



## **NPTEL ONLINE CERTIFICATION COURSES**

**Course Name: Deep Learning**  
**Faculty Name: Prof. P. K. Biswas**  
**Department : E & ECE, IIT Kharagpur**

### **Topic**

**Lecture 57: Variational Autoencoder**

## CONCEPTS COVERED

### Concepts Covered

- ☐ Generative Model
- ☐ Limitations of usual auto-encoder
- ☐ Intuitions behind VAE
- ☐ Variational Inference
- ☐ Practical Realization of VAE



# Generative Model

- ☐ Big Animal.
- ☐ Has four legs.
- ☐ Big ears.
- ☐ Long trunk.
- ☐ A pair of tusks
- ☐ .....

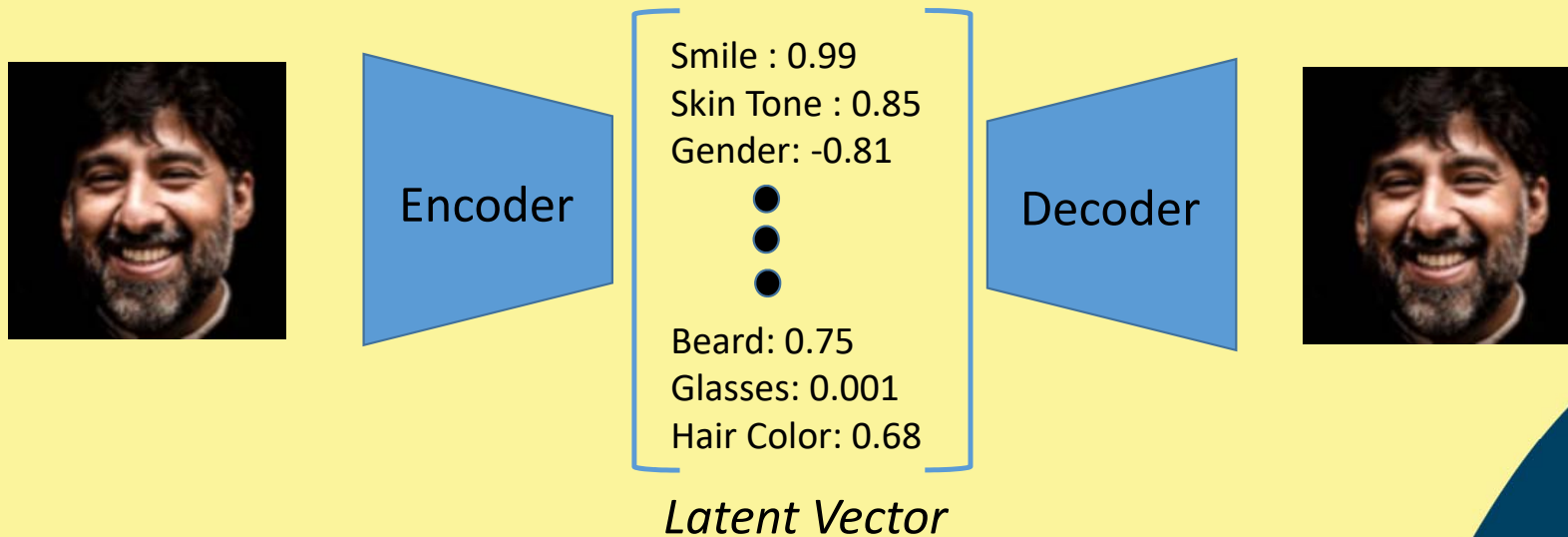


*Latent Variables*



# Traditional Autoencoder

- ❑ Maps an input image via an encoder to a deterministic latent code
- ❑ Decoder maps the latent code to reconstruct the input image



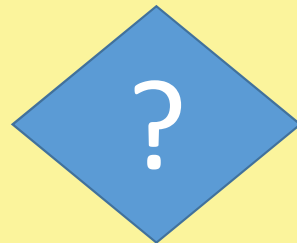
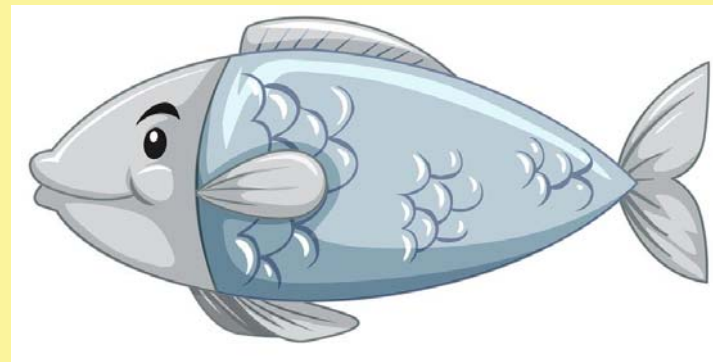
<https://www.jeremyjordan.me/variational-autoencoders/>

# Traditional Autoencoder : Limitations

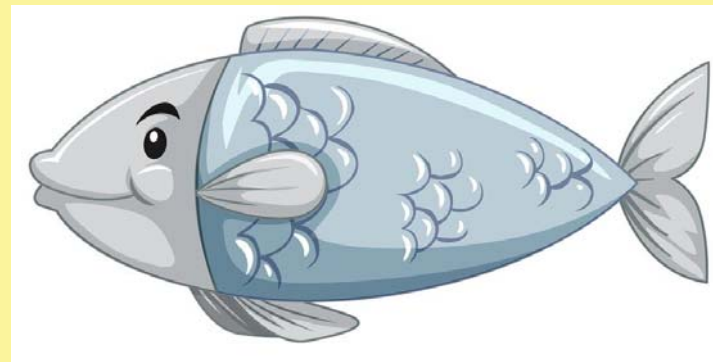
- ❑ In pursuit of compact representations, auto-encoders tends to create a latent space which is not continuous
- ❑ As a generative model, we need a latent space from which we can smoothly sample and yet get realistic reconstructions
- ❑ Auto-encoders do not allow such easy interpolations in latent space



# Traditional Autoencoder : Limitations

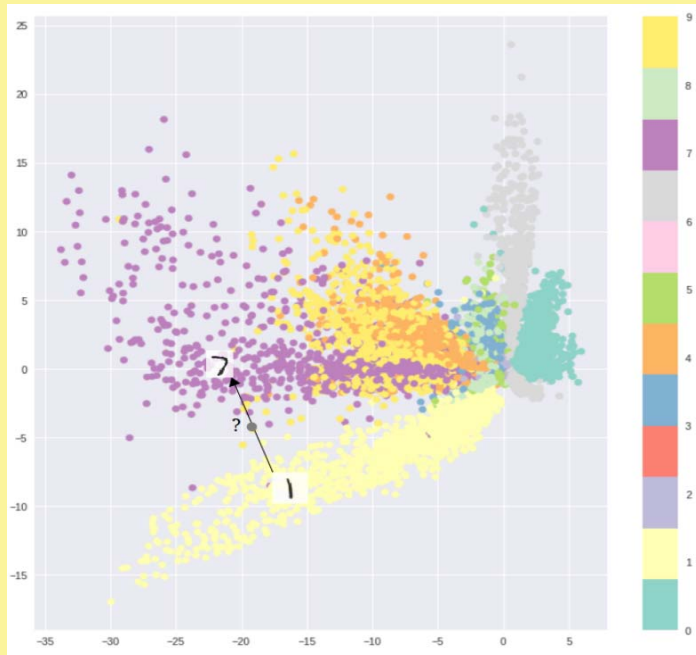


# Traditional Autoencoder : Limitations





# Traditional Autoencoder : Limitations



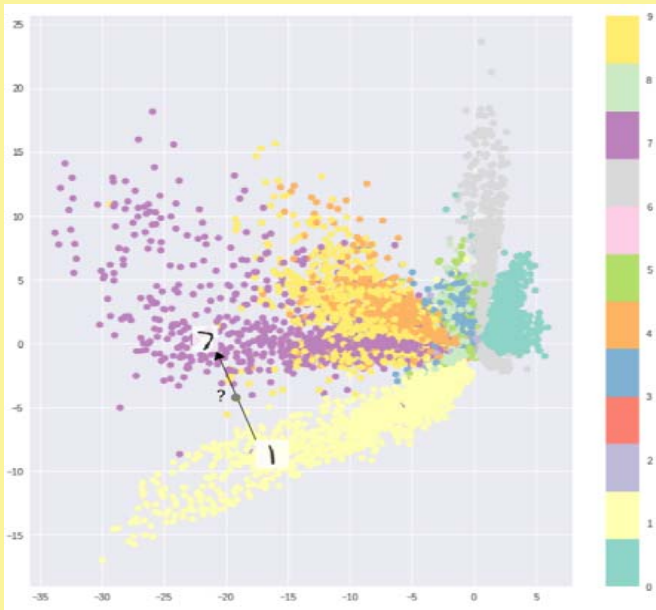
- ❑ Distinct cluster for each class
- ❑ Not easy for decoder to reconstruct since we need different distinct codes for each image



Image Source: <https://towardsdatascience.com/intuitively-understanding-variational-autoencoders-1bfe67eb5daf>



# Traditional Autoencoder : Limitations



- ❑ Discontinuous latent space means decoder never reconstructed from such unexplored points
- ❑ If we sample from such points, decoder will give unrealistic output
- ❑ **Aim:** Try to make latent space continuous yet maintain the class specific compactness



Image Source: <https://towardsdatascience.com/intuitively-understanding-variational-autoencoders-1bfe67eb5daf>

# Variational Autoencoder Intuition

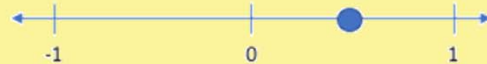
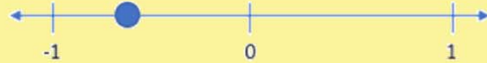
- ❑ Instead of deterministic latent code we might be interested to learn a distribution over the latent code
- ❑ For example, it is more intuitive to determine a range of “smile” value for a face instead of an absolute “smile” value
- ❑ Instead of deterministic code, we will now output the mean and standard deviation of each component of the vector (assuming each component is independent of each other)



# Autoencoder Intuition vs. VAE Latent Space

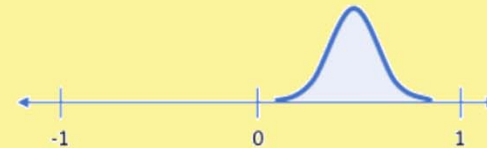


Smile (discrete value)



AutoEncoder Latent Space

Smile (probability distribution)



VAE Latent Space

vs.



<https://www.jeremyjordan.me/variational-autoencoders/>

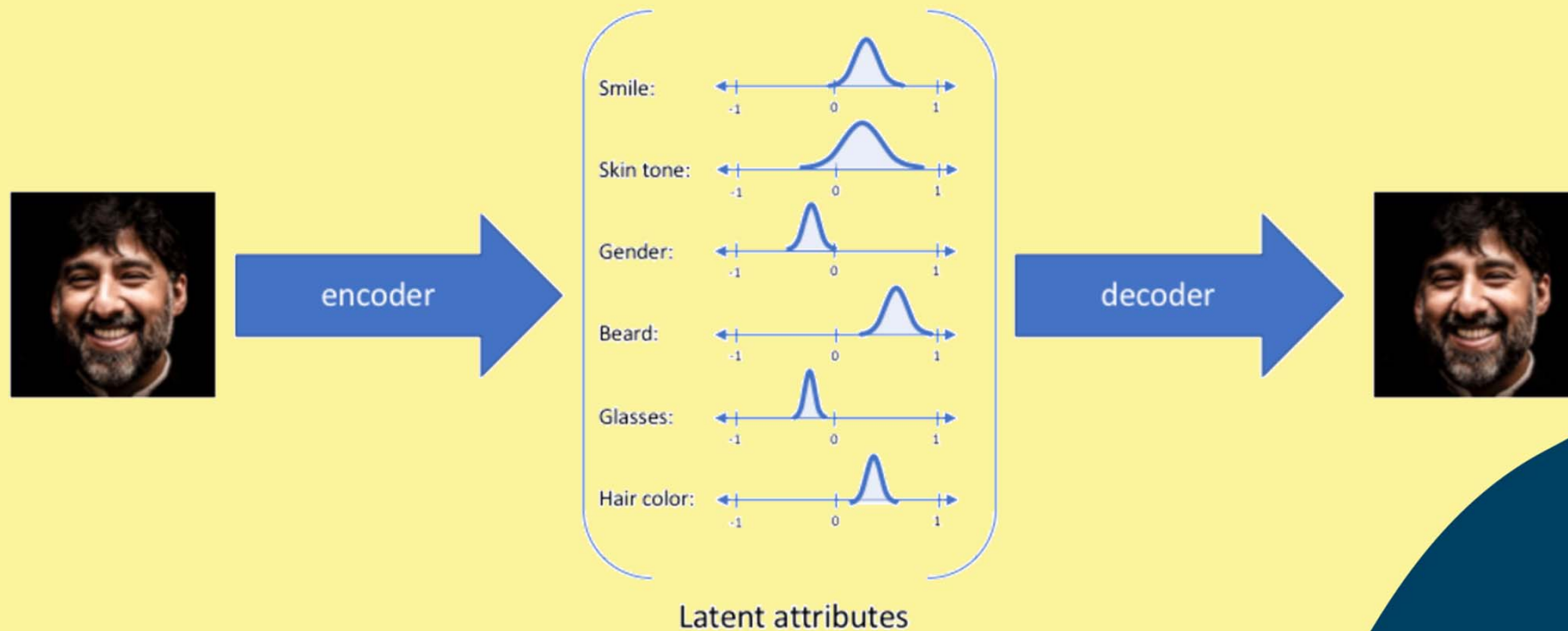
# Variational Autoencoder Intuition

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- ❑ With this setup we can represent each latent factor as a probability distribution
- ❑ We can sample from such distribution
- ❑ Then the sampled vector can be passed through Decoder (Generator) to generate an image



# Variational Autoencoder Intuition



<https://www.jeremyjordan.me/variational-autoencoders/>

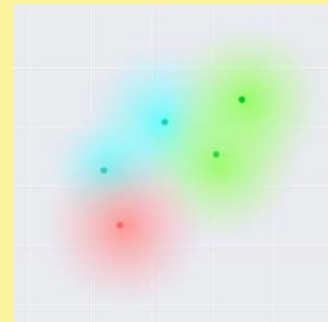
# Variational Autoencoder Intuition

- ❑ Mean vector controls where the encoding of an input should be centered around
- ❑ Standard deviation controls the “area”, how much from the mean the encoding can vary
- ❑ As encodings are generated at random from inside a hyper-sphere (distribution) decoder learns that not only is a single point in latent space referring to a sample of that class, but all nearby points refer to the same as well

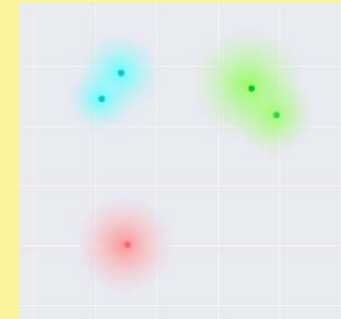


# Variational Autoencoder Intuition

- ❑ For smooth interpolations, ideally, we want overlap between samples that are not very similar too, in order to interpolate between classes.
- ❑ However  $\mu$  and  $\sigma$  can take any value and learn to cluster the mean vectors of different classes far apart (and minimize  $\sigma$ ) to reduce uncertainty for the Decoder



Our goal



Network might converge to



Image Source: <https://towardsdatascience.com/intuitively-understanding-variational-autoencoders-1bfe67eb5daf>



# Variational Autoencoder Intuition

- ❑ In order to enforce smooth transition we will apply Kullback–Leibler divergence (KL divergence) between the distribution of encoded vectors and a prior distribution asserted on latent distribution space
- ❑ KL divergence between two probability distributions simply measures how much they diverge from each other.
- ❑ Minimizing the KL divergence here means optimizing the probability distribution parameters ( $\mu$  and  $\sigma$ ) to closely resemble that of the target distribution.



# Variational Autoencoder Intuition

- ❑ In VAE, it is usually assumed that the distribution of the latent space follows a zero mean Normal distribution with diagonal covariance matrix (each component is independent of the other)
- ❑ KL divergence loss will encourage encodings from different inputs to be clustered about the center of the latent space
- ❑ If network creates clusters in specific regions then KL divergence loss will penalize such clusters formation

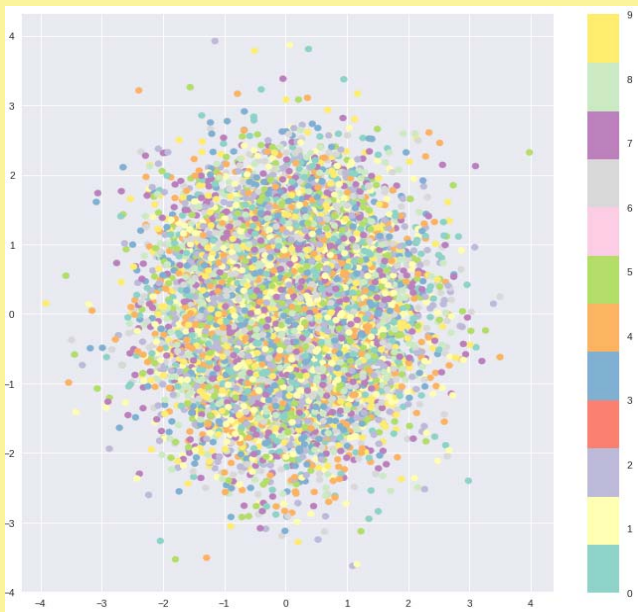


# Variational Autoencoder Intuition

- ❑ But, only KL loss results in a latent space encodings densely placed randomly, near the center of the target distribution, with little regard for similarity/dis-similarity of input samples.
- ❑ The decoder finds it impossible to decode anything meaningful from this space, simply because there really isn't any structure/context specific meaning.



# Variational Autoencoder Intuition



Latent space after training on MNIST when only optimized with KL loss



Image Source: <https://towardsdatascience.com/intuitively-understanding-variational-autoencoders-1bfe67eb5daf>

# Variational Autoencoder Intuition

- ❑ Optimizing reconstruction loss + KL divergence loss results in the generation of a latent space which maintains the similarity of nearby encodings on the local scale via clustering
- ❑ Yet globally, is very densely packed near the latent space origin

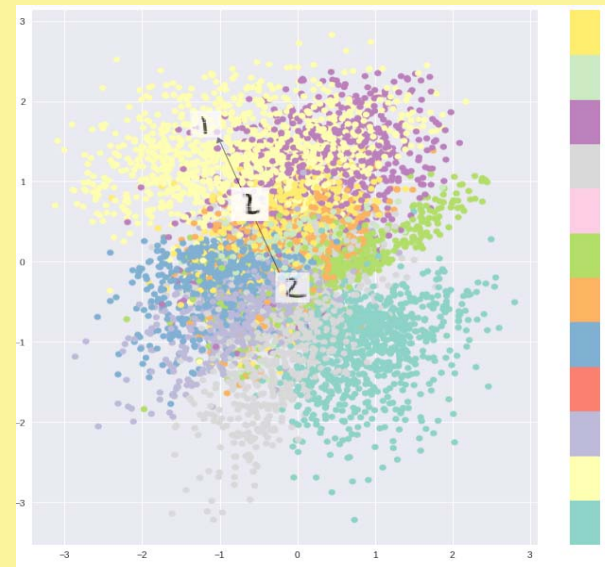
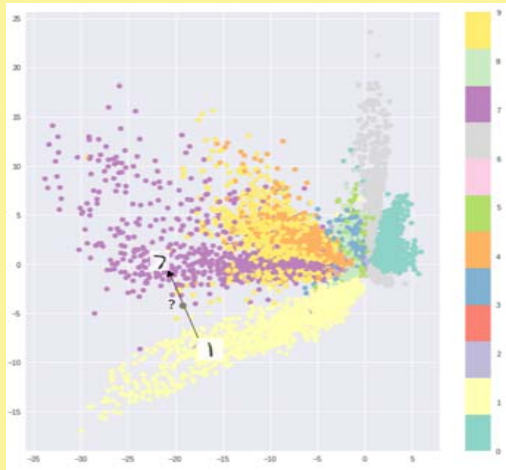
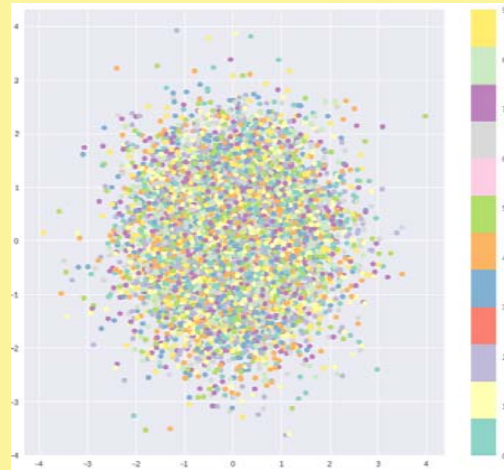


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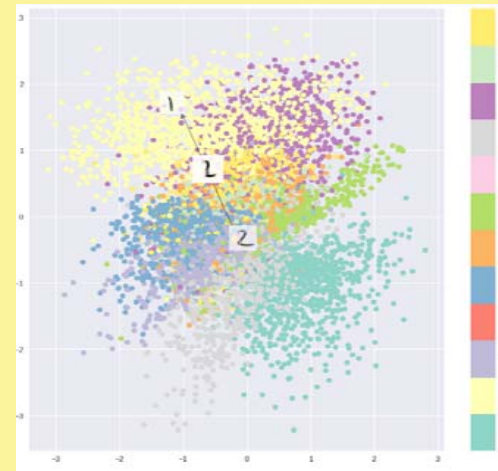
# Variational Autoencoder Intuition



Reconstruction Loss



KL Divergence Loss



KL Divergence +  
Reconstruction Loss



Image Source: <https://towardsdatascience.com/intuitively-understanding-variational-autoencoders-1bfe67eb5daf>





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*Thank  
you*

