

## VI. MATHEMATICAL PROBLEM TO BE SOLVED USING ADMM AND VERIFY ITS SOLUTION WITH CENTRALIZED OPTIMIZATION

Consider a following optimization problem:

$$\min \sum_{t=0}^5 \left[ 5x^t + 3y^t + 50(\Delta n^t)^2 + 100(y^t - 5) \right] \quad (43)$$

subject to :

$$x^t + y^t + 5n^t = 100 \quad (44)$$

$$0 \leq y^t \leq 5 \quad (45)$$

$$\Delta n^t = n^t - n^{t-1} \quad (46)$$

$$0 \leq n \leq 8, \quad (n \text{ is an integer variable}) \quad (47)$$

We will separate the objective function (43) in two parts, such as:

$$\min \sum_{t=0}^5 \left[ 5x^t + 3y^t + 50(\Delta n^t)^2 \right] + \min \sum_{t=0}^5 100(y^t - 5) \quad (48)$$

For applying ADMM, we shall separate the common variable  $y$  from both objective by introducing an auxiliary variable  $z$ , such as:

$$\min \sum_{t=0}^5 \left[ 5x^t + 3y^t + 50(\Delta n^t)^2 \right] + \min \sum_{t=0}^5 100(z^t - 5) \quad (49)$$

subject to:

$$y^t - z^t = 0 \quad (50)$$

## VII. THINGS TO PERFORM

- 1) First solve the above optimization with centralized optimization.
- 2) Solve the same problem with integer relaxation using ADMM.
- 3) Solve the same problem with Branch and Bound integrated ADMM.