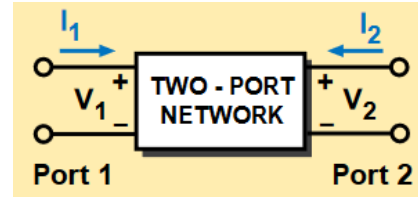


Figure 3: Terminal Voltages and Currents

The variables (a_i) and (b_i) are normalized complex voltage waves incident on and reflected from the i^{th} port of the network. They are defined in terms of the terminal voltage (V_i), the terminal current (I_i) and an arbitrary reference impedance (Z_i):

$$a_i = \frac{V_i + Z_i I_i}{2\sqrt{\text{Re } Z_i}}$$

$$b_i = \frac{V_i - Z_i^* I_i}{2\sqrt{\text{Re } Z_i}}$$

For most measurements and calculations it is convenient to assume that the reference impedance (Z_i) is positive and real. All variables and parameters will be referenced to a positive real impedance (Z_0).

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The independent variables (a_1) and (a_2) are normalized incident voltages:

$$a_1 = \frac{V_1 + I_1 Z_0}{2\sqrt{Z_0}} = \frac{\text{voltage wave incident on port 1}}{\sqrt{Z_0}} = \frac{V_{i1}}{\sqrt{Z_0}}$$

$$a_2 = \frac{V_2 + I_2 Z_0}{2\sqrt{Z_0}} = \frac{\text{voltage wave incident on port 2}}{\sqrt{Z_0}} = \frac{V_{i2}}{\sqrt{Z_0}}$$

The dependent variables (b_1) and (b_2) are normalized reflected voltages:

$$b_1 = \frac{V_1 - I_1 Z_0}{2\sqrt{Z_0}} = \frac{\text{voltage wave reflected from port 1}}{\sqrt{Z_0}} = \frac{V_{r1}}{\sqrt{Z_0}}$$

$$b_2 = \frac{V_2 - I_2 Z_0}{2\sqrt{Z_0}} = \frac{\text{voltage wave reflected from port 2}}{\sqrt{Z_0}} = \frac{V_{r2}}{\sqrt{Z_0}}$$

The linear equations describing the two port network are:

$$b_1 = S_{11}a_1 + S_{12}a_2$$

$$b_2 = S_{21}a_1 + S_{22}a_2$$

The s-parameters S_{11} , S_{22} , S_{21} , S_{12} , are:

$S_{11} = \left. \frac{b_1}{a_1} \right _{a_2=0}$	Input reflection coefficient with the output port terminated by a matched load
$S_{22} = \left. \frac{b_2}{a_2} \right _{a_1=0}$	Output reflection coefficient with the input port terminated by a matched load
$S_{21} = \left. \frac{b_2}{a_1} \right _{a_2=0}$	Forward transmission gain with the output port terminated in a matched load
$S_{12} = \left. \frac{b_1}{a_2} \right _{a_1=0}$	Reverse transmission gain with the input port terminated in a matched load

The following observation can be made:

$$S_{11} = \frac{b_1}{a_1} = \frac{\frac{V_1}{I_1} - Z_0}{\frac{V_1}{I_1} + Z_0} = \frac{Z_1 - Z_0}{Z_1 + Z_0}$$

$$Z_1 = Z_0 \frac{(1 + S_{11})}{(1 - S_{11})} = \frac{V_1}{I_1} = \text{input impedance at port 1}$$

Thus, the reflection coefficients S_{11} and S_{22} can be converted directly to impedance, and manipulated to determine matching networks for optimizing a circuit design.

S-Parameter Simulation with ADS

3) Lab Exercises:

- 1) The scattering matrix of a two-port network is given as:

$$S_{50\Omega} = \begin{bmatrix} 5/13 & j12/13 \\ j12/13 & 5/13 \end{bmatrix}$$

The port impedance is $Z_0 = 50\Omega$.

- (a) Create a (*.snp) file as shown in figure 4, using the given scattering parameters
- SNP stands for the following: s = s-parameters, n = number of ports, p = port
 - Example: For 2 port network, snp = s2p
- (b) Format of a (*.snp) file is as follows:
- The line with the sharp symbol (#) defines the format of the subsequent lines
 - GHz = Frequency to be given in GHz
 - S = S-parameters to be given in the format of Magnitude and Angle (MA)
 - R = Port reference impedance which in this case is set to 50Ω
 - Lines with an exclamation mark (!) are comment lines
- (c) In this problem the s-parameters do not vary with frequency
- To plot the s-parameters with ADS an arbitrary frequency range from 1GHz to 2 GHz is chosen
 - The S-parameter data is given in decimal nomination

#	GHz	S	MA	R	50				
! freq	magS11	angS11	magS21	angS21	magS12	angS12	magS22	angS22	
! freq	5/13	0 deg	12/13	90 deg	12/13	90 deg	5/13	0 deg	
1.0	0.3846153846	0	0.923076923	90	0.923076923	90	0.3846153846	0	
2.0	0.3846153846	0	0.923076923	90	0.923076923	90	0.3846153846	0	

Figure 4: Format of s2p File for S-Parameter Definition

- (d) Create a schematic as shown in figure 5
- Place a SNP element (in this case S2P) in the schematic window using **Data Items palette** in ADS
 - Import the (*.s2p) file into the SNP element
 - Perform two port simulation using S2P element (Start = 1 GHz, Stop = 2 GHz, Step = 100 MHz)

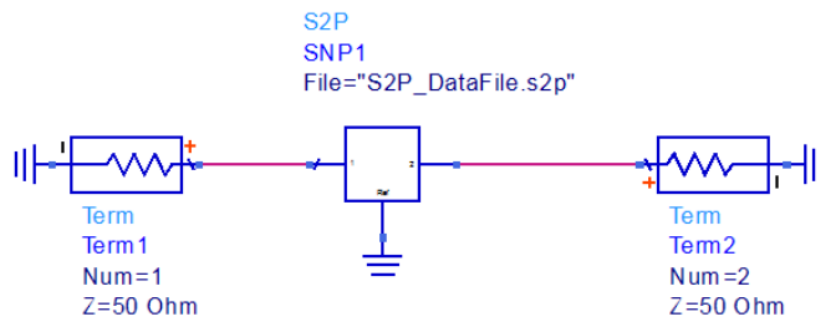


Figure 5: Schematic of Simulating S-Parameters using SNP File

- (e) Use **rectangular plot** to show **magnitude** and **phase** of the scattering parameters versus frequency
- (f) Use a **list plot** to **tabulate** the four scattering parameters (S_{11} , S_{12} , S_{21} , S_{22}) versus frequency

S-Parameter Simulation with ADS

- 2) Repeat the process of the 1st problem using the following scattering matrix:

$$S_{50\Omega} = \begin{bmatrix} 0.3 + j0.7 & j0.6 \\ j0.6 & 0.3 - j0.7 \end{bmatrix}$$

The port impedance is $Z_0 = 50\Omega$.

In this case, the s-parameters are given in real/imaginary (RI) form, so use that form in the (.s2p) file.

- 3) Find the scattering parameters of the 3 dB attenuator circuit given in figure 6. Assume both characteristic and port impedances to be 50Ω .

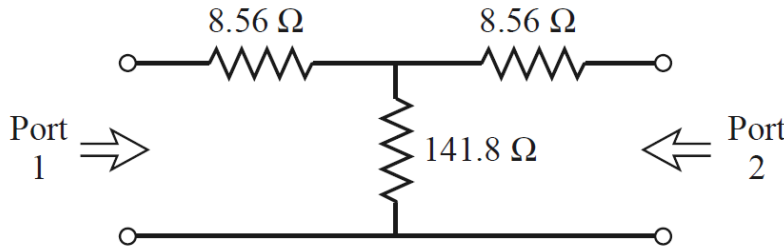


Figure 6: 3-dB Attenuator Circuit

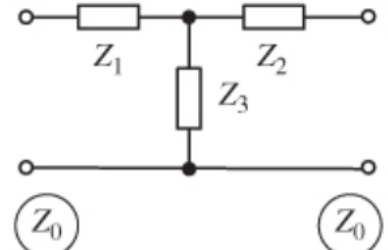


Figure 7: General T-network

- (a) Derive the following relations for the general T-network given in figure 7.

$$Z_{in1} = Z_1 + Z_3 || (Z_2 + Z_0) = Z_1 + \frac{Z_3(Z_2 + Z_0)}{Z_3 + (Z_2 + Z_0)}$$

$$S_{11} = \frac{Z_{in1} - Z_0}{Z_{in1} + Z_0} = \frac{Z_1 Z_2 + Z_1 Z_3 + Z_2 Z_3 + Z_1 Z_0 - Z_2 Z_0 - Z_0^2}{Z_1 Z_2 + Z_1 Z_3 + Z_2 Z_3 + Z_1 Z_0 + Z_2 Z_0 + 2Z_3 Z_0 + Z_0^2}$$

$$S_{22} = \frac{Z_1 Z_2 + Z_1 Z_3 + Z_2 Z_3 - Z_1 Z_0 + Z_2 Z_0 - Z_0^2}{Z_1 Z_2 + Z_1 Z_3 + Z_2 Z_3 + Z_1 Z_0 + Z_2 Z_0 + 2Z_3 Z_0 + Z_0^2}$$

$$S_{21} = S_{12} = \frac{2Z_3 Z_0}{Z_1 Z_2 + Z_1 Z_3 + Z_2 Z_3 + Z_1 Z_0 + Z_2 Z_0 + 2Z_3 Z_0 + Z_0^2}$$

- (b) Apply the formulae obtained in part (a) to the circuit in figure 6
 ➤ Calculate the scattering parameters (S_{11} , S_{12} , S_{21} , S_{22})
 (c) Show that the output power of the circuit in figure 6 is 3dB less than the input power
 (d) Use ADS to simulate the circuit given in figure 6, and compare the result obtained in part (b)
- 4) A vector network analyzer measures the following reflection coefficient at the input terminals of an antenna:

$$r_A = 0.4e^{-j20^\circ}$$

The port reference impedance is $Z_0 = 50\Omega$.

- (a) Determine the input impedance (Z_A) of the antenna
 (b) Validate the result obtained in part (a) using ADS
 ✓ Create a (*.slp) file with the given s-parameters
 ✓ Perform a one port simulation using S1P element (Start = 1 GHz, Stop = 2 GHz, Step = 100 MHz)
 ✓ Plot the magnitude and phase of reflection coefficient (r_A)
 ✓ Plot the real and imaginary part of input impedance (Z_A)

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- 5) Figure 8 shows a circuit with disconnected terminals in order to calculate the input impedances and reflection coefficients. Assume the following parameters:

$$Z_0 = 50\Omega \quad Z_A = 100\Omega + j\omega L = 100\Omega + j100\Omega, \text{ where } L = 15.92 \text{ nH} \quad Z = 1/(j\omega C), \text{ where } C = 5 \text{ pF}$$

- (a) Calculate the impedances Z_{in1} and Z_{in2}
- (b) Calculate the reflection coefficients r_1 and r_2

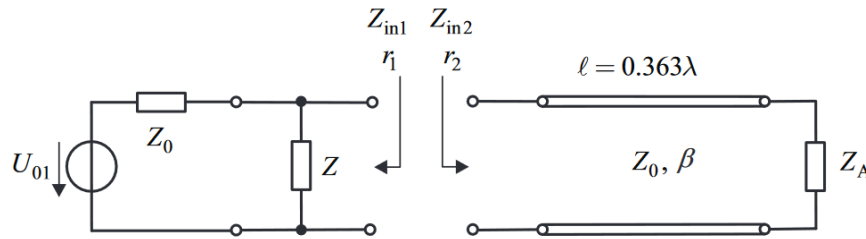


Figure 8: Circuit with Disconnected Terminals

The input impedance Z_{in1} is:

$$Z_{in1} = Z_0 \parallel \frac{1}{j\omega C}$$

The reflection coefficient r_1 is:

$$r_1 = \frac{Z_{in1} - Z_0}{Z_{in2} + Z_0}$$

To determine the reflection coefficient (r_2), first consider the reflection coefficient at the end of the transmission line:

$$r'_2 = \frac{Z_A - Z_0}{Z_A + Z_0}$$

The reflection coefficient at the input of the transmission line can be calculated from:

$$r_2 = r'_2 e^{-j2\beta l}$$

Use the **Smith-Chart Utility** (selected from Tools menu of ADS) to calculate the input impedance Z_{in2}

- (c) Validate the circuit performance using ADS using schematics given in figures 9 and 10
 - Use a frequency range from 0.1 GHz to 2 GHz with stepping of 100 MHz
 - Plot the reflection coefficients (magnitude and phase). Use both rectangular and list plots.
 - Plot the input impedances (real and imaginary part). Use both rectangular and list plots.
 - Use markers to validate the analytical results with simulation results at a frequency of 1 GHz
 - Display the reflection parameters using Smith Chart

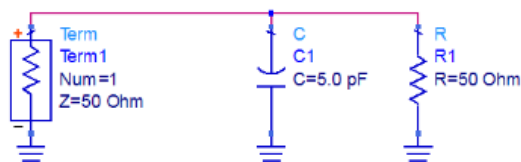


Figure 9: Left Side of Circuit of Figure 8

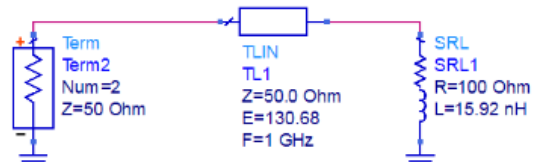


Figure 10: Right Side of Circuit of Figure 8