Scheme + Machine Learning

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Lisp vs. convention

conventional	**Lisp**
`2 + 2`	`(+ 2 2)`
`f(X, Y)`	`(f X Y)`
`[1, 2, 3]`	`'(1 2 3)`
`a = X; b = Y; ...`	`(let* ((a X) (b Y)) ...)`
`a, b = X, Y; ...`	`(let ((a X) (b Y)) ...)`

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Crossing-over

```
(define (cross-over daddy mommy)
  (assert (= (length daddy) (length mommy)))
  (let* ((position (random (length daddy)))
         (sperm (take daddy position))
         (ovum (drop mommy position)))
     `(,@sperm ,@ovum)))

(cross-over '(a b c d e) '(v w x y z))
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Social ceremony

```
(define (procreate population social-status)
   (let* ((census (map (lambda (specimen)
                          `(,(social-status specimen) . ,specimen))
                        population))
          (social-ladder (sort census
                               (lambda ((a . _) (b . _))
                                 (> a b))))
          (population (map (lambda ((status . specimen))
                             specimen)
                           social-ladder))
          (size (length population))
          (males (biased-random-indices size))
          (females (shuffle (biased-random-indices size)))
          (offspring (map (lambda (man woman)
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                              (list-ref population man)
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      (map (on-average-once-in size (mutate not)) offspring)))
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Lottery

```
(define (biased-random-indices size)
  (if (= size 0)
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(define (shuffle l)
  (match (length l)
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    (1 l)
    (n (let ((left right (split-at l
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Mutations

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(define ((on-average-once-in n action) arg)
  (assert (and (integer? n) (> n 0)))
  (if (= (random n) 0)
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     arg))

(define ((mutate how) specimen)
  (let* ((n (random (length specimen)))
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    (alter #;element-number n #;in specimen
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Natural selection

```
(define (evolve population #;towards criterion
                #;for iterations)
  (assert (and (integer? iterations)
               (>= iterations 0)))
  (if (<= iterations 0)
    population
    (evolve (procreate population criterion)
            #;towards criterion
            #;for (- iterations 1))))
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Making history

```
(define (optimize dimension population-size
                  iterations criterion)
  (let* ((population (generate-population
                       population-size
                       dimension))
         (modern-society (evolve population
                              #;towards criterion
                              #;for iterations)))
    (argmax criterion modern-society)))

(define (generate-population size dimension)
  (generate-list size
        (lambda ()
          (generate-specimen dimension))))
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(define (generate-specimen dimension)
  (generate-list dimension
     (lambda () (= (random 2) 0))))

(define (generate-list n generator)
  (assert (and (integer? size) (>= size 0)))
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SAT problem

```
(define (satisfied? formula #;under valuation)
  (match formula
    (('and . clauses)
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```

Dictionary lookup

```
(define (lookup key #;in mapping)
  (let* ((((name value) . remaining) mapping))
    (if (eq?  name key)
        value
        (lookup key remaining))))

(lookup 'y '((x 1) (y 2) (z 3)))
===> 2
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SAT problem continued

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(satisfied? '(and p q)
            '((p #true) (q #true)))
(satisfied? '(and p q)
            '((p #true) (q #false)))
(satisfied? '(and p (not p)) '((p #true)))
(satisfied? '(and p (not p)) '((p #false)))
(satisfied? '(and (or x1 (not x3))
                  (or x2 x3 (not x1))) ???)
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SAT problem continued

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Atomic formulas

```
(define (atomic-formulas proposition)
  (match proposition
    ((operator . clauses)
     (delete-duplicates (append-map
                         atomic-formulas
                         clauses)))
    (_
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     `(,proposition))))

(atomic-formulas '(and (or x1 (not x3))
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===> (x1 x3 x2)
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Conjunctive Normal Form

```
(define (number-of-satisfied-subformulas
                  #;of cnf #;for chromosome)
  (let* ((variables (atomic-formulas cnf))
         (valuation (map list variables
                              chromosome))
         (('and . or-clauses) cnf))
    (count (lambda (subformula)
             (satisfied? subformula
                          #;under valuation))
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```

Applying genetic strategy

```
(define (solve-SAT formula/cnf population iterations)
  (let* ((dimension (length (atomic-formulas
                               formula/cnf)))
         (measure (lambda (chromosome)
                    (number-of-satisfied-subformulas
                         #;of formula
                         #;for chromosome))))
    (optimize dimension population iterations measure)))
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