## **Assignment 4: Converting Primal to Dual in Linear Programming using Python**

In this assignment, you have to write a Python program that converts a given primal linear programming (LP) problem into its dual form. For your motivation (how this concept is used in ML) please follow the <a href="link1">link1</a>, <a href="link1">link2</a>.

Linear programming is an optimization technique used to maximize or minimize a linear objective function subject to linear constraints. The primal problem is formulated as:

maximize c<sup>T</sup>x

subject to  $Ax \le b$ ,  $x \ge 0$ 

#### where:

- c is a vector of coefficients of the objective function
- x is a vector of decision variables
- A is a matrix of coefficients of the constraints.
- b is a vector of the right-hand side values of the constraints
- The dual problem of this primal problem is formulated as:

minimize b<sup>T</sup>y

subject to  $A^{T}y \ge c$ ,  $y \ge 0$ 

### where:

y is a vector of coefficients of the constraints in the primal problem

Your task is to write a Python function that takes the coefficients of the primal problem (c, A, b) as input and returns the coefficients of the dual problem  $(b, A^T, c)$ , you also have to handle for any equality constraints (using slack variable).

### Here are some hints to follow (Optional):

- 1. Define the number of decision variables and constraints in the primal problem and dual problem.
- 2. Define the coefficient matrix **A\_dual** for the dual problem as the transpose of the coefficient matrix **A** for the primal problem.
- 3. Define the objective coefficient vector **c\_dual** for the dual problem as the list of constants on the right-hand side of each primal constraint.
- 4. Define the right-hand side vector **b\_dual** for the dual problem as the list of coefficients of the decision variables in the primal objective function.
- 5. Determine the variable types for the dual problem. (non-negative or unrestricted).

# Rules and guidance:

- 1. Please submit the assignment before time.
- 2. Any kind of plagiarism is strictly prohibited.
- 3. If your code is detected by and AI detector, you'll be called for the viva.
- 4. Students are requested to follow <u>PEP 8 Style Guide for Python</u>.

Best wishes for the assignment.