#### Algolab Graph and BGL Introduction

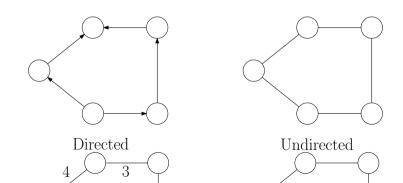
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October 10, 2018

## Graph definitions

A graph has n vertices/nodes V and m edges/arcs E.

- (un-) directed
- ► (non-) weighted
- ► (a-) cyclic
- ► (dis-) connected



# Complexity-driven programming (not yet a real thing):

- $\Theta(V+E) \text{great! } E < 10^{7...9}$
- $ightharpoonup \Theta(V \cdot \log(V + E))$  cool
- $ightharpoonup \Theta(V \cdot E)$  maybe ok
- $ightharpoonup \Theta(2^V)$  slow,  $V < 20 \dots 40$

#### General note:

- ! approach Find shortest paths  $\neq$  algorithm Dijkstra  $\neq$  implementation with adj.matrix
- ! abstract data type  $^{\text{Dictionary}} \neq \text{data structure}^{\text{Red-Black tree}} \neq \text{implementation}^{\text{as in STL}}$

#### **BGL**



A **generic** C++ library of graph data structures and algorithms.

**BGL** docs – your new best friend:

https://www.boost.org/doc/libs/1\_68\_0/libs/graph/doc/index.html and also on the judge:

https://judge.inf.ethz.ch/doc/algolab/bgl/boost\_1\_66\_0/libs/graph Moodle: There's a brief copy & paste manual.

Algolab VM & General: There's a technical instructions page for all things Algolab.

## BGL: A generic library

Genericity type	STL	BGL
Algorithm /	Decoupling of algorithms	Decoupling of graph algorithms
Data-Structure In-	and data-structures	and graph representations
teroperability	Key ingredients: iterators	Vertex iterators, edge iterators,
		adjacency iterators
Parameterization	Element type	Vertex and edge property
	parameterization	multi-parametrization
		Associate multiple properties
		Accessible via property maps
Extensions	through function objects	through a <i>visitor object</i> ,
(not covered		event points and methods
in Algolab)		depend on particular algorithm

# BGL: Graph Representations

Representation	Advantages	Do
Adjacency list	Swiss army knife: Directed/undirected graphs, allow/disallow parallel-edges, efficient insertion, fast adjacency structure exploitation	use this!
Adjacency matrix	Dense graphs	use at your own risk!

### BGL: adjacency\_list

Example without any vertex or edge properties:

```
1 // Easy syntax. Parameters:
2 // OutEdgeList type, VertexList type, Directivity
3 typedef boost::adjacency_list<boost::vecS, boost::directedS> Graph;
4
5 // which is the same as:
6 typedef boost::adjacency_list<boost::vecS, boost::vecS, boost::directedS,
7 boost::no_property, // the graph has no interior vertex properties
8 boost::no_property // the graph has no interior edge properties
9 > Graph;
```

Defines a *directed* Graph where the vertices are stored in a vector (VertexList vecS) and the outgoing edges in each vertex are stored in a vector (OutEdgeList vecS). (Also see *Useful stuff: Options for adjacency\_list, page 44.*)

#### BGL: adjacency\_list

Example with vertex property and multiple edge properties:

Interior properties are stored with the graph. Property Maps allow us to access the interior properties of the graph. Think of these as a mapping (object with operator []). Also see *Useful stuff: Interior property maps, pages 48–49*.

#### Warm-up: Read a Graph

```
7 typedef boost::adjacency list<vecS, vecS, directedS> Graph;
9 int main()
10 {
      Graph G(4);
11
12
      boost::add_edge(0, 1, G);
13
      boost::add_edge(1, 2, G);
14
15
      boost::add edge(2, 3, G);
      boost::add_edge(3, 0, G);
16
17
      boost::graph_traits<Graph>::edge_iterator ebeg, eend;
18
      for(boost::tie(ebeg, eend) = boost::edges(G); ebeg != eend; ++ebeg){
19
           std::cout << "G contains an edge from " << boost::source(*ebeg, G)
20
                        << "to " << boost::target(*ebeg, G) << std::endl:
21
       }
22
23 }
```

## Warm-up: Read a weighted Graph

```
7 typedef boost::adjacency_list<vecS, vecS, directedS, no_property,</pre>
                                        property<edge weight t, int> > Graph;
8
9 typedef boost::property map<Graph, edge weight t>::type WeightMap;
typedef Graph::edge descriptor Edge;
11
12
13 int main()
14 {
15 Graph G(4):
16 WeightMap weights = boost::get(edge_weight, G);
17 bool added:
18 Edge e;
19 boost::tie(e, added) = boost::add_edge(0, 1, G); weights[e]=1;
20 boost::tie(e, added) = boost::add_edge(1, 2, G); weights[e]=3;
21 boost::tie(e, added) = boost::add_edge(2, 3, G); weights[e]=-2;
22 boost::tie(e, added) = boost::add edge(3, 0, G): weights[e]=5;
  graph_traits<Graph>::edge_iterator ebeg, eend;
  for(boost::tie(ebeg, eend) = boost::edges(G); ebeg != eend; ++ebeg)
      std::cout << "Edge (" << boost::source(*ebeg G) << ", " << boost::target(*ebeg, G)
26
                     << ") has weight " << weights[*ebeg] << std::endl;</pre>
27
28 }
```

### BGL: Graph Algorithms

Area	Topic	Details
Basics	Distances	Dijkstra shortest paths
		Kruskal minimum spanning tree
	Components	Connected, biconnected &
		strongly connected components
	General Matchings	General unweighted matching
Flows	Maximum Flow	Graph setup (residual graph)
		Edmonds-Karp and Push-Relabel
	Disjoint paths	Vertex- / Edge-disjoint s-t paths
Advanced Flows	Minimum Cut	Maxflow-Mincut Theorem
	Bipartite Matchings	Vertex Cover & Independent Set
	Mincost Maxflow	Bipartite weighted matching & more

Many more (not in Algolab 2018): planarity testing, sparse matrix ordering, . . . **Prerequisites**: Graph theory, BFS, DFS, topological sorting, Eulerian tours, Union-Find. . .

## Recap: Graph Traversal and Shortest paths

Graph Traversal with vertices partitioned into three sets: visited, enqueued, unknown

- **BFS** closest first,  $\mathcal{O}(V+E)$
- ▶ **DFS** furthest first,  $\mathcal{O}(V+E)$
- ▶ Dijkstra weighted closest first,  $\mathcal{O}(E + V \log V)$  (BGL docs)

Shortest paths with negative weights: Induction on number of edges in subpaths

- **Bellman Ford** shortest paths from a single source,  $\mathcal{O}(V \cdot E)$  (BGL docs)
- ▶ Floyd–Warshall all-pairs shortest paths,  $\mathcal{O}(V^3)$  (BGL docs)

Both can also be used to detect negative cycles

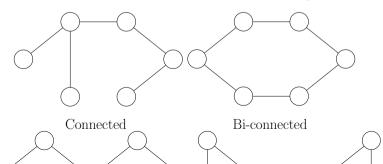
## Recap: Components (Vertex Connectivity)

#### **Undirected Graph:**

- ► Connected vertex pair with a path
- ► Biconnected vertex pair in a cycle
- ► Articulation points vertex disconnecting a component
- ► Bridges edge disconnecting a component

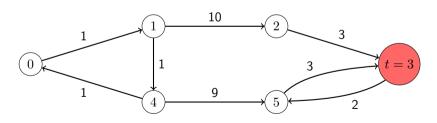
#### Directed Graph:

Strongly connected – vertex pair with directed path in both ways



#### Tutorial problem: statement & example

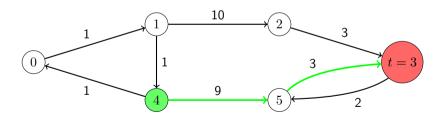
**Input** A directed graph G with positive weights on edges and a vertex t,  $|V(G)| \leq 10^5, \ |E(G)| \leq 2 \cdot 10^5.$ 



### Tutorial problem: statement & example

**Input** A directed graph G with positive weights on edges and a vertex t,  $|V(G)| \leq 10^5, \ |E(G)| \leq 2 \cdot 10^5.$ 

**Definition** We call a vertex u universal if all vertices in G can be reached from it. **Output** Minimum length of a shortest path  $u \to t$  over all universal vertices u. If such a path does not exist, output NO.



#### Tutorial problem: how to start?

Time's short, so hurry up!

- ▶ "Check if there is a unique u with no in-edges, if yes output shortest path  $u \to t$ ." (what if there is no such u?)
- ▶ "For each u check with DFS if u reaches all vertices, then..." (too slow)
- ► Start coding:

```
1 #include <iostream>
2 int main() {
3 // some random algorithm
4 }
```

#### No! Take your time,

model the problem, design the algorithm, understand why it should work,

 $\Rightarrow$  then code.

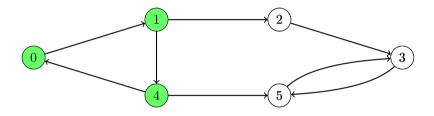
#### Tutorial problem: how to start?

- ► Bad question: Why shouldn't it work?

  ("It is correct on all three examples I came up with", etc.)
- ► Good question: Why should it work? ("How would I prove it works?")

## Tutorial problem: example

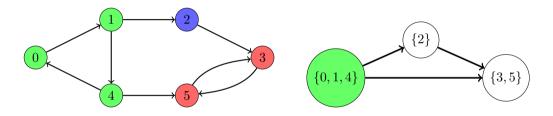
What are the universal vertices?



 $\Rightarrow$  must be related to some sort of connected component concept in directed graphs!

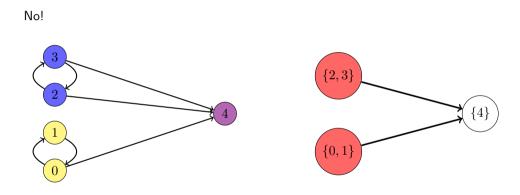
## Tutorial problem: strongly connected components (SCC) example

Strongly connected components:



Is there always a universal vertex?

## Tutorial problem: strongly connected components "NO" example



### Tutorial problem: modeling

Let us call a strongly connected component a *minimal component* if it has no in-edges in the strong condensation of the graph (the directed acyclic graph of the strongly connected components).

#### Fact

If there is more than one minimal component in G, then there is no universal vertex u.

#### Lemma

If there is exactly one minimal component in G, then its vertices are exactly the universal vertices.

## Tutorial problem: modeling

#### New formulation of the problem:

- 1. If there exists > 1 minimal strongly connected component in G, output NO.
- 2. Output the shortest distance  $u \to t$  for best universal vertex u in G.

```
Step 1: O(|V|+|E|) time (DFS)

Step 2: Dijkstra's algorithm \Omega(|V|) times \Rightarrow \Omega(|V|^2 \log |V|+|V||E|) time! I.e. around |V||E| \approx 10^5 \cdot 2 \cdot 10^5 = 2 \underbrace{0'000'000'000}_{\text{too many zeros}} operations.
```

#### Tutorial problem: modeling

#### Another new formulation of the problem:

- 1. We work with the reversed graph  $G_T$ , where all the edges of G are reversed.
- 2. If there exists > 1 maximal strongly connected component in  $G_T$ , output NO. (maximal component: no out-edge & minimal component: no in-edge)
- 3. Output the shortest distance  $t \to u$  for any vertex u in the unique maximal strongly connected component of  $G_T$ .

Now we can work only with  $G_T$  and one single Dijkstra run! I.e. around  $|V|\log |V| + |E| \approx 2 \cdot 10^5 = 200'000$  operations.

#### Tutorial problem: implementation

How to implement this now?

First and foremost, BGL docs:

- ► How to find the strong\_components.
- How to check how many maximal components are there? topological\_sort?
  - Maybe there is a simple ad hoc solution?
- lacktriangle Compute shortest t-u path on  $G_T$  with dijkstra\_shortest\_paths.

#### Tutorial problem: code – preamble

```
10 // STL includes
11 #include <iostream>
12 #include <vector>
13 #include <algorithm>
14 #include <limits>
15 // BGL includes
16 #include <boost/graph/adjacency_list.hpp>
17 #include <boost/graph/strong_components.hpp>
18 #include <boost/graph/dijkstra_shortest_paths.hpp>
```

#### Tutorial problem: code – typedefs

### Tutorial problem: code – reading the input

```
38 void testcase() {
39 // Read and build graph
40 int V, E, t; // 1st line: <vertex_no> <edge no> <target>
41 std::cin >> V >> E >> t:
42 Graph GT(V); // Creates an empty graph on V vertices
43 WeightMap weightmap = boost::get(boost::edge_weight, GT);
44 for (int i = 0; i < E; ++i) {
      int u, v, w; // Each edge: <from> <to> <weight>
45
      std::cin >> u >> v >> w;
46
     Edge e; bool success: // *** We swap u and v to create ***
47
      boost::tie(e, success) = boost::add_edge(v, u, GT); // *** the reversed graph GT! ***
48
      weightmap[e] = w:
49
50 }
```

#### Tutorial problem: code – strong components

```
50 void testcase() {
51 ...
52 // Store index of the vertices' strong component; index range [0,nscc)
53 std::vector<int> sccmap(V); // Use this vector as exterior property map
54 int nscc = boost::strong_components(GT, // Total number of components
55 boost::make_iterator_property_map(
56 sccmap.begin(), boost::get(boost::vertex_index, GT)));
```

**Exterior property:** strong\_components assigns to each vertex the index of its strong component. This is a *property* of the vertex stored *outside* of the graph itself, namely in the vector sccmap. To access the vector, we turn it into an *exterior property map*, i.e., using boost::make\_iterator\_property\_map.

#### Tutorial problem: code – maximal SCCs

```
56 void testcase() {
57 . . . .
58 // Find universal strong component (if any)
59 // Why does this approach work? Exercise.
60 std::vector<bool> is max(nscc. true):
61 EdgeIt ebeg, eend;
62 // Iterate over all edges.
63 for (boost::tie(ebeg, eend) = boost::edges(GT); ebeg != eend; ++ebeg) {
64 // ebeg is an iterator, *ebeg is a descriptor.
      Vertex u = boost::source(*ebeg, GT), v = boost::target(*ebeg, GT);
65
      if (sccmap[u] != sccmap[v]) is max[sccmap[u]] = false;
66
      // this edge (u,v) in GT implies that component sccmap[u] is not minimal in G
67
69 int max count = std::count(is max.begin(), is max.end(), true);
70 if (max_count != 1) {
      std::cout << "NO" << std::endl:
72 return;
73 }
```

#### Tutorial problem: code – Dijkstra

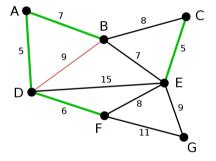
```
73 void testcase() {
74
75 // Compute shortest t-u path in GT
76 std::vector<int> distmap(V): // We must use at least one of these
77 std::vector<Vertex> predmap(V); // vectors as an exterior property map.
78 boost::dijkstra shortest paths(GT, t,
79 predecessor_map(boost::make_iterator_property_map( // named parameters
80 predmap.begin(), boost::get(boost::vertex_index, GT))).
81 distance map(boost::make iterator property map( // concatenated by .
82 distmap.begin(), boost::get(boost::vertex_index, GT))));
83 int res = std::numeric limits<int>::max():
84 for (int u = 0; u < V; ++u)
      // Minimum of distances to 'maximal' universal vertices
  if (is max[sccmap[u]])
          res = std::min(res, distmap[u]):
87
std::cout << res << std::endl:</pre>
89 }
```

#### Tutorial problem: code – main

```
94 // Main function looping over the testcases
95 int main() {
96 std::ios_base::sync_with_stdio(false);
97 int T; std::cin >> T; // First input line: Number of testcases.
98 while(T--) testcase();
99 }
```

## Recap: Minimum spanning trees

For a connected graph G=(V,E), a minimum spanning tree of G is a subgraph of G connecting all vertices in V with the minimum sum of edge weights.



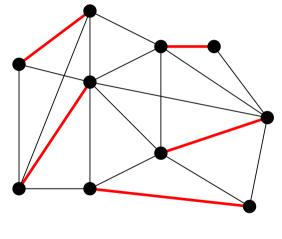
Intermediate step of Kruskal's algorithm to compute a Minimum Spanning Tree.

#### Minimum spanning tree implementations

We need to provide an edge vector to Kruskal's algorithm for storing MST edges.

#### Kruskal's algorithm

#### Recap: Maximum matching



- ightharpoonup G = (V, E)
- $ightharpoonup M\subseteq E$  is a matching if and only if no two edges of M are adjacent.
- In an unweighted graph, a maximum matching is a matching of maximum cardinality.
- ► In a weighted graph, a maximum matching is a matching such that the weight sum over the included edges is maximum.
- BGL does not provide weighted matching algorithms.

## Maximum matching: invoking algorithm

```
1 // Compute Matching
2 std::vector<Vertex> matemap(V);
3 // Use the vector as an Exterior Property Map: Vertex -> Matched mate
4 boost::edmonds maximum cardinality matching(G, boost::make iterator property map(
5 matemap.begin(), boost::get(boost::vertex_index, G)));
7 // Look at the matching
8 // Matching size
9 int matchingsize = boost::matching size(G, boost::make iterator property map(
no matemap.begin(), boost::get(boost::vertex_index, G)));
12 // unmatched vertices get the NULL VERTEX as mate.
13 const Vertex NULL_VERTEX = boost::graph_traits<Graph>::null_vertex();
14 for (int i = 0; i < V; ++i) {
       if (matemap[i] != NULL_VERTEX && i < matemap[i]) {</pre>
16
```

#### Setup: BGL installation

- Pre-installed in ETH computer rooms and the Algolab Virtualbox Image.
   Most likely also already installed on your system if you installed CGAL last week.
- On "standard" Linux distributions try getting a package from the repository. On macOS package from Homebrew.
- Comments on the versions:
  - 1.61: This version is recommended (current Ubuntu LTS, Algolab VM).
  - 1.55+: These versions have Mincost-maxflow, should be fine.
- See the technical instructions page for more details.

# Setup: BGL without installing

- BGL is a Header-only library.
- ▶ Download recent version from: http://www.boost.org/users/download/.
- ▶ Just unpack the .tar.bz2 file, no installation required, see Section 3 here: http: //www.boost.org/doc/libs/1\_58\_0/more/getting\_started/unix-variants.html.
- ► To build using this version of boost use this command: g++ -03 -std=c++11 -I path/to/boost\_1\_61\_0 test.cpp -o test
- Explanation: The '-l' flag tells the compiler to include all the files from this directory, so that it can find header files like 'boost/graph/adjacency\_list.hpp'

### Setup: compilation problems

#### Error messages can be terrible.

- Consider re-compiling the code after every line after it is first written. This will help to identify the problem quickly.
- Especially after the typedefs, and again after building the graph, before you do anything else!
- ► There will be confusing typedefs, nested types, iterators etc. Come up with a naming pattern and stick to it.

### Setup: runtime problems

- ▶ Isolate the smallest possible example where the program misbehaves.
- Watch out for invalidated iterators.
- ▶ Print a graph and see if it looks as expected. In particular, check if the number of vertices didn't increase due to mistakes in your edge insertion.

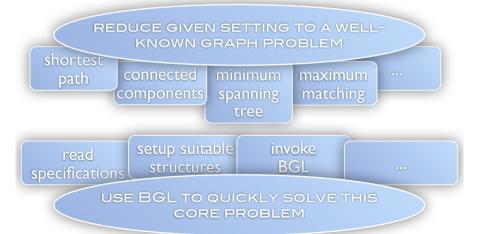
# Setup: Problem of the week

As usual, on Monday. Don't miss it! Be advised it doesn't have to be BGL. Anything already covered in the course can be used.

#### Conclusion



# BGL THE BOOST GRAPH LIBRARY



# Useful stuff: Algolab BGL documentation

Copy & paste

For more information please have a look at the following provided files:

A PDF manual containing code snippets and some detailed explanations of the concepts presented in all BGL tutorials.

Tutorial problem Code and Input file of today's tutorial problem.

**Code snippets** Self contained code demonstrating many useful code snippets.

Some of it can also be found in the rest of this Section.

# Useful stuff: Options for adjacency\_list

adjacency\_list is the class you almost always need.

```
1 // Graph Type, OutEdgeList Type, VertexList Type, (un)directedS
typedef adjacency list<vecS, vecS, undirectedS,</pre>
                             // nested vertex properties
3 no property,
4 property<edge_weight_t, int> // nested edge properties
5 >
                                  Graph:
   OutEdgeList (1st vecS) — for each vertex, adjacency list kept in a vector.
                Choosing setS instead disallows parallel edges.
     VertexList (2nd vecS) — a list of all edges is kept in a vector. Use this!
     Directivity directedS — directed graph.
                Other choices: undirectedS (undirected graph).
                Rarely needed: bidirectionalS (efficient access to incoming edges)
```

# Useful stuff: Building a graph

```
1 Graph G(n);  // Constructs empty graph with n vertices
2 ...
3 Edge e;
4 bool success;
5 tie(e, success) = add_edge(u, v, G);
```

- Adds edge from u to v in G.
- ► Caveat: if u or v don't exist in the graph, G is automatically extended.
- Returns an (Edge, bool) pair. First coordinate is an edge descriptor. If parallel edges are allowed, second coordinate is always true. Otherwise it is false in case of a failure (when the edge is a duplicate).

# Useful stuff: Removing vertices and edges, Clearing a graph

**Dangerous:** Deletions of single vertices and edges.

Takes time, invalidates descriptors and iterators, might behave counterintuitively. Consult the docs. Not recommended.

```
remove_edge(u, v, G);
remove_edge(e, G);
clear_vertex(u, G);
clear_out_edges(u, G);
remove_vertex(u, G);
```

**OK**: Clearing a graph once it is no longer needed.

```
1 G.clear(); // Removes all edges and vertices.
2 G = Graph(n); // Destroys old graph; creates a new one with n vertices.
```

#### Useful stuff: Iterators

```
1 // Iterating over vertices
2 for (u = 0; u < num_vertices(G); ++u) {
3 ...
4 // Iterating over edges
5 EdgeIt eit, eend;
6 for (tie(eit, eend) = edges(G); eit != eend; ++eit) {
7 // eit is EdgeIterator, *eit is EdgeDescriptor}
8 Vertex u = source(*eit, G), v = target(*eit, G);
9 ...</pre>
```

- edges(G) returns a pair of iterators which define a range of all edges.
- For undirected graphs each edge is visited once, with some orientation.

```
10 // Iterating over outgoing edges
11 OutEdgeIt oeit, oeend;
12 for (tie(oeit, oeend) = out_edges(u, G); oeit != oeend; ++oeit) {
13 Vertex v = target(*oeit, G);
14 ...
```

▶ source(\*eit, G) is guaranteed to be u, even in an undirected graph.

# Useful stuff: Interior property maps – vertices

Think of a **property map** as a map (i.e., object with operator []) indexed by vertices or edges. Property maps of vertices could be simulated with a vector, but maps of edges are very convenient.

```
1 // Note the nested syntax for defining more than one vertex property.
2 typedef adjacency_list<vecS, vecS, directedS,
3 property<vertex_name_t, string,
4 property<vertex_distance_t, int> >> Graph;
5 typedef property_map<Graph, vertex_name_t>::type NameMap;
6 typedef property_map<Graph, vertex_distance_t>::type DistMap;
7 ...
8 NameMap namemap = get(vertex_name, G);
9 namemap[u] = "Hans";
```

- ▶ namemap is just a handle (pointer), copying it costs  $\mathcal{O}(1)$ .
- vertex\_name\_t is a predefined tag. It is purely conventional (you can create property<vertex\_name\_t, int> and store distances), but algorithms use them as default choices if not instructed otherwise.

# Useful stuff: Interior property maps – edges

weightmap is used by many algorithms (Prim, Dijkstra, Kruskal, ...) as default choice for the edge weight.

### Useful stuff: Predefined properties

Some *predefined* vertex and edge properties:

- vertex\_name\_t
- vertex\_distance\_t
- vertex\_color\_t
- vertex\_degree\_t
- edge\_name\_t
- edge\_weight\_t
- edge\_weight2\_t

Do not be misled into, e.g., thinking that vertex\_degree\_t will automatically keep track of the degree for you.

More in the source code

#### Useful stuff: Custom properties

Can be defined if you want to keep additional info associated with edges.

```
1 enum edge_info_t { edge_info };
2 namespace boost {
      BOOST INSTALL PROPERTY(edge, info);
4 }
5 struct EdgeInfo {
6 . . .
7 }:
9 typedef adjacency_list<vecS, vecS, directedS,</pre>
10 no_property,
property<edge_info_t, EdgeInfo> > Graph;
12 typedef property_map<Graph, edge_info_t>::type InfoMap;
13 . . . .
14 InfoMap infomap = get(edge_info, G);
15 infomap[e] = ...
```

# Useful stuff: Named parameters I

Using named parameters is a way to pass parameters (usually property maps) to functions (BGL algorithms) which is useful in two cases:

1. Many algorithms have a long list of parameters. Without named parameters, all of these must be provided in the correct order, even if only some are actually needed:

```
1 // Prim non-named parameters example
2 prim_minimum_spanning_tree(G, startvertex,
3 make_iterator_property_map(predmap.begin(), get(vertex_index, G)),
4 make_iterator_property_map(distmap.begin(), get(vertex_index, G)),
5 get(edge_weight,G), get(vertex_index,G), default_dijkstra_visitor());
6 // Prim named parameters:
7 // PredecessorMap must be provided, all other parameters optional
8 prim_minimum_spanning_tree(G,
9 make_iterator_property_map(predmap.begin(), get(vertex_index, G)),
10 root_vertex(startvertex));
```

For e.g. Dijkstra calling the non-named parameter version is even worse!

# Useful stuff: Named parameters II

Using named parameters is a way to pass parameters (usually property maps) to functions (BGL algorithms) which is useful in two cases:

2. Some algorithms can record additional information to exterior property maps if provided by named parameters.

```
1 // Kruskal standard example
2 kruskal_minimum_spanning_tree(G, back_inserter(mst));
3 // Kruskal recording Union-Find information
4 vector<int> rankmap(num_vertices(G)); // used by Union-Find
5 vector<Vertex> predmap(num_vertices(G)); // in Union-Find, not the MST!
6 kruskal_minimum_spanning_tree(G, back_inserter(mst),
7 rank_map(make_iterator_property_map(
8 rankmap.begin(), get(vertex_index, G))). // concatenate with .
9 predecessor_map(make_iterator_property_map(
10 predmap.begin(), get(vertex_index, G))));
```

Always concatenate named parameters by a . Do not pass them as separate parameters (i.e. separated by a ,).

#### Useful stuff: Where to be careful

Be careful when you deviate from the provided instructions, in particular if. . .

...you use a pointer type as a property map (see e.g. here):
 Buggy for Dijkstra calls in combination with Strong components header.

```
1 // What we teach (and what works):
2 dijkstra_shortest_paths(G, 0, distance_map(
3 make_iterator_property_map(dist.begin(), get(vertex_index, G))));
4 // Using a pointer type (works most of the time):
5 dijkstra_shortest_paths(G, 0, distance_map(&dist[0]));
```